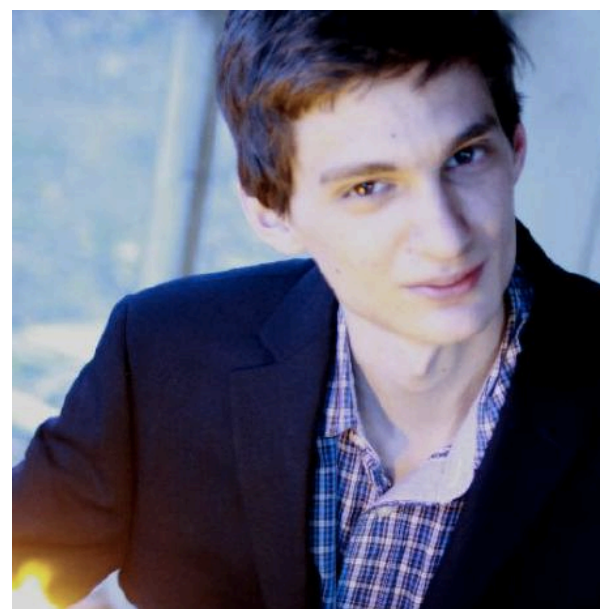


Clockwork Finance: Automated Analysis of Economic Security in Smart Contracts

To Appear in IEEE S&P'23



**Kushal
Babel**



Philip
Daian



Mahimna
Kelkar



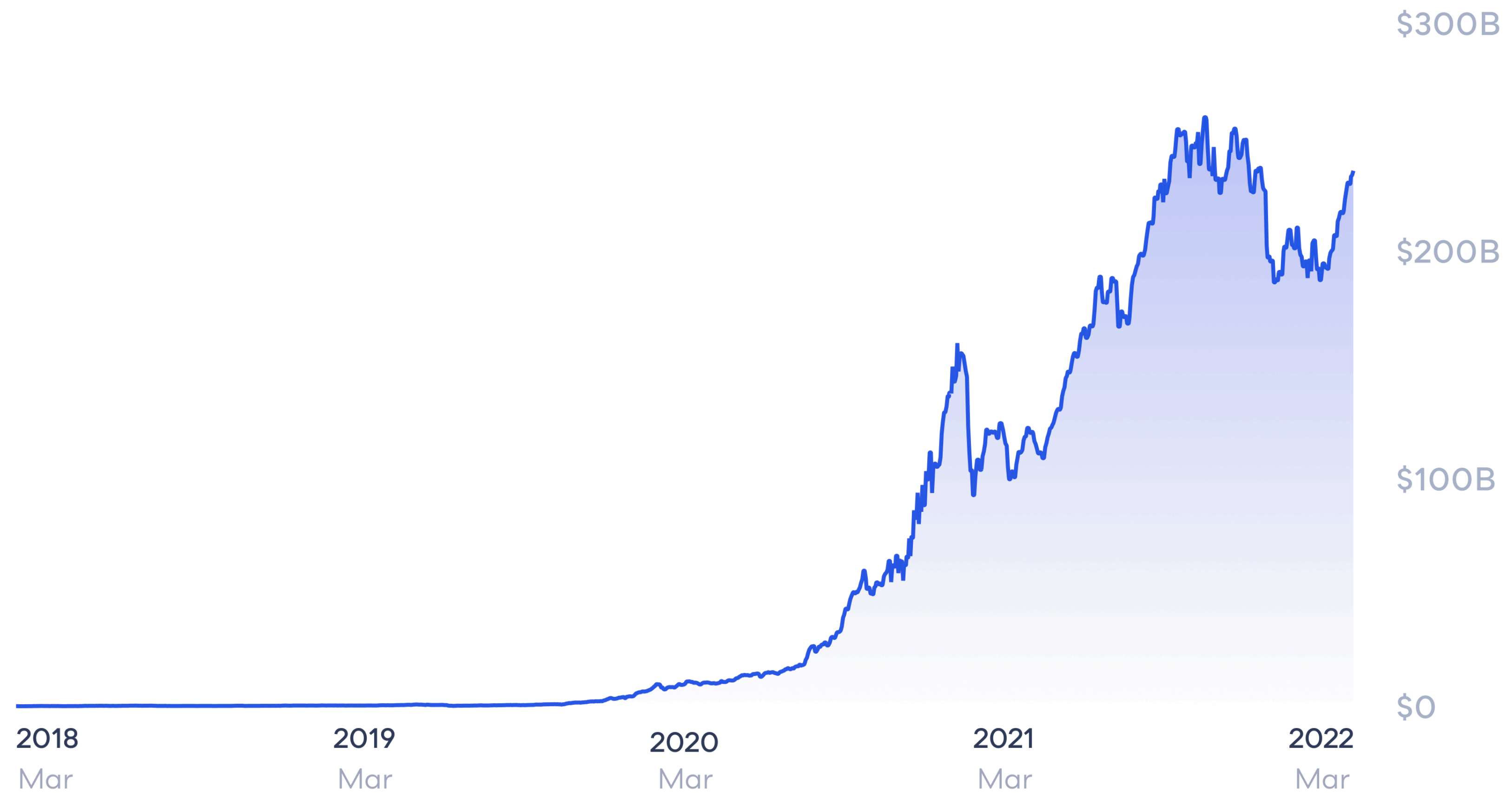
Ari
Juels

(First three authors contributed equally)

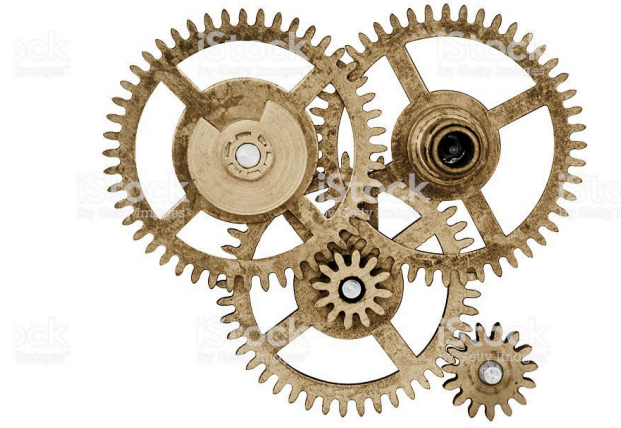
DeFi

DeFi total TVL

revix

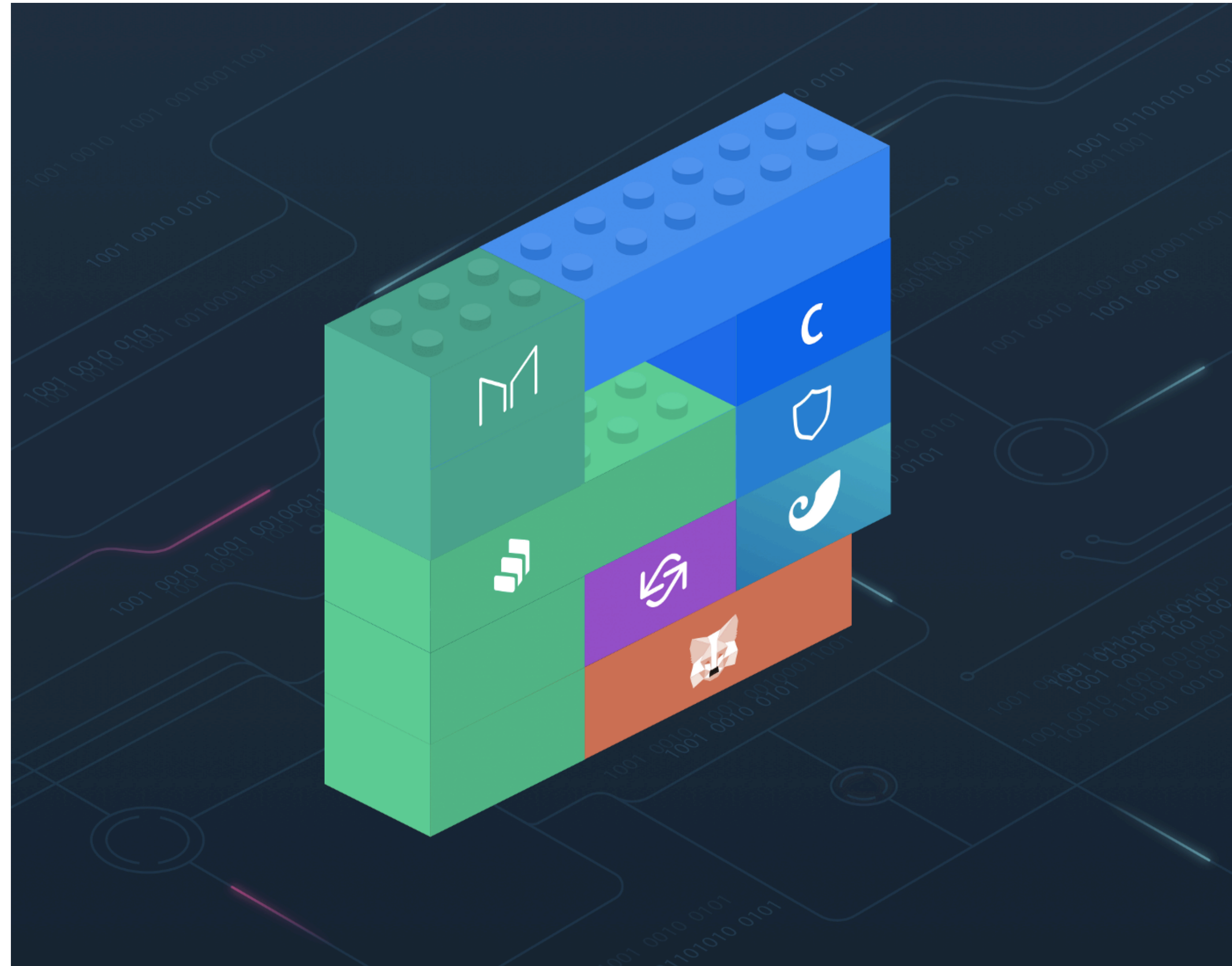


Smart Contracts, Like Clockwork!



- Smart contracts execute in sequential and atomic transactions
- Execution is deterministic
- Most blockchains have transparent execution
- Therefore: Easy interoperability among smart contracts and novel financial instruments

