

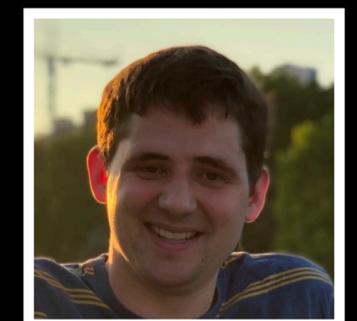
Code: [bit.ly/csc-kdd-code](https://bit.ly/csc-kdd-code)  
Slides: [bit.ly/csc-kdd-slides](https://bit.ly/csc-kdd-slides)

$$\Pr(\text{dog} \mid \{\text{cat}, \text{dog}\}) = 1/2$$

$$\Pr(\text{dog} \mid \{\text{cat}, \text{dog}, \text{fish}\}) = 7/10$$

# Choice Set Confounding in Discrete Choice

Kiran Tomlinson  
PhD Student, Cornell



with Johan Ugander & Austin R. Benson

# Choices and context effects

# Discrete choices are everywhere



amazon.com

Amazon's Choice

KDD Chocolate Flavored Milk 180ML (18 PACK)  
6 Fl Oz (Pack of 18)  
★★★★☆ ~ 57  
\$27<sup>99</sup> (\$0.26/Fl Oz)  
Save \$2.00 with coupon  
✓prime FREE Delivery Thu, Jun 24

KDD Banana Flavored Milk 180ML (18 PACK)  
6.33 Fl Oz (Pack of 18)  
★★★★☆ ~ 31  
\$27<sup>99</sup> (\$0.26/Fl Oz)  
Save \$2.00 with coupon  
✓prime FREE Delivery Thu, Jun 24

KDD Original Milk 180ML (18 PACK)  
★★★★★ ~ 2  
\$27<sup>99</sup> (\$4.60/Ounce)  
✓prime FREE Delivery Thu, Jun 24

Ad

**Best Western University Inn**  
Ithaca

**Black Friday / Cyber Monday Deals Now**  
Free Shuttle Transportation, Grab & Go Breakfast, WiFi & Parking. Pet friendly, Outdoor Pool, Fitness Center. Sanitizing Daily

Breakfast included

3.9/5 Good (999 reviews)

**\$63**  
per night  
**\$71 total**  
Includes taxes & fees

Ad

**Quality Inn Ithaca - University Area**  
Ithaca

**Black Friday / Cyber Monday Deals Now**  
Complimentary Breakfast. Free Airport Shuttle, WiFi & parking. Close to Ithaca College & Cornell University. Pets welcome.

Breakfast included

3.6/5 Good (694 reviews)

**Member Price available**

**\$59**  
per night  
**\$66 total**  
Includes taxes & fees

Ad

**Hotel Ithaca**  
Ithaca

4.0/5 Very Good (842 reviews)

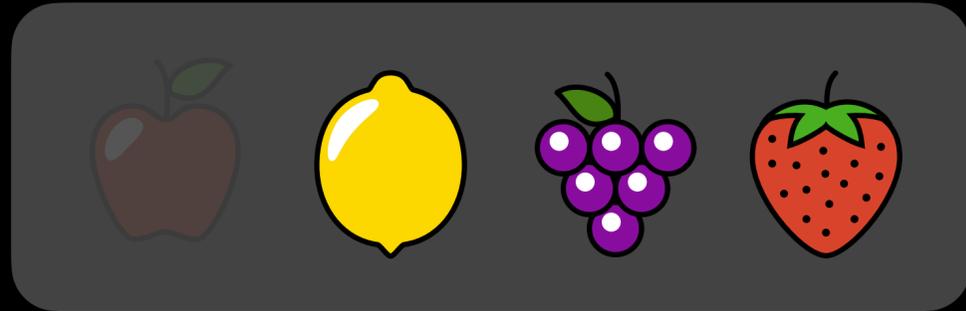
**Member Price available**

**\$94**  
per night  
**\$106 total**  
Includes taxes & fees

**The goal of choice modeling: learn  $\Pr(i | C)$**

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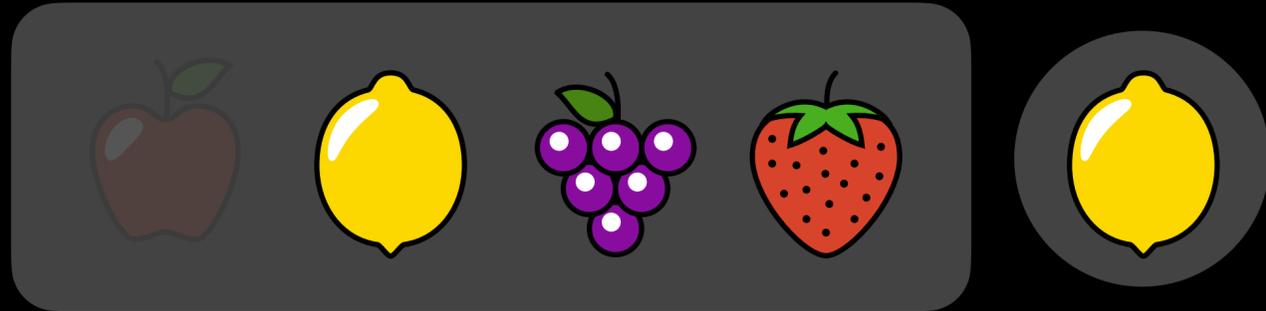
*choice set*



The goal of choice modeling: learn  $\Pr(i | C)$

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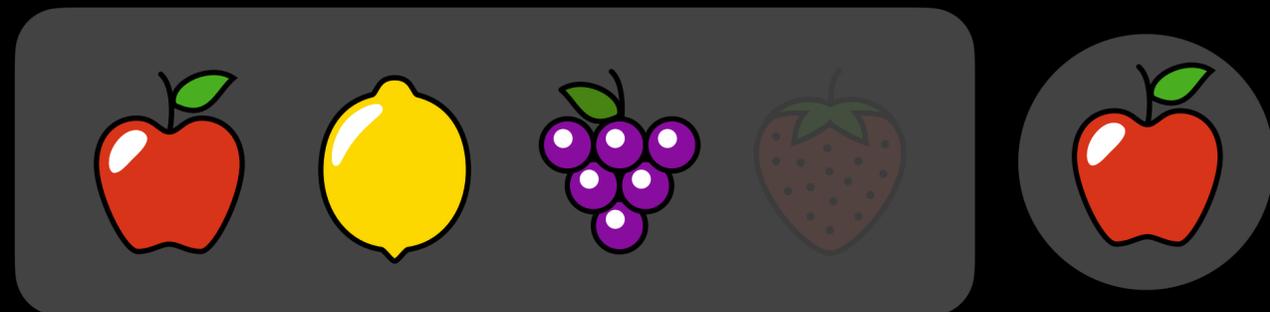
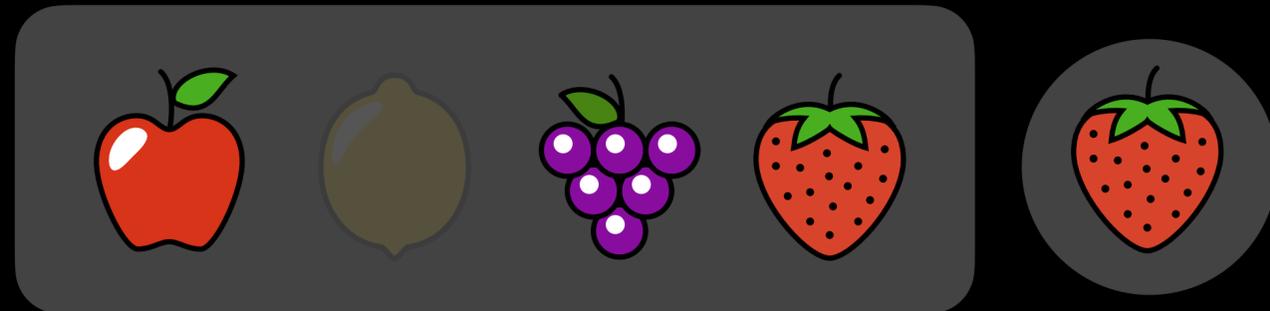
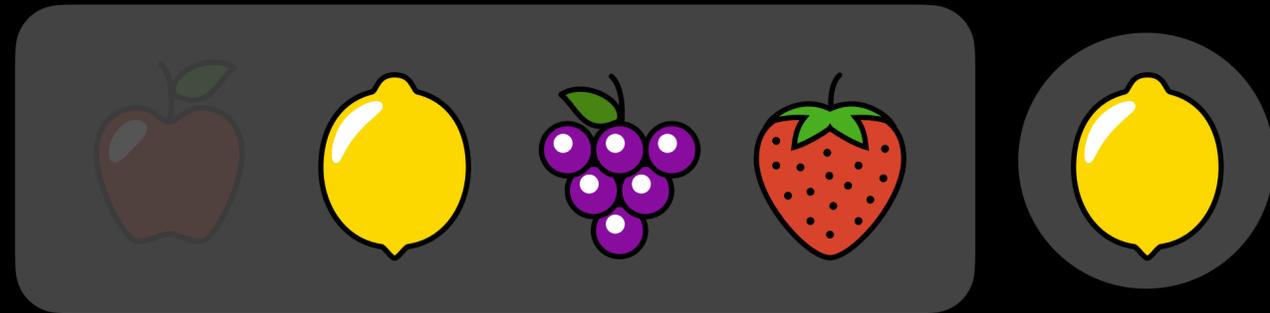
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# The goal of choice modeling: learn $\Pr(i | C)$

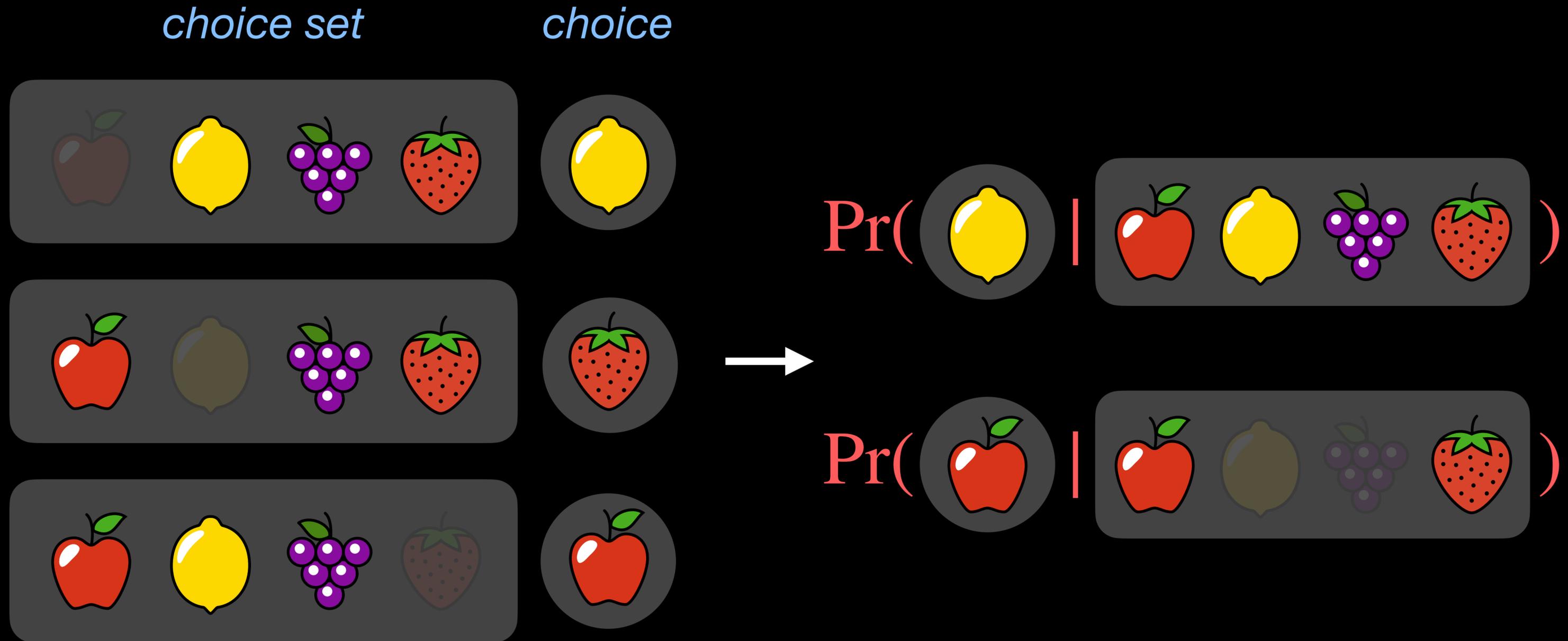
*choice set*

*choice*



...

