

CS 4700: Foundations of Artificial Intelligence  
Spring 2018  
Homework 4  
Due: Friday, April 13, 1:25PM

1. The outputs of a sigmoidal activation function range from 0 to 1. Imagine if you need a 0/1 output for a given problem you take the final output of the neural network and return 1 if its value is  $\geq 0.5$  and 0 otherwise.

Consider using this approach to use a neuron with a sigmoidal activation function to represent an AND gate – where inputs are two variables  $x_1$  and  $x_2$ , each either 0 (false) or 1 (true), and returns 0 or 1 using the threshold of 0.5 described above, so that the output equals what you would get for  $x_1 \wedge x_2$ . Give a set of weights for this neuron that would correctly implement this AND gate.

2. Imagine you use  $g(z) = z$  as the activation function in your neural network. Consider a network where there are  $d$  inputs  $x_1, \dots, x_d$ , (each represented by level-one neurons  $a_1, \dots, a_d$  as described in class), two hidden units  $d+1$  and  $d+2$  receiving inputs from  $a_1, \dots, a_d$ , and one output unit  $d+3$  that receives as its inputs the activation from neurons  $d+1$  and  $d+2$ . Show how this neural network can be represented by a single neuron using the same activation function. Your answer should give the weights of the new neuron as a function of the weights of the original network.
3. Imagine you use  $g(z) = z^3$  as the activation function in your neural network. Consider the back-propagation algorithm found in Figure 18.24 of the textbook. What do the update rules for  $\Delta[j]$  and  $\Delta[i]$  in the lower third of the algorithm become for this activation function?
4. The function of a single perceptron does not change if you double all the weights. What happens to a single neuron using the sigmoidal activation function if you double all the weights? (This question is about the function that the neuron computes, not about the update rule.)