Money Legos

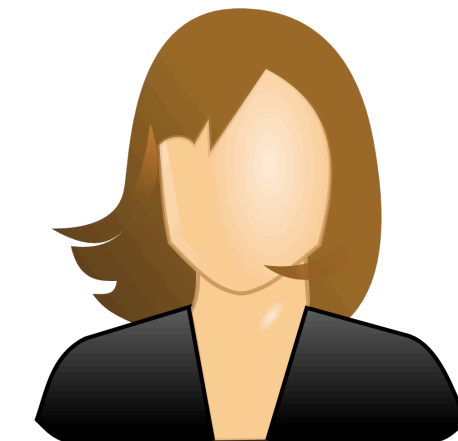


Source: <https://medium.com/totle/building-with-money-legos-ab63a58ae764>

Unintended Behaviour



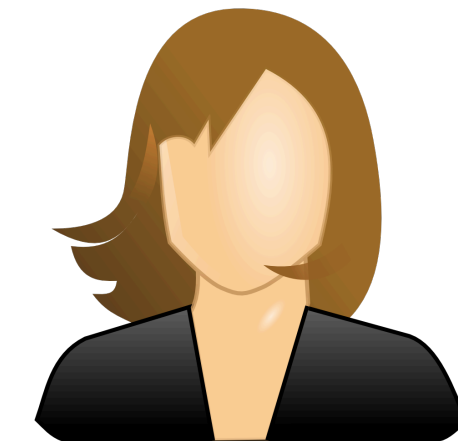
Swap 1,000 **USD** into **ETH**



Unintended Behaviour



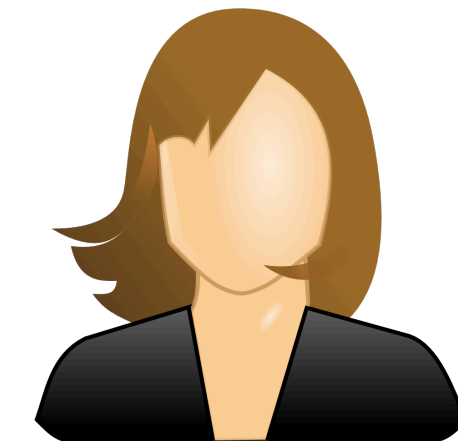
Swap 1,000 **USD** into **ETH**




Unintended Behaviour



Swap 1,000 USD into ETH



ETH Price 

Unintended Behaviour



ETH Price



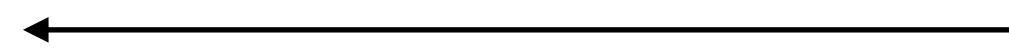
Swap X **USD** into **ETH**



Swap 1,000 **USD** into **ETH**



Swap Y **ETH** into **USD**



Sandwich



Unintended Behaviour



ETH Price



Sandwich

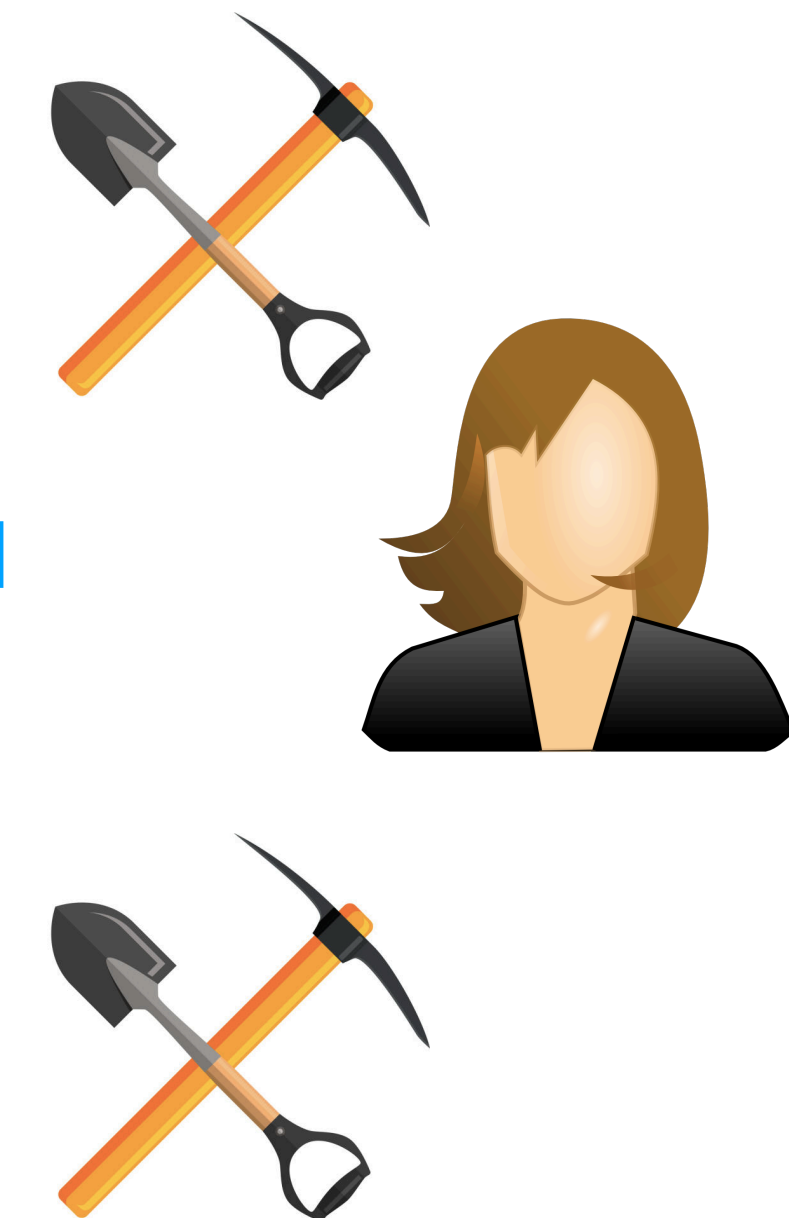
Swap X USD into ETH



Swap 1,000 USD into ETH

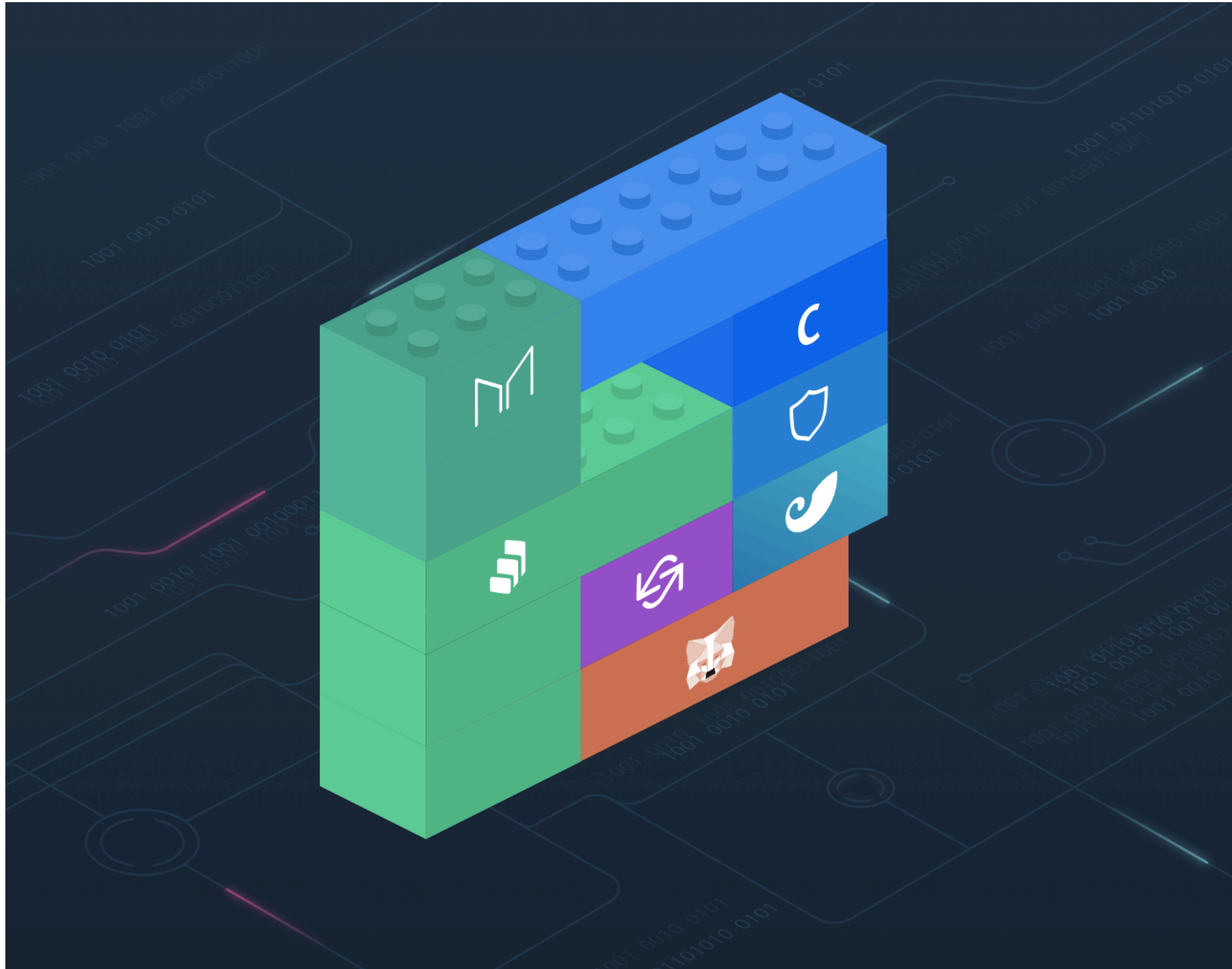


Swap Y ETH into USD



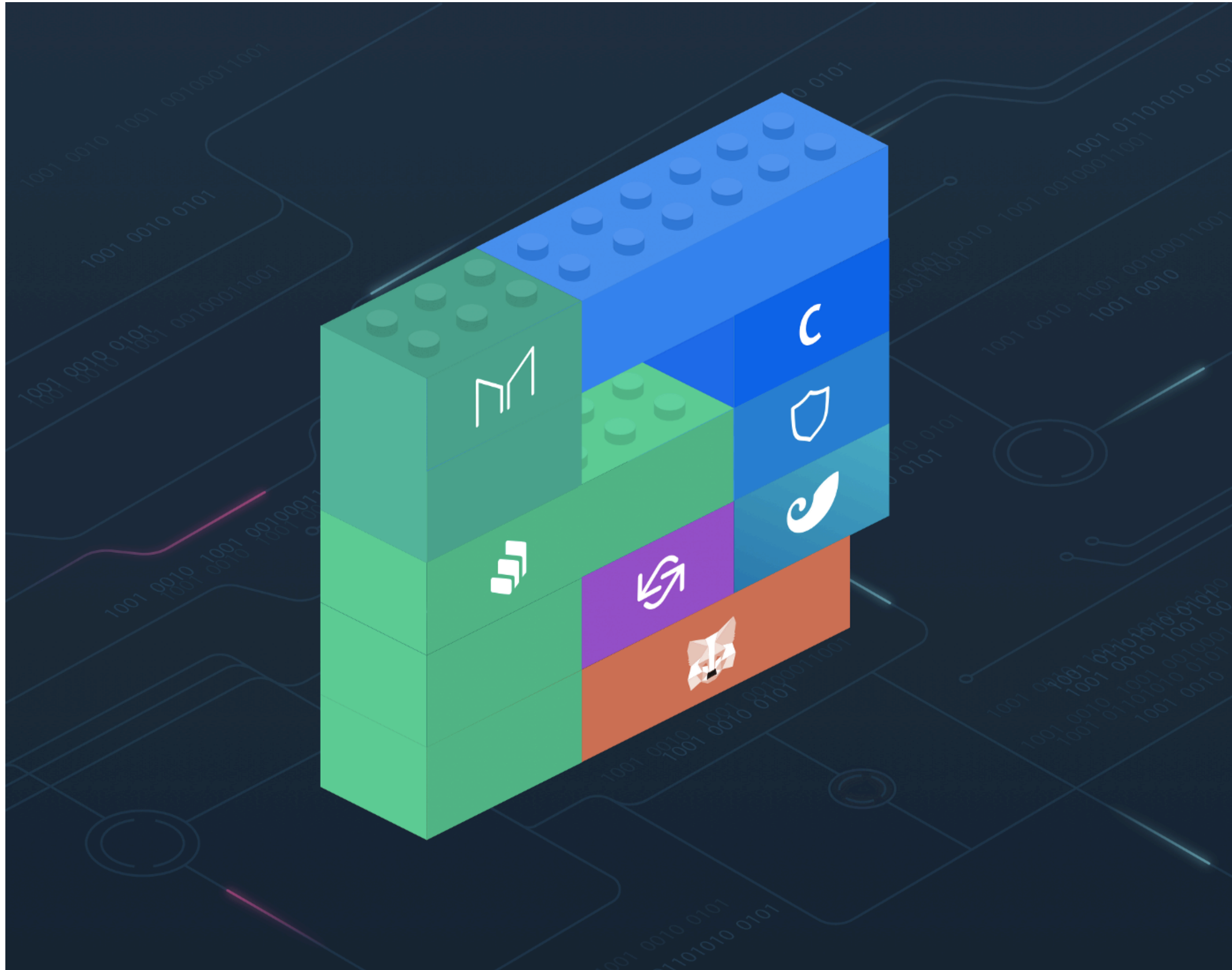
MEV = Miner Extractable Value (or Maximal Extractable Value) - Ability to extract value by reordering, inserting or censoring transactions

Contract Composition



Source: <https://medium.com/totle/building-with-money-legos-ab63a58ae764>

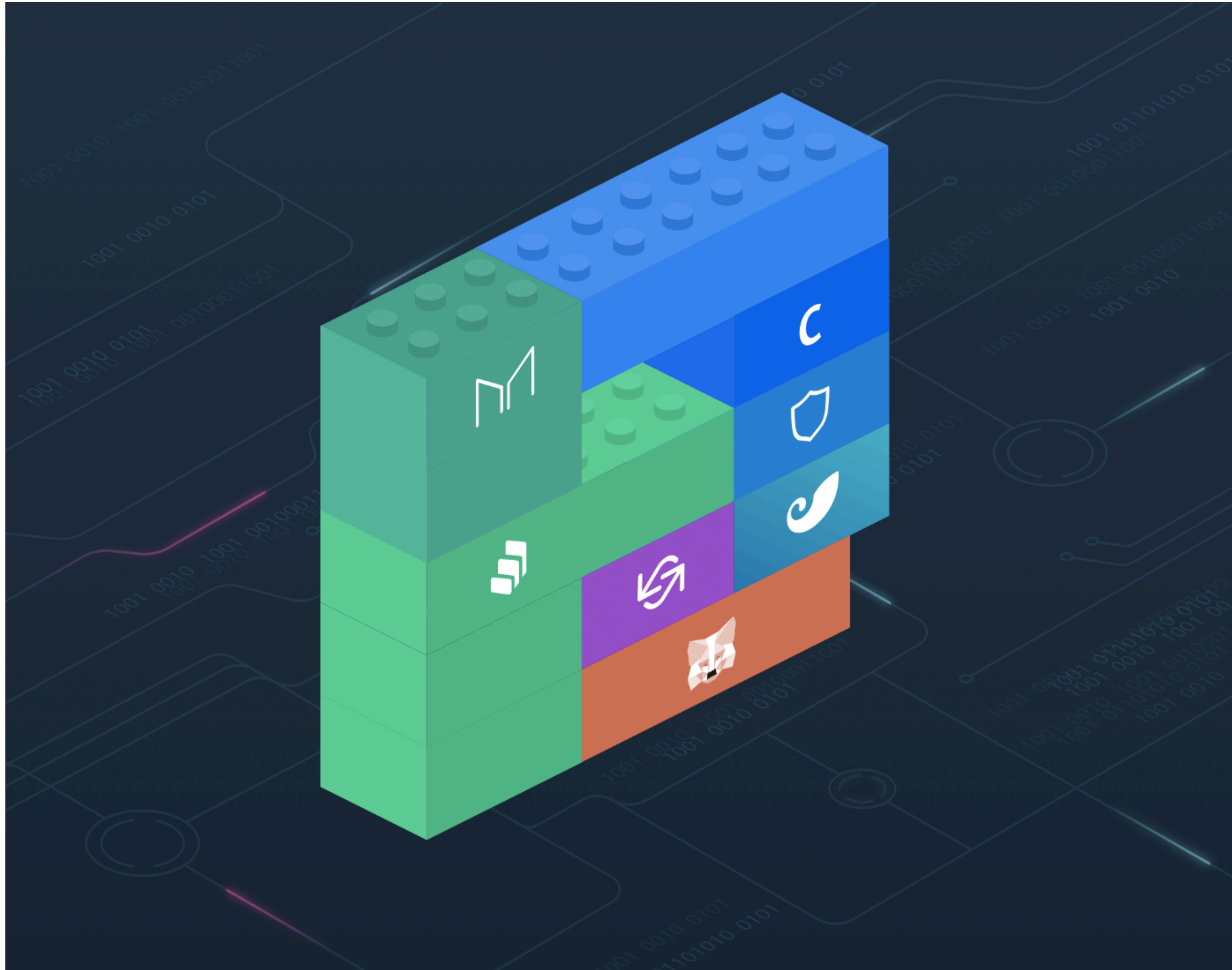
Contract Composition



- Flashloans + DEX

Source: <https://medium.com/totle/building-with-money-legos-ab63a58ae764>

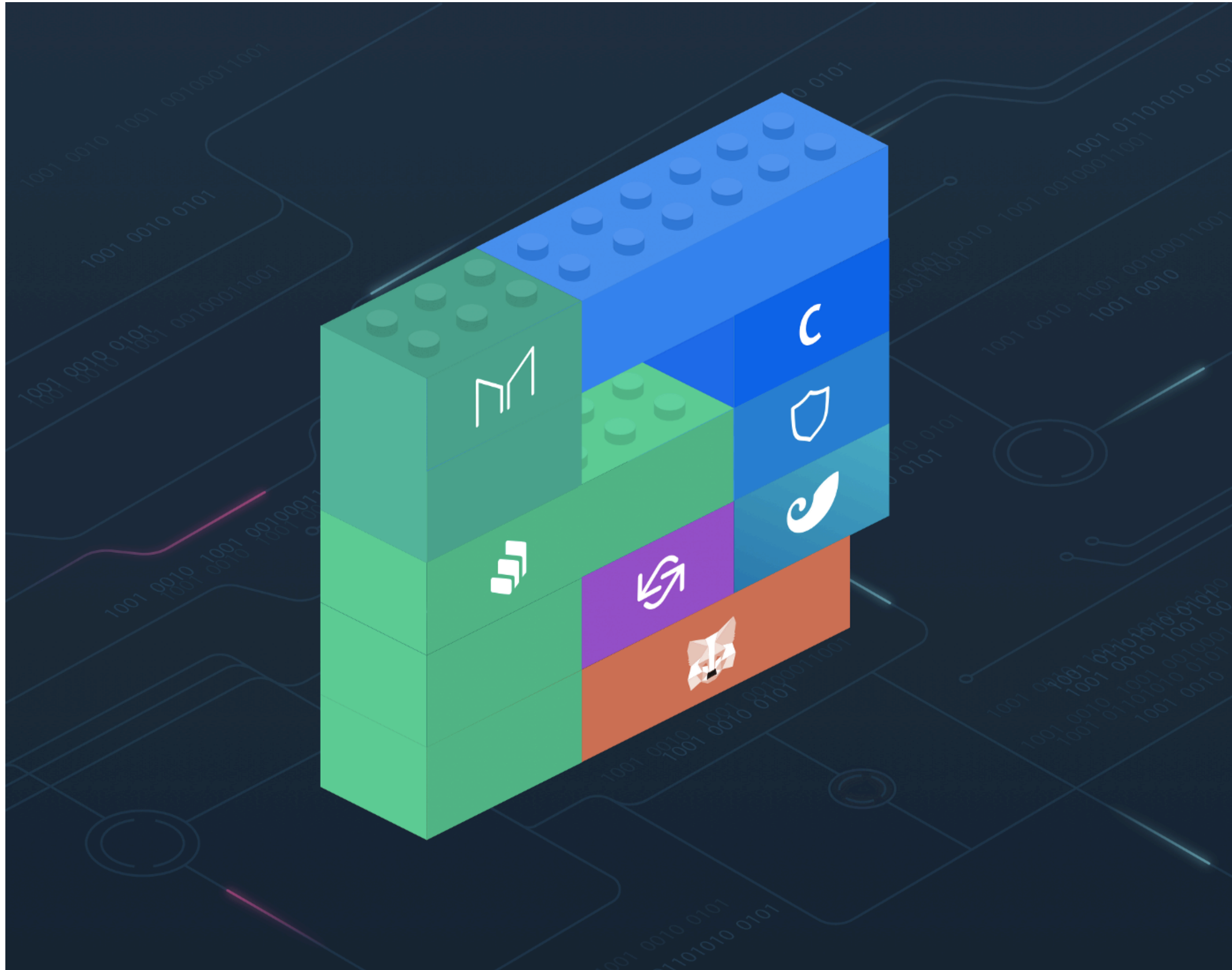
Contract Composition



- Flashloans + DEX
- Lending contracts using DEX to price the debt

Source: <https://medium.com/totle/building-with-money-legos-ab63a58ae764>

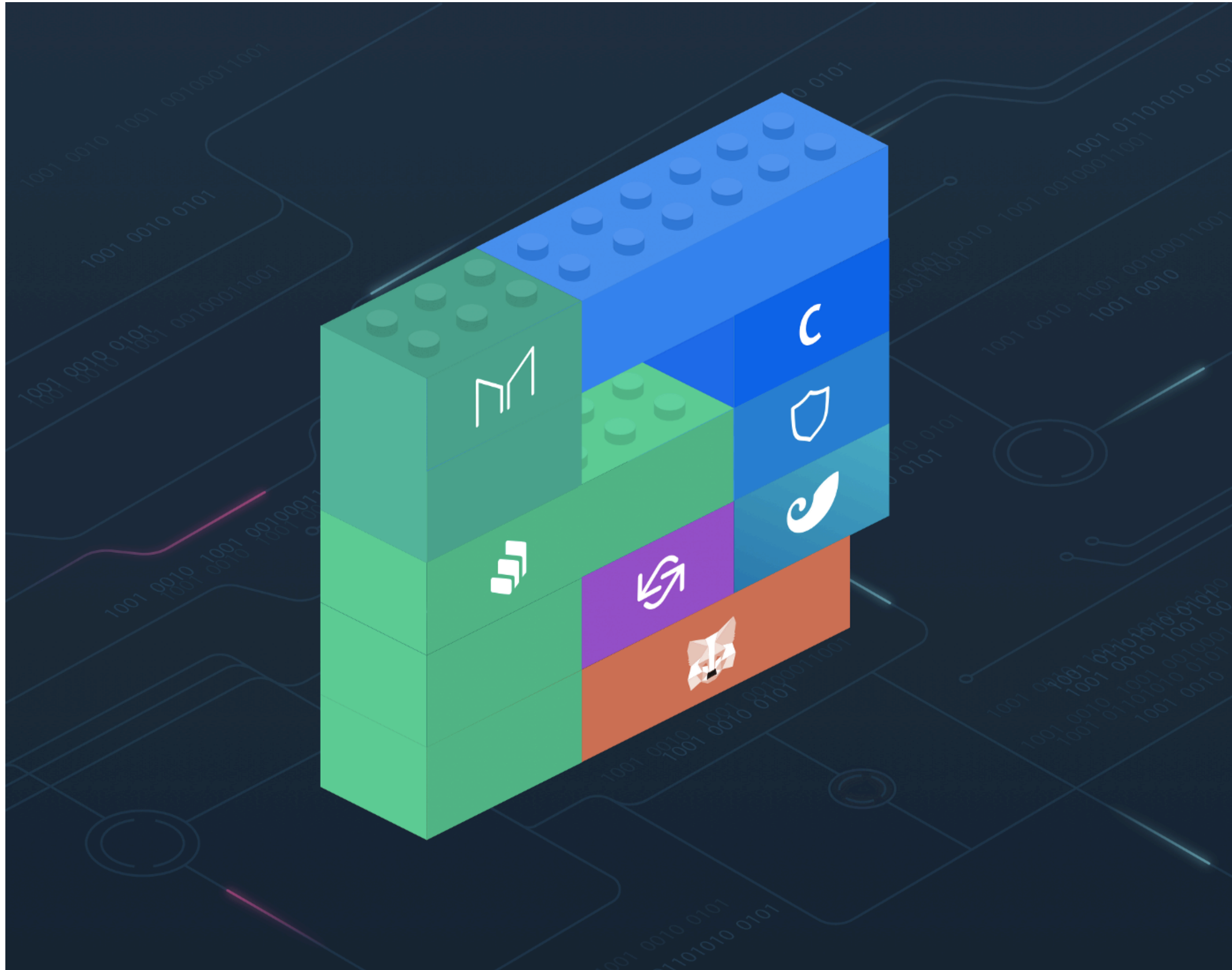
Contract Composition



- Flashloans + DEX
- Lending contracts using DEX to price the debt
- Flashloans + Governance Contract

Source: <https://medium.com/totle/building-with-money-legos-ab63a58ae764>

Contract Composition



Source: <https://medium.com/totle/building-with-money-legos-ab63a58ae764>

- Flashloans + DEX
- Lending contracts using DEX to price the debt
- Flashloans + Governance Contract
- DEX + DEX + DEX ...

Unintended Behaviour

09 May 2022 00:53 GMT-7 · 2 min read



Tech

Solana DeFi Protocol Nirvana Drained of Liquidity After Flash Loan Exploit

The price of the protocol's ANA token fell almost 80% following the attack.

By Shaurya Malwa  Jul 28, 2022 at 4:41 a.m. PDT Updated Jul 28, 2022 at 8:06 a.m. PDT

DeFi Lending Protocol Fortress Loses All Funds in Oracle Price Manipulation Attack



JESSE COGLAN

JUN 17, 2022

Inverse Finance exploited again for \$1.2M in flash loan oracle attack

No user funds have been affected by the exploit, but Inverse Finance has incurred debt and offered the attacker a bounty to

BAYC ApeCoin Suffers \$800k Flash Loan "Attack" During Airdrop

Posted on Mar 30, 2022 | [BLOG](#)



MEV...An Industry

\$674,300,932
Total Extracted MEV

\$6,930,451
Last 30 days Extracted MEV

\$113k
Last 24h Extracted MEV

Cumulative Extracted MEV - Gross Profit



Existing Techniques for Security

- Human Auditing
- Fuzz Testing
- Static Analysis (eg. Slither)
- Formal Verification of functional correctness

Focus on Bug Hunting, Functional Correctness and Secret Leaks

This Work - Clockwork Finance

Directly reason about **economic properties** of smart contracts (and their interactions) by leveraging existing formal verification techniques

Unlike Traditional Finance, Smart Contracts execution is **deterministic, sequential, transparent** and **atomic** — allowing for formal verification of the behaviour of DeFi applications

Benefits to the ecosystem

Developers - **Prove** bounds on the value exposed by their contracts and interaction of their contracts with other contracts

Users - Find bounds on the value extractable from their transactions

Consensus Researchers - Rigorously study the impact of MEV on consensus

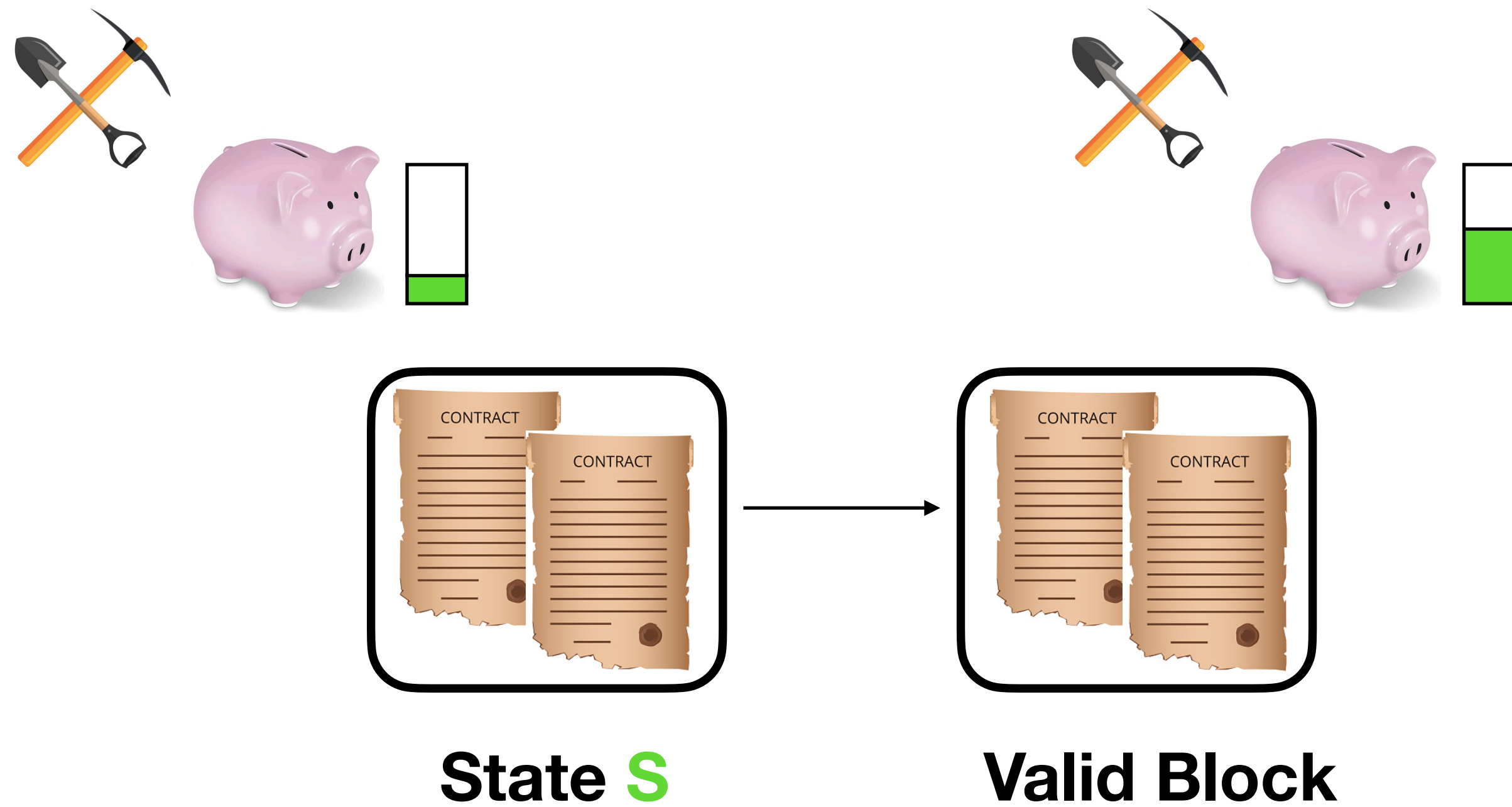
Outline

- Definitional tools
 - Defining (M)EV
 - Defining Secure Composition
- Practical Instantiation into Clockwork Finance Framework (CFF)
 - Design
 - Use for proofs
 - Use for finding attacks