# The goal of choice modeling: learn $\Pr(i | C)$



# The classic model: *logit*

(McFadden, *Frontiers in Econometrics* 1973)

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Assume *item*  $i$  has *utility*  $u_i$

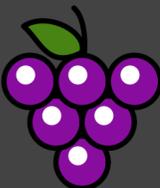
$$\Pr(i \mid C) = \frac{\exp(u_i)}{\sum_{j \in C} \exp(u_j)}$$

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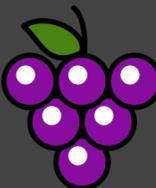
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$u_i$	1	-1	0	2
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Unique choice model satisfying  
*independence of irrelevant alternatives (IIA)*:

(Luce, *Individual Choice Behavior* 1959)

$$\frac{\Pr(i | C)}{\Pr(j | C)} = \frac{\Pr(i | C')}{\Pr(j | C')}$$

**Accurate models need to account for *context effects***

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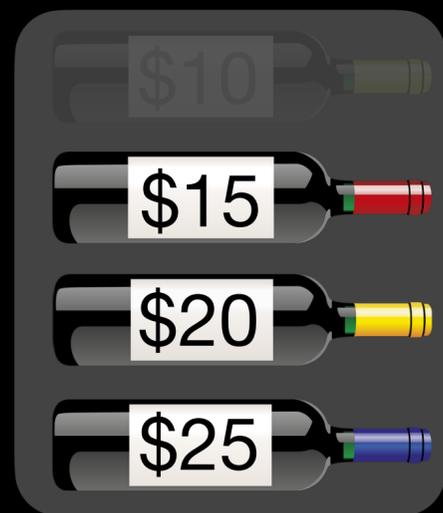


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 David Perdue* ✓	Rep.	2,462,617	49.7%
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Violations of IIA:

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## Recent contextual modeling

Chen & Joachims (KDD '16)  
Ragain & Ugander (NeurIPS '16)  
Seshadri et al. (ICML '19)  
Bower & Balzano (ICML '20)  
Rosenfeld et al. (ICML '20)  
Tomlinson & Benson (KDD '21)

# Choice set confounding

**What if our data has heterogeneous preferences?**

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Each chooser  $a$  has their own choice probabilities:  $\Pr(i \mid a, C)$

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*If we learn a model for  $\Pr(i \mid C)$ , will this accurately reflect average choice behavior  $\mathbb{E}_a \Pr(i \mid a, C)$ ?*

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→ **Not in general.** You either need

*chooser-independent preferences:*  $\Pr(i \mid a, C) = \Pr(i \mid C)$

or

*chooser-independent choice sets:*  $\Pr(C) = \Pr(C \mid a)$

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*chooser-dependent preferences **and** chooser-dependent choice sets*  
→ *choice set confounding*

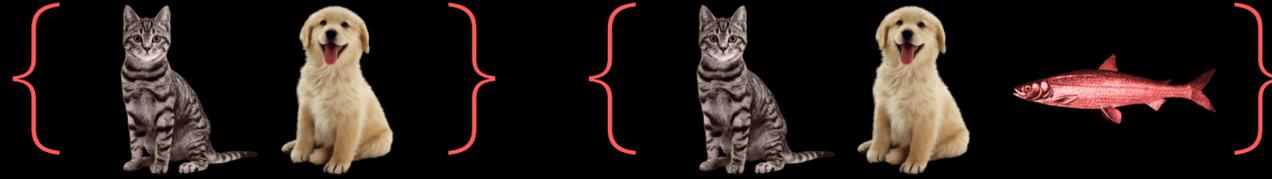
# Choice set confounding example



1/4



3/4



# Choice set confounding example

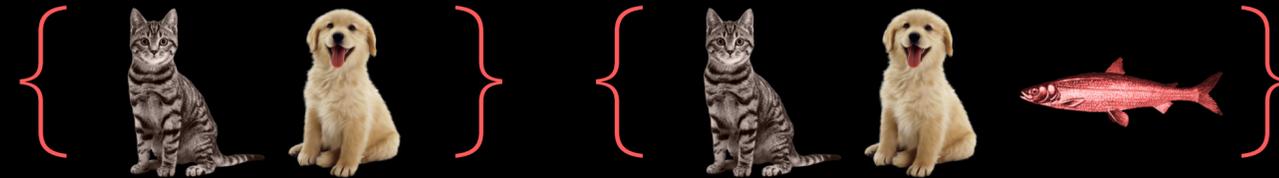


1/4



3/4

Choice probabilities:



3/4 1/4

3/4 1/4 0



1/4 3/4

1/4 3/4 0

# Choice set confounding example

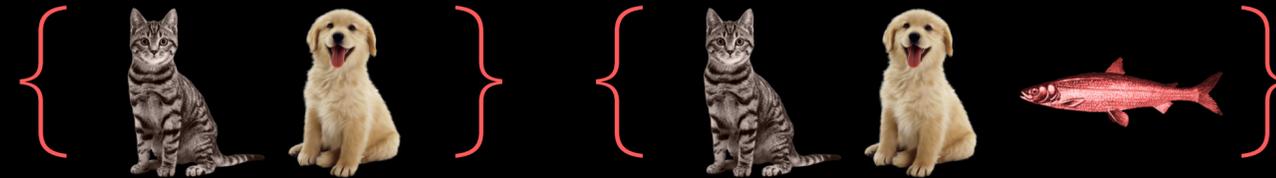


1/4



3/4

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3/4 1/4

3/4 1/4 0



1/4 3/4

1/4 3/4 0

Choice set assignment probabilities:



3/4

1/4



1/4

3/4

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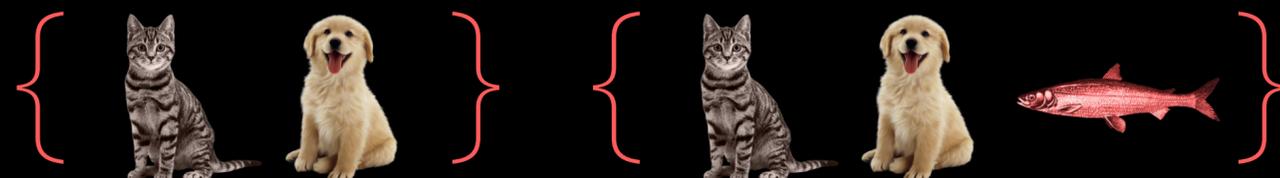


1/4



3/4

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3/4 1/4

3/4 1/4 0



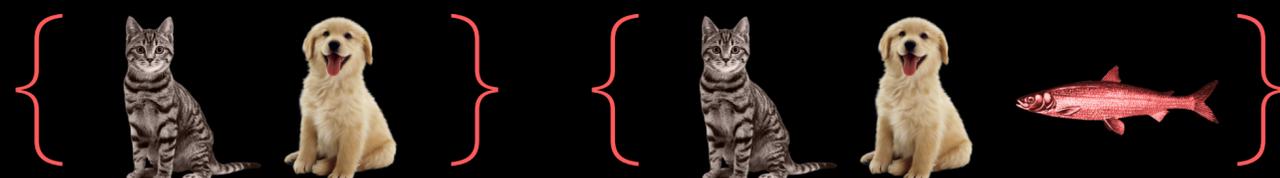
1/4 3/4

1/4 3/4 0

$$\mathbb{E}_a \Pr(\text{Golden Retriever} \mid a, \{ \text{Cat}, \text{Golden Retriever} \})$$

$$= \mathbb{E}_a \Pr(\text{Golden Retriever} \mid a, \{ \text{Cat}, \text{Golden Retriever}, \text{Salmon} \})$$

Choice set assignment probabilities:



3/4

1/4



1/4

3/4

# Choice set confounding example

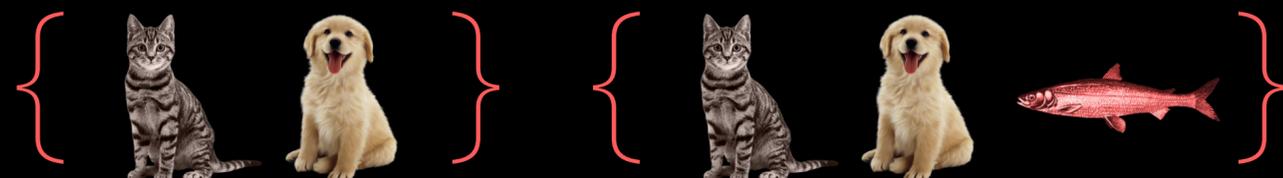


1/4



3/4

Choice probabilities:



3/4 1/4

3/4 1/4 0



1/4 3/4

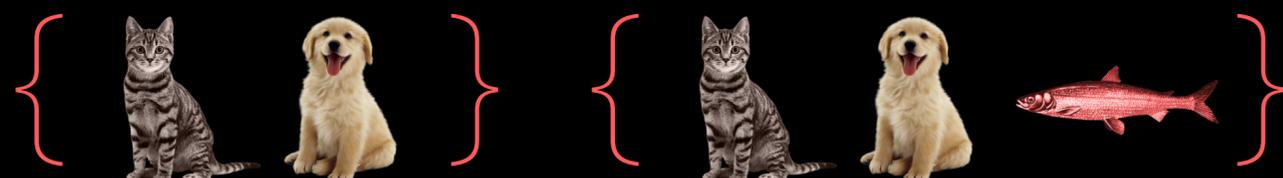
1/4 3/4 0

$$\mathbb{E}_a \Pr(\text{Golden Retriever} \mid a, \{ \text{Cat}, \text{Golden Retriever} \})$$

$$= \mathbb{E}_a \Pr(\text{Golden Retriever} \mid a, \{ \text{Cat}, \text{Golden Retriever}, \text{Salmon} \})$$

But...

Choice set assignment probabilities:



3/4

1/4



1/4

3/4

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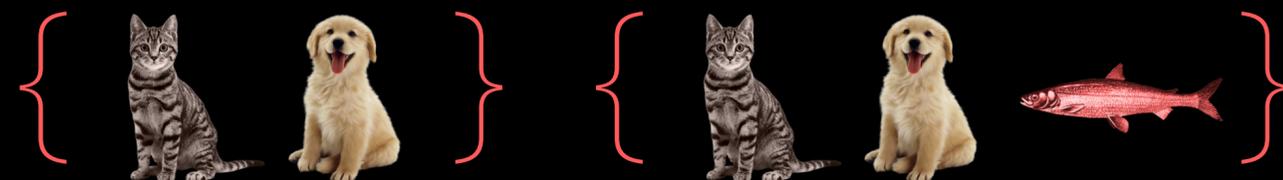


1/4



3/4

Choice probabilities:



3/4 1/4

3/4 1/4 0



1/4 3/4

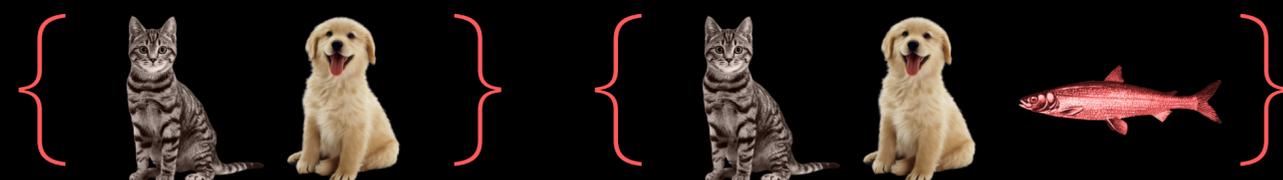
1/4 3/4 0

$$\mathbb{E}_a \Pr(\text{dog} \mid a, \{ \text{cat}, \text{dog} \})$$

$$= \mathbb{E}_a \Pr(\text{dog} \mid a, \{ \text{cat}, \text{dog}, \text{fish} \})$$

But...

