

①

Today: semantic parsing
with CCG

Combinatory
Categorical
Grammar

$f: \text{sentences} \xrightarrow{\text{CCG}} \lambda$ ← learn

- Lambda calculus]
- CCG]
- Learning

②

Lambda Calc.

- Formal rep. lang.
- higher order functions $\longrightarrow$ you can take func. as arguments
- typed

Type Typing System:

arg1: city
arg2: student
return: t

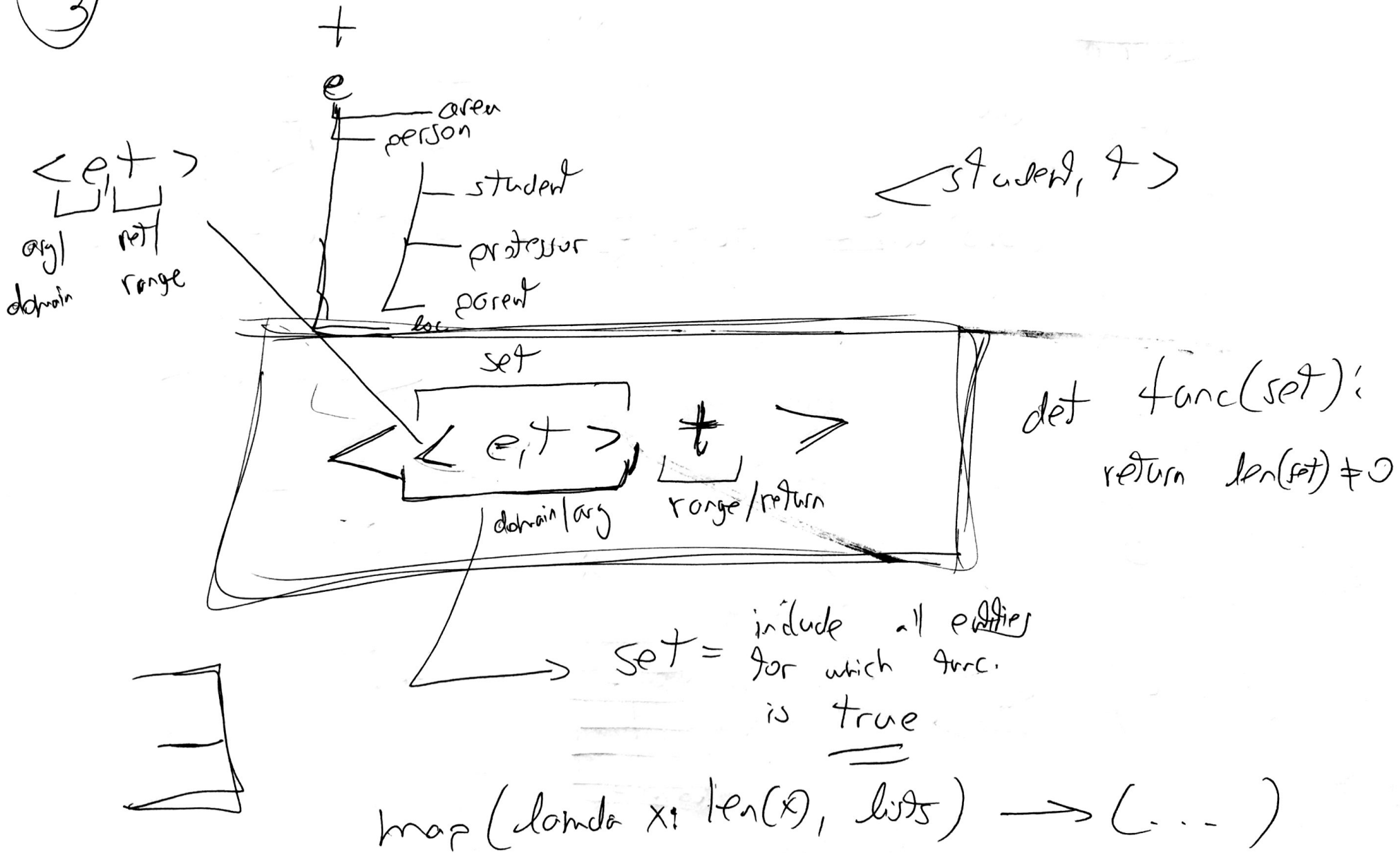
- entity, truth value, event, city, airport, student

- complex type: $\langle \rangle$, $\langle \rangle$
 domain range

$\langle \langle \text{city, student} \rangle, t \rangle$

$\langle \text{city}, \langle \text{student}, t \rangle \rangle$

3



④

~~Land~~

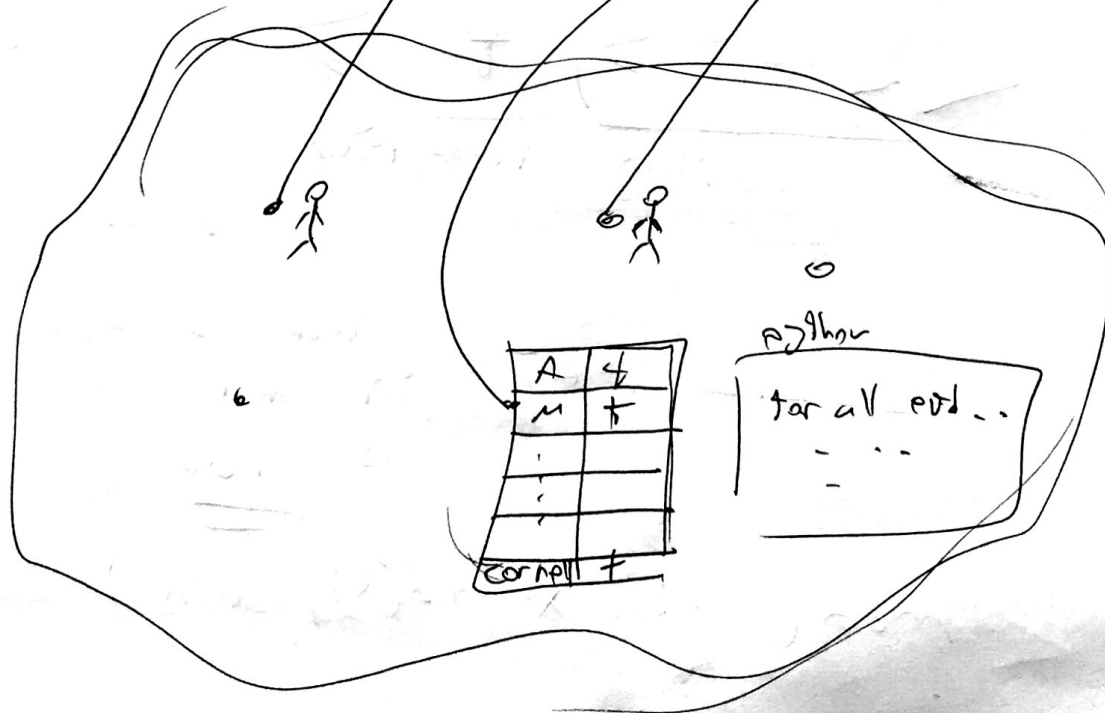
λ -calculus!

- 1) constant - $(\text{ALAN}_{\text{student}}, \text{MAX}_{\text{student}}, \text{Studies_in})$
- 2)
- 3)
- 4)

$\text{Student}_{\langle \text{entity}, + \rangle}$

$\text{MAX}_{\text{student}}, \text{Studies_in}$

$\langle \text{student}, \langle \text{loc}, + \rangle \rangle$



5

2) Variable x_e y_t $\langle \text{student}, t \rangle$

1

3) Literal $\text{predicate}(\text{term}, \dots, \text{term})$

$\text{Student}_{\langle \text{entity}, t \rangle}(\text{ALAN}_{\text{E}_{\text{student}}})$

