

# CS6787: Advanced Machine Learning Systems

CS6787 Lecture 1 — Spring 2026

**Fundamentals  
of Machine  
Learning**



**Machine  
Learning in  
Practice**

**this course**

What's missing in the basic stuff?

**Efficiency!**  
**Scalability!**

Motivation:

Machine learning applications  
involve large amounts of data

**More data → Better services**

**Better systems → More data**

**How do practitioners make  
their systems better?**

# How do we improve our systems?

## Course outline

- Build frameworks/software that make it easy to express & train a machine learning/deep learning model.

### **Part 1**

- Use methods for accelerating convergence of learning algorithms — learn in fewer iterations.

### **Part 2**

- Automatically configure learning systems by using hyperparameter optimization

### **Part 3**

- Use large pre-trained models to improve performance of downstream tasks — “foundation models”

### **Part 4**

- Use methods for improving hardware efficiency — run each iteration faster, with less energy, etc.

### **Part 5**

# Course Format

## One half

Traditional lectures  
Broad description of  
techniques

## One half

Important papers  
Presentations by **you**  
In-class discussions  
Reviews of each paper

# Prerequisites

- Basic ML knowledge (CS 3780)
- Math/statistics knowledge
  - At the level of the entrance exam for CS 3780
- Also useful, but not a prerequisite:
  - Knowledge of computer systems, computer hardware, NLP, and computer vision



# Grading

- Paper presentations
- Discussion participation
- Paper reviews
- Programming assignments
- Final project

# Paper presentations

- Papers listed on the website
  - 20-minute presentation slot for each paper
  - Presenting in groups of two-to-three
- **Signups by Monday!**
  - Survey is on the website
- **Learning goal:**
  - Practice digesting, unpacking, and talking about other people's work

# Paper Reading and Discussion

- Each presentation is followed by a period of questions and breakout discussion
- Please read at least one of the papers before class
  - And at least skim the other paper, so you know what to expect
- Note: grade is not for attendance, but rather on participation and bringing insightful ideas to the table
- **Learning goal: practice how to deeply read and critique a paper in context**

# Paper Reviews

- For each class period, **submit a mock review** of one of the two papers
  - (Only if you are not presenting.)
- Review the paper as if you were doing peer review on a newly submitted work
- Reviews due a few days after our in-class discussion
- **Learning goal: build technical reading and writing skills, and get some sense of how peer review works.**

# Programming Assignments

- Two short assignments in the first part of the semester only
- **Learning goal: become familiar with ML frameworks/tools**
  - ...and the principles that underlie them
  - This will build skills for the final project
  - Especially useful for folks from non-CS background

**Do you guys already know  
PyTorch and deep learning?**

# Final Project

- **Open-ended**: work on what you think is interesting!
  - Learning goal: **do a bit of non-trivial research on your own**
- Groups of **up to three**
- Your proposed project must include:
  - The **implementation** of a machine learning system for some task
  - Exploring one or more of the **techniques discussed in the course**
  - To **empirically evaluate performance** and compare with a baseline, using both a ML-side and systems-side metric

# Late Policy

- This is a graduate level course
- Two free late days for each of the paper reviews and programming assignments
- No late days on the final project
  - To make things easy on the graders
- No late days on the presentations (for obvious reasons)



**Questions?**

## Today's Topic

# Stochastic Gradient Descent: The Workhorse of Machine Learning

CS6787 Lecture 1 — Spring 2026

# But first...an icebreaker activity!

For each person:

- What is your name?
- What are you studying?
- **What do you hope to learn from CS6787?**

Then discuss together:

**Why do we use stochastic gradient descent?**  
(And its related algorithms: Adam, AdaGrad, etc.)

# Optimization

- Much of machine learning can be written as an optimization problem

The diagram shows the optimization problem 
$$\min_{w \in \mathbb{R}^d} \frac{1}{n} \sum_{i=1}^n f(w; x_i)$$
 with three callout boxes. A box labeled "model" points to the parameter  $w$ . A box labeled "loss function" points to the function  $f$ . A box labeled "training examples" points to the input  $x_i$ .

- Example loss functions: logistic regression, linear regression, principal component analysis, neural network loss, empirical risk minimization

# Types of Optimization

- Convex optimization
  - The **easy case**
  - Includes logistic regression, linear regression, SVM

- Non-convex optimization
  - **NP-hard in general**
  - Includes deep learning

A good strategy for ML optimization:

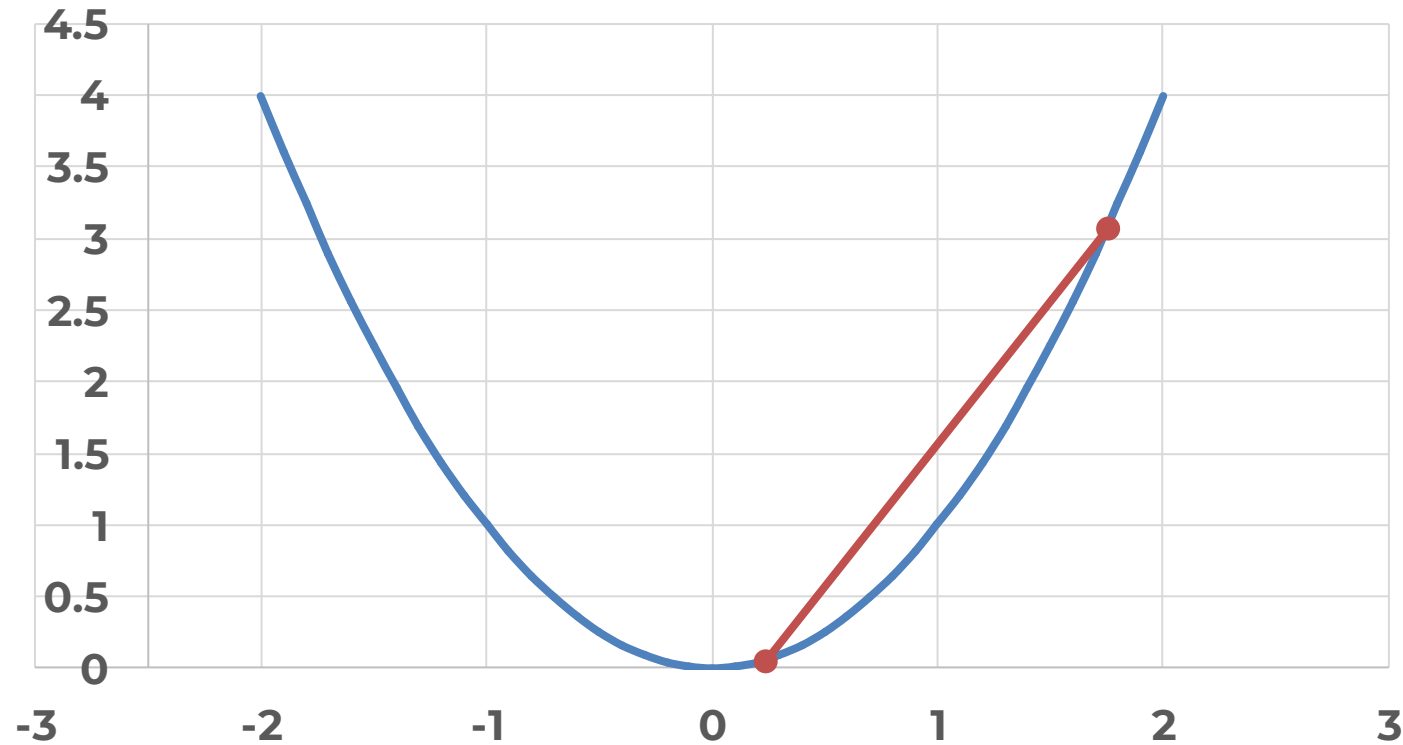
**Build theoretical intuition about techniques from the convex case where we can prove things...**

**...and apply it to better understand more complicated systems.**

# An Abridged Introduction to Convex Functions

# Convex Functions

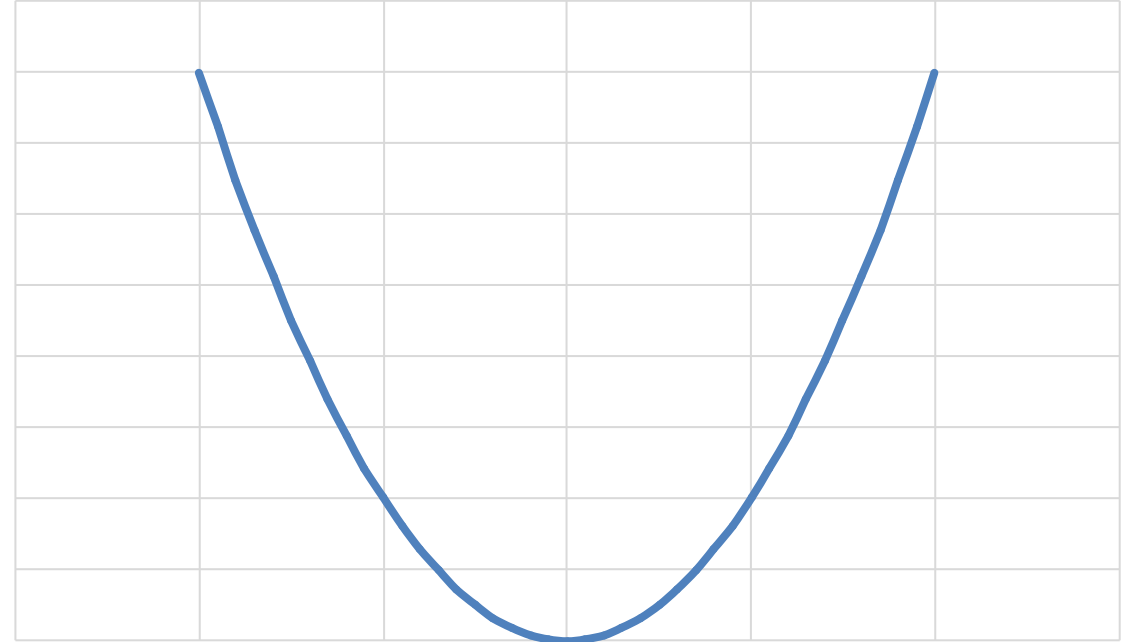
$$\forall \alpha \in [0, 1], f(\alpha x + (1 - \alpha)y) \leq \alpha f(x) + (1 - \alpha)f(y)$$