Choice set assignment probabilities:



3/4

1/4



1/4

3/4

$$\Pr(\text{dog} \mid \{ \text{cat}, \text{dog} \}) = 1/2$$

$$\Pr(\text{dog} \mid \{ \text{cat}, \text{dog}, \text{fish} \}) = 7/10$$

# Choice set confounding example

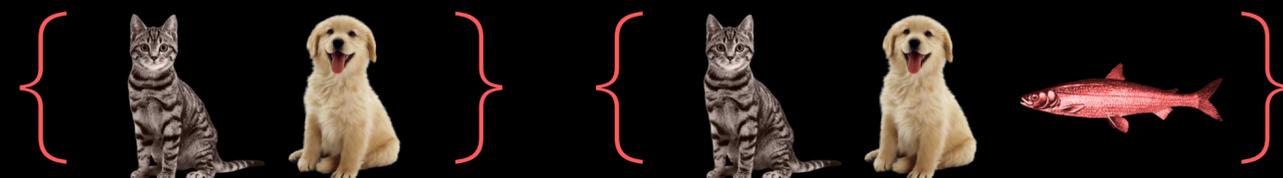


1/4



3/4

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3/4 1/4

3/4 1/4 0



1/4 3/4

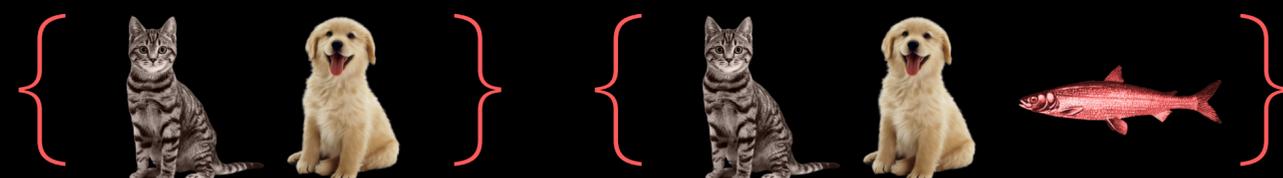
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But...

Choice set assignment probabilities:



3/4

1/4



1/4

3/4

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Context effect?

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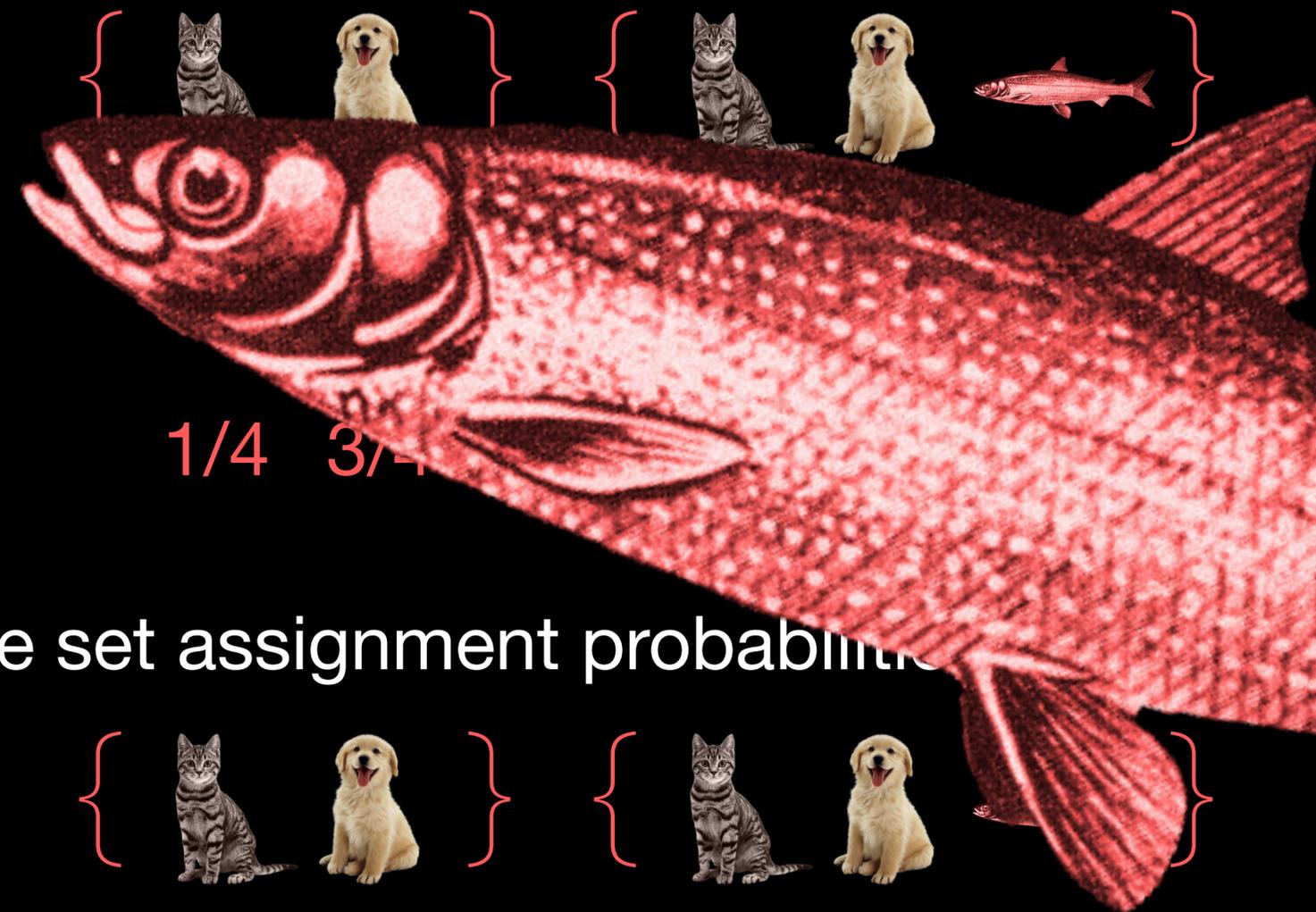


1/4



3/4

Choice probabilities:



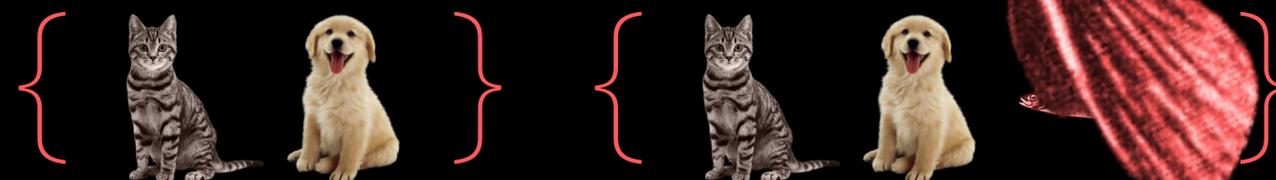
1/4 3/4



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Choice set assignment probabilities



$$\Pr(\text{cat} \mid \{\text{cat}, \text{dog}\}) = 1/2$$

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3/4

1/4



1/4

3/4

Context effect?

# Choice set confounding in real data

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SFWork & SFShop

(Koppelman & Bhat, 2006)

San Francisco transportation data

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**Used to test context effect models:**

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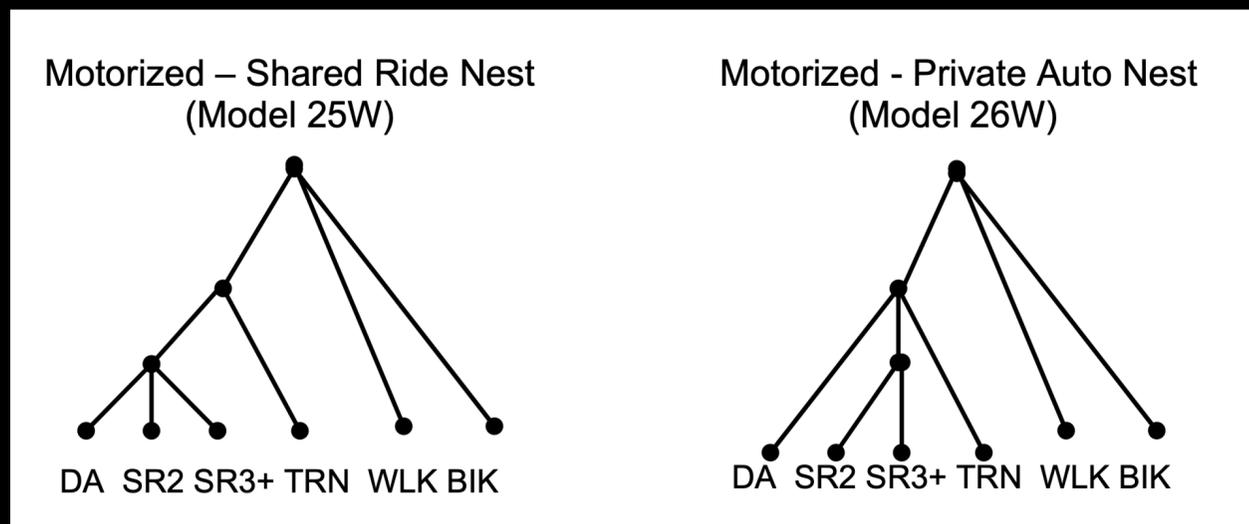
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## SFWork & SFShop

(Koppelman & Bhat, 2006)

## San Francisco transportation data

*Has regularity violations!*

SF-WORK Choice set (C)	Pr(DA   C)	N
{DA, SR 2, SR 3+, Transit}	0.72	1661
{DA, SR 2, SR 3+, Transit, Bike}	0.83	829

## Used to test context effect models:

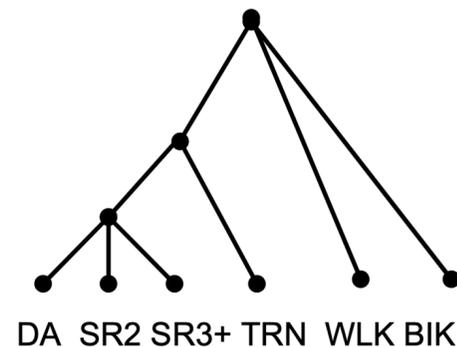
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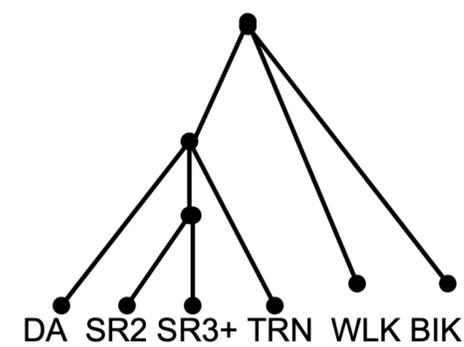
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Motorized – Shared Ride Nest  
(Model 25W)



Motorized - Private Auto Nest  
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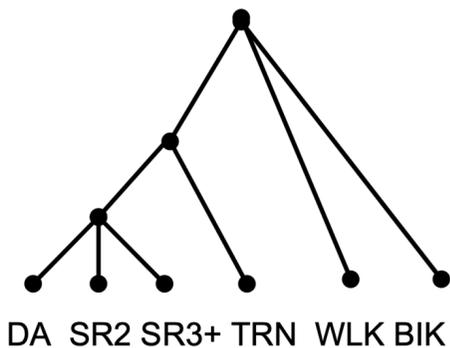
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## Context effects