$\text{studies-in}(\text{ALAN}_{\text{E}})$

$\langle \text{loc}, t \rangle$

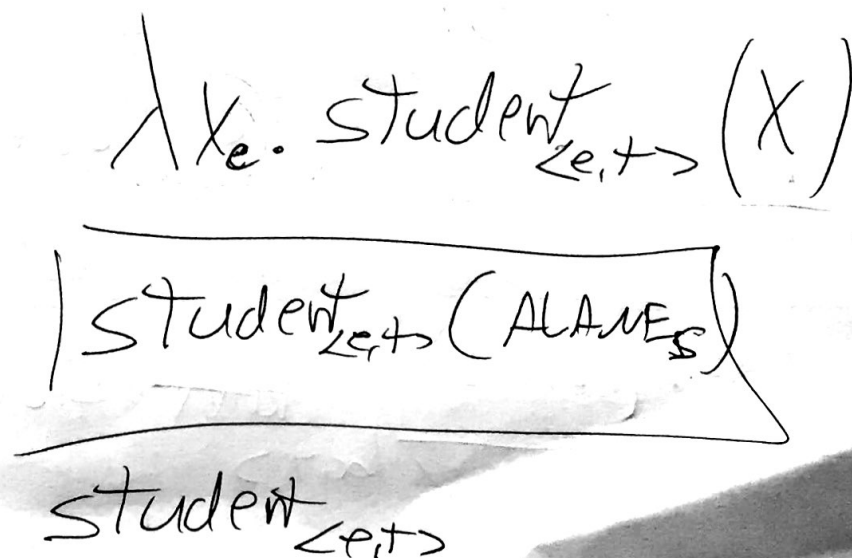
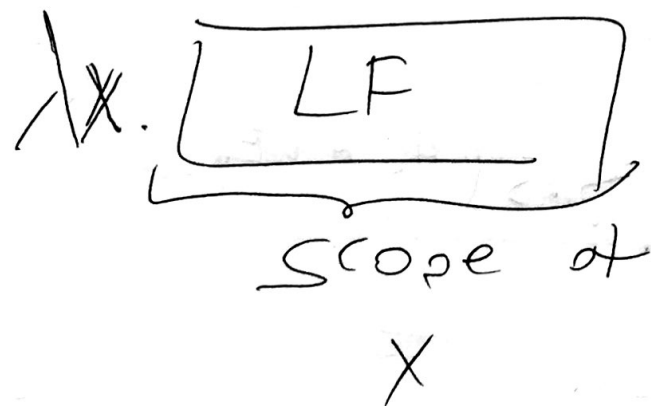
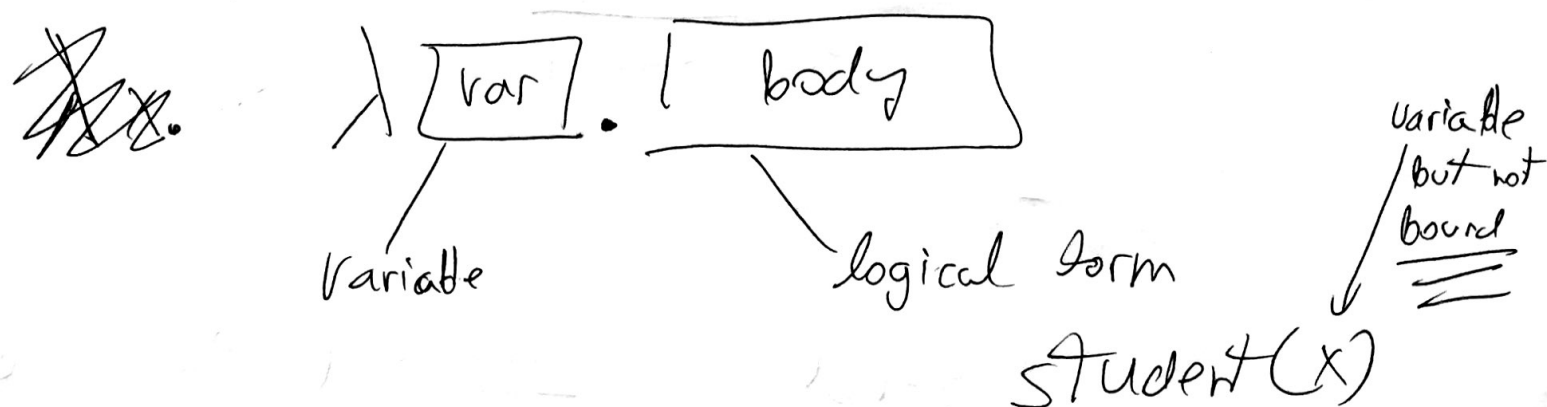
~~studies-in~~

$\text{studies-in}_{\langle \text{student}, \langle \text{loc}, t \rangle \rangle}(\text{ALAN}_{\text{E}_{\text{student}}}, \text{Cornell}_{\text{area}})$

④

4) Lambda term

— anonymous function



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$$\text{set } \{e \mid f(e) = \text{true}\}$$

$$f = \lambda x. \text{student}(x)$$

$$f(5, 6)$$

$$\underline{5+6}$$

function: $\text{arg} \rightarrow \text{t/f}$

if the arg
is a student

conj

$$\lambda(\text{arg1}, \text{arg2})$$

$$\lambda \langle t, \langle t, t \rangle \rangle$$

type
of

disj

$$\lambda(\lambda(\text{arg1}, \text{arg2}), \text{arg3}) \Rightarrow \text{arg1} \wedge \text{arg2} \wedge \text{arg3}$$

$$\text{arg1} \vee \text{arg2} \vee \text{arg3} \vee \text{arg4} \dots$$

~~arg1~~

⑥

- application
- composition

Application

$(\boxed{LF}) (\boxed{arg})$

$(\lambda x. \text{student}(x)) (ESI\mathcal{N})$

$\downarrow$
ESI $\mathcal{N}$

|

$\text{student}(x) \xrightarrow{x \rightarrow ESI\mathcal{N}} \text{student}(ESI\mathcal{N})$

~~$(\lambda x. \text{student}(x)) (\lambda x. \text{student}(x))$~~ bad & going

⑦

Composition

$$g \circ f = g(f(x)) \leftarrow \text{func. composition}$$

$$g = \lambda t. \lambda x. t(x) \mid \text{red}(x)$$

↓
func

$$f = \lambda x. t(x) \mid \text{square}(x)$$

↑
func

~~$$\lambda t. \lambda x. t(x)$$~~

$$\lambda t. \lambda x. t(x) \mid \text{red}(x) \mid \text{square}(x)$$

⑧

Alone is a student.

