## HW for 2019-06-05

(due: 2019-06-12)

1: How many factors? The (economy) pivoted QR factorization is used for factor selection least squares; we compute

$$A\Pi = QR$$

and then only fit based on the first k columns of  $\Pi$ . Given Q and b, write a code to compute the mean LOOCV statistic

$$LOOCV = \frac{1}{m} \sum_{i=1}^{m} r_{(-i)}^2$$

for k = 1, ..., n. Ideally, your code should take O(mn) time.

*Note:* You really do only need Q and b!

2: Maximum likelihood for least squares Consider the statistical model

$$y = Ax + e$$

where  $e \sim \mathcal{N}(0, \sigma^2 I)$ . Derive the maximum likelihood estimates for x and  $\sigma^2$  given observed data y.