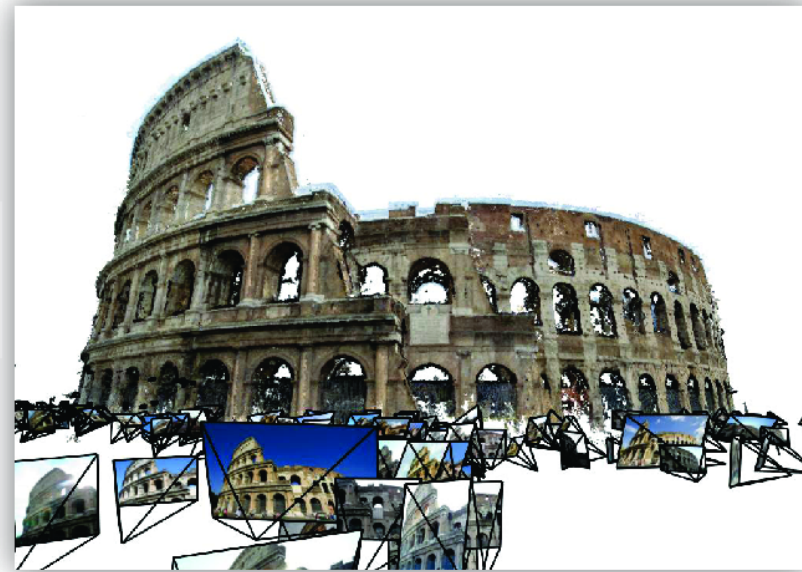
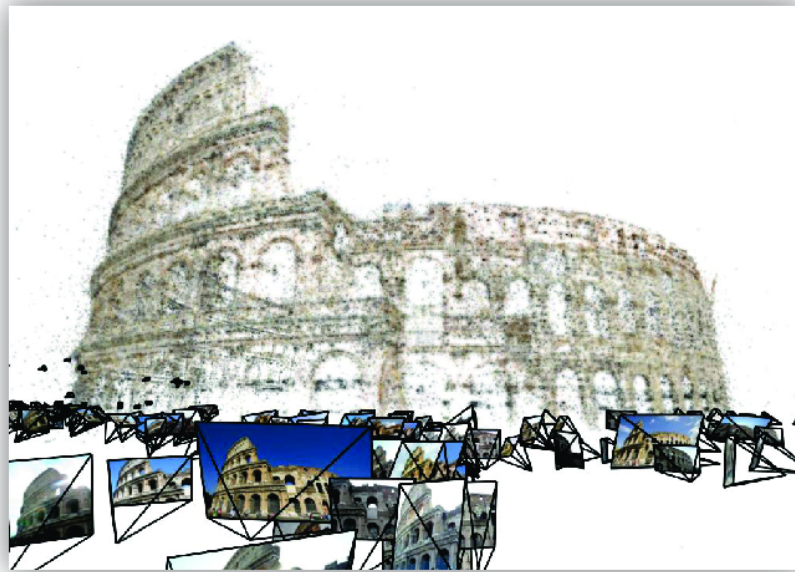


# CS5670: Computer Vision

Abe Davis (with most slides from Noah Snavely)

## Multi-view stereo



# Announcements

- Assignment 3 due this Friday (March 27) at 11:59pm
- Artifact due at the same time
  
- We are working on a revised grading policy
  - The hope is to provide more flexibility given the COVID-19 situation
  - Details forthcoming

# Recommended Reading

- Szeliski Chapter 11.6
- *Multi-View Stereo: A Tutorial*, Furukawa and Hernandez, 2015
  - [http://carlos-hernandez.org/papers/fnt\\_mvs\\_2015.pdf](http://carlos-hernandez.org/papers/fnt_mvs_2015.pdf)

# Multi-view Stereo

- **Problem formulation:** given several images of the same object or scene, compute a representation of its 3D shape