$\Rightarrow$ CCG

- Categorical formalism

- many symbols $\rightarrow$ unbounded
- very few rules

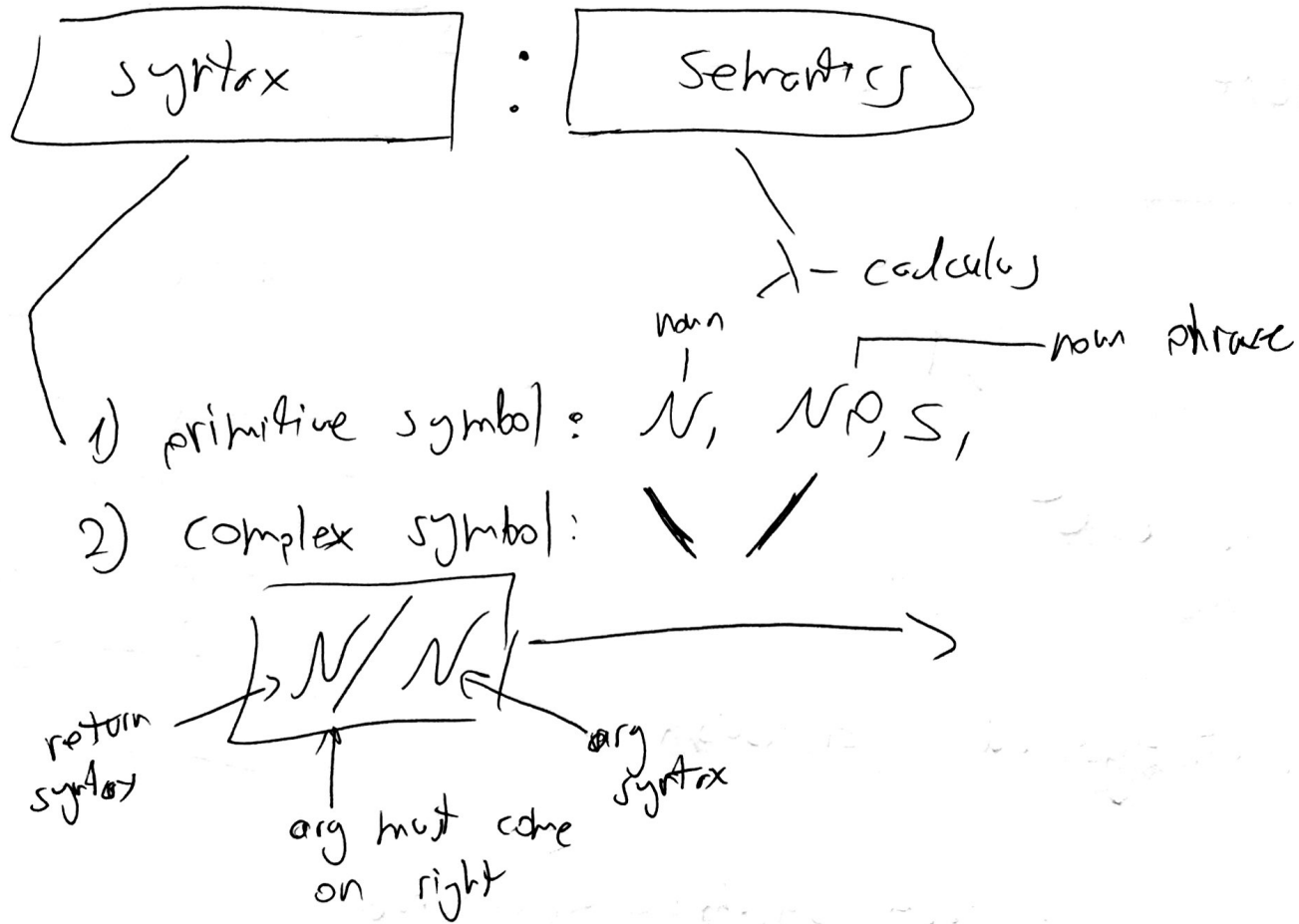
- interface for
syntax - semantics

CFG

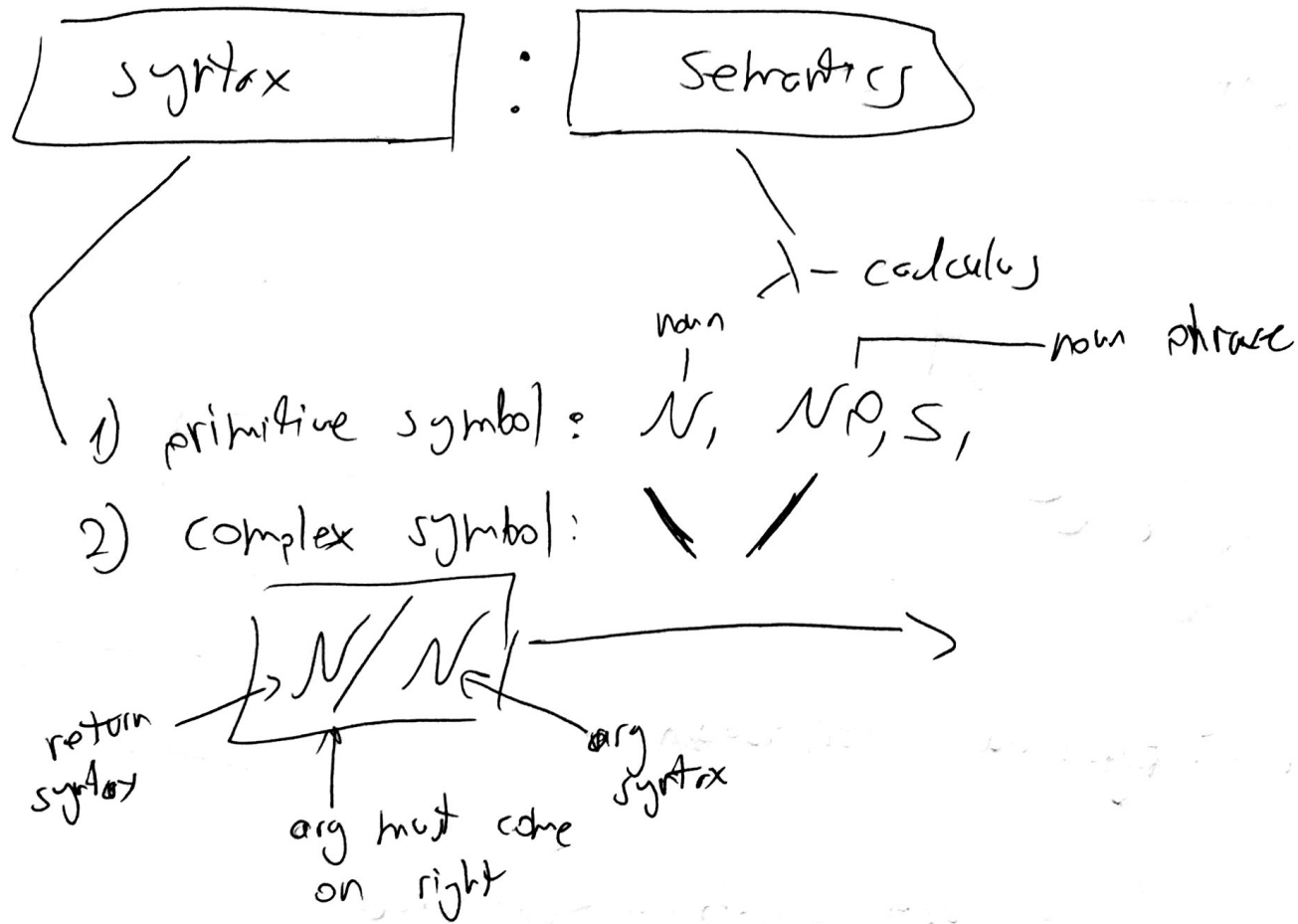
- set of symbols
 $A, B, C, \dots$
- set of rules
 $A \rightarrow BCD$

categories

9



9



Function Application

$$\begin{aligned} & (\lambda f_{\langle\langle e,t\rangle,\langle e,t\rangle\rangle}.f(\lambda x_e.\text{book}_{\langle e,t\rangle}(x)))(\lambda g_{\langle e,t\rangle}.\lambda y_e.g(y) \wedge \text{red}_{\langle e,t\rangle}(y)) \\ & \mapsto (\lambda g_{\langle e,t\rangle}.\lambda y_e.g(y) \wedge \text{red}_{\langle e,t\rangle}(y))(\lambda x_e.\text{book}_{\langle e,t\rangle}(x)) \\ & \mapsto \lambda y_e.(\lambda x_e.\text{book}_{\langle e,t\rangle}(x))(y) \wedge \text{red}_{\langle e,t\rangle}(y) \\ & \mapsto \lambda y_e.\text{book}_{\langle e,t\rangle}(y) \wedge \text{red}_{\langle e,t\rangle}(y) \end{aligned}$$

Function Composition

$$g_{\langle\langle e,t\rangle,\langle e,t\rangle\rangle} = \lambda h_{\langle e,t\rangle}.\lambda x_e.h(x) \wedge \text{yellow}(x)$$

$$f_{\langle\langle e,t\rangle,\langle e,t\rangle\rangle} = \lambda k_{\langle e,t\rangle}.\lambda y_e.k(y) \wedge \text{square}(y)$$

Let $A_{\langle e,t\rangle}$ be a $\langle e,t\rangle$ -typed logical expression

$$\begin{aligned} g_{\langle\langle e,t\rangle,\langle e,t\rangle\rangle}(A_{\langle e,t\rangle}) &= (\lambda h_{\langle e,t\rangle}.\lambda x_e.h(x) \wedge \text{yellow}(x))(A_{\langle e,t\rangle}) = \\ &= (\lambda x_e.h(x) \wedge \text{yellow}(x))[h \mapsto A_{\langle e,t\rangle}] = \\ &= \lambda x_e.A_{\langle e,t\rangle}(x) \wedge \text{yellow}(x) \end{aligned}$$

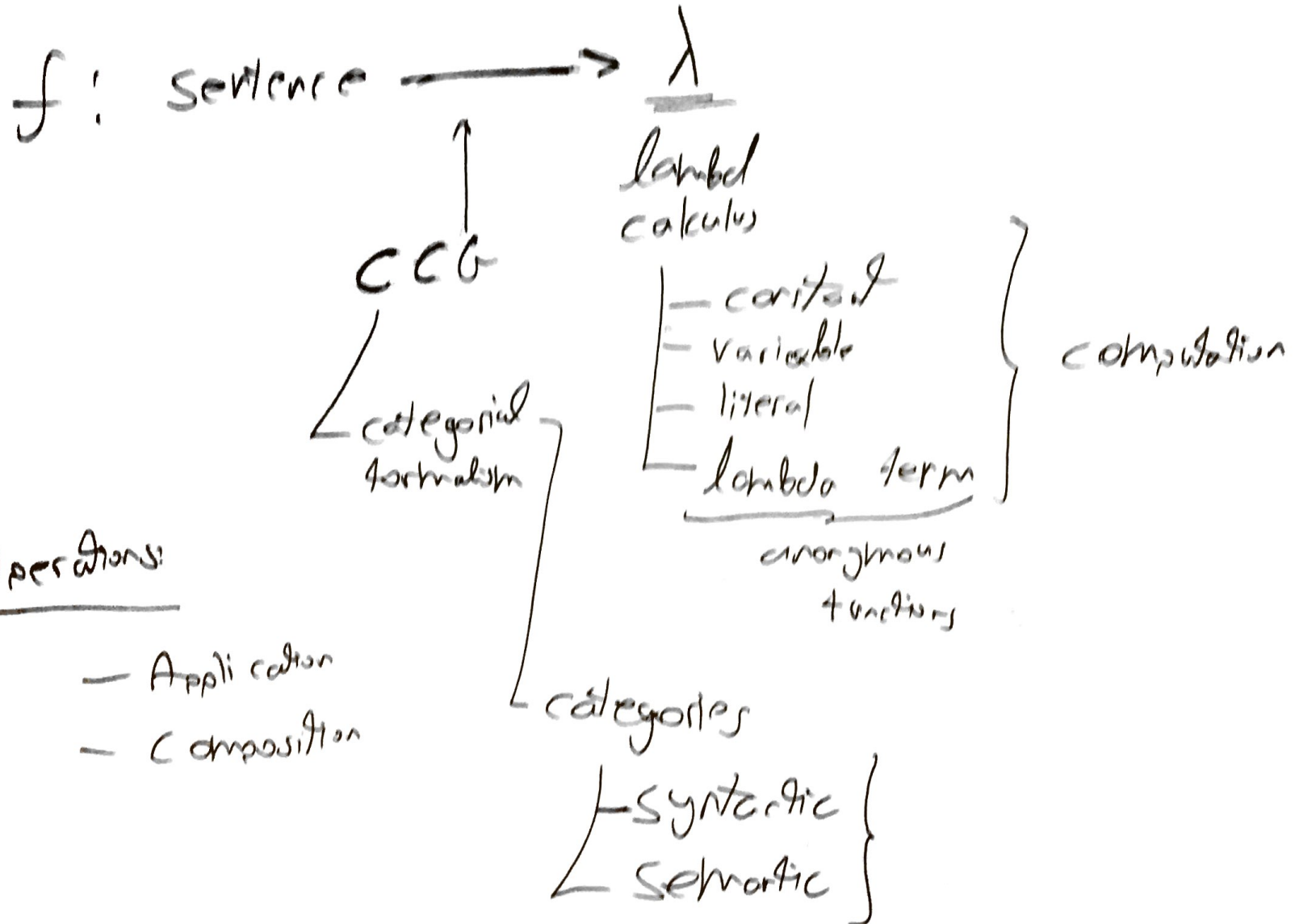
$$\begin{aligned} f_{\langle\langle e,t\rangle,\langle e,t\rangle\rangle}(h_{\langle\langle e,t\rangle,\langle e,t\rangle\rangle}(A_{\langle e,t\rangle})) &= \\ &= (\lambda k_{\langle e,t\rangle}.\lambda y_e.k(y) \wedge \text{square}(y))(\lambda x_e.A_{\langle e,t\rangle}(x) \wedge \text{yellow}(x)) = \\ &= (\lambda y_e.k(y) \wedge \text{square}(y))[k \mapsto \lambda x_e.A_{\langle e,t\rangle}(x) \wedge \text{yellow}(x)] = \\ &= \lambda y_e.(\lambda x_e.A_{\langle e,t\rangle}(x) \wedge \text{yellow}(x))(y) \wedge \text{square}(y) = \\ &= \lambda y_e.(A_{\langle e,t\rangle}(y) \wedge \text{yellow}(y))[x \mapsto y] \wedge \text{square}(y) = \\ &= \lambda y_e.A_{\langle e,t\rangle}(y) \wedge \text{yellow}(y) \wedge \text{square}(y) \end{aligned}$$