$$f(x) = x^2$$

# Example: Quadratic

$$f(x) = x^2$$

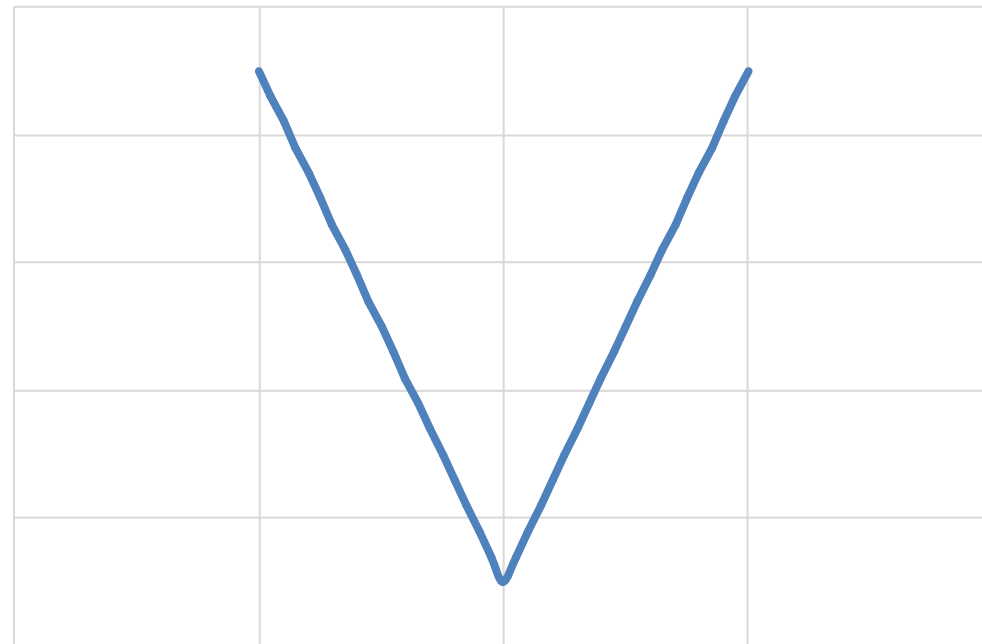


$$\begin{aligned}(\alpha x + (1 - \alpha)y)^2 &= \alpha^2 x^2 + 2\alpha(1 - \alpha)xy + (1 - \alpha)^2 y^2 \\&= \alpha x^2 + (1 - \alpha)y^2 - \alpha(1 - \alpha)(x^2 + 2xy + y^2) \\&\leq \alpha x^2 + (1 - \alpha)y^2\end{aligned}$$



Example: Abs

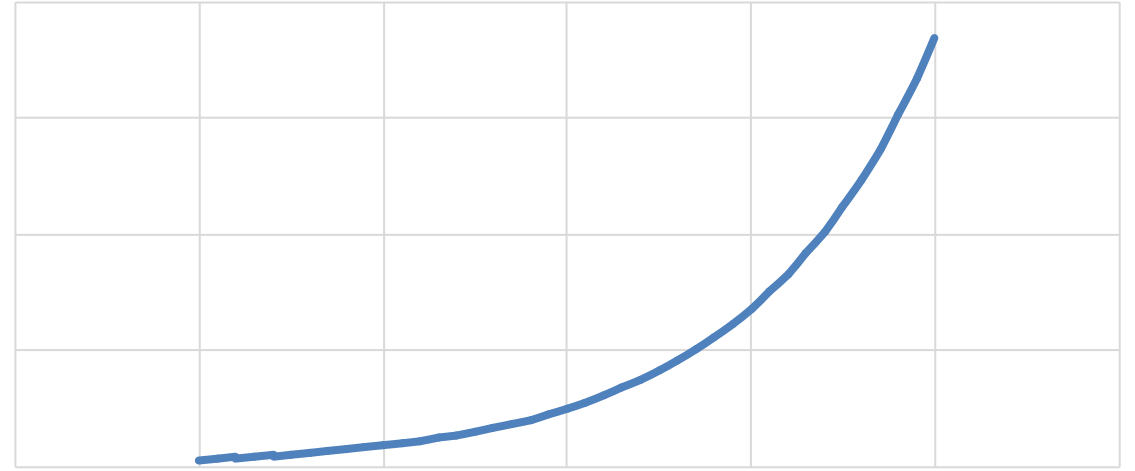
$$f(x) = |x|$$



$$\begin{aligned} |\alpha x + (1 - \alpha)y| &\leq |\alpha x| + |(1 - \alpha)y| \\ &= \alpha|x| + (1 - \alpha)|y| \end{aligned}$$

# Example: Exponential

$$f(x) = e^x$$



$$\begin{aligned} e^{\alpha x + (1-\alpha)y} &= e^y e^{\alpha(x-y)} = e^y \sum_{n=0}^{\infty} \frac{1}{n!} \alpha^n (x-y)^n \\ &\leq e^y \left( 1 + \alpha \sum_{n=1}^{\infty} \frac{1}{n!} (x-y)^n \right) \quad (\text{if } x > y) \\ &= e^y \left( (1-\alpha) + \alpha e^{x-y} \right) \\ &= (1-\alpha)e^y + \alpha e^x \end{aligned}$$

# Properties of convex functions

- Any line segment we draw between two points lies above the curve
- Corollary: every local minimum is a global minimum
  - **Why?**
- This is what makes convex optimization easy
  - It suffices to find a local minimum, because we know it will be global

# Properties of convex functions (continued)

- Non-negative combinations of convex functions are convex

$$h(x) = af(x) + bg(x)$$

- Affine scalings of convex functions are convex

$$h(x) = f(Ax + b)$$

- Compositions of convex functions are **NOT** generally convex
  - Neural nets are like this