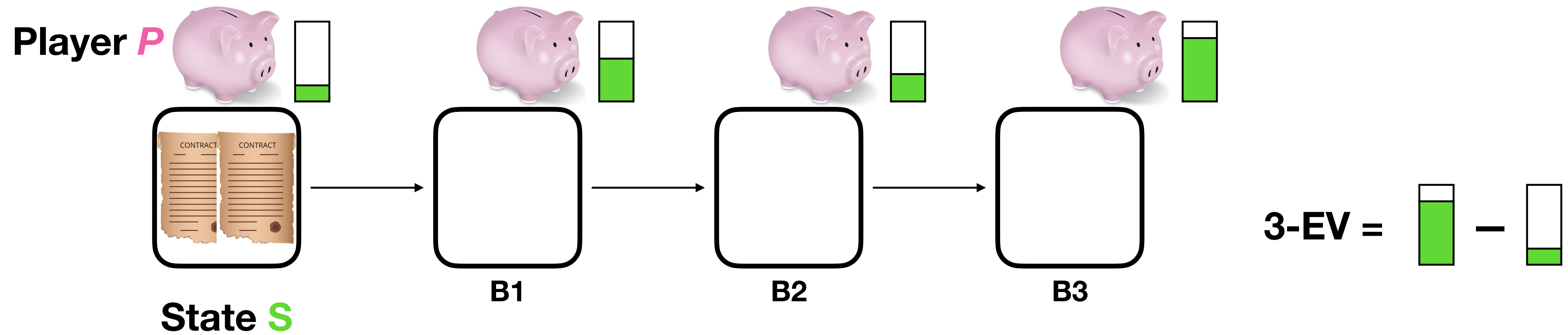
Outline

- Definitional tools
 - Defining (M)EV
 - Defining Secure Composition
- Practical Instantiation into Clockwork Finance Framework (CFF)
 - Design
 - Use for proofs
 - Use for finding attacks

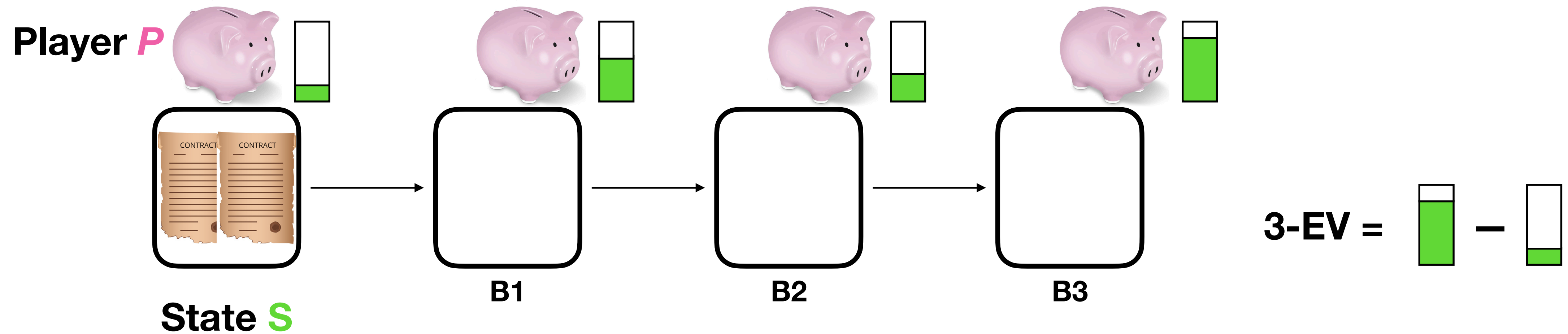
Miner Extractable Value (MEV)



Extractable Value (EV)

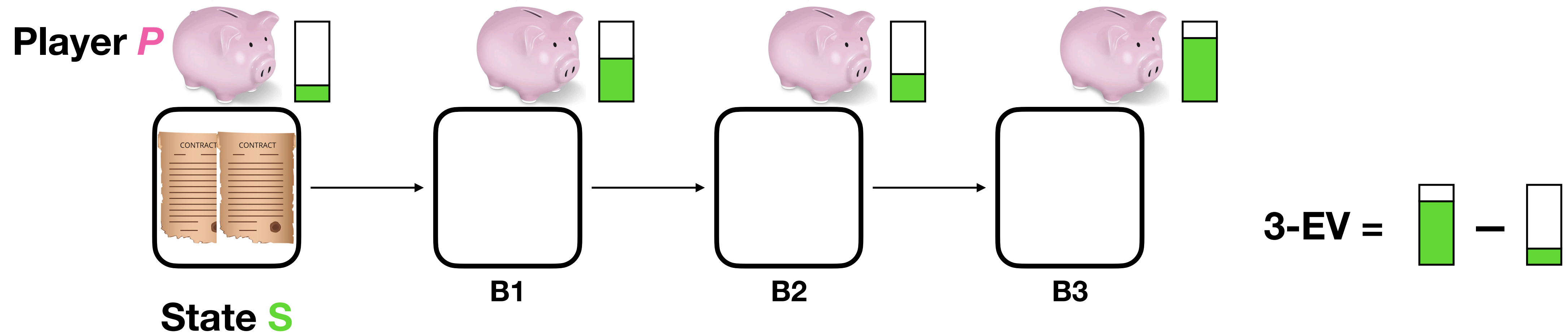


Extractable Value (EV)

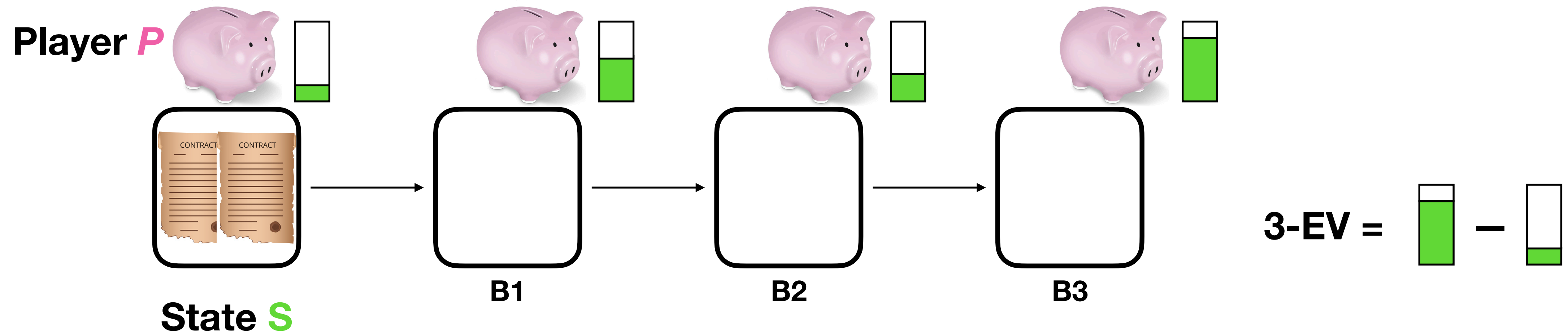


$$EV(P, \mathcal{B}, s) = \max_{(B_1, \dots, B_k) \in \mathcal{B}} \left\{ \sum_{a \in A_P} \text{balance}_k(a)[0] - \text{balance}_0(a)[0] \right\}$$

Extractable Value (EV)



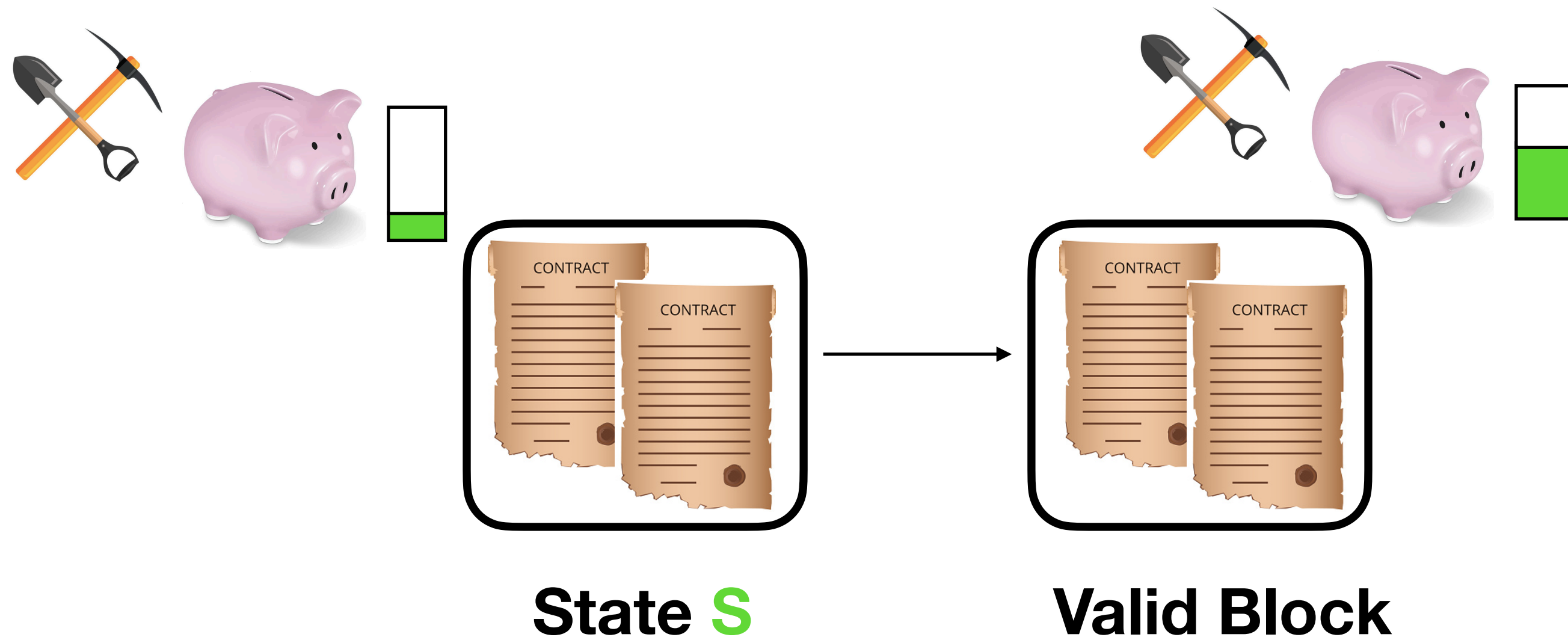
Extractable Value (EV)



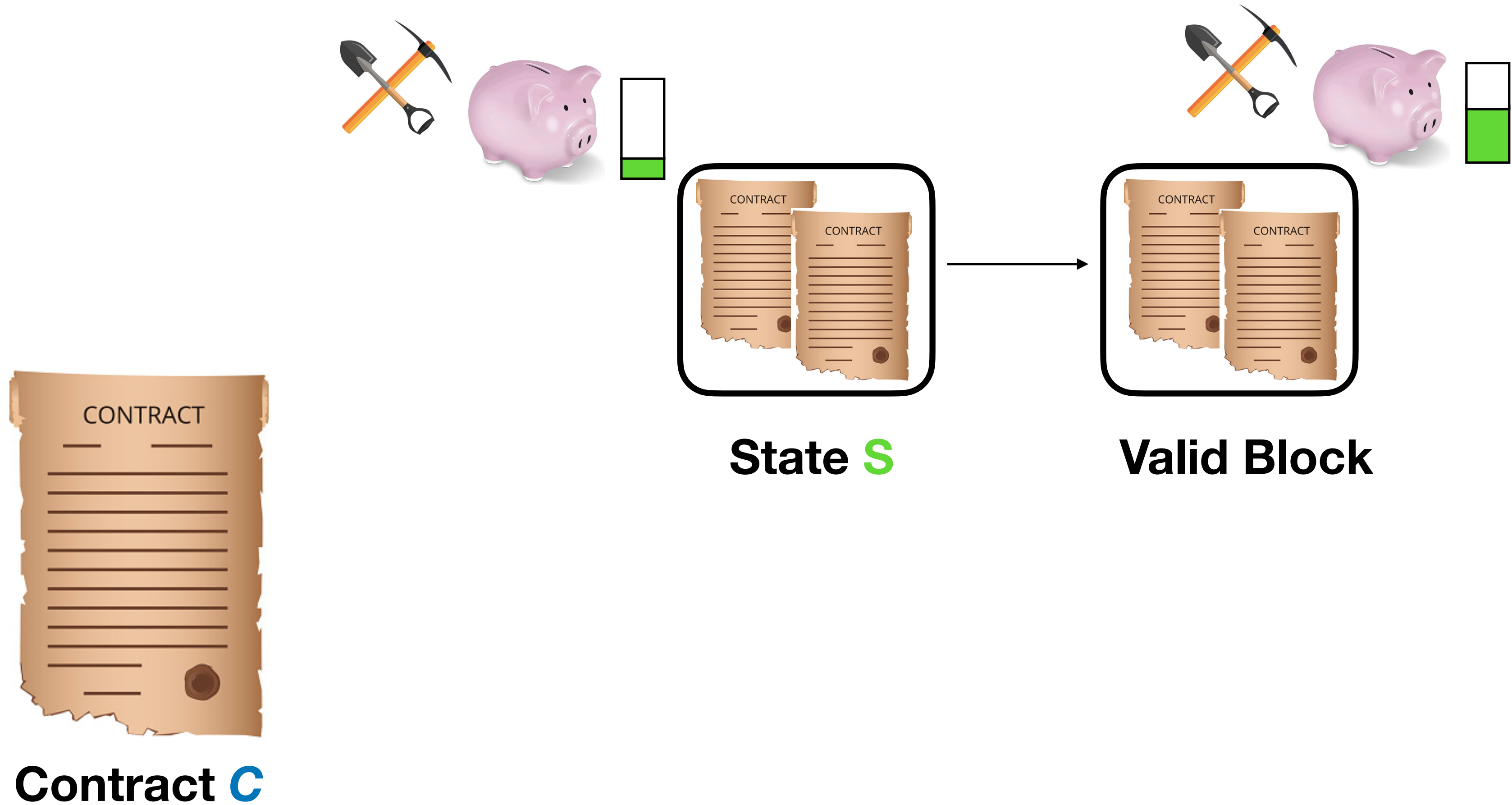
Use MEV as the measure of economic security

Miner is the most powerful out of all permissionless players - MEV subsumes all other attacks

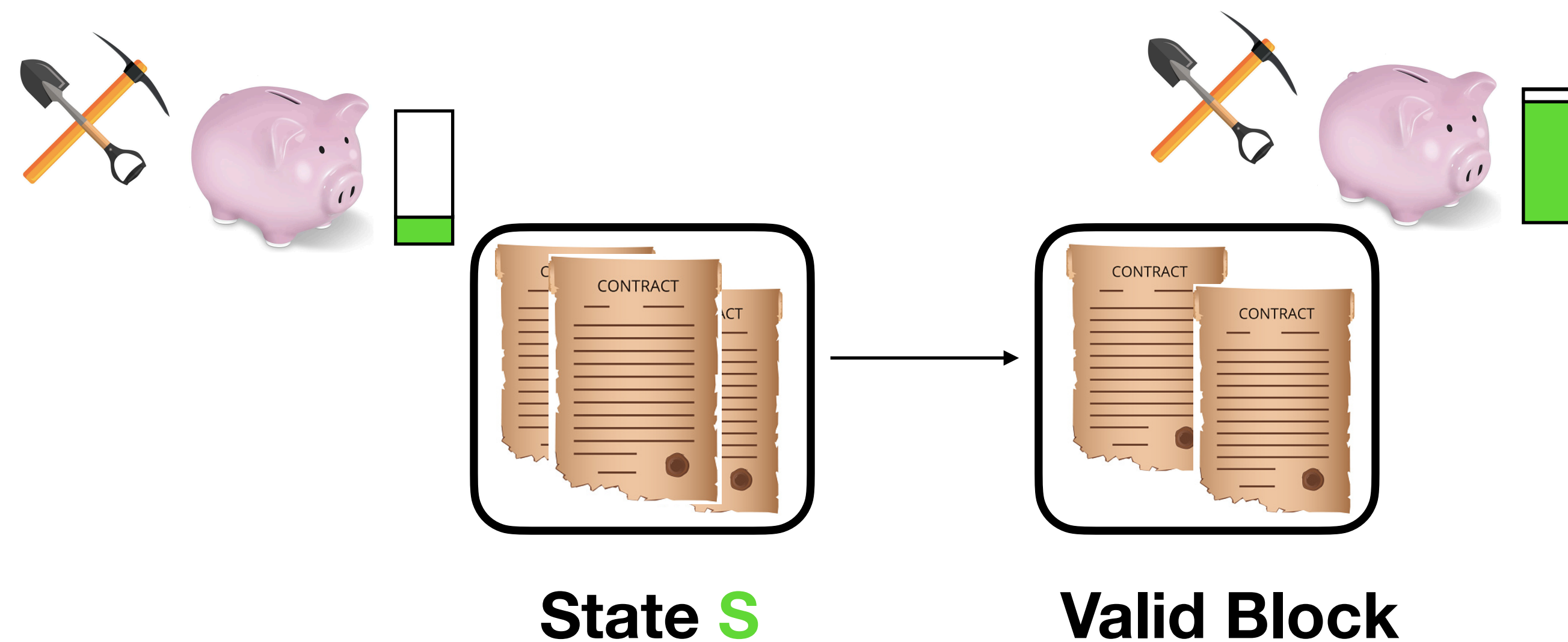
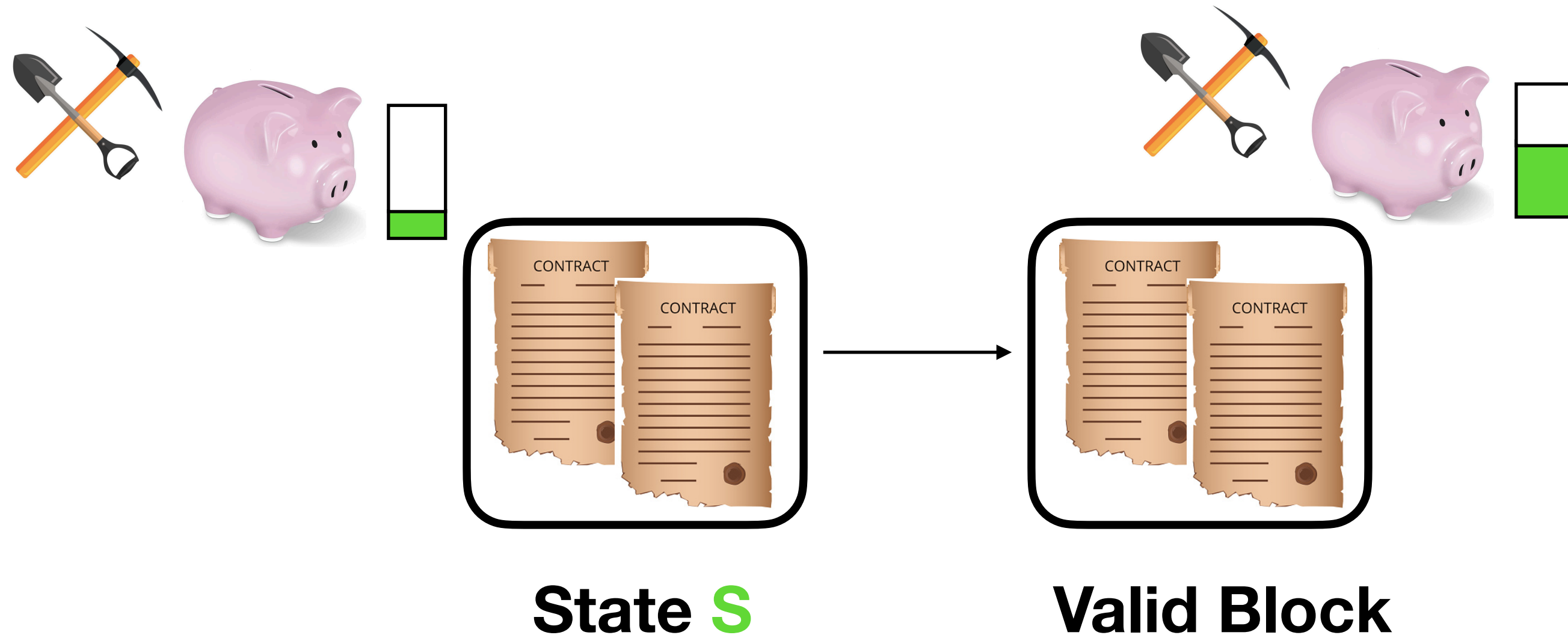
Secure Composition