Stereo



Multi-view stereo

# Multi-view Stereo: Multi-camera Systems



[Point Grey's](#) Bumblebee XB3

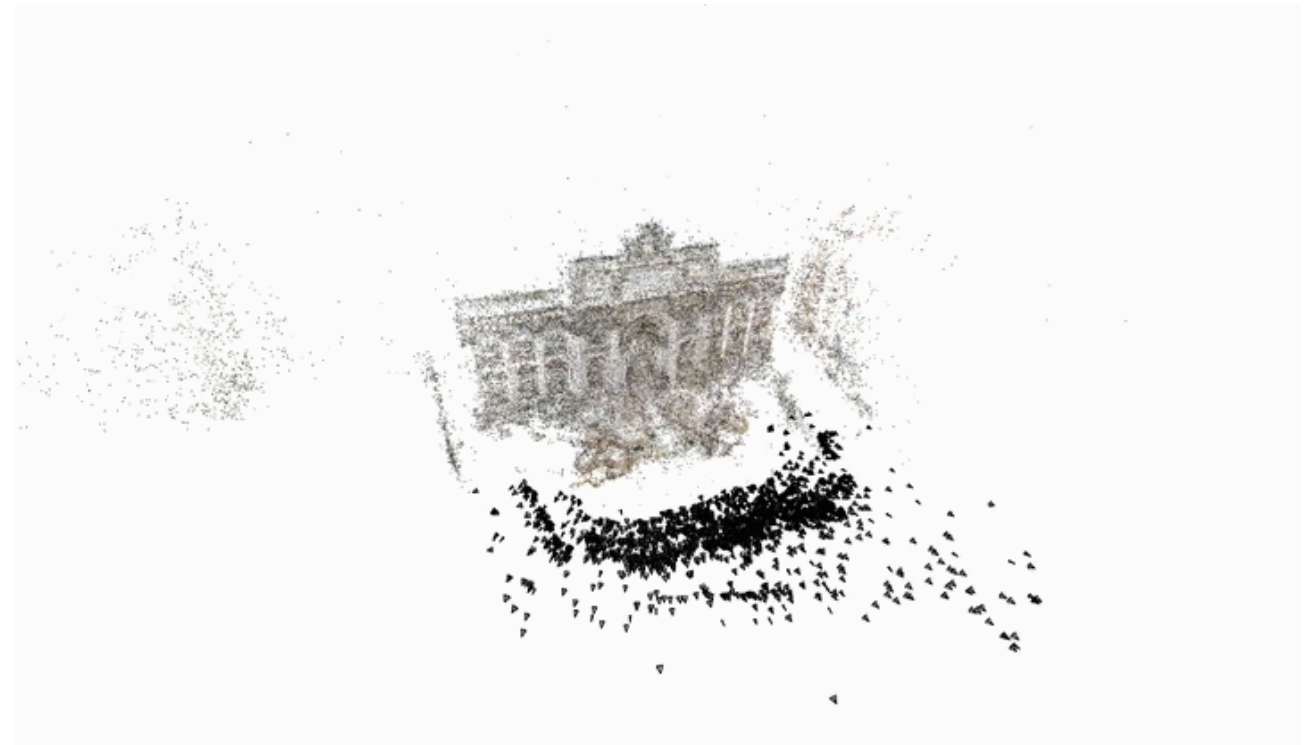
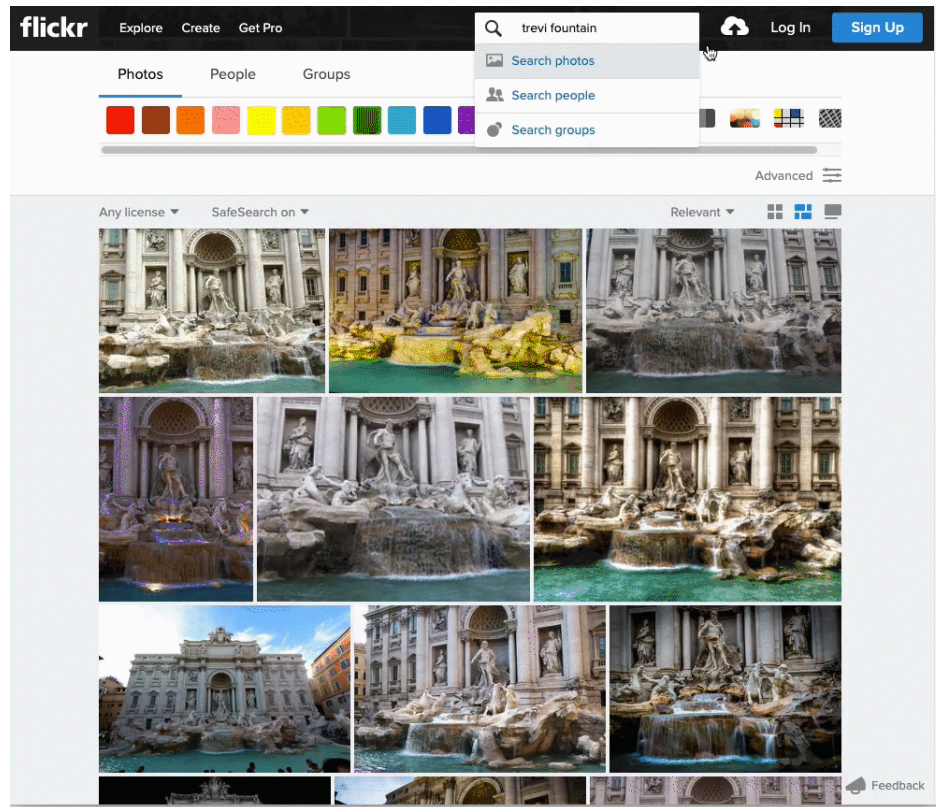