Add a new variable and mapping: $\lambda z_{\langle e,t\rangle}.f_{\langle\langle e,t\rangle,\langle e,t\rangle\rangle}(g_{\langle\langle e,t\rangle,\langle e,t\rangle\rangle}(A_{\langle e,t\rangle}))[A \mapsto z] =$

$$\begin{aligned} &= (\lambda z_{\langle e,t\rangle}.\lambda y_e.A_{\langle e,t\rangle}(y) \wedge \text{yellow}(y) \wedge \text{square}(y))[A \mapsto z] = \\ &= \lambda z_{\langle e,t\rangle}.\lambda y_e.z(y) \wedge \text{yellow}(y) \wedge \text{square}(y) = (f_{\langle\langle e,t\rangle,\langle e,t\rangle\rangle} \cdot g_{\langle\langle e,t\rangle,\langle e,t\rangle\rangle})_{\langle\langle e,t\rangle,\langle e,t\rangle\rangle} \end{aligned}$$

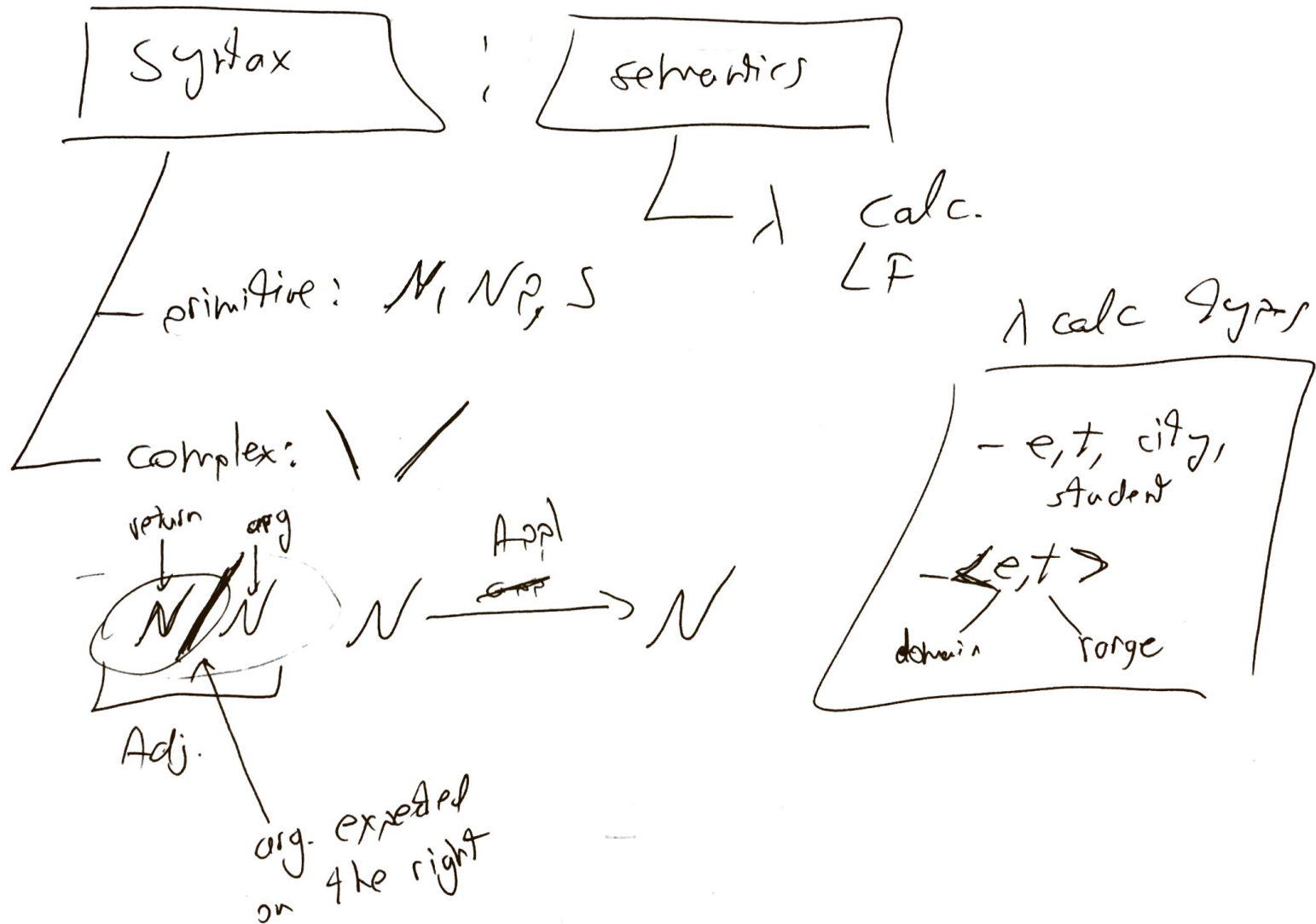
①

Goal: recover formal meaning representation



2

Categories



3

$$\begin{array}{c} \mathcal{N}/\mathcal{N} \\ \lambda t \lambda x. t(x) \wedge \text{red}(x) \\ \hline \downarrow \\ \langle e, t \rangle \end{array}$$

$f(x)$
↑
variable

$$\mathcal{N} \longrightarrow \lambda x. \text{car}(x) \wedge \text{red}(x)$$

$$\left(\lambda t \lambda x. t(x) \wedge \text{red}(x) \right) \left(\lambda x. \text{car}(x) \right)$$

$$\lambda x. \left(\lambda x. \text{car}(x) \right)(x) \wedge \text{red}(x)$$

$$\lambda x. \text{car}(x) \wedge \text{red}(x)$$

④ ADJ
 $\lambda x. \text{square}(x)$

$\lambda x. \text{car}(x) \text{red}(x)$

I ADJ
 $\lambda x. \text{red}(x)$

$\lambda + \lambda x. \text{car}(x) \text{red}(x)$

II $\left[\begin{array}{l} N/N \\ \lambda + \lambda x. f(x) \text{red}(x) \end{array} \right] \lambda x. \text{car}(x)$ + recursion

5

lexicon

rules

λ - iota $\rightarrow$ selection operator

consuming
arg $\rightarrow$ constraint

set of
of a
certain
type

move

S

$\lambda a. \text{move}(a)$

events

for word

S/S

$\lambda t \lambda a. t(a)$
 $\lambda \text{dir}(a, F)$

to

$S/S/NP$

$\lambda x \lambda t \lambda a. t(a) \lambda$
 $\text{dest}(a, x)$

the

NP/N

$\lambda t. \lambda(t)$

chair

N

$\lambda x. \text{chair}(x)$

NP

$\lambda(\lambda x. \text{chair}(x))$

$\lambda a. \text{move}(a) \lambda \text{dir}(a, F)$

S/S

$\lambda t \lambda a. t(a) \lambda \text{dest}(a, \lambda(\lambda x. \text{chair}(x)))$

LF $\rightarrow \lambda a. \text{move}(a) \lambda \text{dir}(a, F) \lambda \text{dest}(a, \lambda(\lambda x. \text{chair}(x)))$