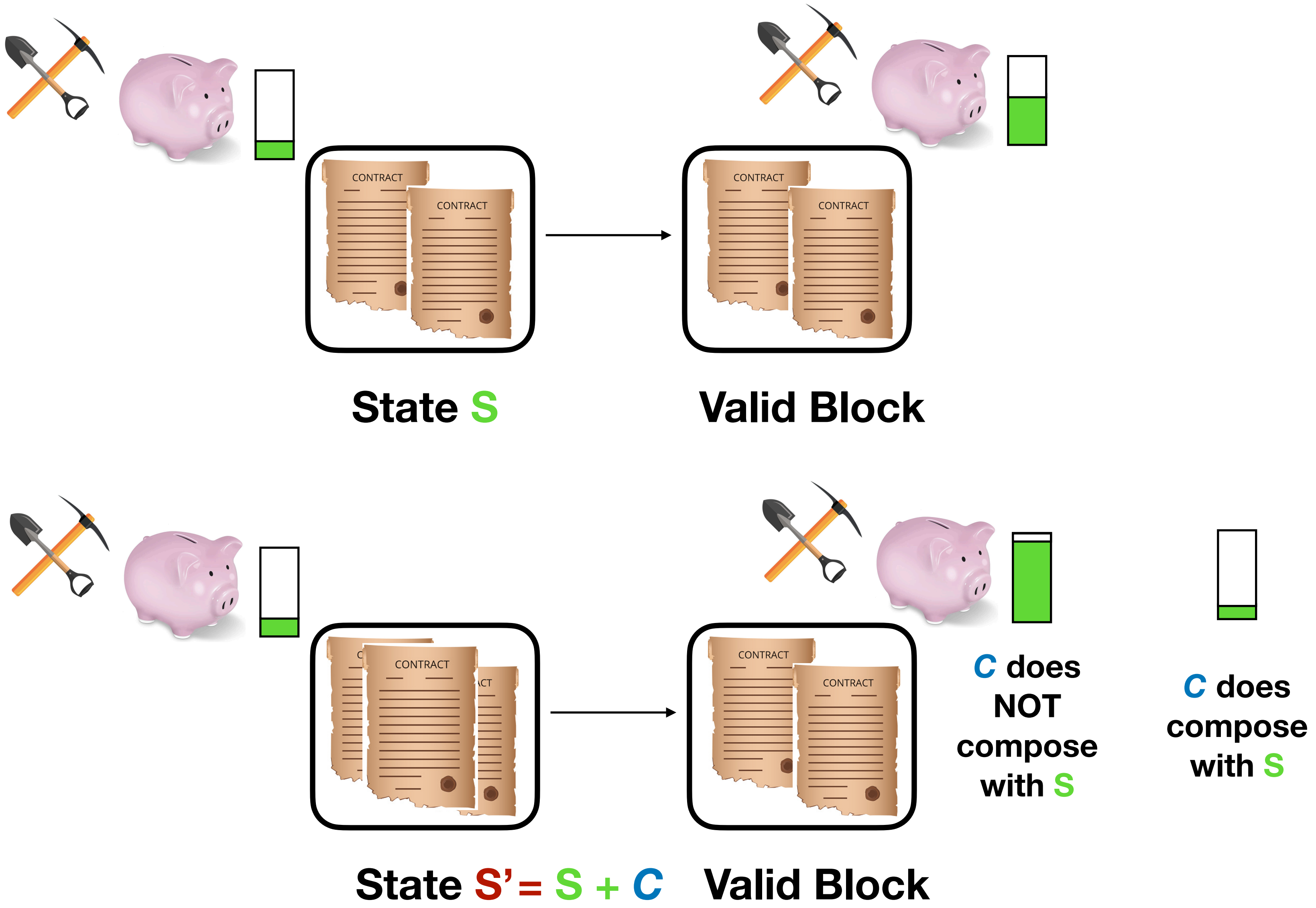
Secure Composition



Secure Composition



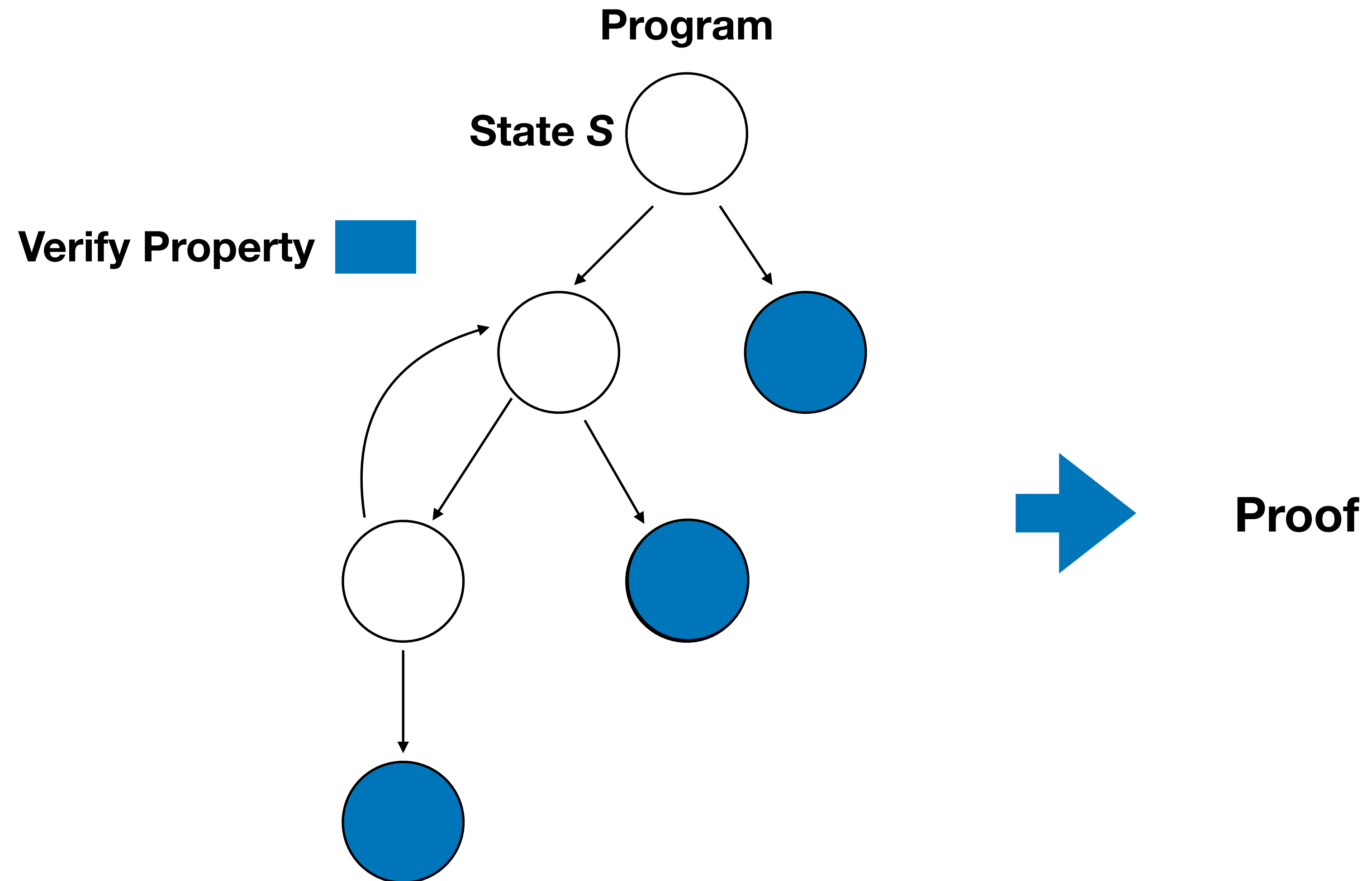
Secure Composition



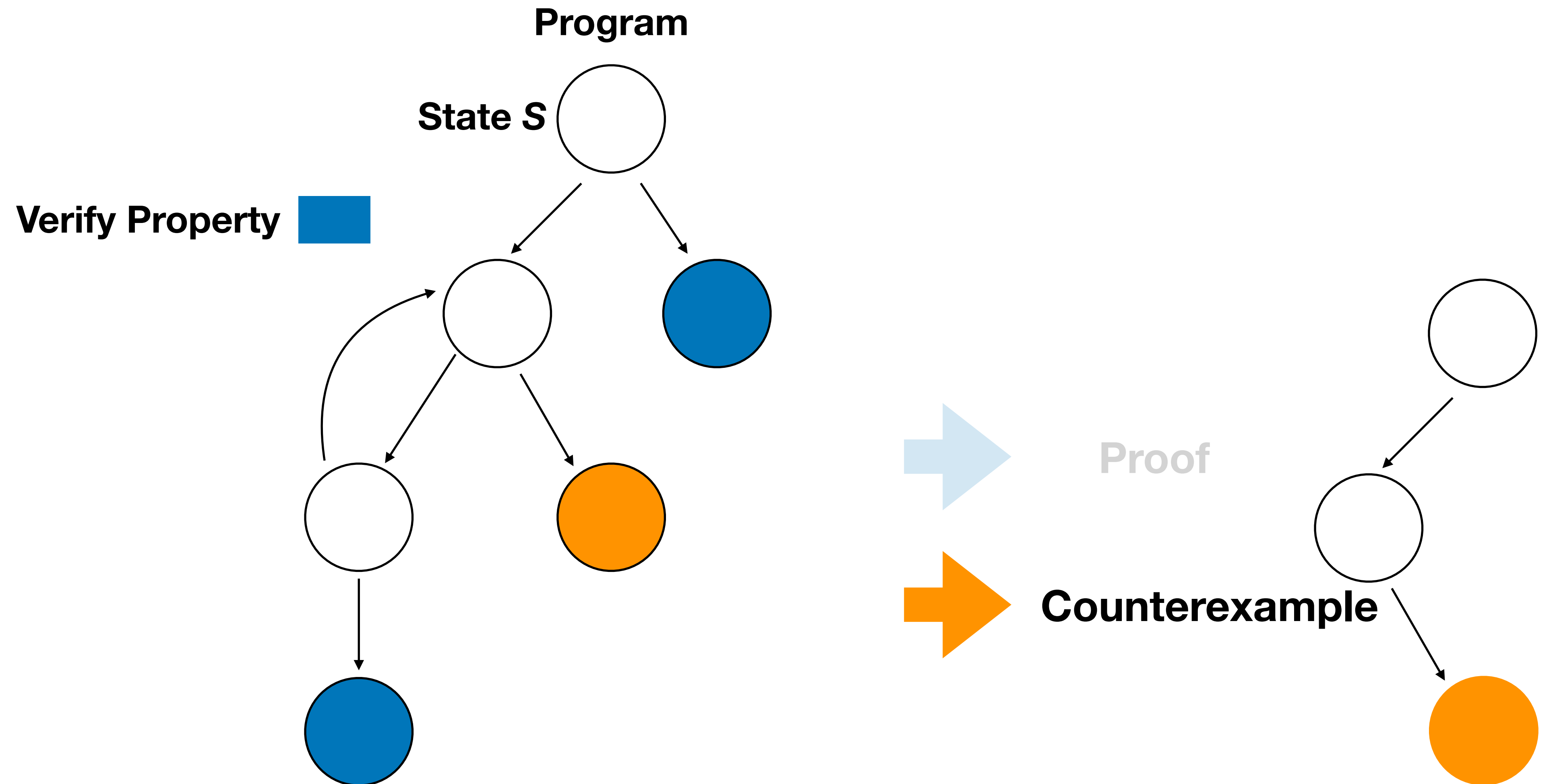
Outline

- Closer look at an example
- Definitional tools
 - Defining EV
 - Defining Secure Composition
- Practical Instantiation into Clockwork Finance Framework (CFF)
 - Design
 - Use for proofs
 - Use for finding attacks

Formal Verification



Formal Verification



Clockwork Finance Framework (CFF)

Clockwork Finance Framework (CFF)



(Symbolic) Transactions = tx1, tx2, tx3

Verify Property: $MEV < \delta$

Clockwork Finance Framework (CFF)



(Symbolic) Transactions = tx1, tx2, tx3

Swap **X** Eth for **Y** USD
X ≥ 0 , **Y** ≥ 0

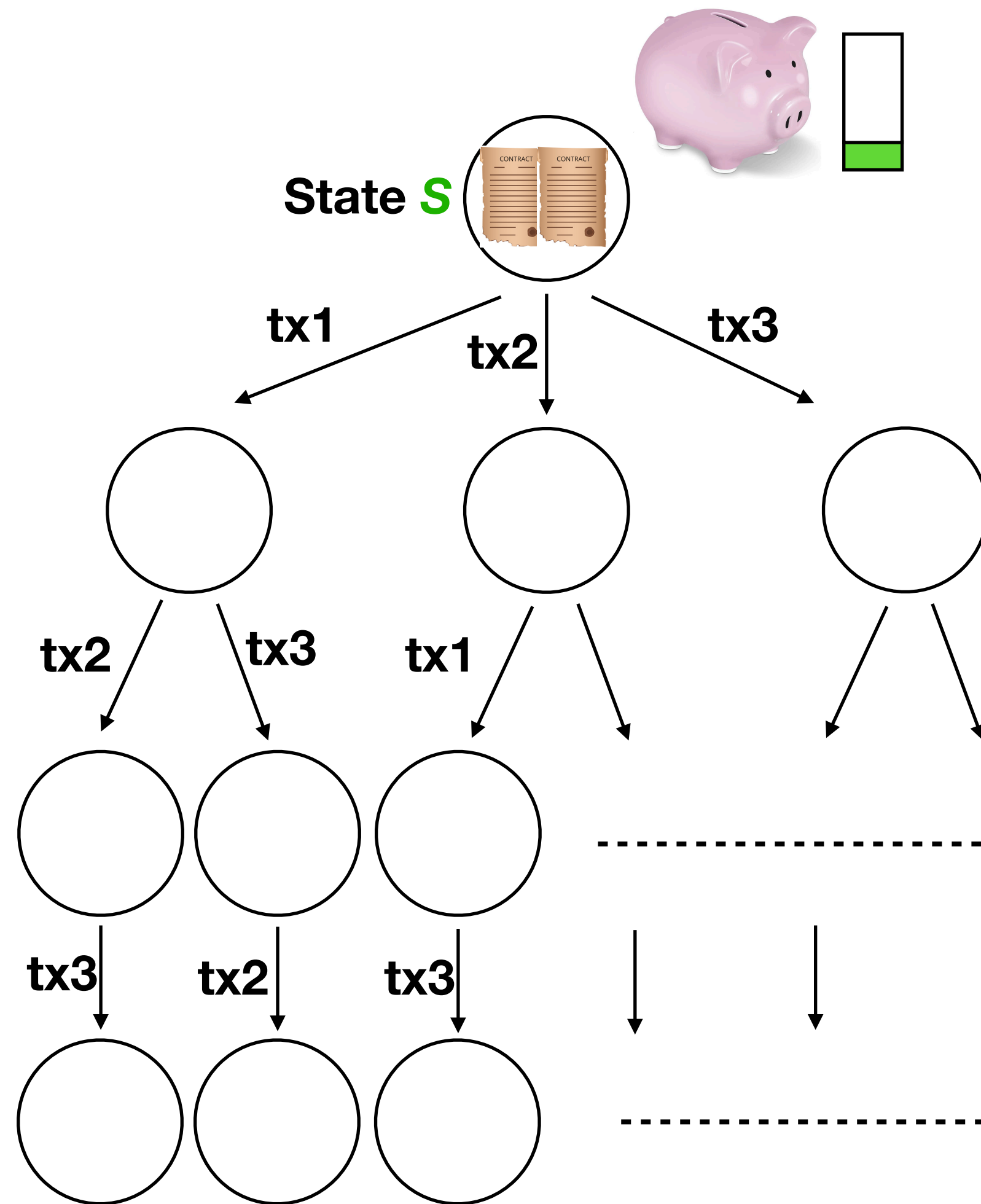
Verify Property: $MEV < \delta$

Clockwork Finance Framework (CFF)

(Symbolic) Transactions = tx1, tx2, tx3

Swap \mathbf{X} Eth for \mathbf{Y} USD
 $\mathbf{X} \geq 0, \mathbf{Y} \geq 0$

Verify Property: $MEV < \delta$

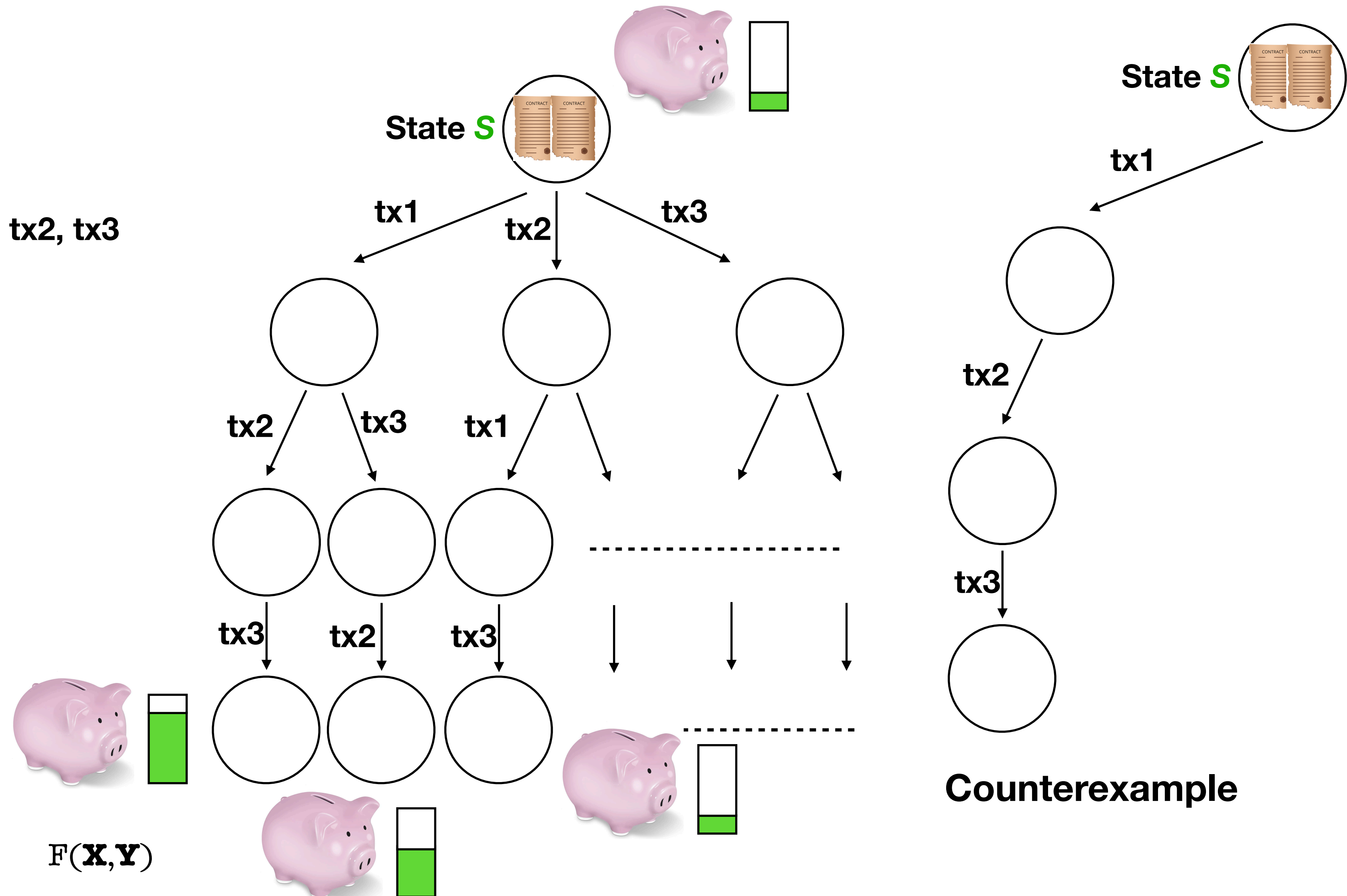


Clockwork Finance Framework (CFF)