[Point Grey's](#) ProFusion 25



CMU's [3D Room](#)

# Next Lecture: Structure from Motion



**Unstructured photo collections:  
E.g., Flickr Search Results for  
“Trevi Fountain”**

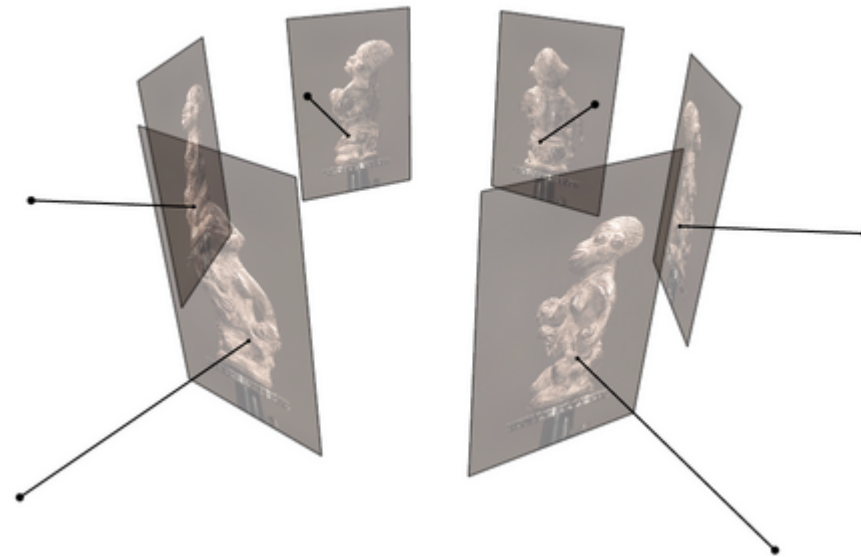


**3D Reconstructions for  
Virtual Tourism, Historical Preservation,  
Inspection, etc.**

# Multi-view Stereo

**Input:** calibrated images from several viewpoints  
(known intrinsics and extrinsics)

**Output:** 3D object model



Figures by Carlos Hernandez