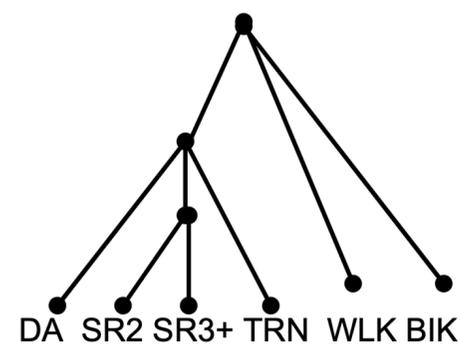
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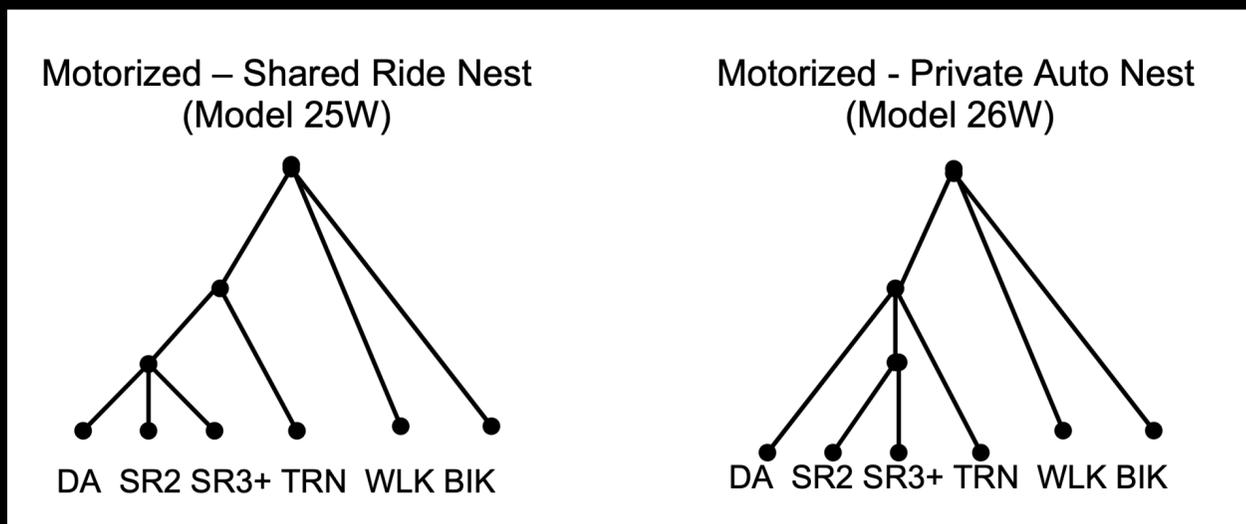
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## Context effects

or

## choice set confounding?

Comparison	Testing	Controlling	$\Delta \ell$	LRT $p$
SF-WORK				
Logit to MNL	covariates	—	883	$< 10^{-10}$
Logit to CDM	context	—	85	$< 10^{-10}$
CDM to MCDM	covariates	context	819	$< 10^{-10}$
MNL to MCDM	context	covariates	20	0.08
SF-SHOP				
Logit to MNL	covariates	—	343	$< 10^{-10}$
Logit to CDM	context	—	96	$< 10^{-10}$
CDM to MCDM	covariates	context	276	$< 10^{-10}$
MNL to MCDM	context	covariates	29	0.36



(Koppelman & Bhat, 2006)

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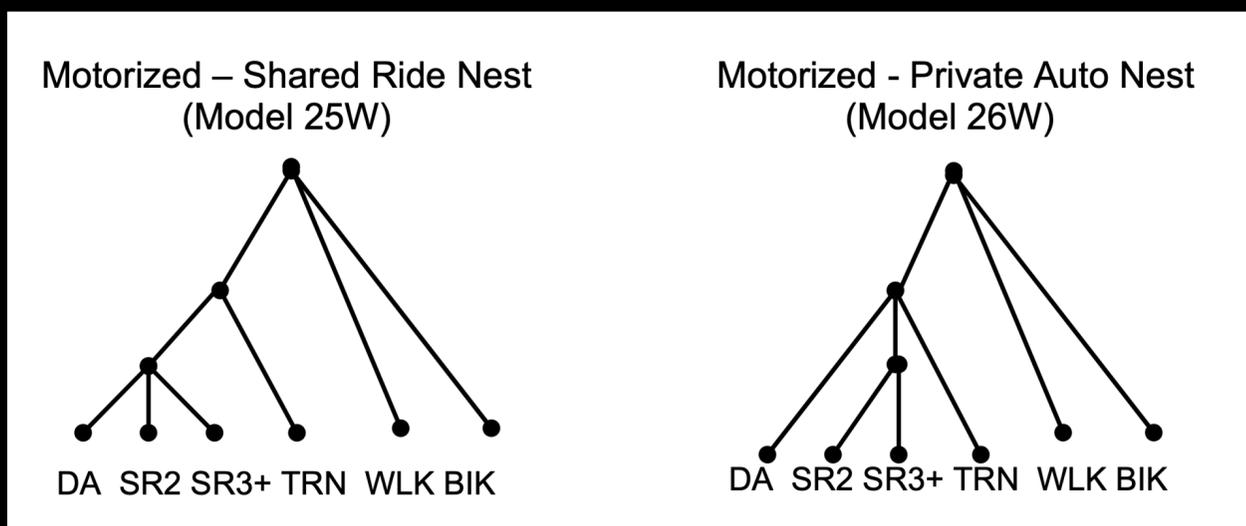
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(Koppelman & Bhat, 2006)

**CDM**: context effect model (Seshadri et al, 2019) 10

This is a *causal inference* problem

# Causal inference methods

# Option 1: *inverse probability weighting (IPW)*

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learn model from reweighed log-likelihood:

$$\ell(\theta; \mathcal{D}) = \sum_{(i,C,a) \in \mathcal{D}} \log \Pr_{\theta}(i \mid C)$$

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## Guarantee

Can learn a model as if choice sets were uniformly random

# Option 2: *regression*

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Logit:

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$$\Pr(i | C) = \frac{\exp(u_i)}{\sum_{j \in C} \exp(u_j)} \quad \longrightarrow$$

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$$\Pr(i | a, C) = \frac{\exp(u_i + \beta_i x_a)}{\sum_{j \in C} \exp(u_j + \beta_j x_a)}$$

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Combine IPW and regression  
→ *doubly robust*

# Causal inference results

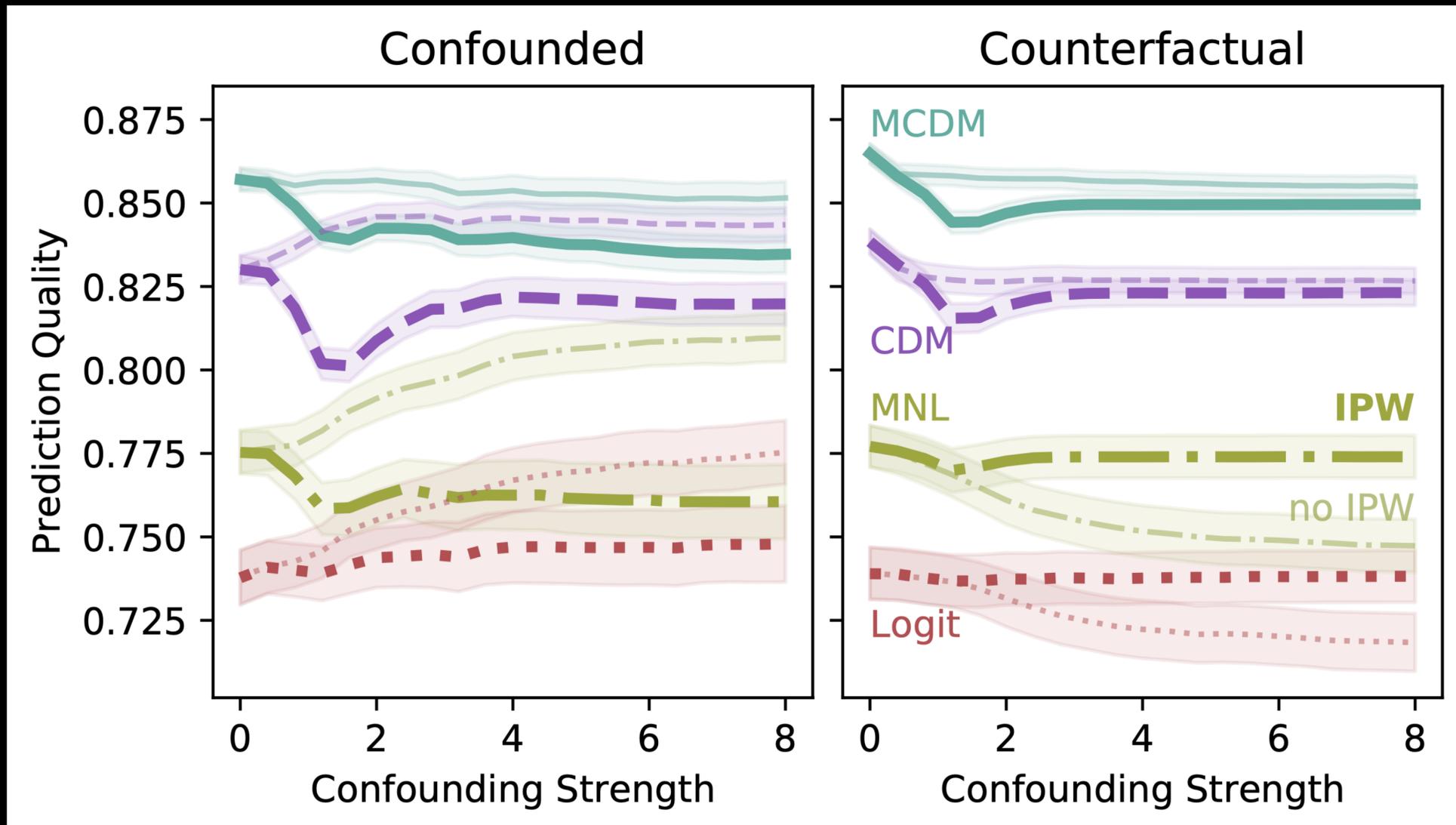
# Synthetic CDM data

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*counterfactuals*: new instances not drawn from data distribution