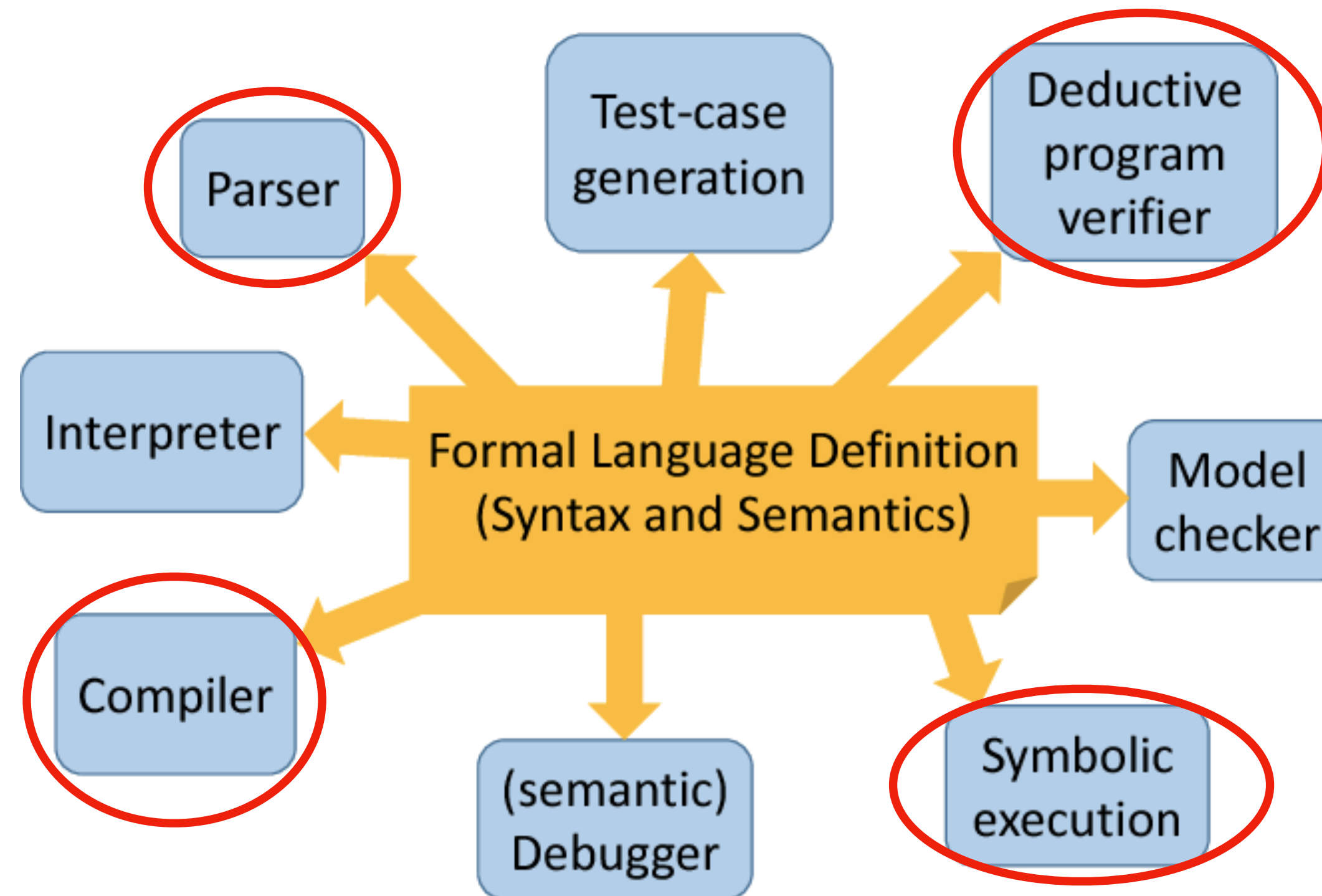
(Symbolic) Transactions = tx1, tx2, tx3

Swap X Eth for Y USD
 $X \geq 0, Y \geq 0$

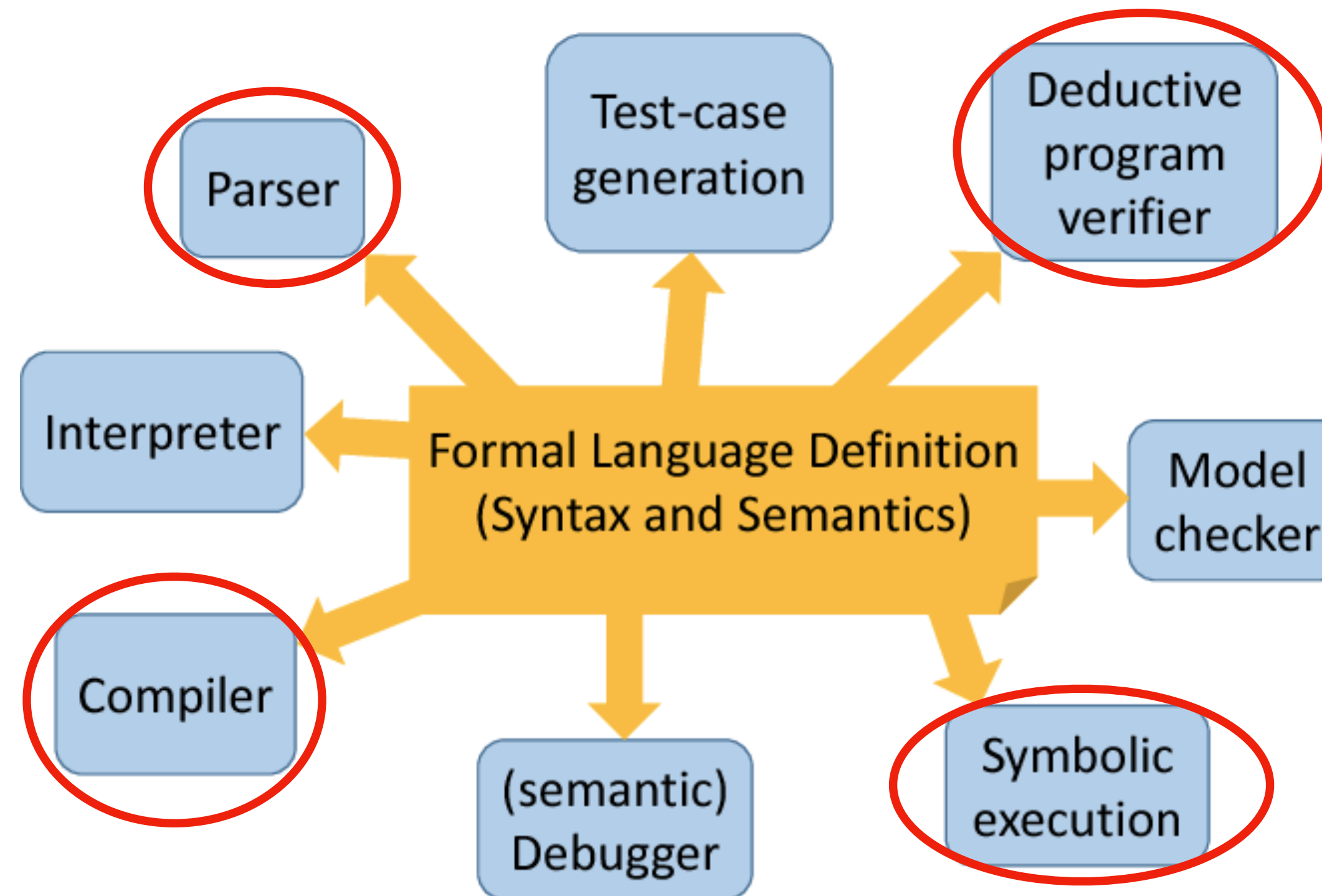
Verify Property: $MEV < \delta$



K Framework



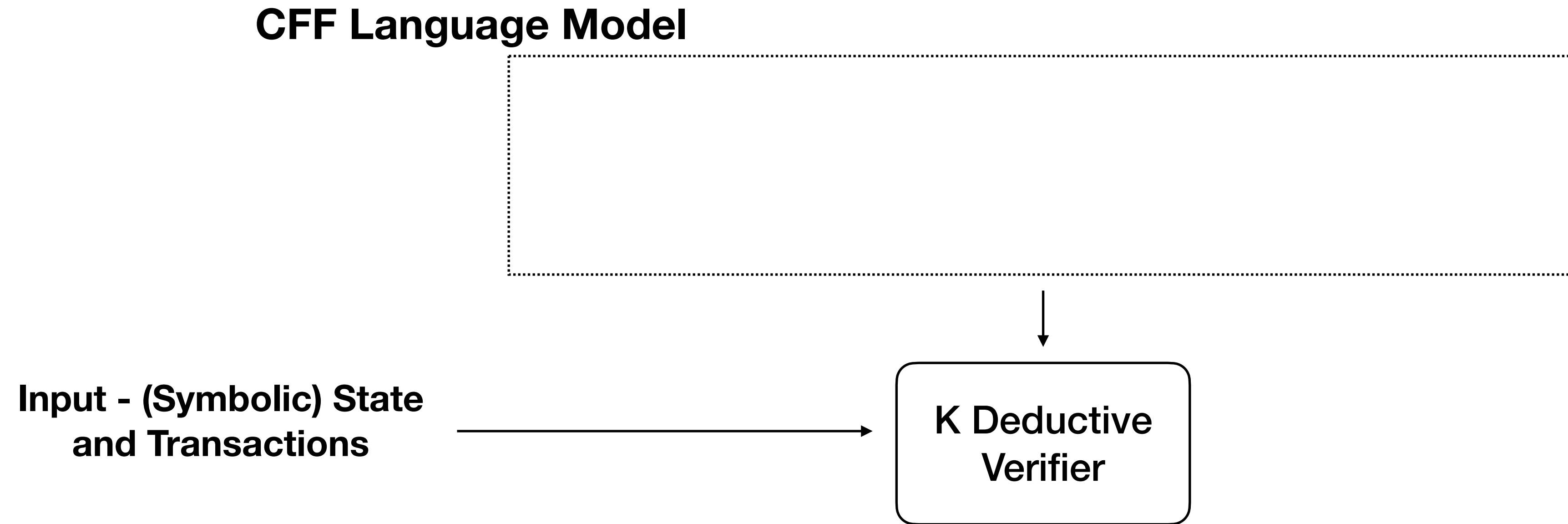
K Framework



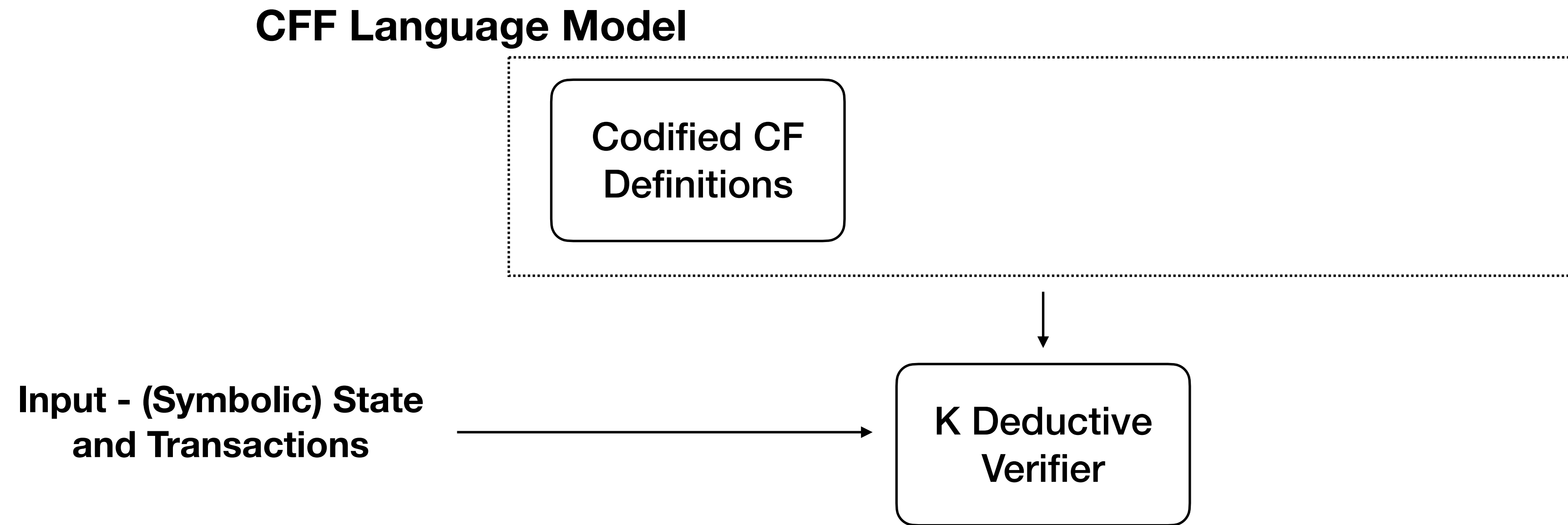
- Human Readable Formal Specification
- KEVM - Formal Ethereum Semantics in K