$$h(x) = f(g(x))$$

# Convex Functions: Alternative Definitions

- First-order condition

$$\langle x - y, \nabla f(x) - \nabla f(y) \rangle \geq 0$$

- Second-order condition

$$\nabla^2 f(x) \succeq 0$$

- This means that the matrix of second derivatives is positive semidefinite

$$A \succeq 0 \Leftrightarrow \forall x, \langle x, Ax \rangle \geq 0$$

Example: Quadratic

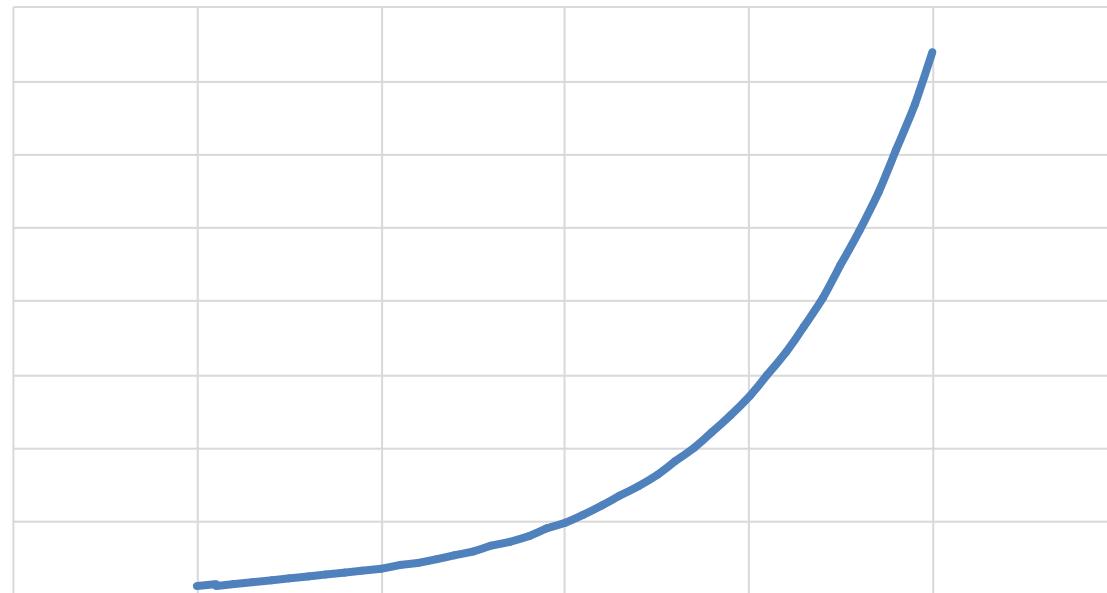
$$f(x) = x^2$$



$$f''(x) = 2 \geq 0$$

# Example: Exponential

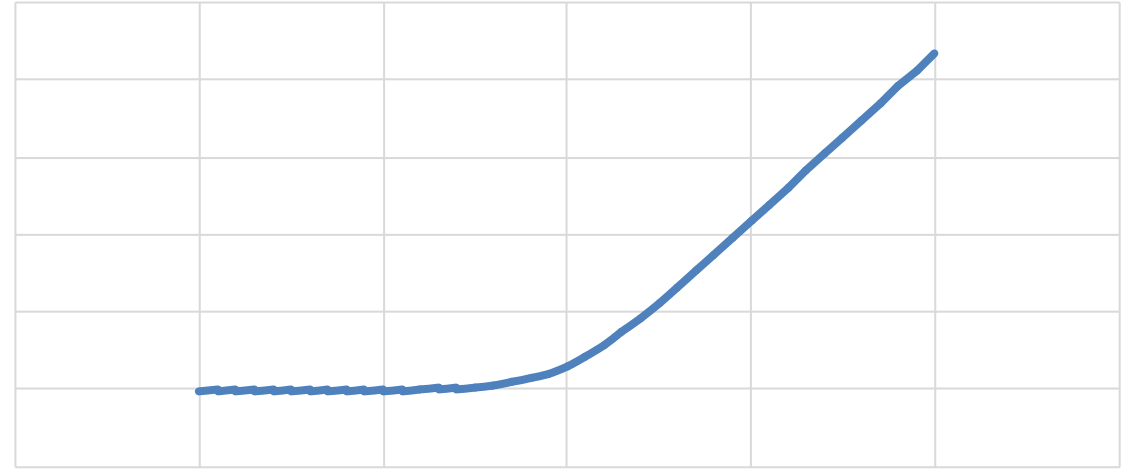
$$f(x) = e^x$$



$$f''(x) = e^x \geq 0$$

# Example: Logistic Loss

$$f(x) = \log(1 + e^x)$$



$$f'(x) = \frac{e^x}{1 + e^x} = \frac{1}{1 + e^{-x}}$$

$$f''(x) = -\frac{-e^{-x}}{(1 + e^{-x})^2} = \frac{1}{(1 + e^x)(1 + e^{-x})} \geq 0.$$



# Strongly Convex Functions

- Basically the easiest class of functions for optimization
  - First-order condition:

$$\langle x - y, \nabla f(x) - \nabla f(y) \rangle \geq \mu \|x - y\|^2$$

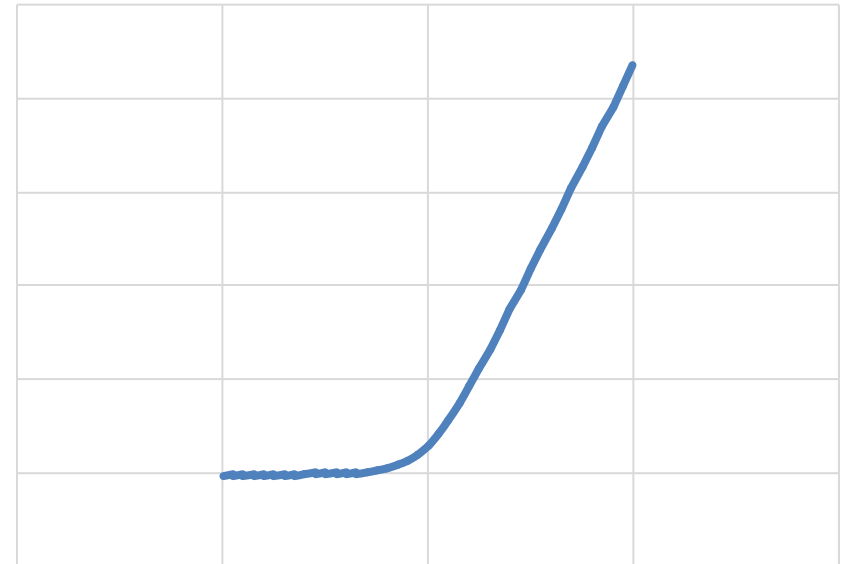
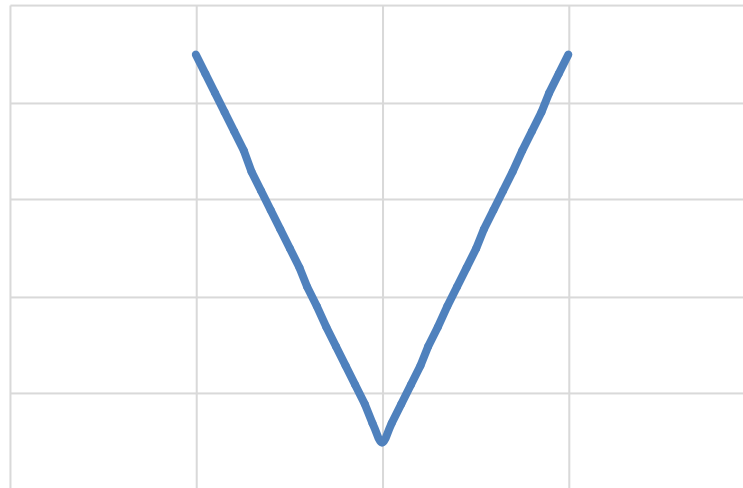
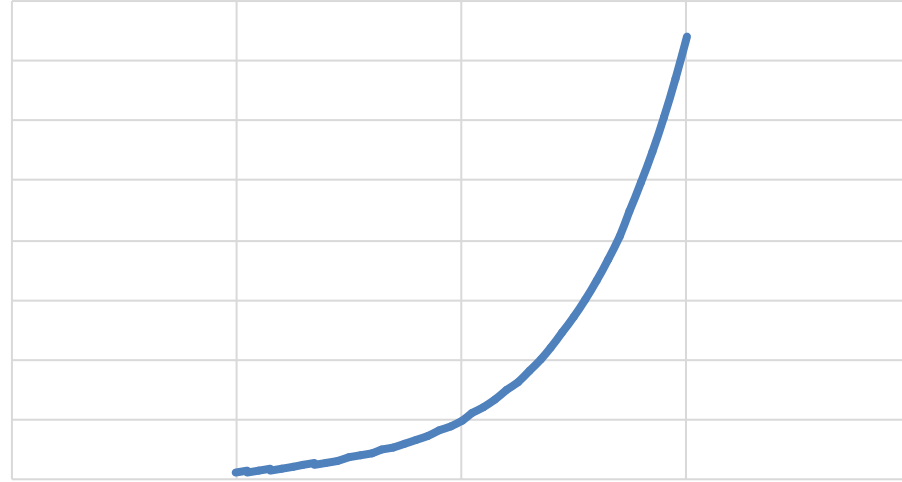
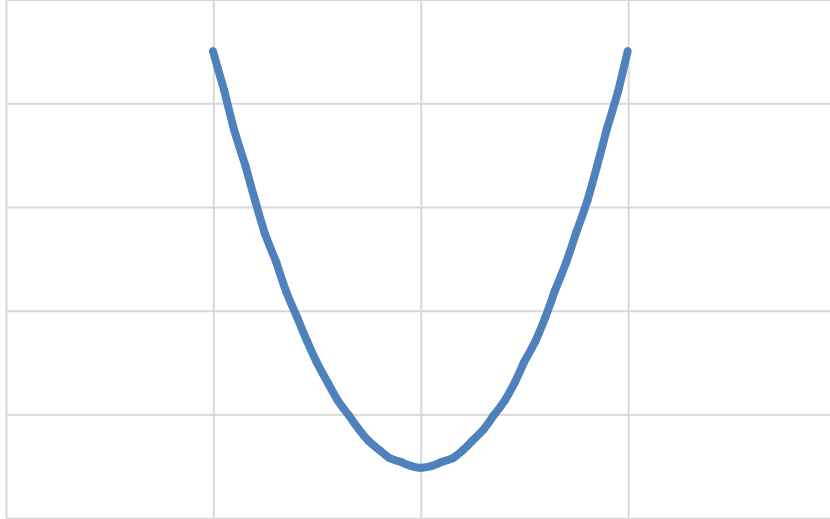