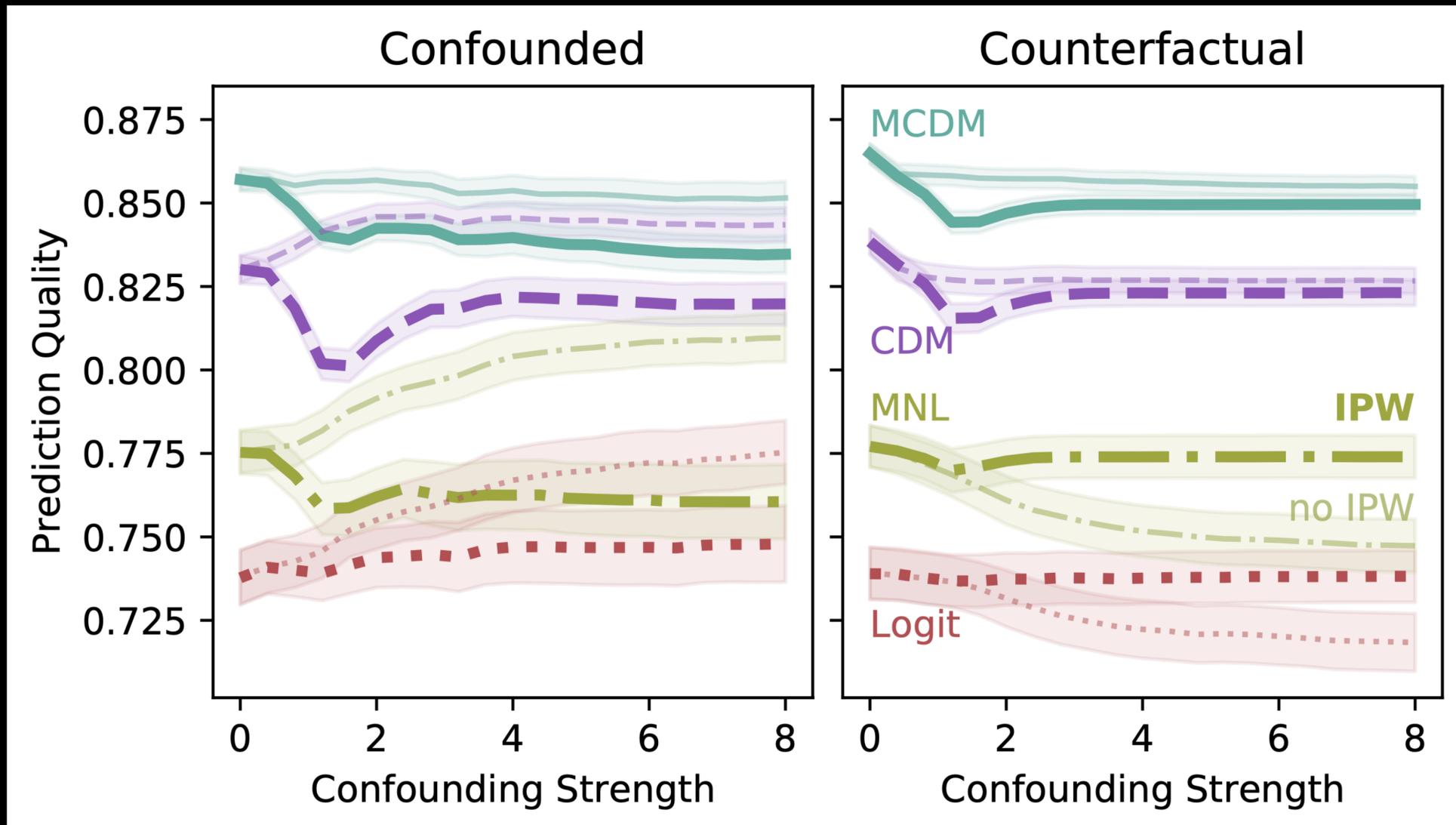
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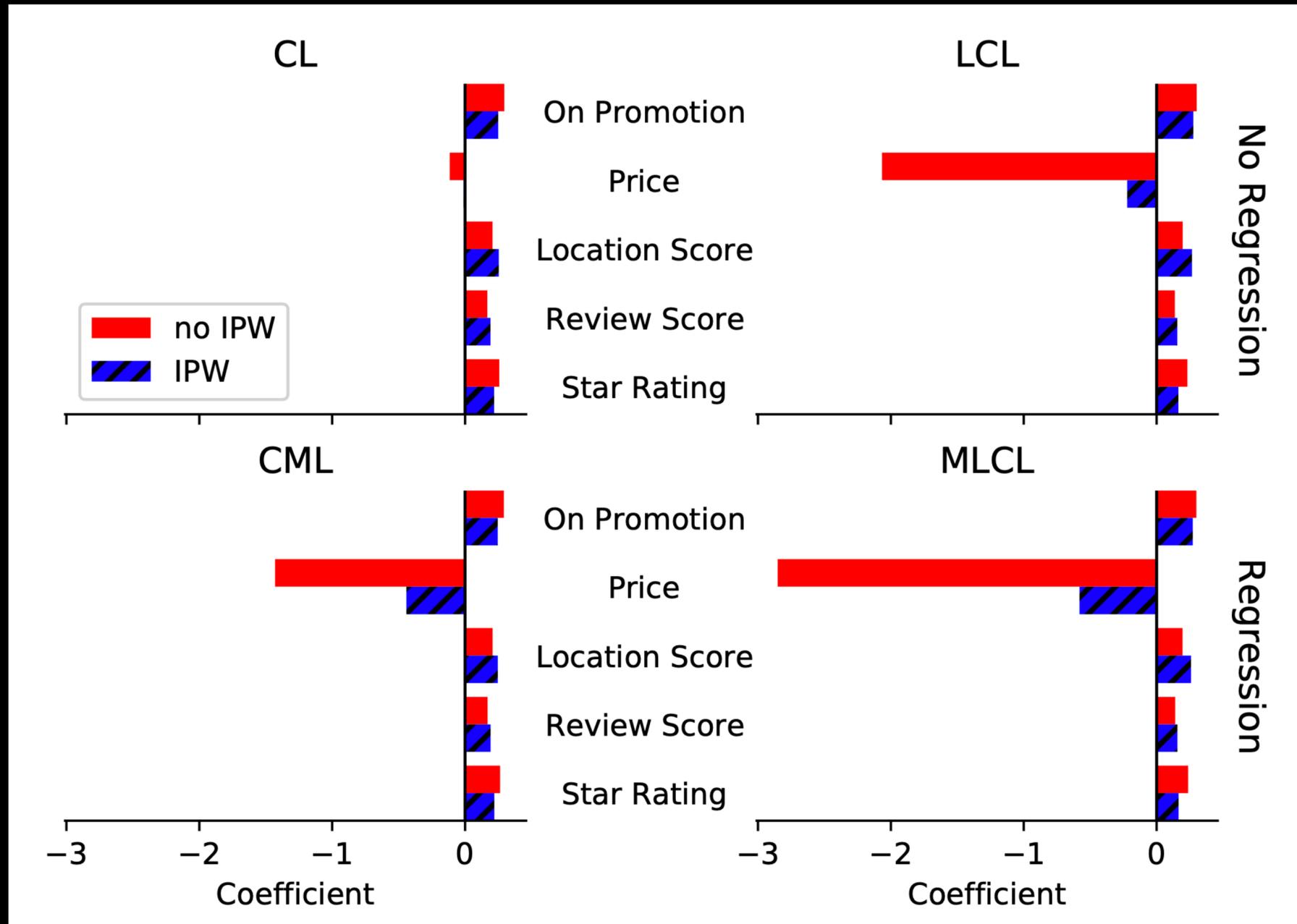


## IPW & regression

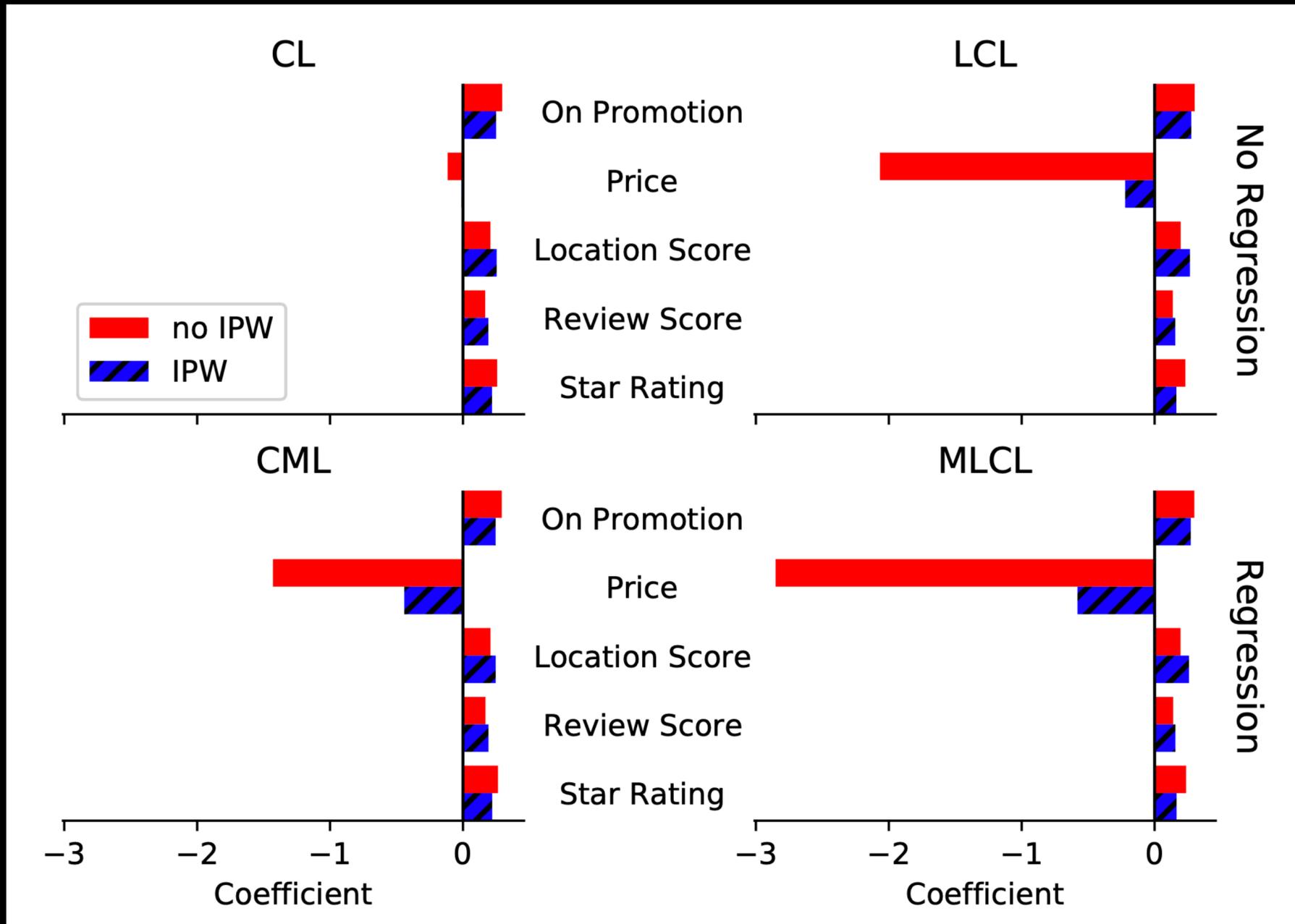
- (a) improve counterfactual prediction
- (b) prevent overconfidence on confounded data

# Expedia hotel booking data

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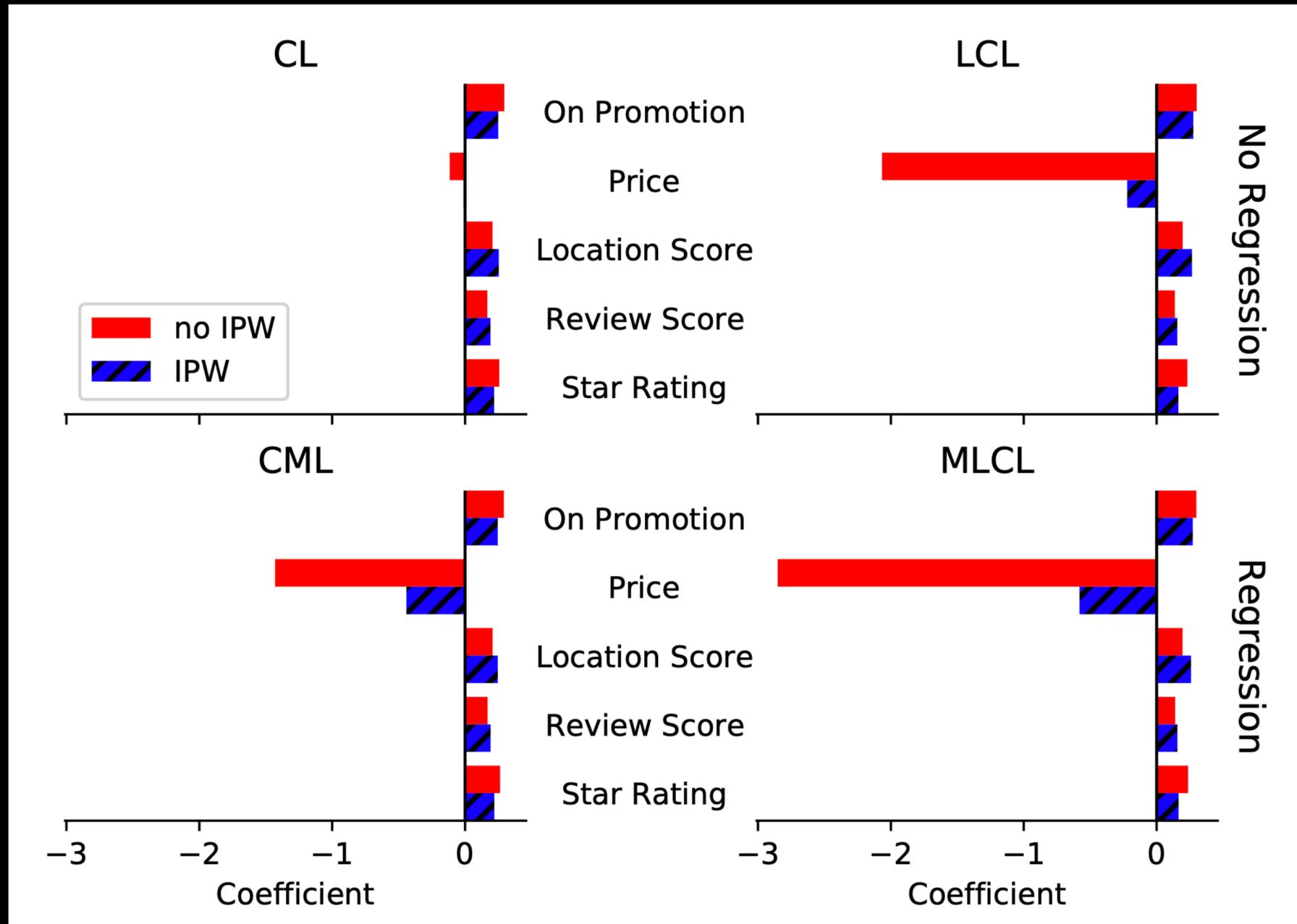