CFF Design

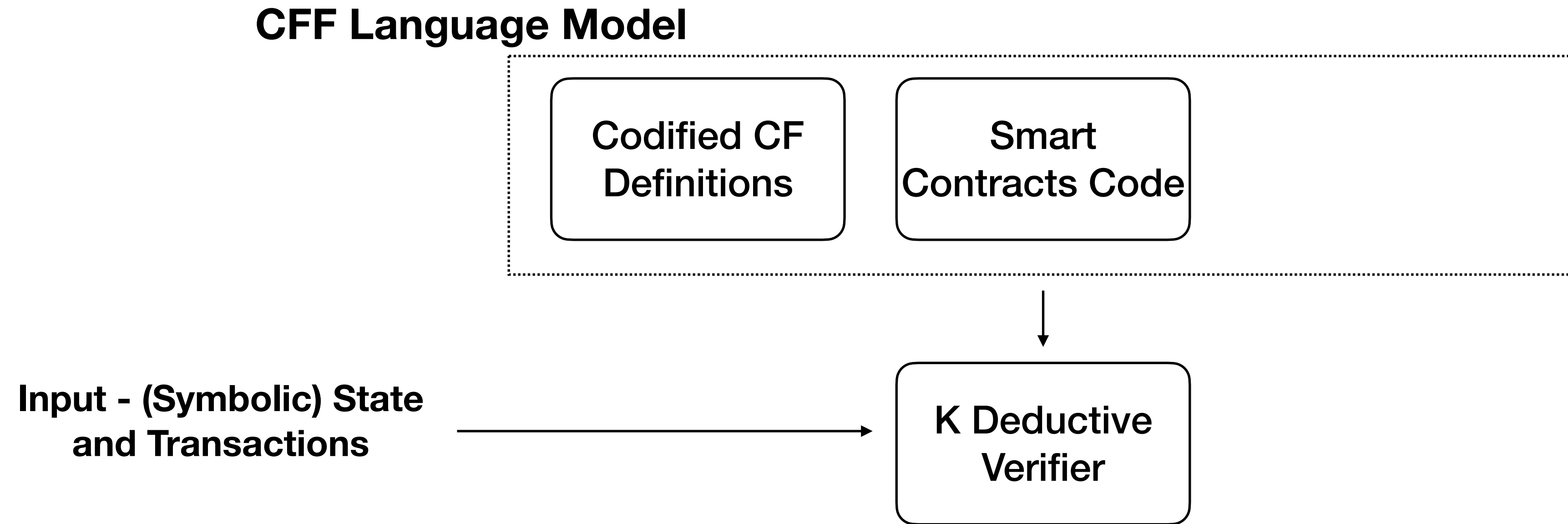
CFF Design



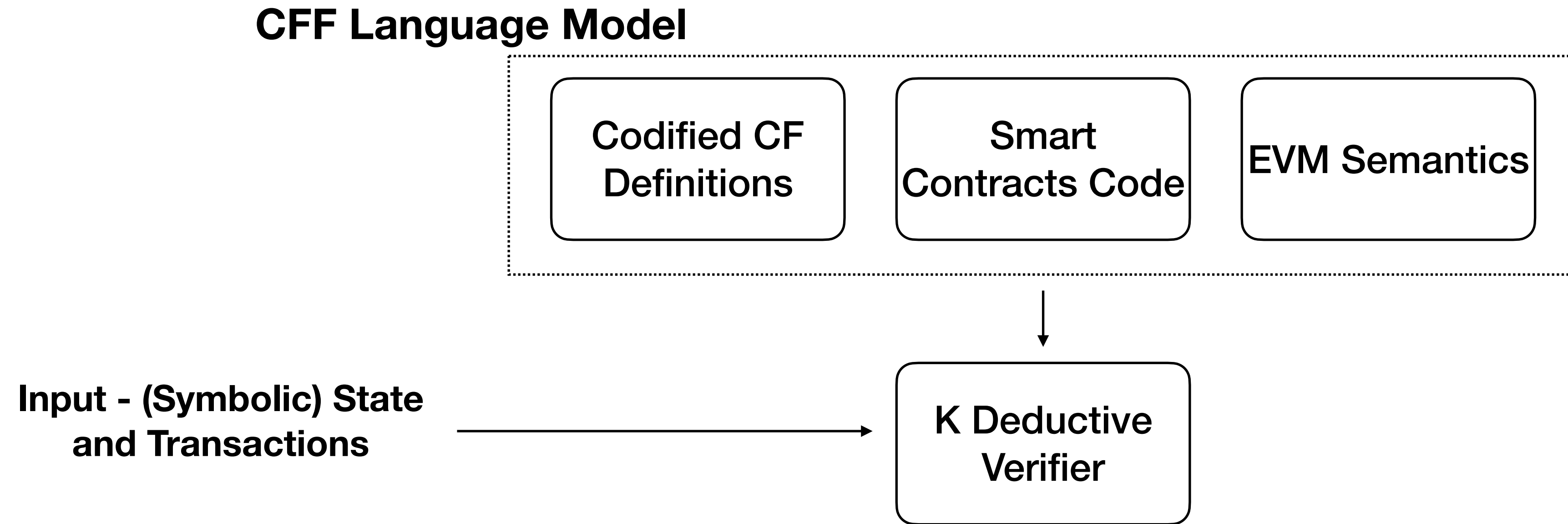
CFF Design



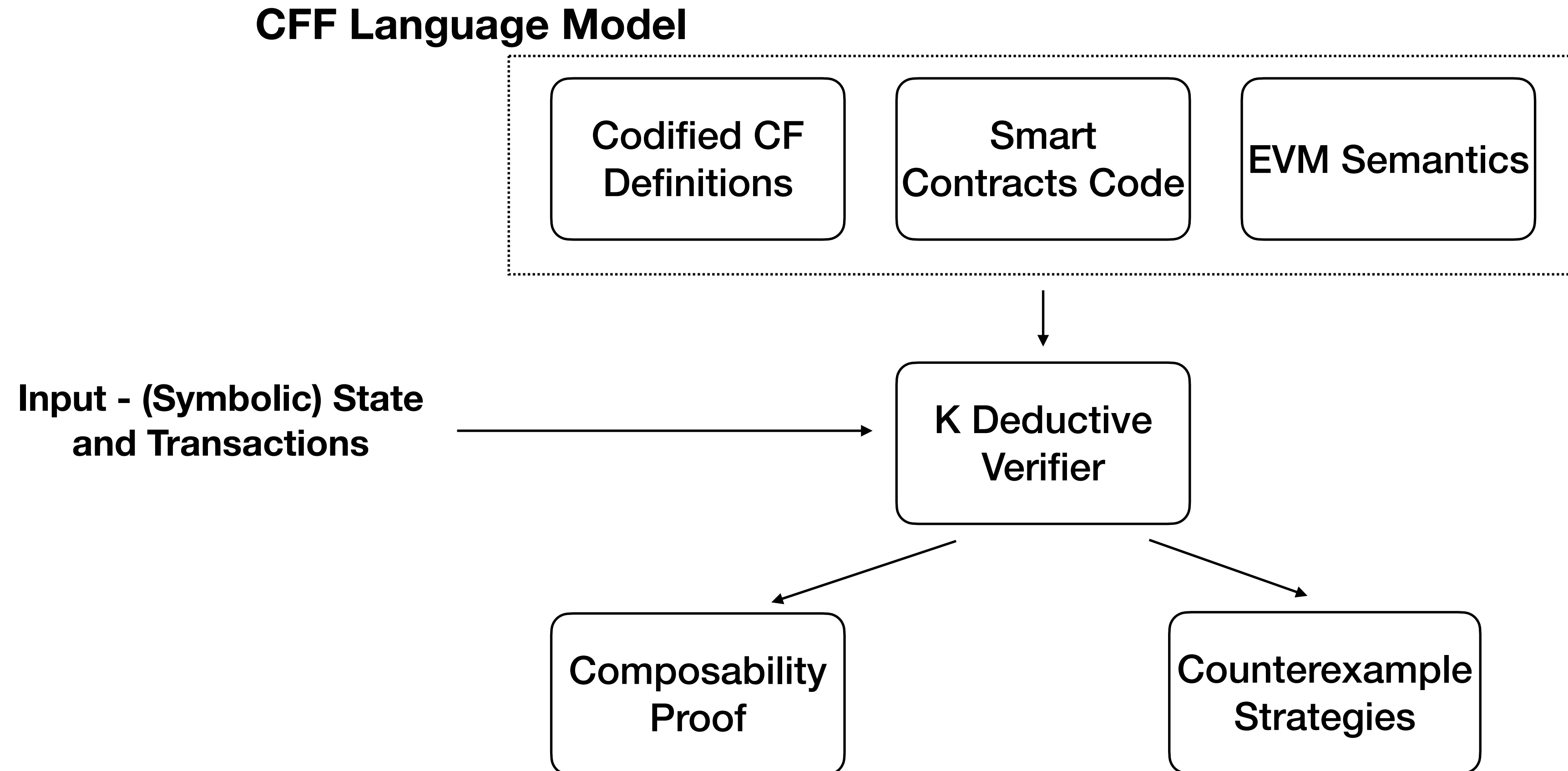
CFF Design



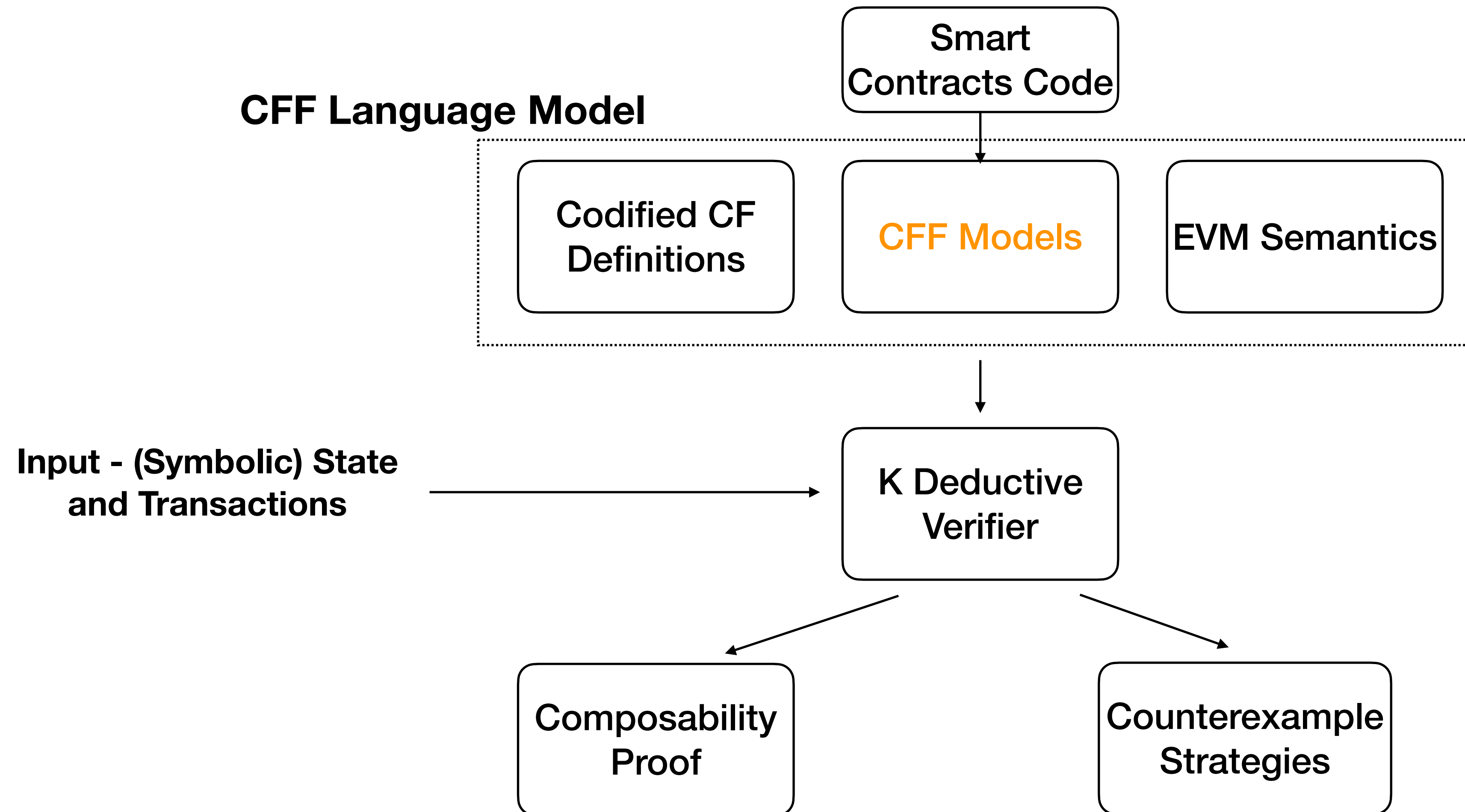
CFF Design



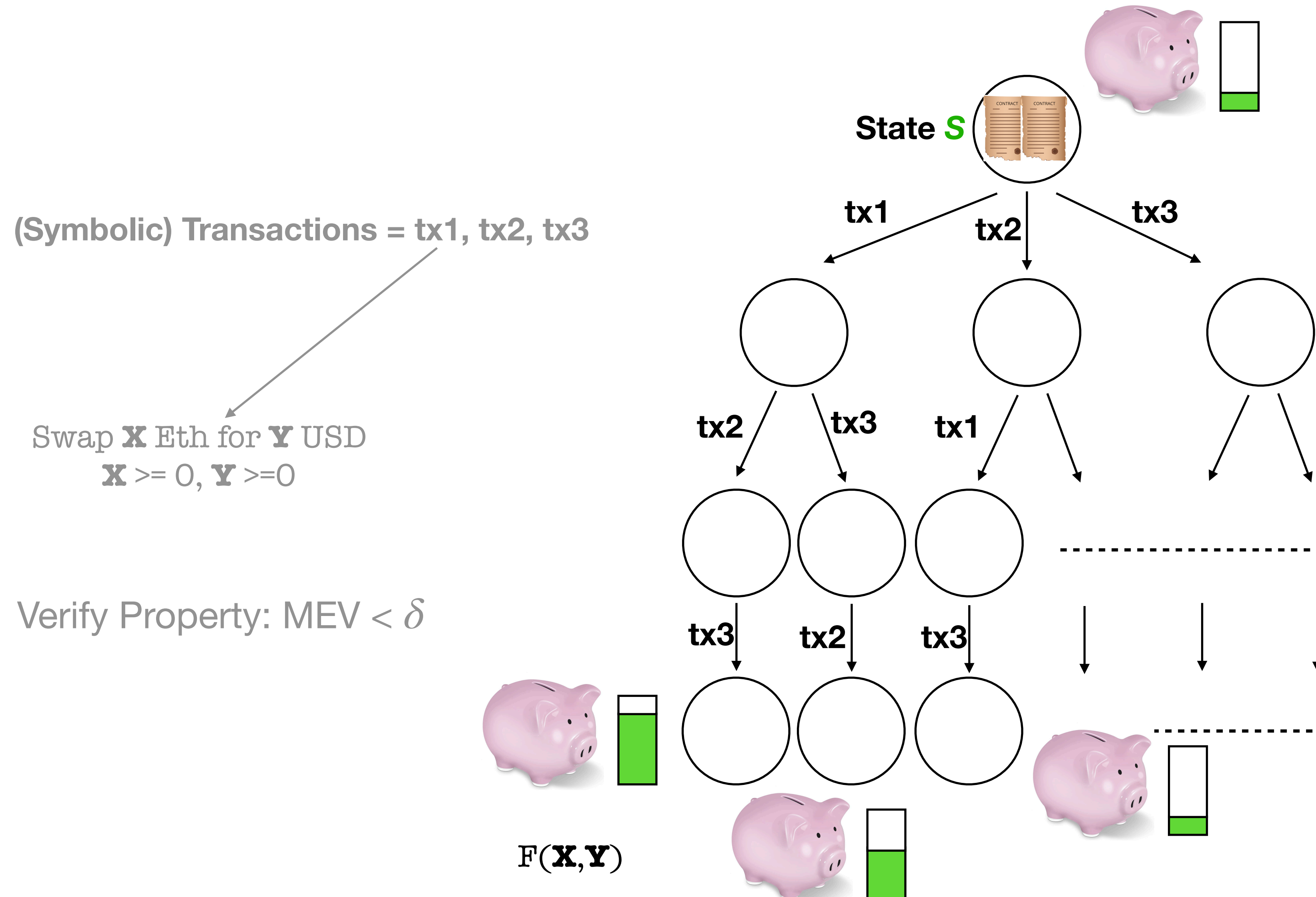
CFF Design



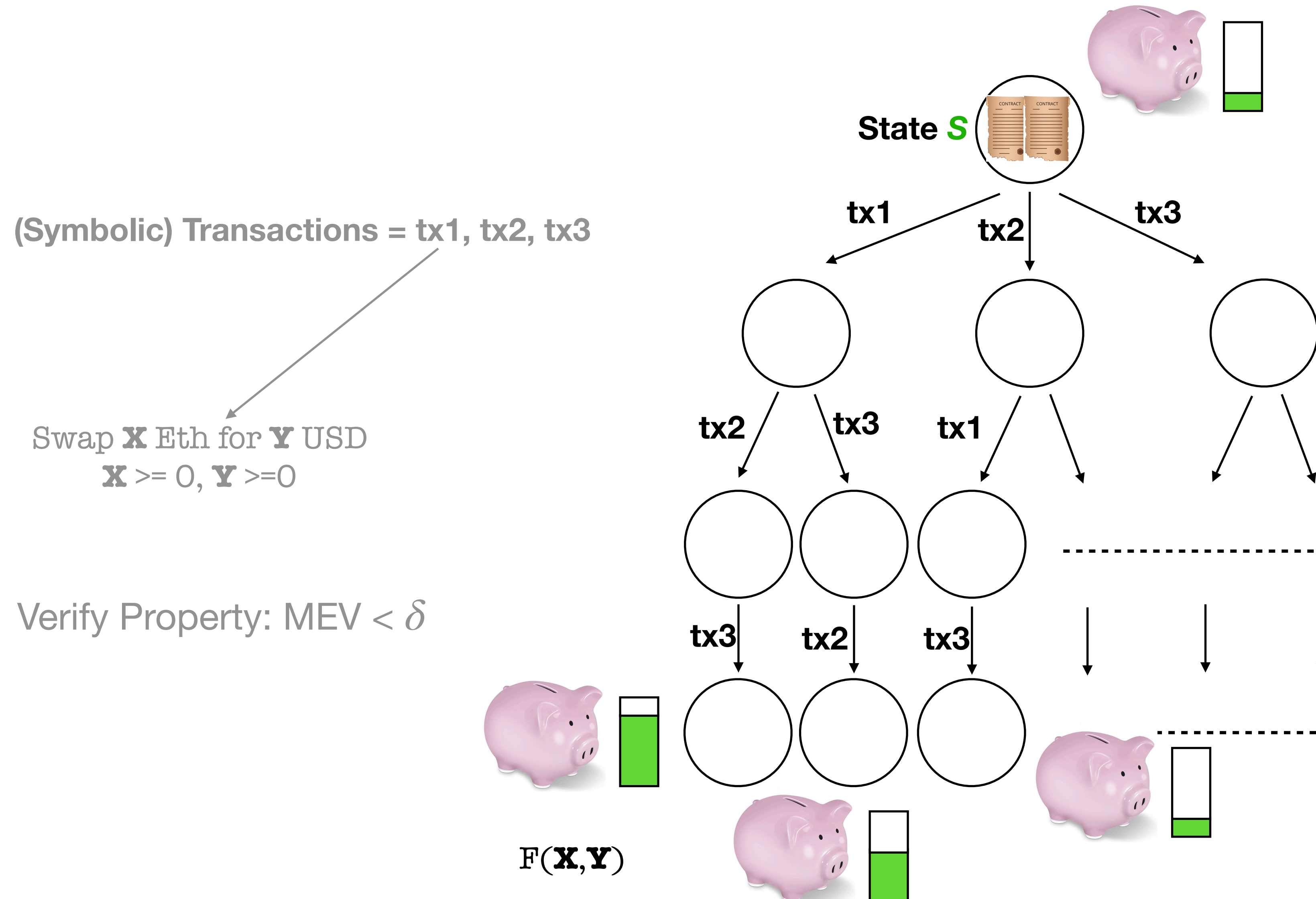
CFF Design



CFF Models

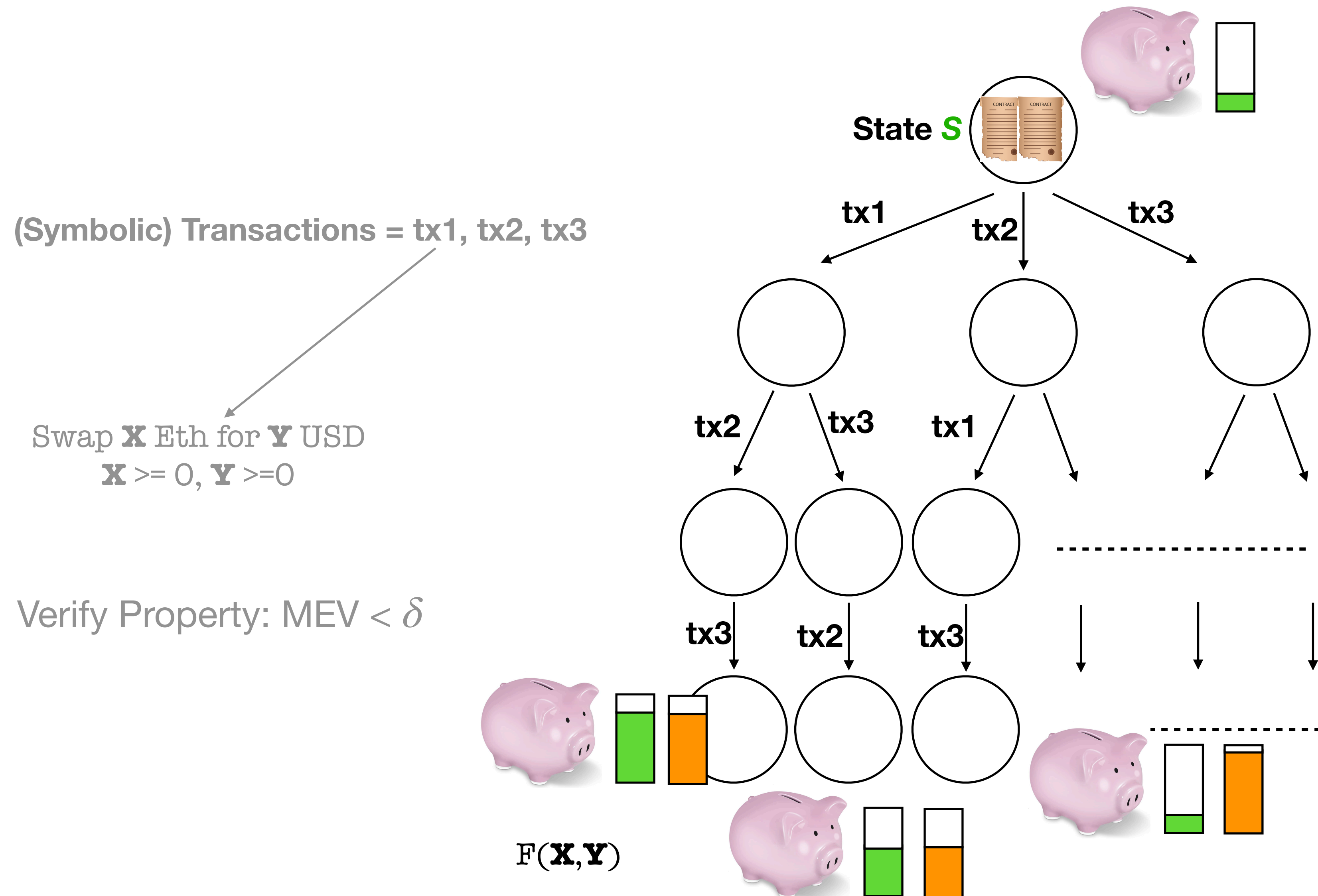


CFF Models



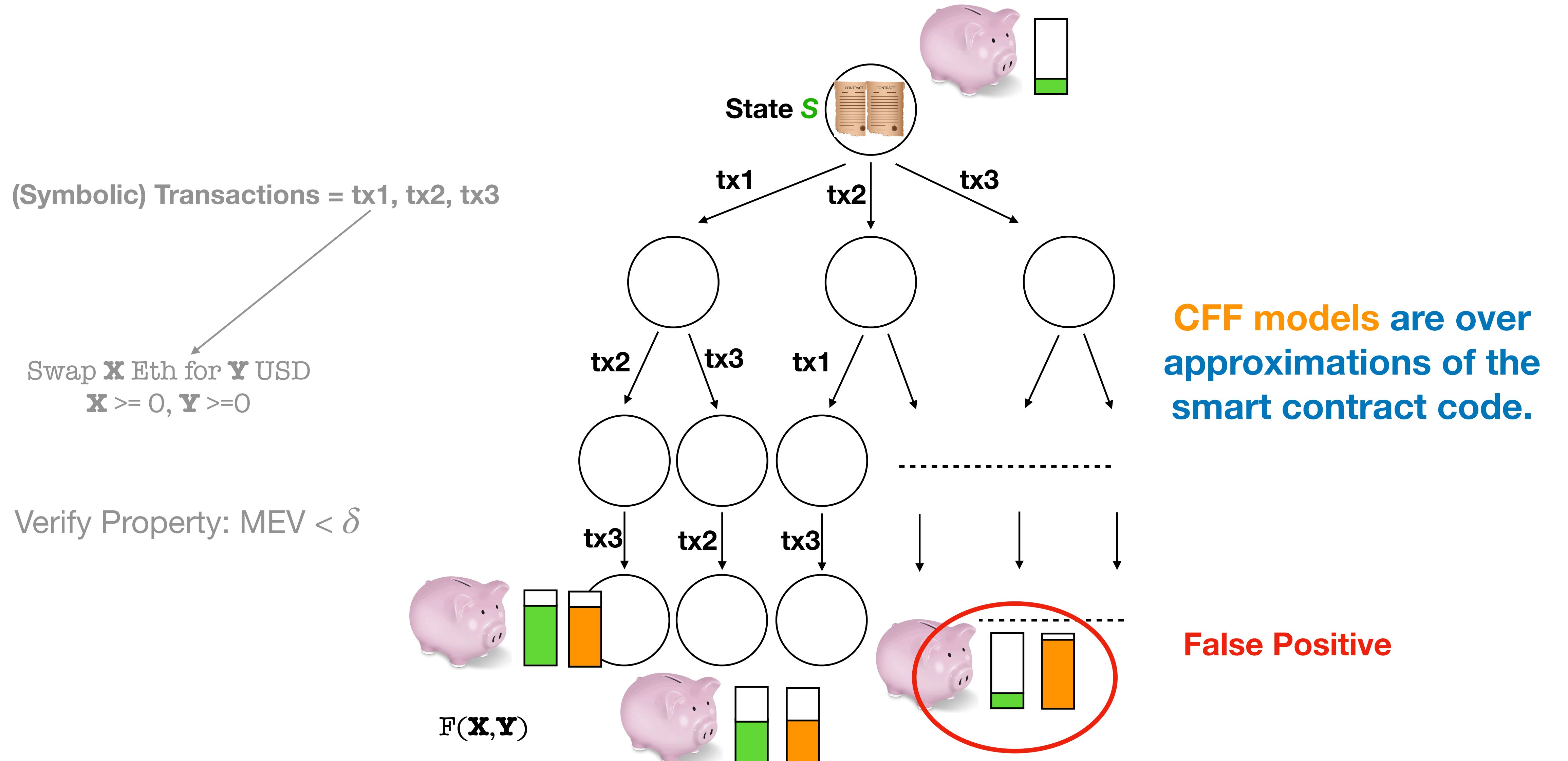
CFF models are over approximations of the smart contract code.