Complex Conjunction with Composition

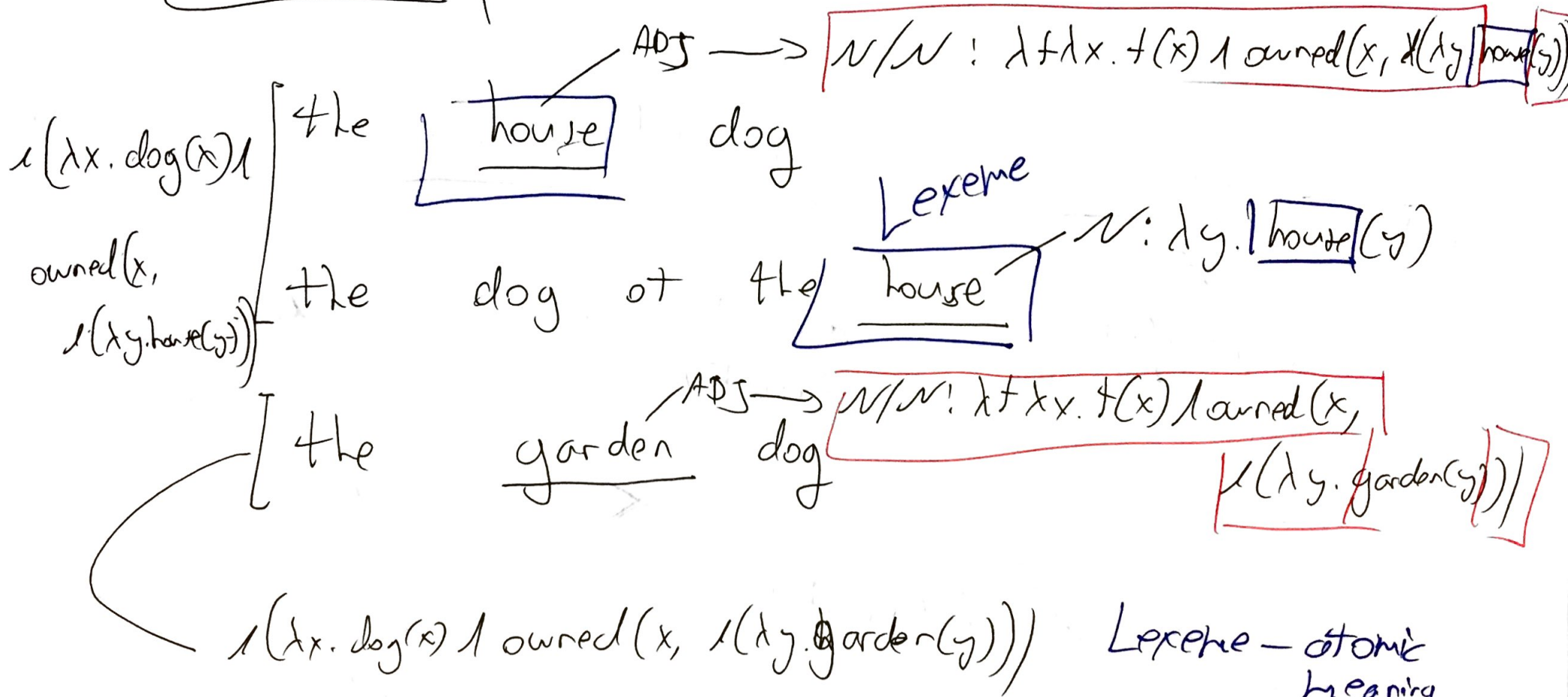
$$\begin{array}{c}
 \begin{array}{c} \text{square} \\ \hline N/N \\ \lambda f.\lambda x.f(x) \wedge \text{square}(x) \end{array} \quad \begin{array}{c} \text{blue} \\ \hline N/N \\ \lambda f.\lambda x.f(x) \wedge \text{blue}(x) \end{array} \quad \begin{array}{c} \text{or} \\ \hline (N/N) \backslash (N/N) / (N/N) \\ \lambda h.\lambda g.\lambda f.\lambda x.f(x) \wedge (g(\lambda y.\text{true}, x) \vee f(\lambda y.\text{true}, x)) \end{array} \quad \begin{array}{c} \text{round} \\ \hline N/N \\ \lambda f.\lambda x.f(x) \wedge \text{round}(x) \end{array} \quad \begin{array}{c} \text{yellow} \\ \hline N/N \\ \lambda f.\lambda x.f(x) \wedge \text{yellow}(x) \end{array} \quad \begin{array}{c} \text{pillow} \\ \hline N \\ \lambda x.\text{pillow}(x) \end{array} \\
 \hline
 \begin{array}{c} N/N \\ \lambda f.\lambda x.f(x) \wedge \text{square}(x) \wedge \text{blue}(x) \end{array} \xrightarrow{\mathbf{B}} \quad \begin{array}{c} N/N \\ \lambda f.\lambda x.f(x) \wedge \text{round}(x) \wedge \text{yellow}(x) \end{array} \xrightarrow{\mathbf{B}} \\
 \hline
 \begin{array}{c} (N/N) \backslash (N/N) \\ \lambda g.\lambda f.\lambda x.f(x) \wedge (g(\lambda y.\text{true}, x) \vee (\text{round}(x) \wedge \text{yellow}(x))) \end{array} \xrightarrow{\quad} \\
 \hline
 \begin{array}{c} N/N \\ \lambda f.\lambda x.f(x) \wedge ((\text{square}(x) \wedge \text{blue}(x)) \vee (\text{round}(x) \wedge \text{yellow}(x))) \end{array} \xrightarrow{\quad} \\
 \hline
 \begin{array}{c} N \\ \lambda x.\text{pillow}(x) \wedge ((\text{square}(x) \wedge \text{blue}(x)) \vee (\text{round}(x) \wedge \text{yellow}(x))) \end{array} \xrightarrow{\quad}
 \end{array}$$

6

lexicon

the $\vdash N/N: \lambda t. \lambda (t)$

Templates



Lexeme - atomic meaning
w/o compositionality
Template - compositionality
of category

7

Factored Lexicon

Original Lexicon

flight $\vdash S|NP : \lambda x. \underline{flight}(x)$

flight $\vdash S|NP/(S|NP) : \lambda f. \lambda x. \underline{flight}(x) \wedge f(x)$

flight $\vdash S|NP \setminus (S|NP) : \lambda f. \lambda x. \underline{flight}(x) \wedge f(x)$

ground transport $\vdash S|NP : \lambda x. trans(x)$

ground transport $\vdash S|NP/(S|NP) : \lambda f. \lambda x. \underline{trans}(x) \wedge f(x)$

ground transport $\vdash S|NP \setminus (S|NP) : \lambda f. \lambda x. \underline{trans}(x) \wedge f(x)$

Factored Lexicon

(flight, {flight})

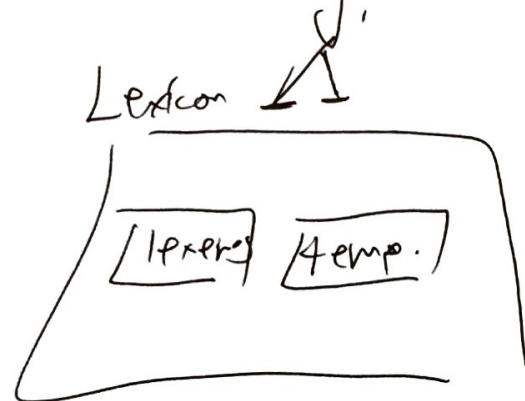
(ground transport, {trans})

$\lambda(\omega, \{v_i\}_1^n). [\omega \vdash S|NP : \lambda x. v_1(x)]$

$\lambda(\omega, \{v_i\}_1^n). [\omega \vdash S|NP/(S|NP) : \lambda f. \lambda x. v_1(x) \wedge f(x)]$

$\lambda(\omega, \{v_i\}_1^n). [\omega \vdash S|NP \setminus (S|NP) : \lambda f. \lambda x. v_1(x) \wedge f(x)]$

Learning:



Helper functions:

- validation func: $V(y) \rightarrow \text{t/f}$
 - genlex - lexical generation: $\text{genlex}(x, V; \Lambda, \Theta)$
- Annotations for $\text{genlex}(x, V; \Lambda, \Theta)$:
- x : (over) generate potential lexical entries
 - V : parse
 - Λ : lexicon
 - Θ : weights

Structured Perceptron

- Simple additive updates
 - Only requires efficient decoding (argmax)
 - Closely related to MaxEnt and other feature rich models
 - Provably finds linear separator in finite updates, if one exists
- Challenge: learning with hidden variables

Structured Perceptron

Data: $\{(x_i, y_i) : i = 1 \dots n\}$

For $t = 1 \dots T$:

For $i = 1 \dots n$:

$$y^* \leftarrow \arg \max_y \langle \theta, \Phi(x_i, y) \rangle$$

If $y^* \neq y_i$:

$$\theta \leftarrow \theta + \Phi(x_i, y_i) - \Phi(x_i, y^*)$$

[iterate epochs]

[iterate examples]

[predict]

[check]

[update]

weight/parameters

feature
function

value

gold
label

argmax

One Derivation of the Perceptron

Log-linear model: $p(y|x) = \frac{e^{w \cdot f(x,y)}}{\sum_{y'} e^{w \cdot f(x,y')}}$

Step 1: Differentiate, to maximize data log-likelihood

$$update = \sum_i f(x_i, y_i) - E_{p(y|x_i)} f(x_i, y)$$

Step 2: Use online, stochastic gradient updates, for example i :

$$update_i = f(x_i, y_i) - E_{p(y|x_i)} f(x_i, y)$$

Step 3: Replace expectations with maxes (Viterbi approx.)

$$update_i = f(x_i, y_i) - f(x_i, y^*) \text{ where } y^* = \arg \max_y w \cdot f(x_i, y)$$

Hidden Variable Perceptron

Data: $\{(x_i, y_i) : i = 1 \dots n\}$

For $t = 1 \dots T$:

For $i = 1 \dots n$:

$y^*, h^* \leftarrow \arg \max_{y, h} \langle \theta, \Phi(x_i, h, y) \rangle$ [iterate epochs] [predict]

If $y^* \neq y_i$: [check]