# Expedia hotel booking data



Without IPW, importance of price is exaggerated

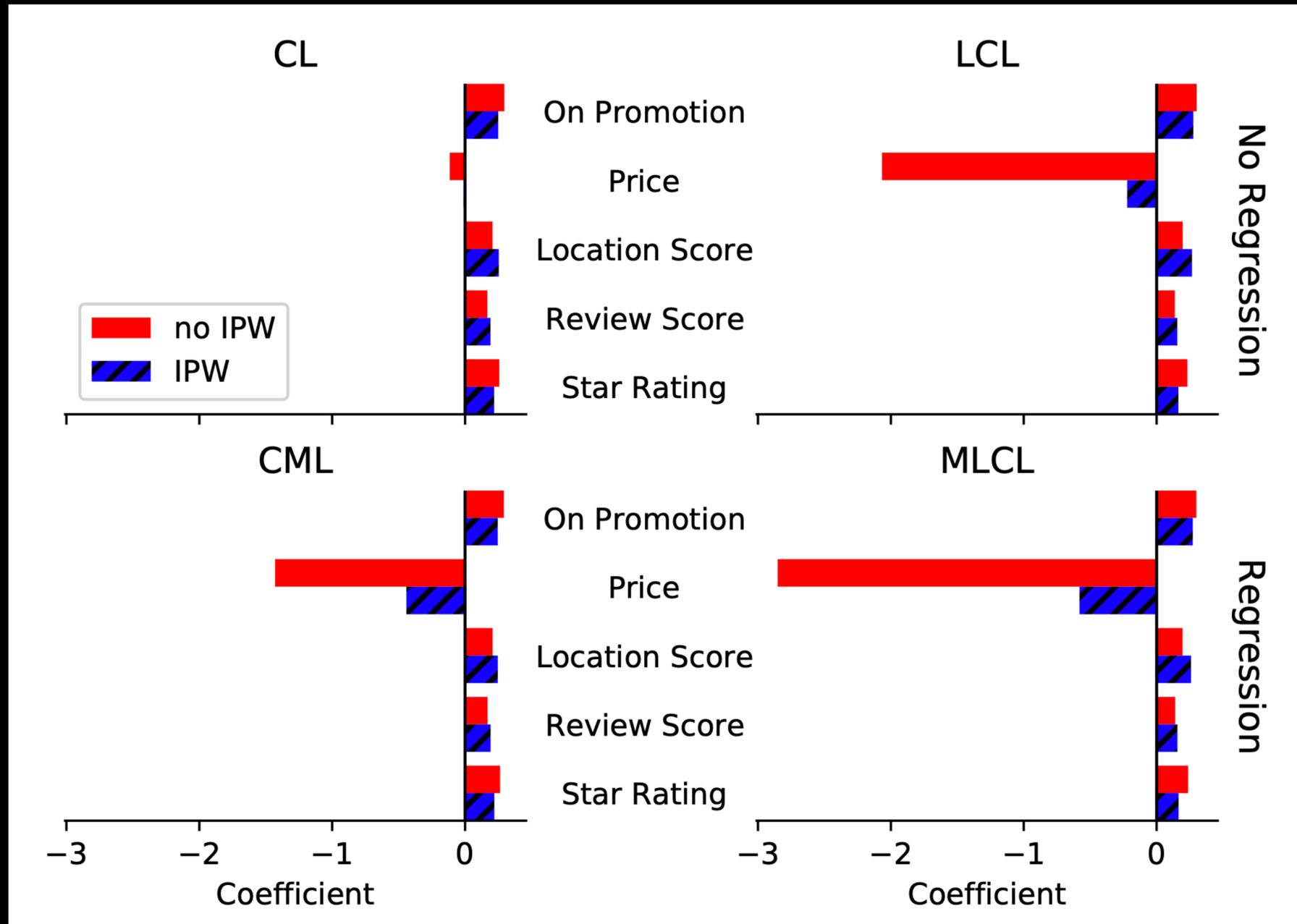
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Expedia covariates more informative about choice sets than preferences  
→ IPW > regression

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Dataset log-likelihood:

Model	Confounded	IPW-adjusted
CL	-839499	-786653
CML	-838281	-785753
LCL	-837154	-784770
MLCL	-835986	-783928

# Managing without covariates

# Clustering based on choice sets

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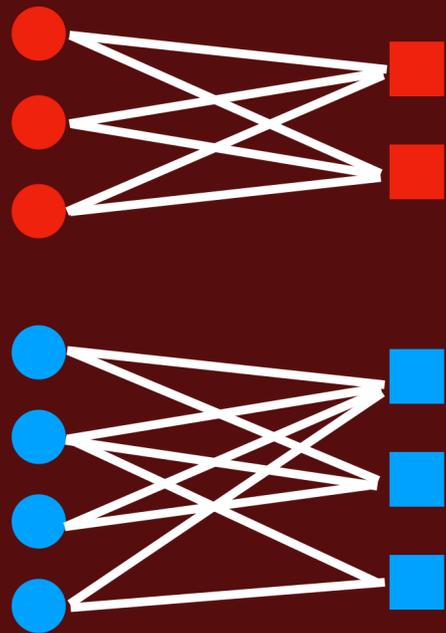
**Idea:** take advantage of the correlation between choice sets and preferences

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## Example: movie recommendations

users      movies

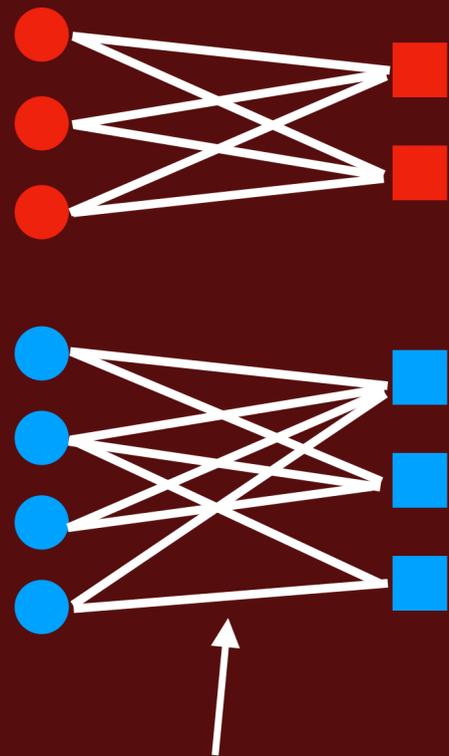


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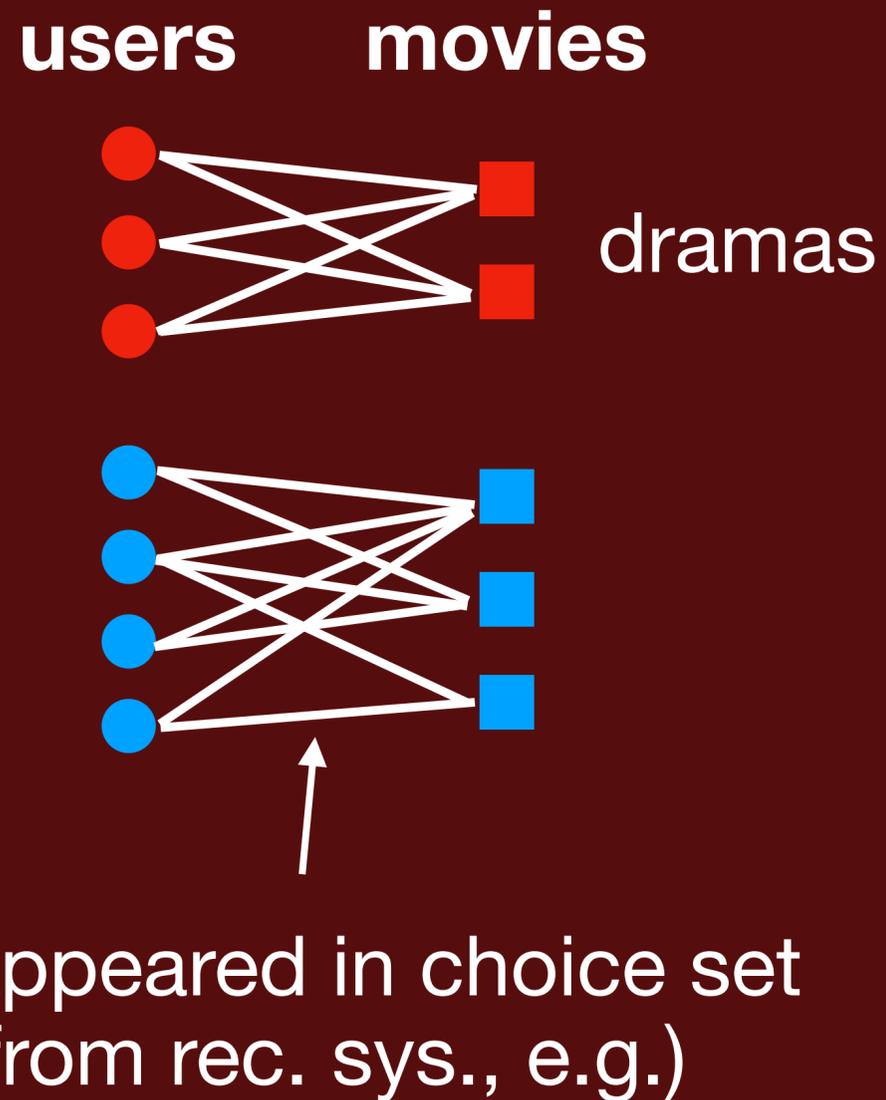


appeared in choice set  
(from rec. sys., e.g.)