CFF Models

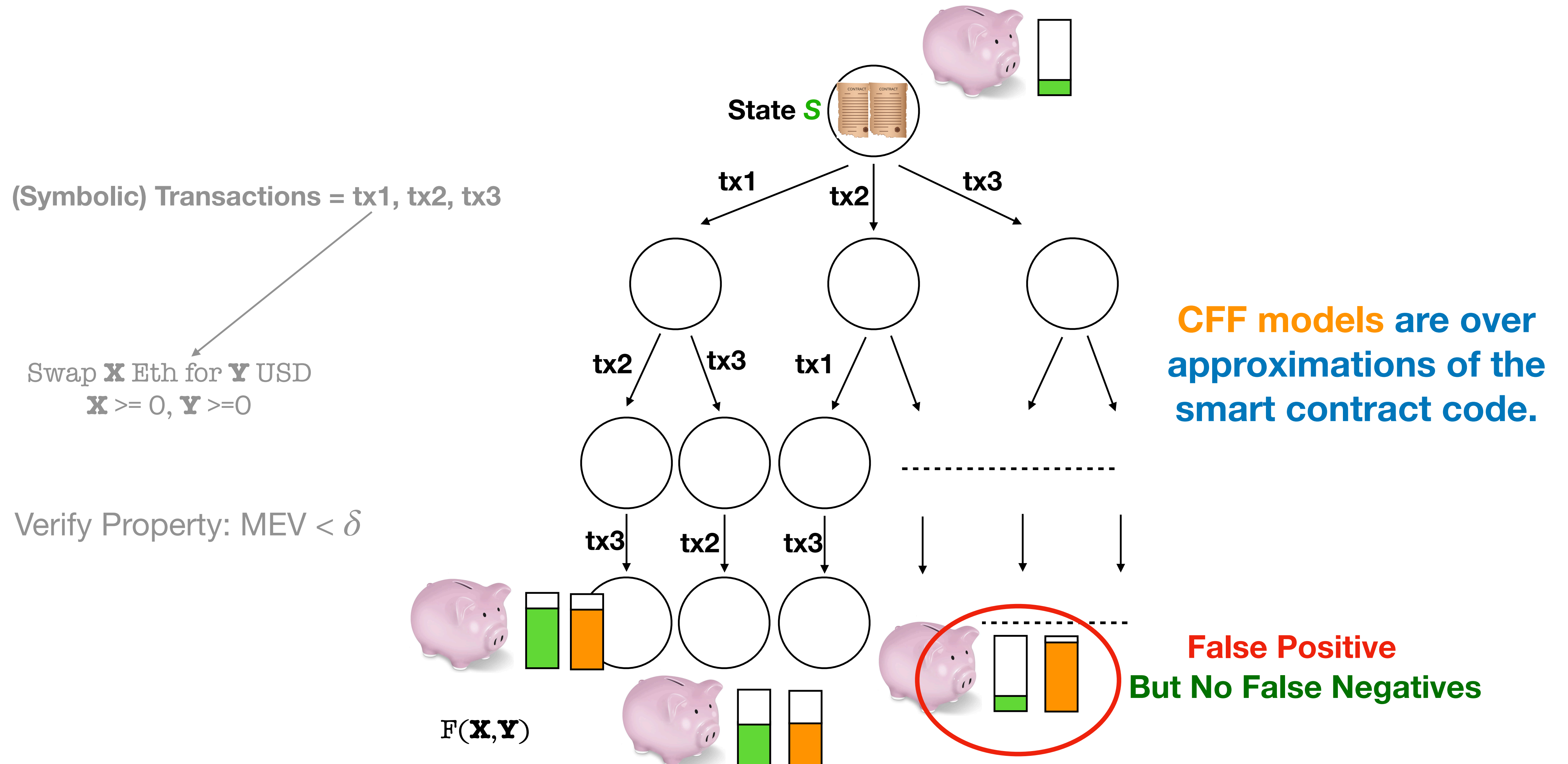


CFF models are over approximations of the smart contract code.

CFF Models



CFF Models



CFF Models

```
def ethToTokenInput(eth_sold: uint256(wei), min_tokens: uint256, deadline: timestamp,
    assert deadline >= block.timestamp and (eth_sold > 0 and min_tokens > 0)
    token_reserve: uint256 = self.token.balanceOf(self)
    tokens_bought: uint256 = self.getInputPrice(as_unitless_number(eth_sold), as_unit
    assert tokens_bought >= min_tokens
    assert self.token.transfer(recipient, tokens_bought)
    log.TokenPurchase(buyer, eth_sold, tokens_bought)
```

Process : Manual translation by pruning irrelevant code paths.

Becomes easier if the contract has been verified formally for functional correctness

Open sourced CFF models for UniswapV1, UniswapV2, MakerDAO, FlashLoans, Airdrops

CFF Models

```
def ethToTokenInput(eth_sold: uint256(wei), min_tokens: uint256, deadline: timestamp,
assert deadline >= block.timestamp and (eth_sold > 0 and min_tokens > 0)
    token_reserve: uint256 = self.token.balanceOf(self)
    tokens_bought: uint256 = self.getInputPrice(as_unitless_number(eth_sold), as_unitless_number(token_reserve))
    assert tokens_bought >= min_tokens
    assert self.token.transfer(recipient, tokens_bought)
    log.TokenPurchase(buyer, eth_sold, tokens_bought)
```

Process : Manual translation by pruning irrelevant code paths.

Becomes easier if the contract has been verified formally for functional correctness

Open sourced CFF models for UniswapV1, UniswapV2, MakerDAO, FlashLoans, Airdrops

CFF Models

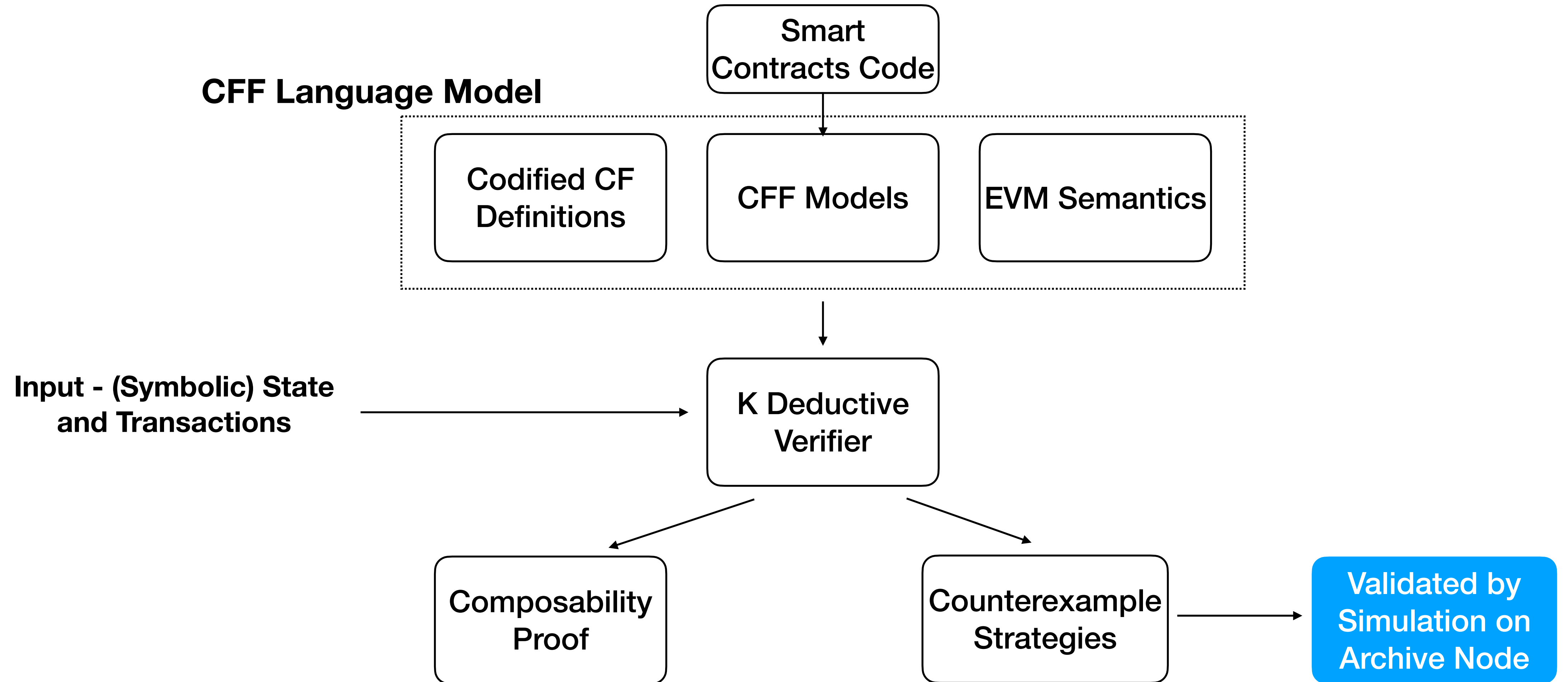
```
def ethToTokenInput(eth_sold: uint256(wei), min_tokens: uint256, deadline: timestamp,
assert deadline >= block.timestamp and (eth_sold > 0 and min_tokens > 0)
    token_reserve: uint256 = self.token.balanceOf(self)
    tokens_bought: uint256 = self.getInputPrice(as_unitless_number(eth_sold), as_unitless_number(token_reserve))
assert tokens_bought >= min_tokens
    assert self.token.transfer(recipient, tokens_bought)
    log.TokenPurchase(buyer, eth_sold, tokens_bought)
```

Process : Manual translation by pruning irrelevant code paths.

Becomes easier if the contract has been verified formally for functional correctness

Open sourced CFF models for UniswapV1, UniswapV2, MakerDAO, FlashLoans, Airdrops

CFF Design



More Scaling Optimisations

1. General Optimisations

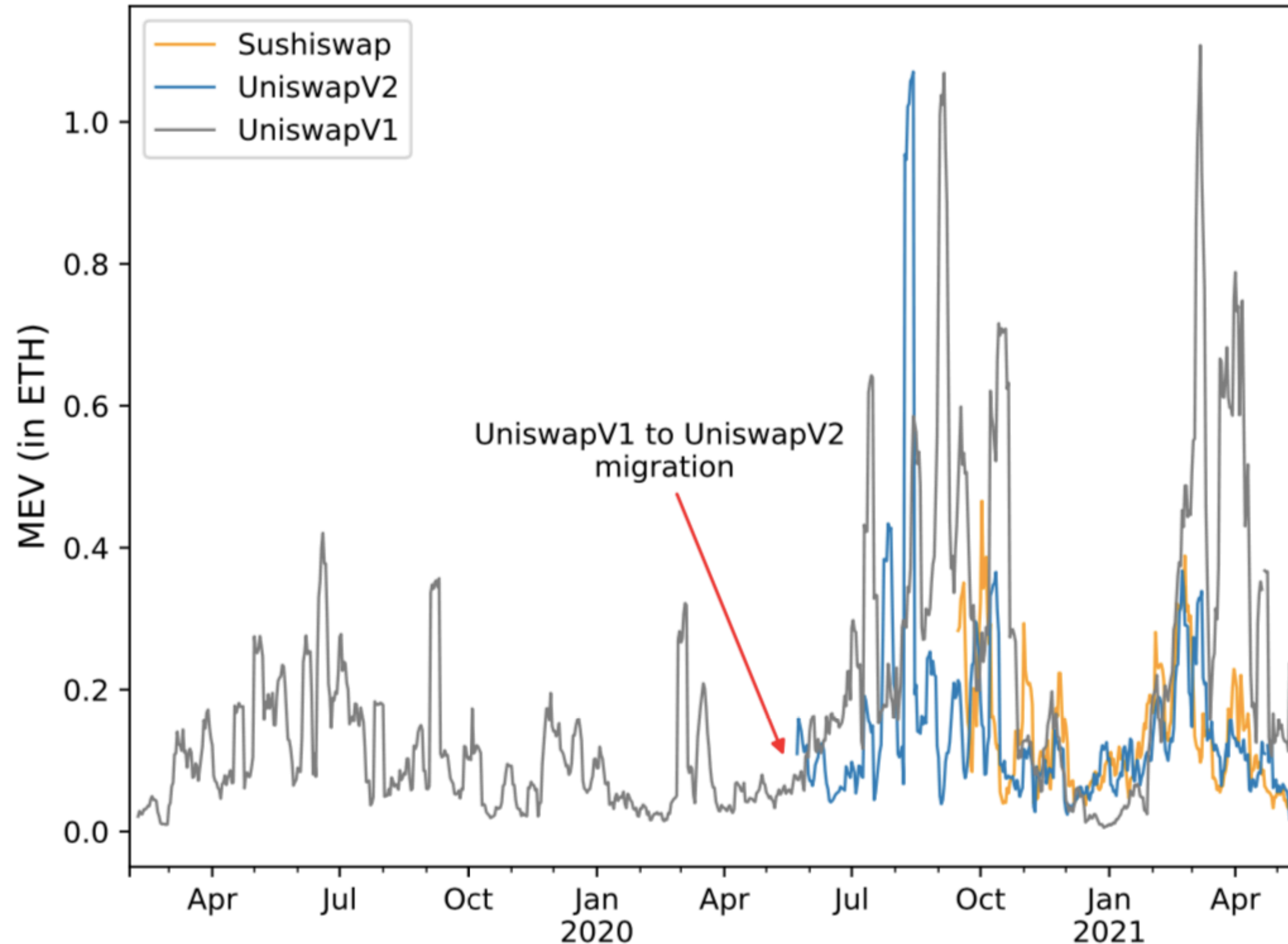
1. Transactions for a sender need to be serialised using “nonces”. Many invalid orderings are equivalent
2. Reorderings across different non interacting contracts are equivalent
3. Randomised reorderings lead to better convergence in practice.

2. Contract Specific Optimisations

1. Uniswap-like AMMs are path independent

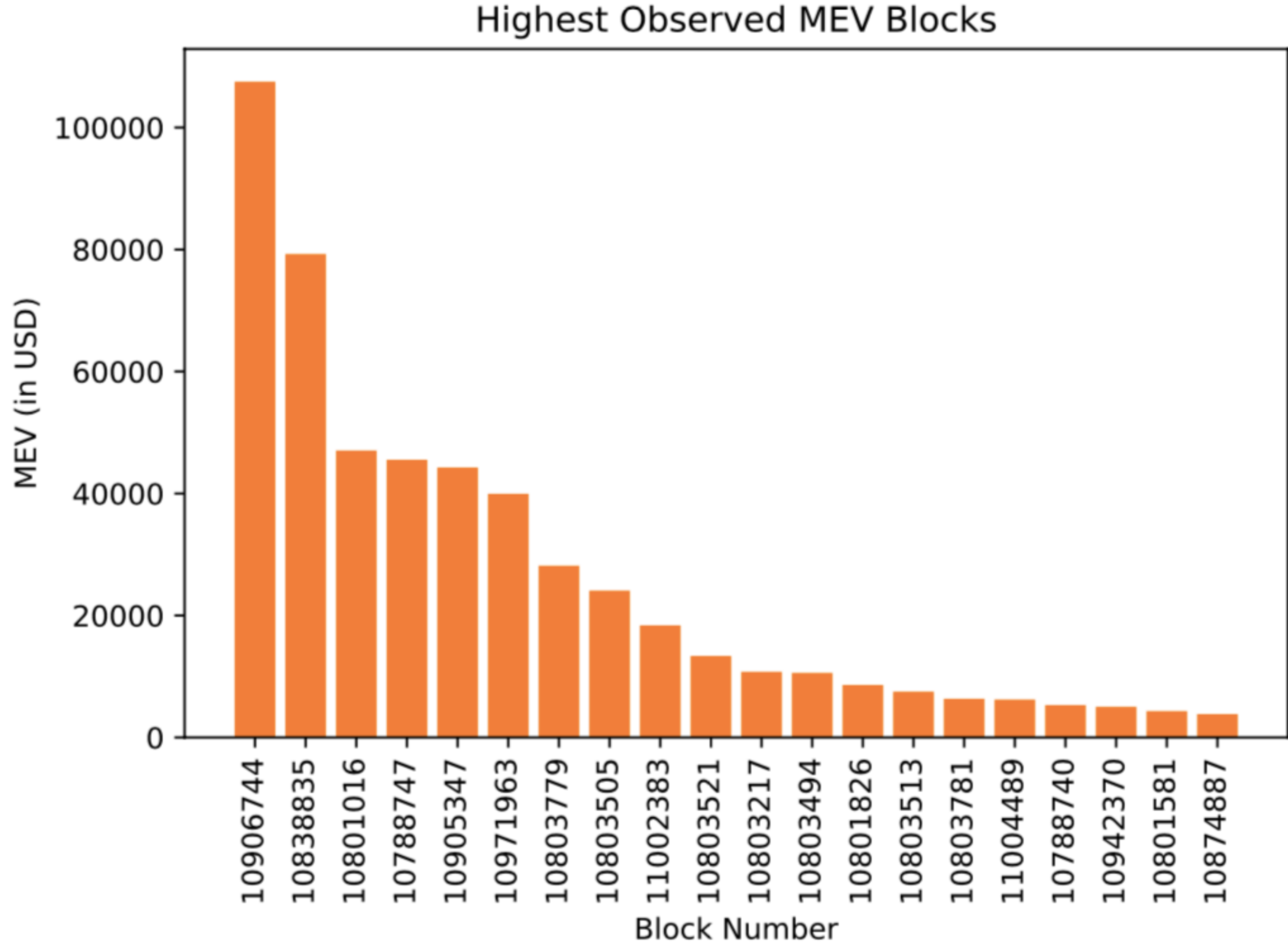
CFF Evaluation - AMM

7-day moving average of
MEV per block in a sample
of 1000 random blocks in
each month



CFF Evaluation - Maker + Uniswap

Uniswap price used as oracle in Maker



CFF Model for Maker abstracts out liquidation auction

CFF Evaluation

**Many More in the paper...
Governance, Flashloans, Airdrops**

Conclusion

- Initiated the formal study of economic behaviour of smart contracts through the lens of MEV
 - Definitions for MEV and Secure Composition
 - Clockwork Finance Framework (CFF) : **Practical Proof System** based on Formal Verification
- Developers can use CFF to generate proofs of bounds on the MEV exposed by their contracts, and users can use CFF to analyse the MEV extractable from their transactions.