$h' \leftarrow \arg \max_h \langle \theta, \Phi(x_i, h, y_i) \rangle$ [predict hidden]

$\theta \leftarrow \theta + \Phi(x_i, h', y_i) - \Phi(x_i, h^*, y^*)$ [update]

hidden
variables



The Perceptron with Hidden Variables

Log-linear

model: $p(y|x) = \sum_h p(y, h|x)$

$$p(y, \overset{\text{hidden variable}}{h}|x) = \frac{e^{w \cdot f(x, h, y)}}{\sum_{y', h'} e^{w \cdot f(x, h', y')}}$$

Step 1: Differentiate marginal, to maximize data log-likelihood

$$update = \sum_i E_{p(h|y_i, x_i)}[f(x_i, h, y_i)] - E_{p(y, h|x_i)}[f(x_i, h, y)]$$

Step 2: Use online, stochastic gradient updates, for example i :

$$update_i = E_{p(y_i, h|x_i)}[f(x_i, h, y_i)] - E_{p(y, h|x_i)}[f(x_i, h, y)]$$

Step 3: Replace expectations with maxes (Viterbi approx.)

$$update_i = f(x_i, h', y_i) - f(x_i, h^*, y^*) \text{ where}$$

$$y^*, h^* = \arg \max_{y, h} w \cdot f(x_i, h, y) \quad \text{and} \quad h' = \arg \max_h w \cdot f(x_i, h, y_i)$$

Hidden Variable Perceptron

- No known convergence guarantees
 - Log-linear version is non-convex
- Simple and easy to implement
 - Works well with careful initialization
- Modifications for semantic parsing
 - Lots of different hidden information
 - Can add a margin constraint, do probabilistic version, etc.

Learning Algorithm

Initialize θ using Λ_0 , $\Lambda \leftarrow \Lambda_0$

For $t = 1 \dots T, i = 1 \dots n$:

Step 1: (Lexical generation)

Step 2: (Update parameters)

Output: Parameters θ and lexicon Λ

- Online

- Input:

$$\{(x_i, \mathcal{V}_i) : i = 1 \dots n\}$$

- 2 steps:

- Lexical generation

- Parameter update

Initialize θ using Λ_0 , $\Lambda \leftarrow \Lambda_0$

Initial lexicon

lexicon of our grammar

For $t = 1 \dots T, i = 1 \dots n$:

iteration

Step 1: (Lexical generation)

a. Set $\lambda_G \leftarrow \text{GENLEX}(x_i, v_i; \Lambda, \theta)$,
 $\underline{\lambda} \leftarrow \underline{\Lambda} \cup \underline{\lambda}_G$

temp. lexicon

b. Let Y be the k highest scoring parses from $\text{GEN}(x_i; \underline{\lambda})$

potential early exit

c. Select lexical entries from the highest scoring valid parses:

$$\underline{\lambda}_i \leftarrow \bigcup_{y \in \text{MAX}_{V_i}(Y; \theta)} \text{LEX}(y)$$

d. Update lexicon: $\underline{\Lambda} \leftarrow \underline{\Lambda} \cup \underline{\lambda}_i$

Step 2: (Update parameters)

Output: Parameters θ and lexicon Λ

CCG lexicon

operator

determined

all parses that are valid $\leftarrow V_i$ and are max-scoring

Lexical entries

GEN $\rightarrow$ solves a search problem

all parses that are highest scoring

GENLEX overgenerator

n-number of training samples

Λ - current lexicon

risk!

Initialize θ using Λ_0 , $\Lambda \leftarrow \Lambda_0$

For $t = 1 \dots T, i = 1 \dots n$:

Step 1: (Lexical generation)

Step 2: (Update parameters)

- a. Set $G_i \leftarrow \text{MAX}_{V_i}(\text{GEN}(x_i; \Lambda); \theta)$ good parses
 and $B_i \leftarrow \{e | e \in \text{GEN}(x_i; \Lambda) \wedge \neg V_i(y)\}$ bad parses $\rightarrow$ not valid parse

- b. Construct sets of margin violating good and bad parses:

not balanced

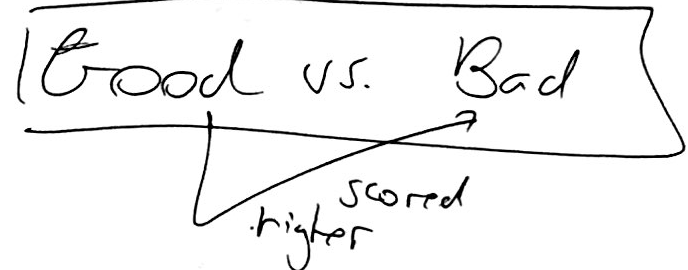
$$\begin{aligned} \rightarrow R_i &\leftarrow \{g | g \in G_i \wedge \exists b \in B_i \\ &\quad \text{s.t. } \langle \theta, \Phi_i(g) - \Phi_i(b) \rangle < \gamma \Delta_i(g, b)\} \\ \rightarrow E_i &\leftarrow \{b | b \in B_i \wedge \exists g \in G_i \\ &\quad \text{s.t. } \langle \theta, \Phi_i(g) - \Phi_i(b) \rangle < \gamma \Delta_i(g, b)\} \end{aligned}$$

- c. Apply the additive update:

$$\theta \leftarrow \theta + \left[\frac{1}{|R_i|} \sum_{r \in R_i} \Phi_i(r) - \frac{1}{|E_i|} \sum_{e \in E_i} \Phi_i(e) \right]$$

$\rightarrow$ towards the good
 $\rightarrow$ away from the bad

max-scoring valid $\rightarrow V_i$



Output: Parameters θ and lexicon Λ

1) Validation $\rightarrow$ is the LF of the root of a tree ~~is~~ equivalent to z_i

2) G_{en}lex

love(Lucy, I) $\xrightarrow{V_i}$ X

$D = \{(x_i, z_i)\}_{i=1}^N$

 | |

sentence LF

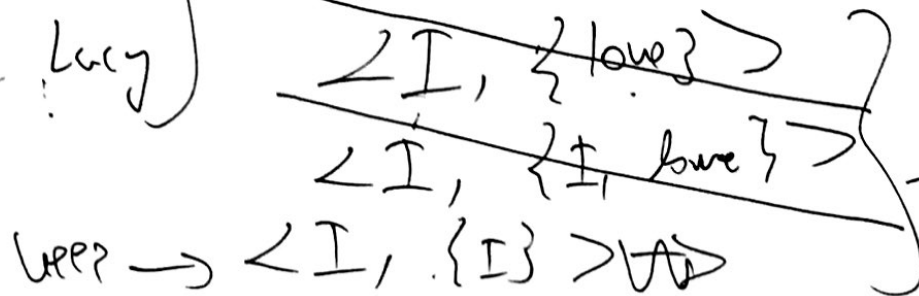
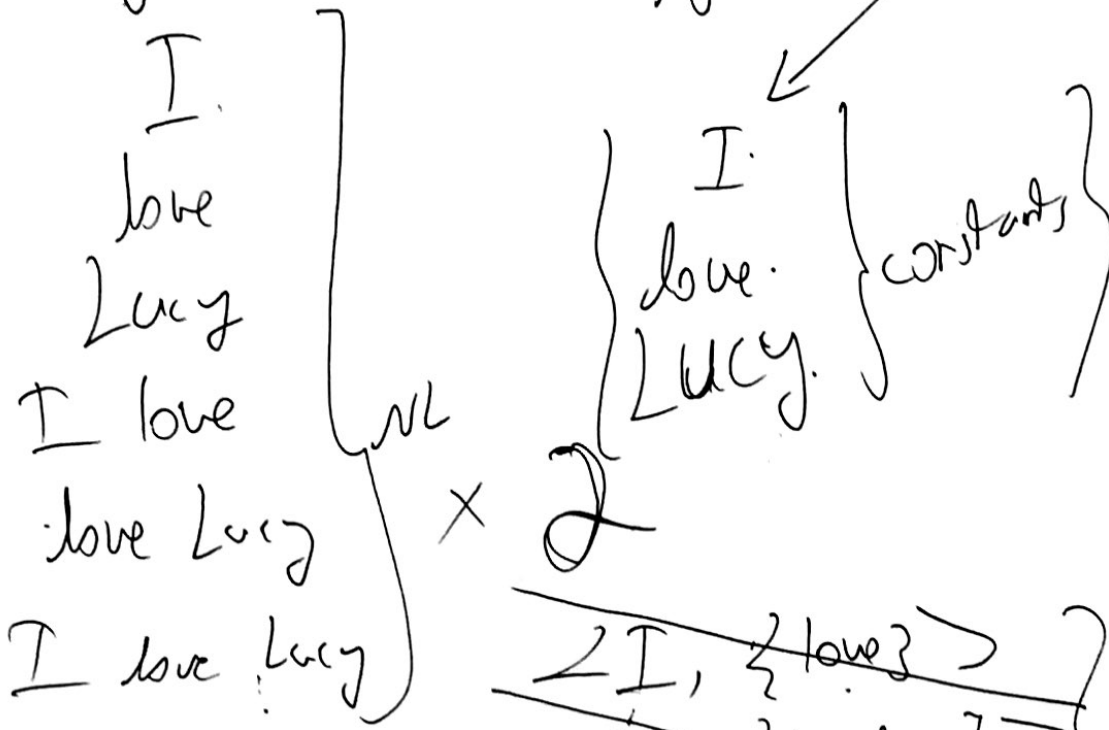
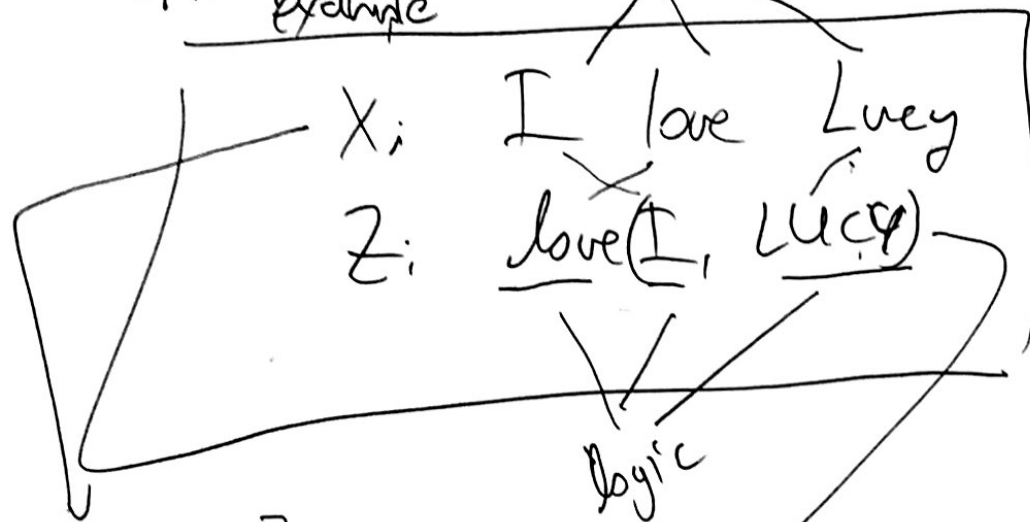
y_i - free latent