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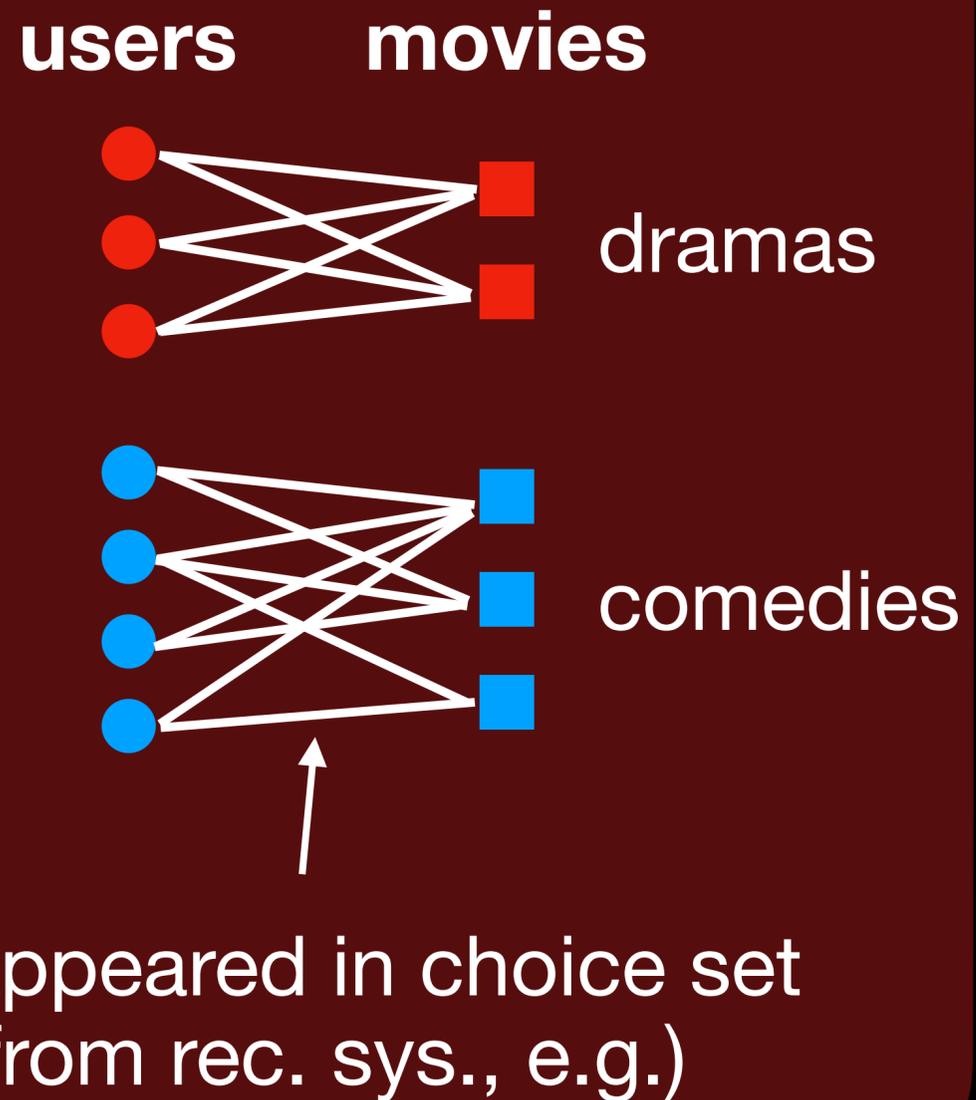
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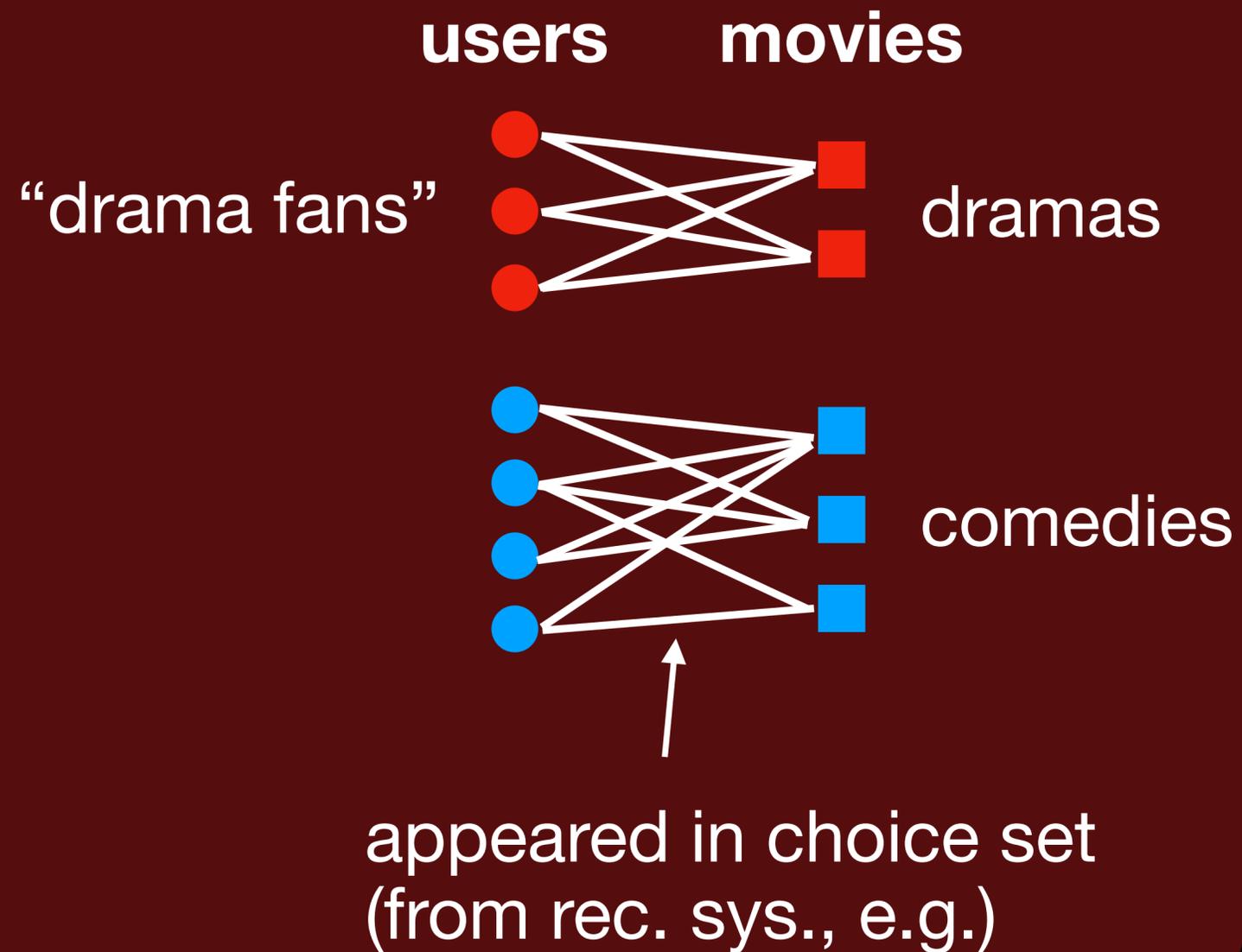
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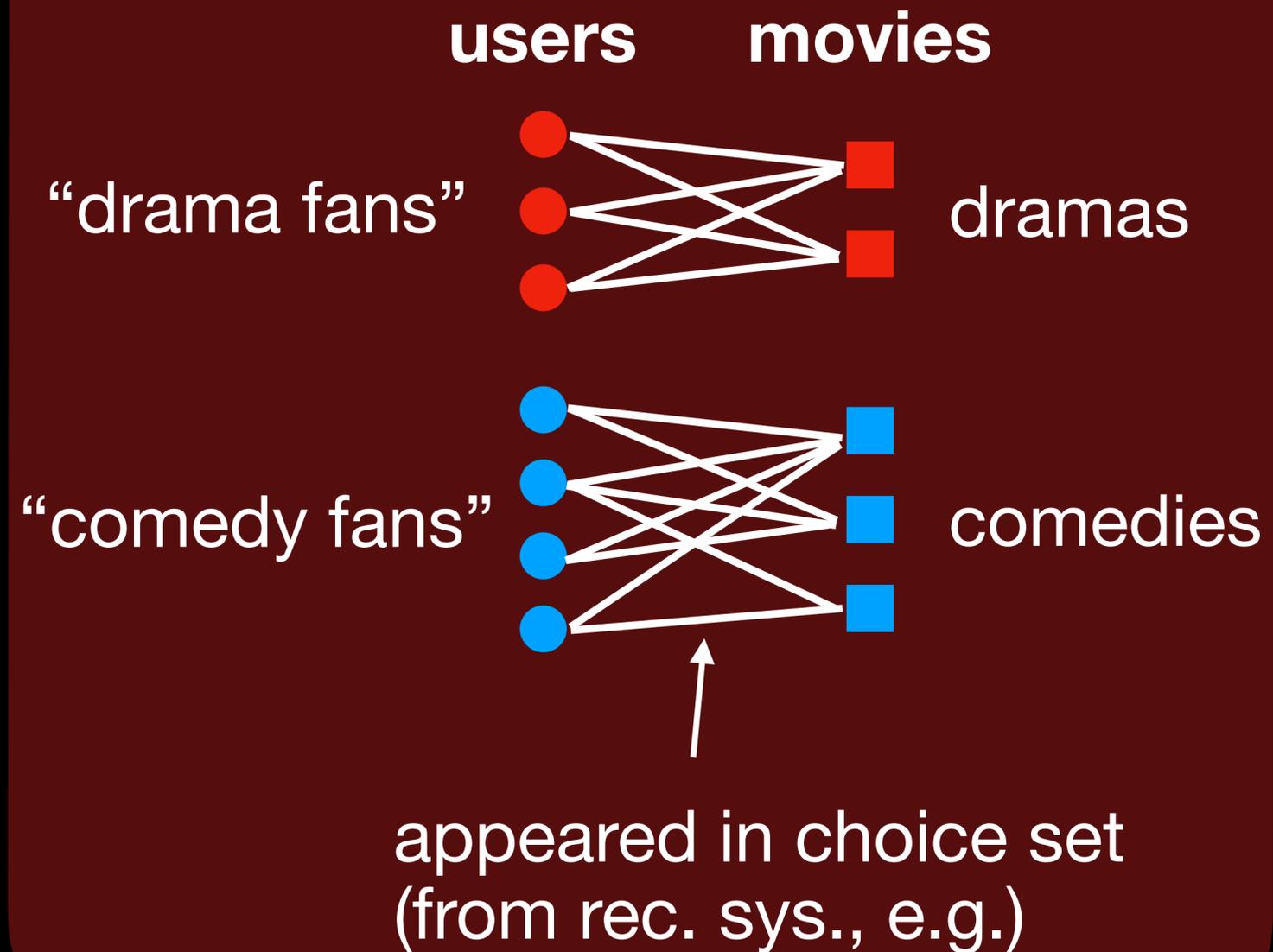
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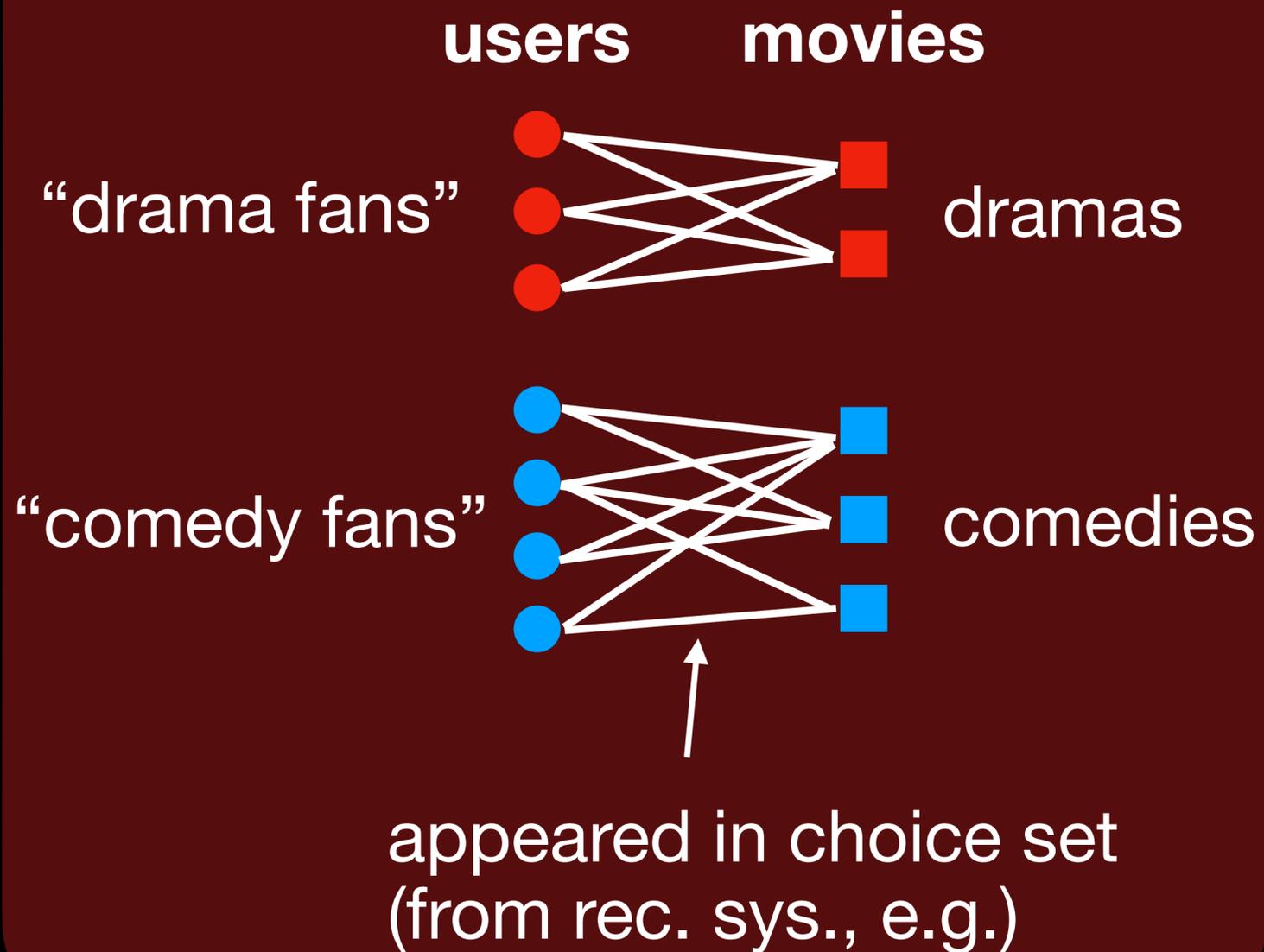
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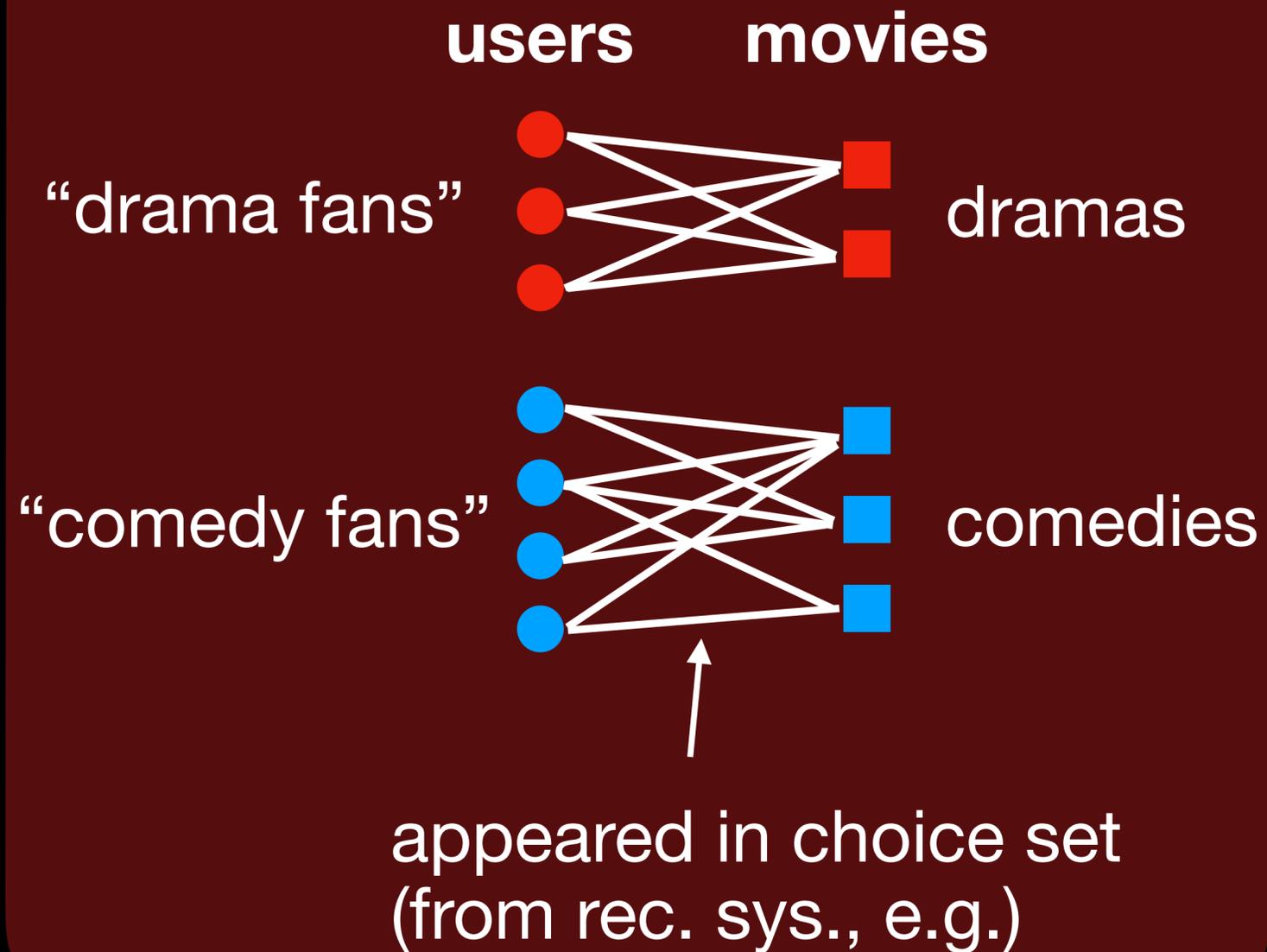