- Second-order condition:

$$\nabla^2 f(x) \succeq \mu I$$

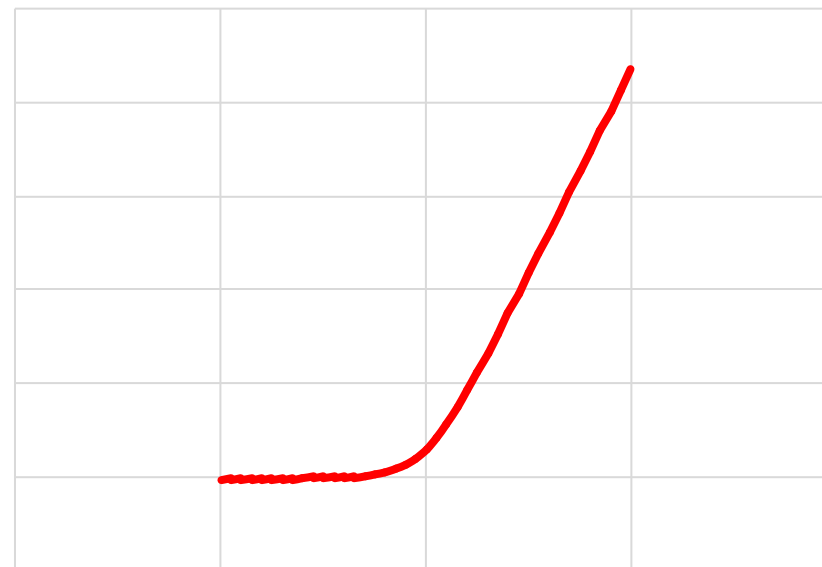
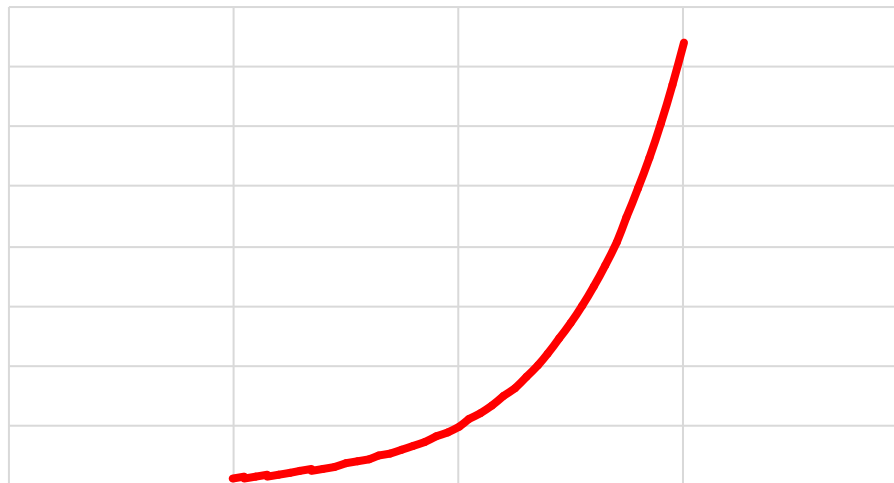
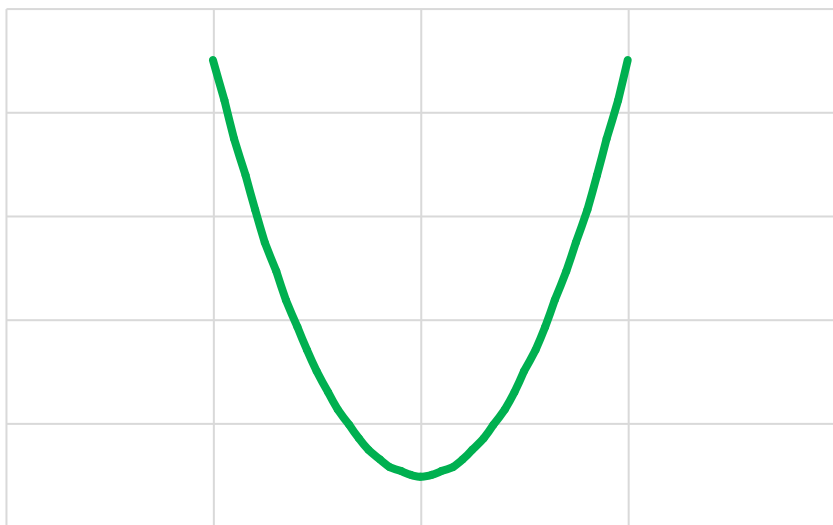
- Equivalently:

$$h(x) = f(x) - \frac{\mu}{2} \|x\|^2 \text{ is convex}$$

# Which of the functions we've looked at are strongly convex?



Which of the functions we've looked at are strongly convex?



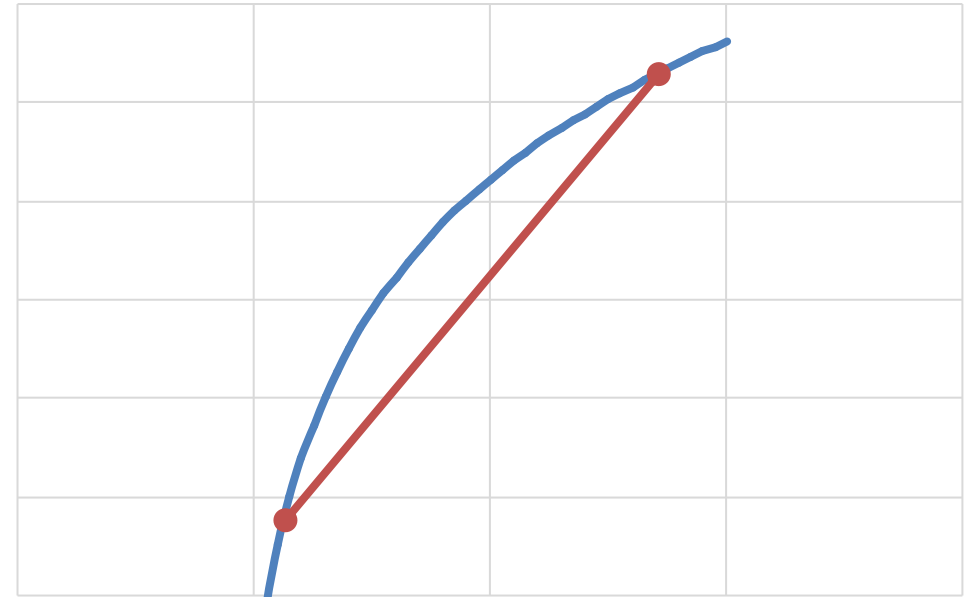
# Concave functions

- A function is concave if its negation is convex

$$f \text{ is convex} \Leftrightarrow h(x) = -f(x) \text{ is concave}$$

- Example:  $f(x) = \log(x)$

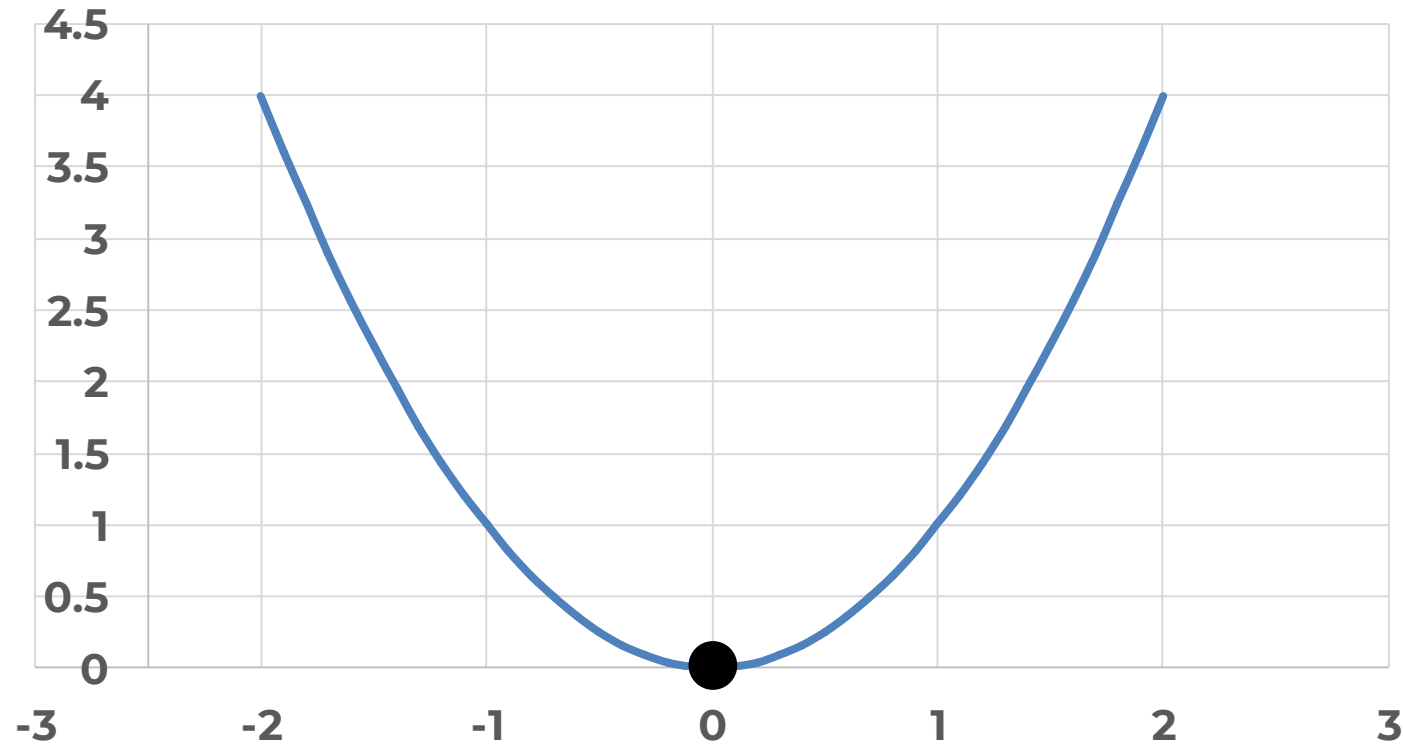
$$f''(x) = -\frac{1}{x^2} \leq 0$$



Why care about convex functions?

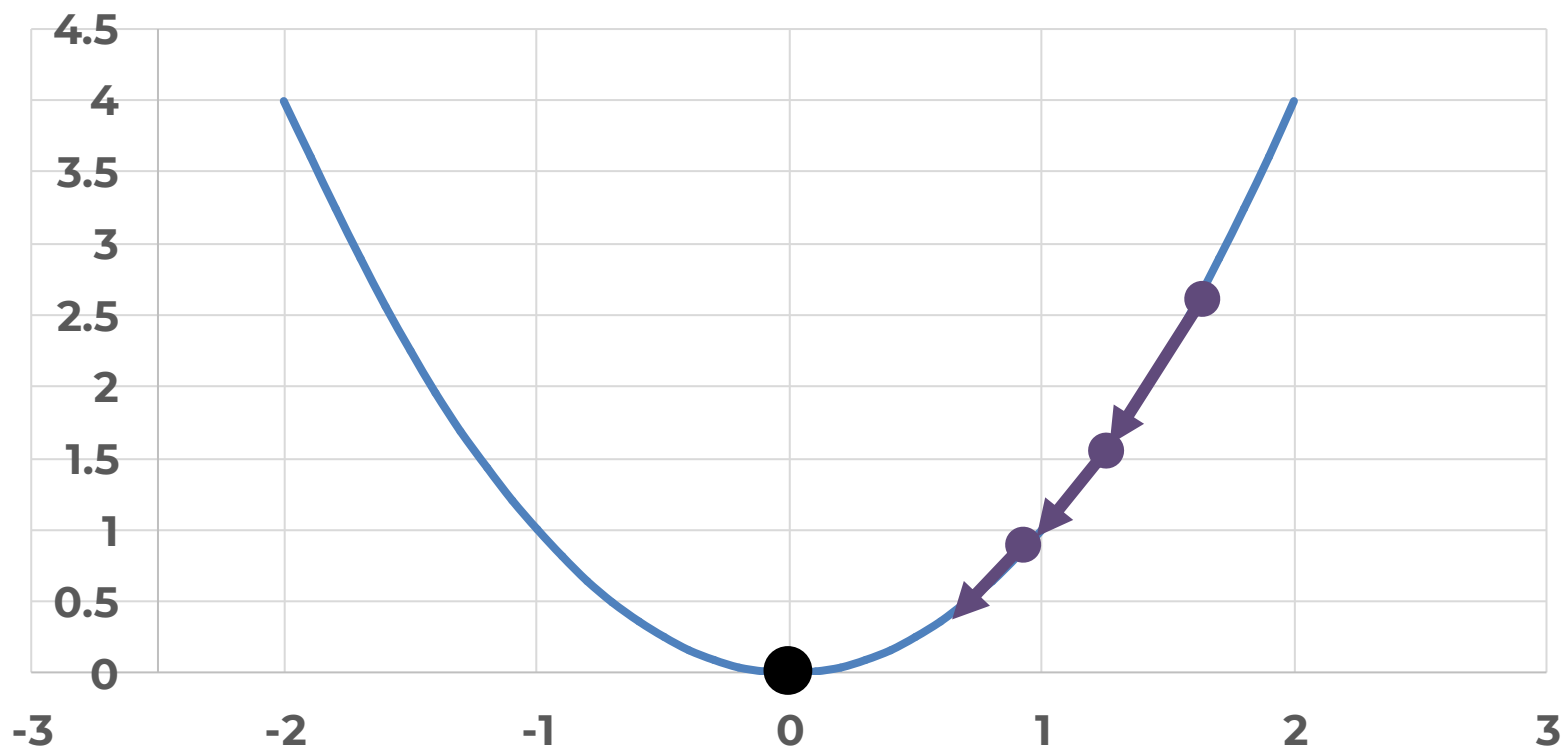
# Convex Optimization

- Goal is to minimize a convex function



# Gradient Descent

$$w \leftarrow w - \alpha \nabla f(w)$$



# Gradient Descent Converges

- A simple proof, but not necessarily the best rate.
- Iterative definition of gradient descent

$$w_{t+1} = w_t - \alpha \nabla f(w_t)$$

- Assumptions/terminology:

Global optimum is  $x^*$

Bounded second derivative  $\mu I \preceq \nabla^2 f(x) \preceq L I$



# Gradient Descent Converges (continued)

$$\begin{aligned}w_{t+1} - w^* &= w_t - w^* - \alpha (\nabla f(w_t) - \nabla f(w^*)) \\&= w_t - w^* - \alpha \nabla^2 f(\zeta_t) (w_t - w^*) \\&= (I - \alpha \nabla^2 f(\zeta_t)) (w_t - w^*) .\end{aligned}$$

Taking the norm

$$\begin{aligned}\|w_{t+1} - w^*\| &\leq \|I - \alpha \nabla^2 f(\zeta_t)\|_2 \cdot \|w_t - w^*\| \\&\leq \max(|1 - \alpha\mu|, |1 - \alpha L|) \cdot \|w_t - w^*\| .\end{aligned}$$

# Gradient Descent Converges (continued)

- So if we set  $\alpha = 2/(L + \mu)$  then

$$\|w_{t+1} - w^*\| \leq \frac{L - \mu}{L + \mu} \cdot \|w_t - w^*\|$$

- And recursively

$$\|w_K - w^*\| \leq \left( \frac{L - \mu}{L + \mu} \right)^K \cdot \|w_0 - w^*\|$$

- Called **convergence at a linear rate** or sometimes (confusingly) exponential rate

# The Problem with Gradient Descent

- Large-scale optimization

$$h(w) = \frac{1}{n} \sum_{i=1}^n f(w; x_i)$$

- Computing the gradient takes  $O(n)$  time

$$\nabla h(w) = \frac{1}{n} \sum_{i=1}^n \nabla f(w; x_i)$$

# Gradient Descent with More Data

- Suppose we add more examples to our training set
  - For simplicity, imagine we just add an extra copy of every training example

$$\nabla h(w) = \frac{1}{2n} \sum_{i=1}^n \nabla f(w; x_i) + \frac{1}{2n} \sum_{i=1}^n \nabla f(w; x_i)$$

- **Same objective function**
  - But gradients take **2x the time to compute** (unless we cheat)
- We want to **scale up to huge datasets**, so how can we do this?

# Stochastic Gradient Descent

- Idea: rather than using the full gradient, just use one training example

- Super fast to compute

$$w_{t+1} = w_t - \alpha \nabla f(w_t, x_{i_t})$$

- In expectation, it's just gradient descent:

$$\mathbf{E}[w_{t+1}] = \mathbf{E}[w_t] - \alpha \cdot \mathbf{E}[\nabla f(w_t, x_{i_t})]$$

$$= \mathbf{E}[w_t] - \alpha \cdot \frac{1}{n} \sum_{i=1}^n \nabla f(w_t, x_i)$$

This is an example selected uniformly at random from the dataset.

# Stochastic Gradient Descent Convergence

- Can SGD converge using just one example to estimate the gradient?

$$\begin{aligned}w_{t+1} - w^* &= w_t - w^* - \alpha (\nabla h(w_t) - \nabla h(w^*)) - \alpha (\nabla f(w_t; x_{i_t}) - \nabla h(w_t)) \\ &= (I - \alpha \nabla^2 h(\zeta_t)) (w_t - w^*) - \alpha (\nabla f(w_t; x_{i_t}) - \nabla h(w_t))\end{aligned}$$

- How do we handle this extra noise term?
- **One answer: bound it using the second moment!**

# Stochastic Gradient Descent Convergence

$$\begin{aligned}\mathbf{E} \left[ \|w_{t+1} - w^*\|^2 \right] &= \mathbf{E} \left[ \left\| (I - \alpha \nabla^2 h(\zeta_t)) (w_t - w^*) - \alpha (\nabla f(w_t; x_{i_t}) - \nabla h(w_t)) \right\|^2 \right] \\&= \mathbf{E} \left[ \left\| (I - \alpha \nabla^2 h(\zeta_t)) (w_t - w^*) \right\|^2 \right] \\&\quad - \alpha \mathbf{E} \left[ (\nabla f(w_t; x_{i_t}) - \nabla h(w_t))^T (I - \alpha \nabla^2 h(\zeta_t)) (w_t - w^*) \right] \\&\quad + \alpha^2 \mathbf{E} \left[ \left\| (\nabla f(w_t; x_{i_t}) - \nabla h(w_t)) \right\|^2 \right] \\&= \mathbf{E} \left[ \left\| (I - \alpha \nabla^2 h(\zeta_t)) (w_t - w^*) \right\|^2 \right] + \alpha^2 \mathbf{E} \left[ \left\| (\nabla f(w_t; x_{i_t}) - \nabla h(w_t)) \right\|^2 \right] \\&\leq (1 - \alpha\mu)^2 \cdot \mathbf{E} \left[ \|w_t - w^*\|^2 \right] + \alpha^2 M\end{aligned}$$

assuming small enough  $\alpha$  and the bound  $\mathbf{E} \left[ \left\| (\nabla f(w; x_i) - \nabla h(w)) \right\|^2 \right] \leq M$ .

# Stochastic Gradient Descent Convergence

- Already we can see that this converges to a fixed point of

$$\lim_{t \rightarrow \infty} \mathbf{E} \left[ \|w_t - w^*\|^2 \right] \leq \frac{\alpha M}{2\mu - \alpha\mu^2}$$

- This phenomenon is called converging to a **noise ball**
  - Rather than approaching the optimum, SGD (with a constant step size) converges to a region of low variance around the optimum
  - This is okay for a lot of applications that **only need approximate solutions**



**Stochastic gradient descent  
is super popular.**

But how SGD is implemented in practice is not exactly what I've just shown you...

...and we'll see how it's different in the upcoming lectures.

# To Do

- If you have any papers you particularly want us to cover or topics you think might be interesting, send me an email before noon-ish tomorrow.
- Be on the lookout for an email with the paper presentation signup survey.