x_i : I love Lucy

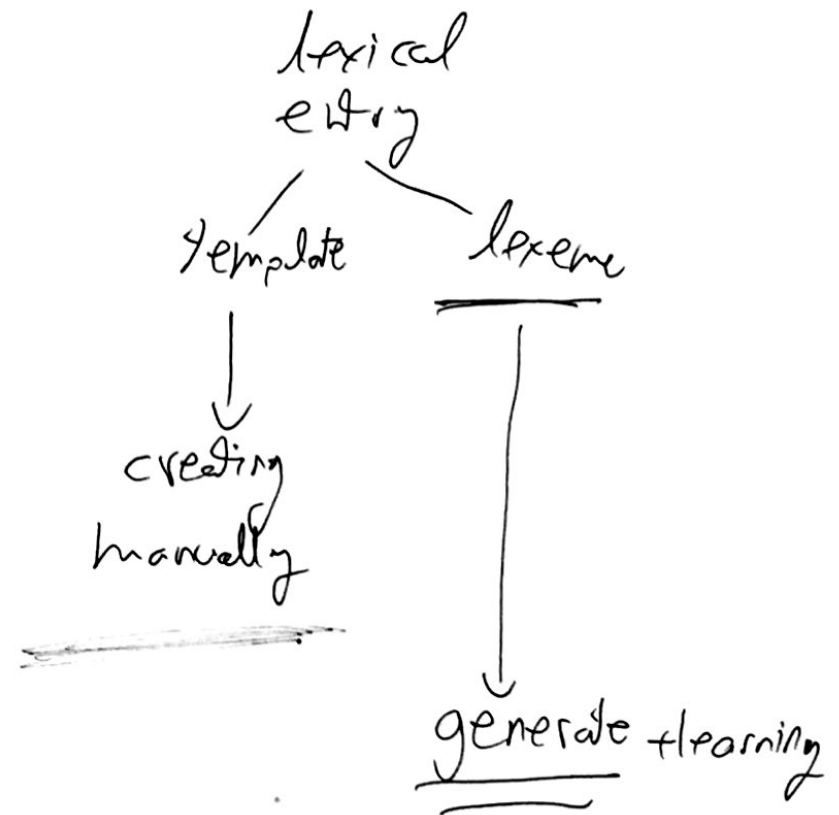
z_i : love(I, Lucy)

4 training
example

words



101 (111, 234)



<nl, set of constants>

+ templates → lexical entry → λ

Learning Algorithm: Step-by-step

Unified Learning Algorithm

Initialize θ using Λ_0 , $\Lambda \leftarrow \Lambda_0$

For $t = 1 \dots T, i = 1 \dots n$:

Step 1: (Lexical generation)

Step 2: (Update parameters)

Output: Parameters θ and lexicon Λ

- Online

- Input:

$$\{(x_i, \mathcal{V}_i) : i = 1 \dots n\}$$

- 2 steps:

- Lexical generation

- Parameter update

Initialize θ using Λ_0 , $\Lambda \leftarrow \Lambda_0$

For $t = 1 \dots T, i = 1 \dots n$:

Step 1: (Lexical generation)

Step 2: (Update parameters)

Output: Parameters θ and lexicon Λ

Initialize parameters and
lexicon

θ weights

Λ_0 initial lexicon

Initialize θ using Λ_0 , $\Lambda \leftarrow \Lambda_0$

For $t = 1 \dots T, i = 1 \dots n$:

Step 1: (Lexical generation)

Step 2: (Update parameters)

Output: Parameters θ and lexicon Λ

Iterate over data

T # iterations

n # samples

Initialize θ using Λ_0 , $\Lambda \leftarrow \Lambda_0$

For $t = 1 \dots T, i = 1 \dots n$:

Step 1: (Lexical generation)

- a. Set $\lambda_G \leftarrow GENLEX(x_i, \mathcal{V}_i; \Lambda, \theta)$,
 $\lambda \leftarrow \Lambda \cup \lambda_G$
- b. Let Y be the k highest scoring parses from $GEN(x_i; \lambda)$
- c. Select lexical entries from the highest scoring valid parses:
$$\lambda_i \leftarrow \bigcup_{y \in MAXV_i(Y; \theta)} LEX(y)$$
- d. Update lexicon: $\Lambda \leftarrow \Lambda \cup \lambda_i$

Step 2: (Update parameters)

Output: Parameters θ and lexicon Λ

Initialize θ using Λ_0 , $\Lambda \leftarrow \Lambda_0$

For $t = 1 \dots T, i = 1 \dots n$:

Step 1: (Lexical generation)

- a. Set $\lambda_G \leftarrow GENLEX(x_i, \mathcal{V}_i; \Lambda, \theta)$,
 $\lambda \leftarrow \Lambda \cup \lambda_G$
- b. Let Y be the k highest scoring parses from $GEN(x_i; \lambda)$
- c. Select lexical entries from the highest scoring valid parses:
$$\lambda_i \leftarrow \bigcup_{y \in MAX_{V_i}(Y; \theta)} LEX(y)$$
- d. Update lexicon: $\Lambda \leftarrow \Lambda \cup \lambda_i$

Step 2: (Update parameters)

Output: Parameters θ and lexicon Λ

Generate a large set of potential lexical entries

θ weights

x_i sentence

$\mathcal{V}_i$ validation function

$GENLEX(x_i, \mathcal{V}_i; \Lambda, \theta)$

lexical generation function

Initialize θ using Λ_0 , $\Lambda \leftarrow \Lambda_0$

For $t = 1 \dots T, i = 1 \dots n$:

Step 1: (Lexical generation)

- a. Set $\lambda_G \leftarrow GENLEX(x_i, \mathcal{V}_i; \Lambda, \theta)$,
 $\lambda \leftarrow \Lambda \cup \lambda_G$
- b. Let Y be the k highest scoring parses from $GEN(x_i; \lambda)$
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Step 2: (Update parameters)

Output: Parameters θ and lexicon Λ

Generate a large set of potential lexical entries

θ weights

x_i sentence

$\mathcal{V}_i$ validation function

$GENLEX(x_i, \mathcal{V}_i; \Lambda, \theta)$

lexical generation function

Procedure to propose potential new lexical entries for a sentence

Initialize θ using Λ_0 , $\Lambda \leftarrow \Lambda_0$

For $t = 1 \dots T, i = 1 \dots n$:

Step 1: (Lexical generation)

- a. Set $\lambda_G \leftarrow GENLEX(x_i, \mathcal{V}_i; \Lambda, \theta)$,
 $\lambda \leftarrow \Lambda \cup \lambda_G$
- b. Let Y be the k highest scoring parses from $GEN(x_i; \lambda)$
- c. Select lexical entries from the highest scoring valid parses:
$$\lambda_i \leftarrow \bigcup_{y \in MAX_{V_i}(Y; \theta)} LEX(y)$$
- d. Update lexicon: $\Lambda \leftarrow \Lambda \cup \lambda_i$

Step 2: (Update parameters)

Output: Parameters θ and lexicon Λ

Generate a large set of potential lexical entries

θ weights

x_i sentence

$\mathcal{V}_i$ validation function

$GENLEX(x_i, \mathcal{V}_i; \Lambda, \theta)$

lexical generation function

$$\mathcal{V} : \mathcal{Y} \rightarrow \{t, f\}$$

$\mathcal{Y}$ all parses

Initialize θ using Λ_0 , $\Lambda \leftarrow \Lambda_0$

For $t = 1 \dots T, i = 1 \dots n$:

Step 1: (Lexical generation)

- a. Set $\lambda_G \leftarrow GENLEX(x_i, \mathcal{V}_i; \Lambda, \theta)$,
 $\lambda \leftarrow \Lambda \cup \lambda_G$
- b. Let Y be the k highest scoring parses from $GEN(x_i; \lambda)$
- c. Select lexical entries from the highest scoring valid parses:
$$\lambda_i \leftarrow \bigcup_{y \in MAX_{V_i}(Y; \theta)} LEX(y)$$
- d. Update lexicon: $\Lambda \leftarrow \Lambda \cup \lambda_i$

Step 2: (Update parameters)

Output: Parameters θ and lexicon Λ

Get top parses

x_i sentence

k beam size

$GEN(x_i; \lambda)$ set of all parses

Initialize θ using Λ_0 , $\Lambda \leftarrow \Lambda_0$

For $t = 1 \dots T, i = 1 \dots n$:

Step 1: (Lexical generation)

- a. Set $\lambda_G \leftarrow GENLEX(x_i, \mathcal{V}_i; \Lambda, \theta)$,
 $\lambda \leftarrow \Lambda \cup \lambda_G$
- b. Let Y be the k highest scoring parses from $GEN(x_i; \lambda)$
- c. Select lexical entries from the highest scoring valid parses:
$$\lambda_i \leftarrow \bigcup_{y \in MAXV_i(Y; \theta)} LEX(y)$$
- d. Update lexicon: $\Lambda \leftarrow \Lambda \cup \lambda_i$

Step 2: (Update parameters)

Output: Parameters θ and lexicon Λ

Get lexical entries from
highest scoring valid
parses

θ weights

$\mathcal{V}$ validation function

$LEX(y)$ set of lexical entries

$\phi_i(y) = \phi(x_i, y)$

$MAXV_i(Y; \theta) = \{y | y \in Y \wedge \mathcal{V}_i(y) \wedge$
 $\forall y' \in Y. \mathcal{V}_i(y) \implies$
 $\langle \theta, \Phi_i(y') \rangle \leq \langle \theta, \Phi_i(y) \rangle\}$

Initialize θ using Λ_0 , $\Lambda \leftarrow \Lambda_0$

For $t = 1 \dots T, i = 1 \dots n$:

Step 1: (Lexical generation)

- a. Set $\lambda_G \leftarrow GENLEX(x_i, \mathcal{V}_i; \Lambda, \theta)$,
 $\lambda \leftarrow \Lambda \cup \lambda_G$
- b. Let Y be the k highest scoring parses from $GEN(x_i; \lambda)$
- c. Select lexical entries from the highest scoring valid parses:

$$\lambda_i \leftarrow \bigcup_{y \in MAX_{V_i}(Y; \theta)} LEX(y)$$

- d. Update lexicon: $\Lambda \leftarrow \Lambda \cup \lambda_i$

Step 2: (Update parameters)

Output: Parameters θ and lexicon Λ

Update model's lexicon

Initialize θ using Λ_0 , $\Lambda \leftarrow \Lambda_0$

For $t = 1 \dots T, i = 1 \dots n$:

Step 1: (Lexical generation)

Step 2: (Update parameters)

- a. Set $G_i \leftarrow MAXV_i(GEN(x_i; \Lambda); \theta)$
and $B_i \leftarrow \{e | e \in GEN(x_i; \Lambda) \wedge \neg \mathcal{V}_i(y)\}$
- b. Construct sets of margin violating good and bad parses:
$$R_i \leftarrow \{g | g \in G_i \wedge \exists b \in B_i$$
$$s.t. \langle \theta, \Phi_i(g) - \Phi_i(b) \rangle < \gamma \Delta_i(g, b)\}$$
$$E_i \leftarrow \{b | b \in B_i \wedge \exists g \in G_i$$
$$s.t. \langle \theta, \Phi_i(g) - \Phi_i(b) \rangle < \gamma \Delta_i(g, b)\}$$
- c. Apply the additive update:
$$\theta \leftarrow \theta + \frac{1}{|R_i|} \sum_{r \in R_i} \Phi_i(r)$$
$$- \frac{1}{|E_i|} \sum_{e \in E_i} \Phi_i(e)$$

Output: Parameters θ and lexicon Λ

Initialize θ using Λ_0 , $\Lambda \leftarrow \Lambda_0$

For $t = 1 \dots T, i = 1 \dots n$:

Step 1: (Lexical generation)

Step 2: (Update parameters)

- a. Set $G_i \leftarrow MAXV_i(GEN(x_i; \Lambda); \theta)$
and $B_i \leftarrow \{e | e \in GEN(x_i; \Lambda) \wedge \neg \mathcal{V}_i(y)\}$
- b. Construct sets of margin violating good and bad parses:
$$R_i \leftarrow \{g | g \in G_i \wedge \exists b \in B_i$$
$$s.t. \langle \theta, \Phi_i(g) - \Phi_i(b) \rangle < \gamma \Delta_i(g, b)\}$$
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$$\theta \leftarrow \theta + \frac{1}{|R_i|} \sum_{r \in R_i} \Phi_i(r)$$
$$- \frac{1}{|E_i|} \sum_{e \in E_i} \Phi_i(e)$$

Output: Parameters θ and lexicon Λ

Re-parse and group all
parses into ‘good’ and
‘bad’ sets

θ weights

x_i sentence

$\mathcal{V}_i$ validation function

$GEN(x_i; \lambda)$ set of all parses

$\phi_i(y) = \phi(x_i, y)$

$MAXV_i(Y; \theta) = \{y | y \in Y \wedge \mathcal{V}_i(y) \wedge$

$\forall y' \in Y. \mathcal{V}_i(y) \implies$

$\langle \theta, \Phi_i(y') \rangle \leq \langle \theta, \Phi_i(y) \rangle\}$

Initialize θ using Λ_0 , $\Lambda \leftarrow \Lambda_0$

For $t = 1 \dots T, i = 1 \dots n$:

Step 1: (Lexical generation)

Step 2: (Update parameters)

- a. Set $G_i \leftarrow MAXV_i(GEN(x_i; \Lambda); \theta)$
and $B_i \leftarrow \{e | e \in GEN(x_i; \Lambda) \wedge \neg \mathcal{V}_i(y)\}$
- b. Construct sets of margin violating good and bad parses:
$$R_i \leftarrow \{g | g \in G_i \wedge \exists b \in B_i$$
$$s.t. \langle \theta, \Phi_i(g) - \Phi_i(b) \rangle < \gamma \Delta_i(g, b)\}$$
$$E_i \leftarrow \{b | b \in B_i \wedge \exists g \in G_i$$
$$s.t. \langle \theta, \Phi_i(g) - \Phi_i(b) \rangle < \gamma \Delta_i(g, b)\}$$
- c. Apply the additive update:
$$\theta \leftarrow \theta + \frac{1}{|R_i|} \sum_{r \in R_i} \Phi_i(r)$$
$$- \frac{1}{|E_i|} \sum_{e \in E_i} \Phi_i(e)$$

Output: Parameters θ and lexicon Λ

For all pairs of ‘good’ and ‘bad’ parses, if their scores violate the margin, add each to ‘right’ and ‘error’ sets respectively

θ weights

γ margin

$\phi_i(y) = \phi(x_i, y)$

$\Delta_i(y, y') = |\Phi_i(y) - \Phi_i(y')|_1$

Initialize θ using Λ_0 , $\Lambda \leftarrow \Lambda_0$

For $t = 1 \dots T, i = 1 \dots n$:

Step 1: (Lexical generation)

Step 2: (Update parameters)

- a. Set $G_i \leftarrow MAXV_i(GEN(x_i; \Lambda); \theta)$
and $B_i \leftarrow \{e | e \in GEN(x_i; \Lambda) \wedge \neg \mathcal{V}_i(y)\}$
- b. Construct sets of margin violating good and bad parses:

$$R_i \leftarrow \{g | g \in G_i \wedge \exists b \in B_i \\ s.t. \langle \theta, \Phi_i(g) - \Phi_i(b) \rangle < \gamma \Delta_i(g, b)\}$$

$$E_i \leftarrow \{b | b \in B_i \wedge \exists g \in G_i \\ s.t. \langle \theta, \Phi_i(g) - \Phi_i(b) \rangle < \gamma \Delta_i(g, b)\}$$

- c. Apply the additive update:

$$\theta \leftarrow \theta + \frac{1}{|R_i|} \sum_{r \in R_i} \Phi_i(r) \\ - \frac{1}{|E_i|} \sum_{e \in E_i} \Phi_i(e)$$

Output: Parameters θ and lexicon Λ

Update towards
violating ‘good’ parses
and against violating ‘bad’
parses

θ weights

$$\phi_i(y) = \phi(x_i, y)$$

Initialize θ using Λ_0 , $\Lambda \leftarrow \Lambda_0$

For $t = 1 \dots T, i = 1 \dots n$:

Step 1: (Lexical generation)

Step 2: (Update parameters)

Output: Parameters θ and lexicon Λ

Return grammar

θ weights

Λ lexicon

Unified Learning Algorithm

$\mathcal{V}$ validation function

$GENLEX(x, \mathcal{V}; \lambda, \theta)$

lexical generation function

- Two parts of the algorithm we still need to define
- Depend on the task and supervision signal