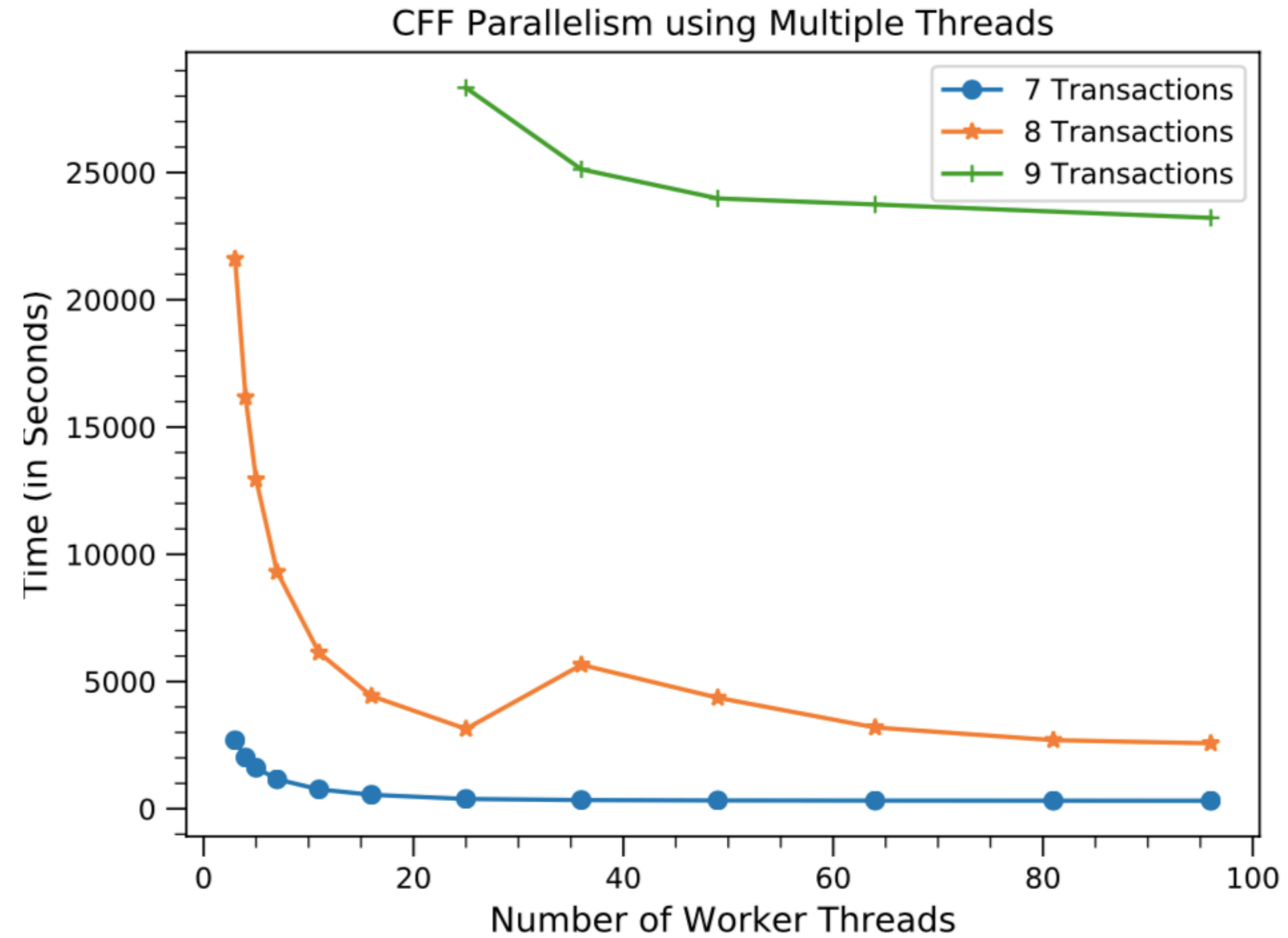
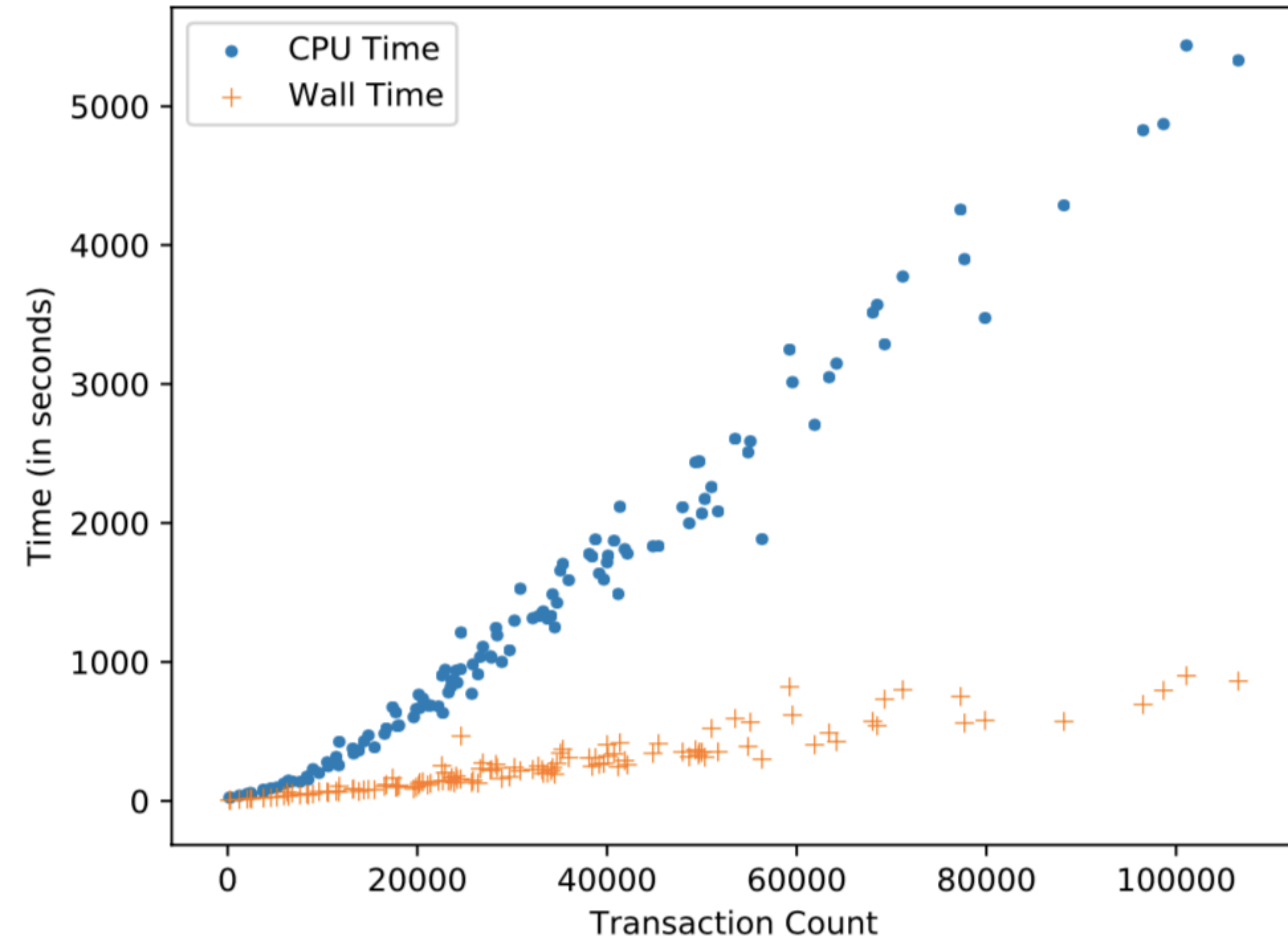
Paper : <https://cs.cornell.edu/~babel/cff.pdf>

Github : <https://github.com/defi-formal/cff>

Contact : babel@cs.cornell.edu

Appendix

Execution and proving times

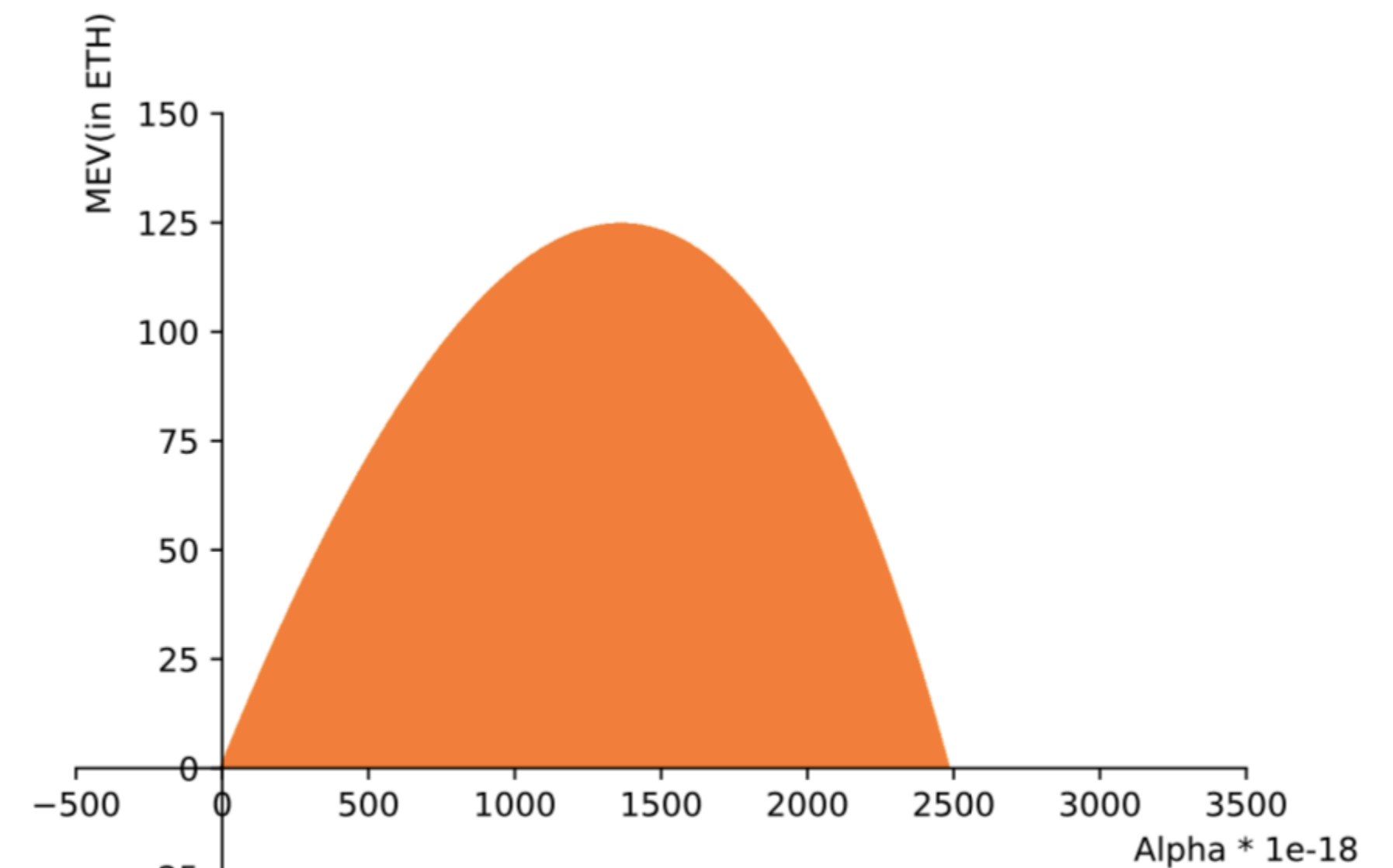


Directions for Future Work

- MEV Definitions for Leaderless Protocols
- Arbitrary Symbolic Transaction Insertions
- Scaling the Backend

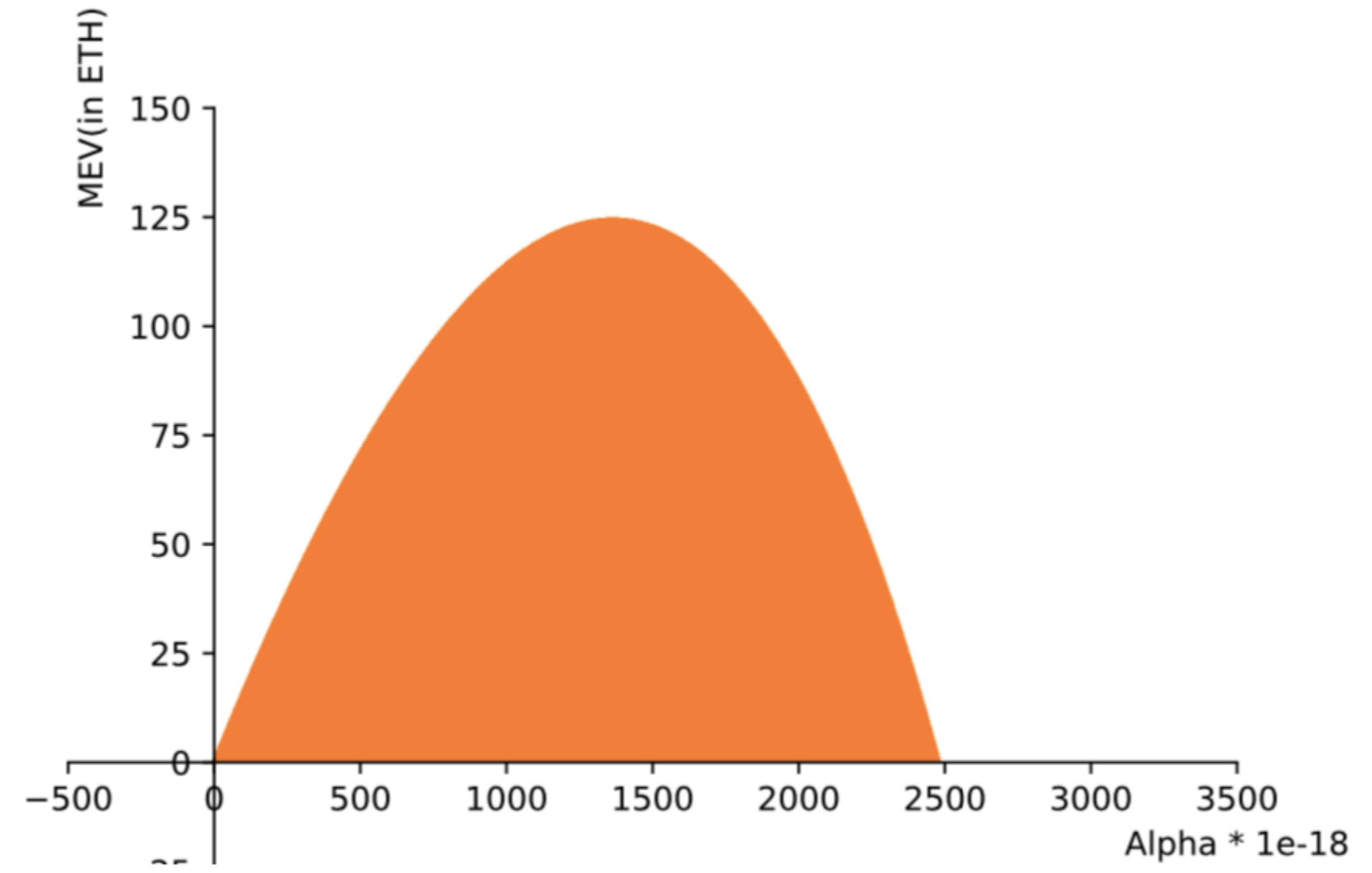
Under the Hood- Sushiswap + Uniswap

```
1 claim <k>
2 On UniswapV2 697323163401596485410334513241460920685086001293 swaps for ETH by providing
  ↳ 13000000000000000000000000 COMP and 0 ETH with change 0 fee 1767957155464 ;
3 On Sushiswap Miner swaps for ETH by providing Alpha: Int COMP and 0 ETH with change 0 fee 0 ;
4 On UniswapV2 Miner swaps for Alpha COMP by providing ETH fee 0 ;
5
6 => .K
7 </k>
8 <S> (Sushiswap in COMP) |-> 107495485843438764484770 (Sushiswap in ETH) |-> 49835502094518088853633
  ↳ (UniswapV2 in COMP) |-> 5945498629669852264883 (UniswapV2 in ETH) |-> 2615599823603823616442 =>
  ↳ ?S:Map </S>
9 <B> .List => ?_ </B>
10 requires (Alpha >Int 0) andBool (Alpha <Int 1000000000000000000000000) //10**22
11 ensures ({?S[Miner in COMP]}:>Int <=Int 0 ) andBool ({?S[Miner in ETH]}:>Int <=Int 0 )
```



Under the Hood- Sushiswap + Uniswap

```
1 claim <k>
2 On UniswapV2 697323163401596485410334513241460920685086001293 swaps for ETH by providing
  ↳ 13000000000000000000000000 COMP and 0 ETH with change 0 fee 1767957155464 ;
3 On Sushiswap Miner swaps for ETH by providing Alpha: Int COMP and 0 ETH with change 0 fee 0 ;
4 On UniswapV2 Miner swaps for Alpha COMP by providing ETH fee 0 ;
5
6 => .K
7 </k>
8 <S> (Sushiswap in COMP) |-> 107495485843438764484770 (Sushiswap in ETH) |-> 49835502094518088853633
  ↳ (UniswapV2 in COMP) |-> 5945498629669852264883 (UniswapV2 in ETH) |-> 2615599823603823616442 =>
  ↳ ?S:Map </S>
9 <B> .List => ?_ </B>
10 requires (Alpha >Int 0) andBool (Alpha <Int 1000000000000000000000000) //10**22
11 ensures ({?S[Miner in COMP]}:>Int <=Int 0 ) andBool ({?S[Miner in ETH]}:>Int <=Int 0 )
```



Under the Hood- Sushiswap + Uniswap

```
1 claim <k>
2 On UniswapV2 697323163401596485410334513241460920685086001293 swaps for ETH by providing
  ↳ 13000000000000000000000000 COMP and 0 ETH with change 0 fee 1767957155464 ;
3 On Sushiswap Miner swaps for ETH by providing Alpha: Int COMP and 0 ETH with change 0 fee 0 ;
4 On UniswapV2 Miner swaps for Alpha COMP by providing ETH fee 0 ;
5
6 => .K
7 </k>
8 <S> (Sushiswap in COMP) |-> 107495485843438764484770 (Sushiswap in ETH) |-> 49835502094518088853633
  ↳ (UniswapV2 in COMP) |-> 5945498629669852264883 (UniswapV2 in ETH) |-> 2615599823603823616442 =>
  ↳ ?S:Map </S>
9 <B> .List => ?_ </B>
10 requires (Alpha >Int 0) andBool (Alpha <Int 1000000000000000000000000) //10**22
11 ensures ({?S[Miner in COMP]}:>Int <=Int 0 ) andBool ({?S[Miner in ETH]}:>Int <=Int 0 )
```