Cluster users (e.g., spectral co-clustering),  
learn choice model per-cluster (Dhillon, 2001)

# Clustering based on choice sets

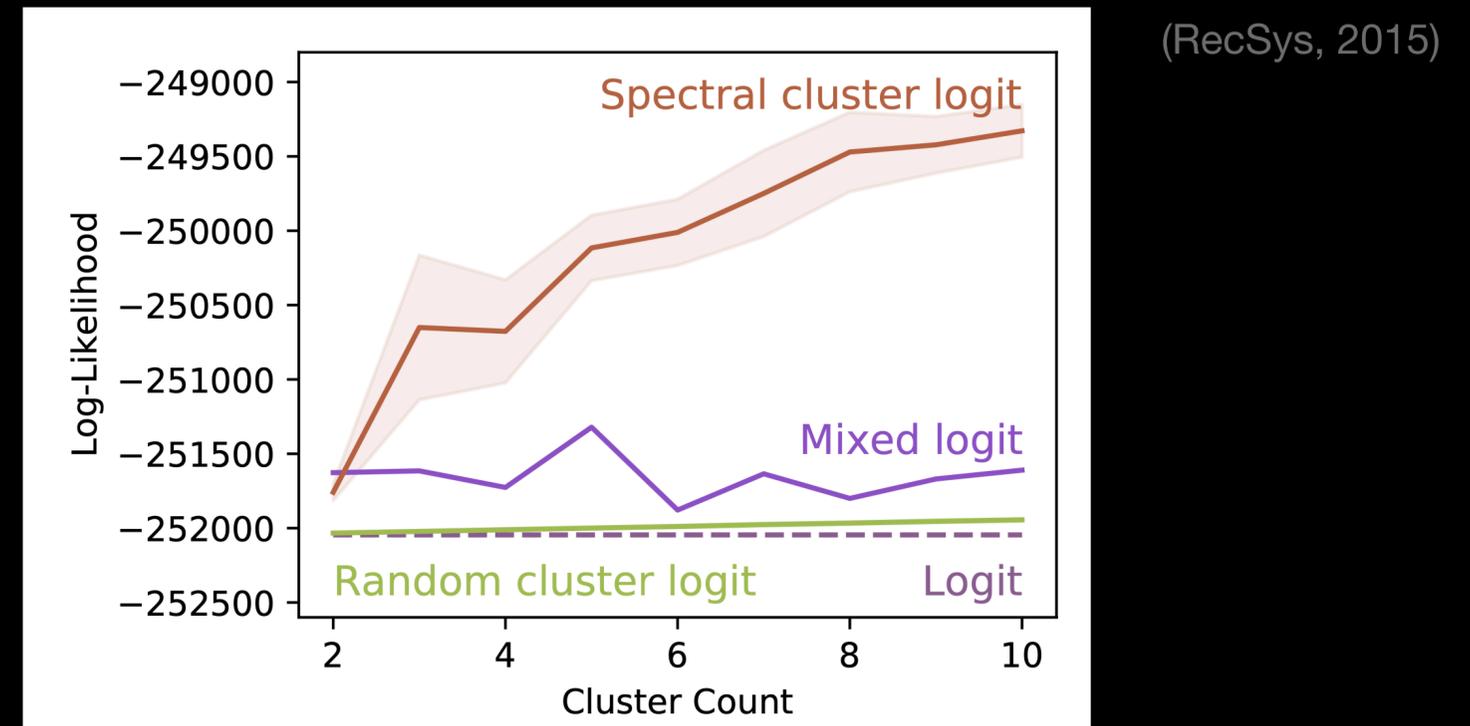
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Much better than mixed logit!  
(YOOCHOOSE online shopping data)



# More things in the paper

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## The power of choice set confounding

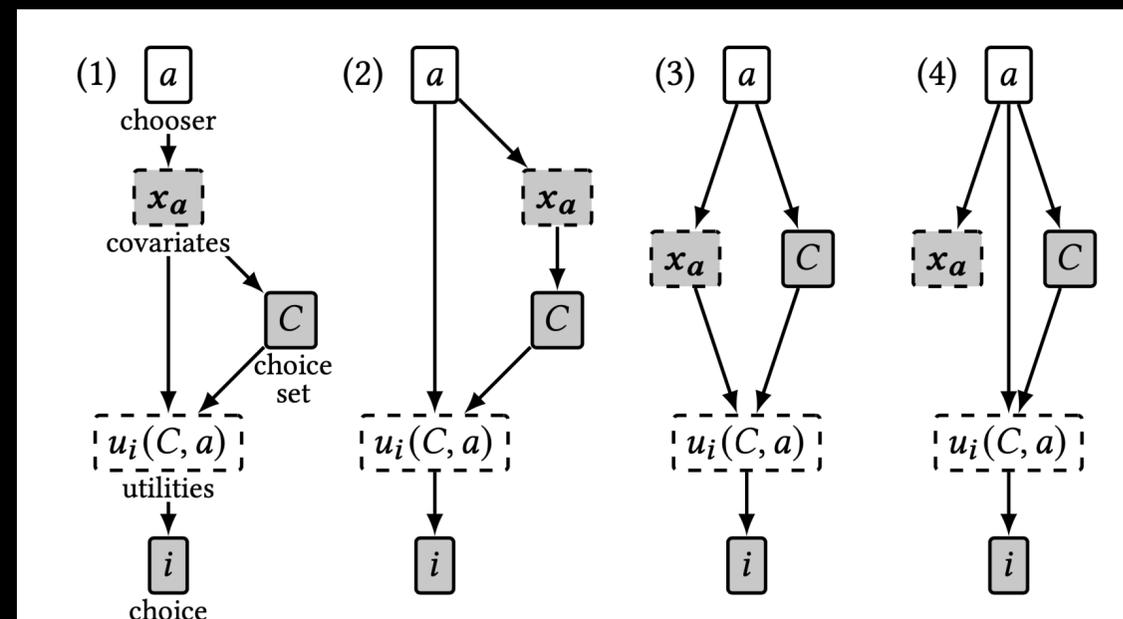
*THEOREM 2. Mixed logit with chooser-dependent choice sets is powerful enough to express any system of choice probabilities.*

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## Graphical intuition about ignorability assumptions

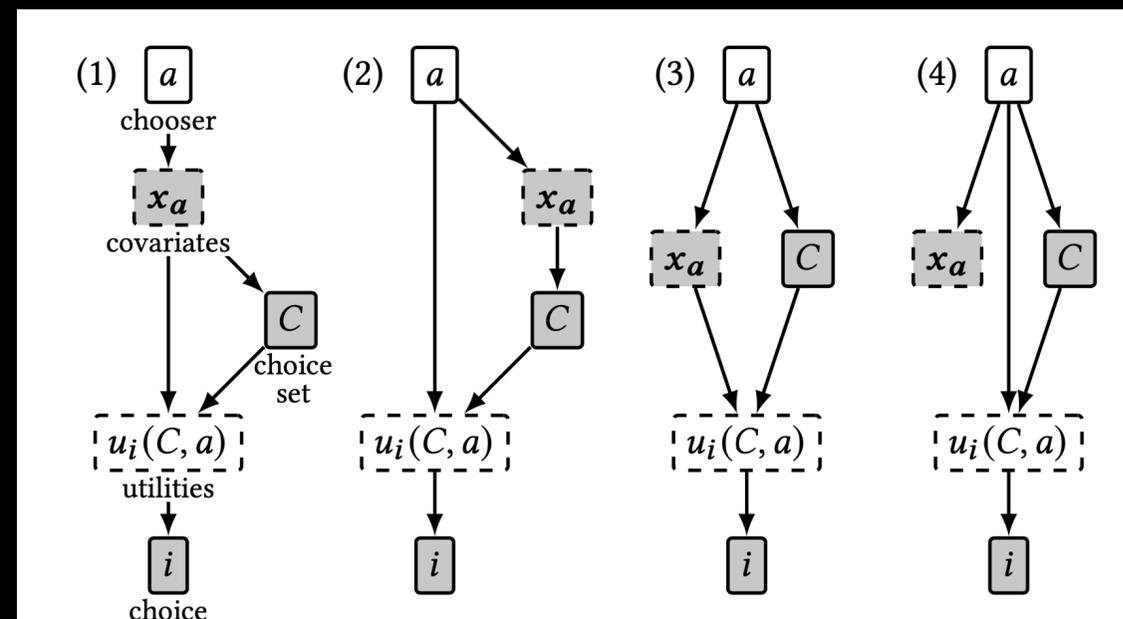


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## Graphical intuition about ignorability assumptions



Duality between context effect models and models of choice set confounding

# Concluding thoughts

Code: [bit.ly/csc-kdd-code](https://bit.ly/csc-kdd-code)  
Slides: [bit.ly/csc-kdd-slides](https://bit.ly/csc-kdd-slides)

## Key takeaways

*Choice set confounding* can mislead choice models  
We can adjust for it using chooser covariates

## Future work

Learning choice set propensities  
Other causal inference methods:  
- instrumental variables?  
- matching?

## Interested in context effect models?

See our other KDD '21 paper:  
“Learning Interpretable Feature Context Effects in Discrete Choice”

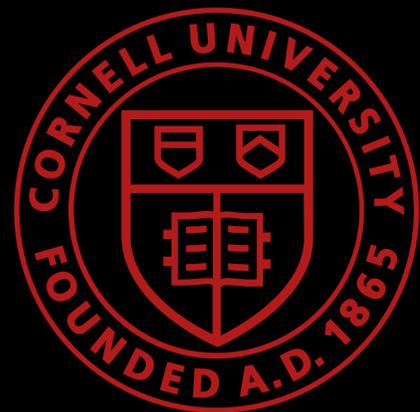
## Submit to our NeurIPS '21 workshop!

[bit.ly/WHMD2021](https://bit.ly/WHMD2021)

## Thank you!

More questions or ideas?  
Email me: [kt@cs.cornell.edu](mailto:kt@cs.cornell.edu)

 @kiran\_tomlinson



## Acknowledgments

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