# Applications





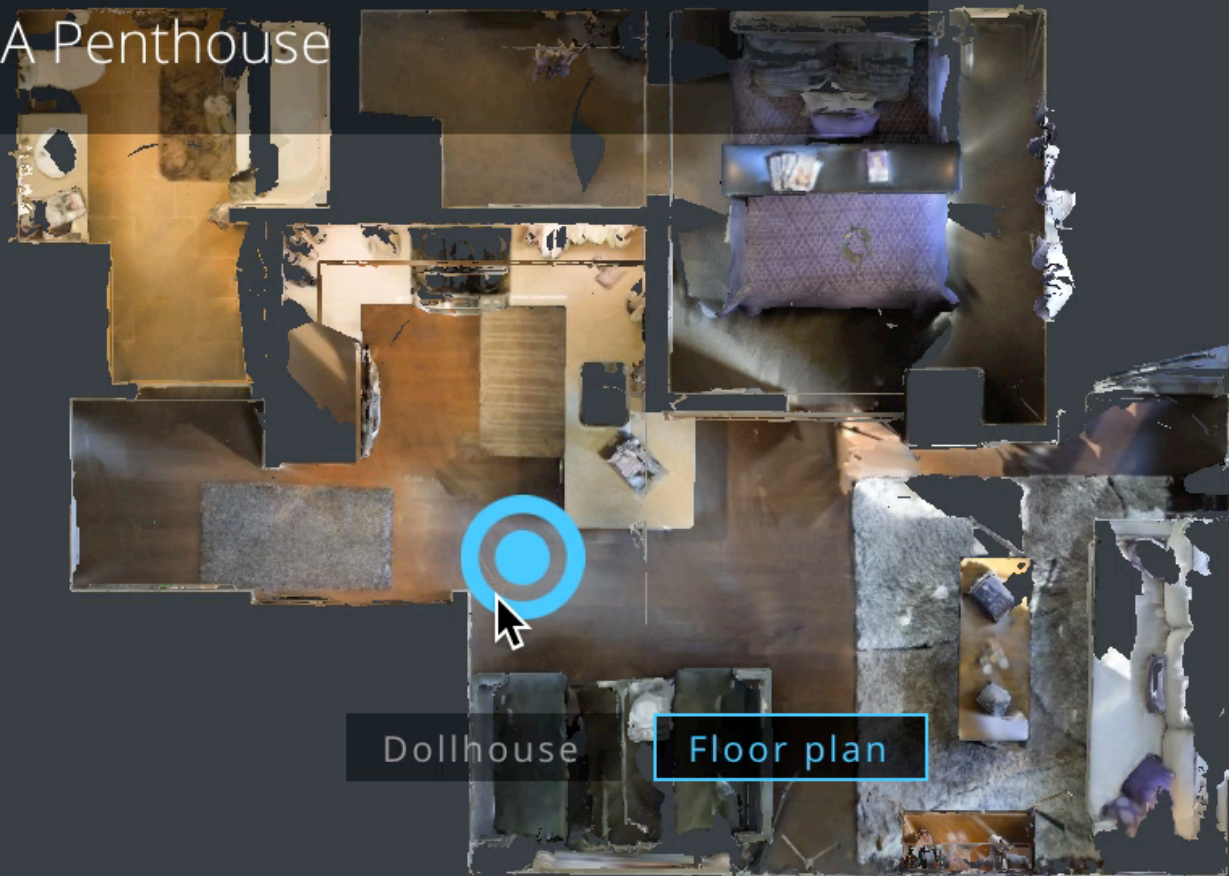
Data SIO, NOAA, U.S. Navy, NGA, GEBCO

Google earth



< 1BR, 1BA Penthouse

Terms



# Whistle in the Form of Female Figure *600 AD - 900 AD*



Details Los Angeles County Museum of Art



Los Angeles County Museum of Art



Sculpture



Mexico

Share

Compare

Saved 0

Discover

Google



THE RENDERPEOPLE MISSION

# IMPROVING THE QUALITY

TY  
LE

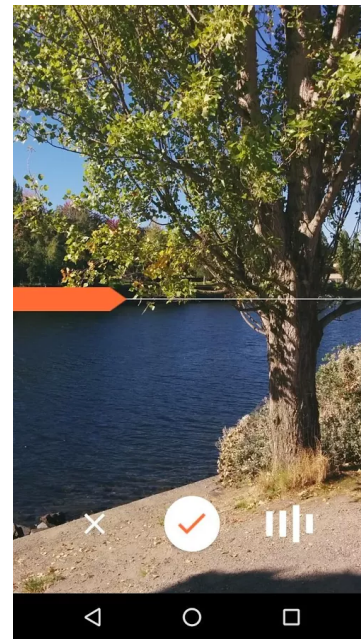


<https://renderpeople.com/about-us/>



JUMP

Google



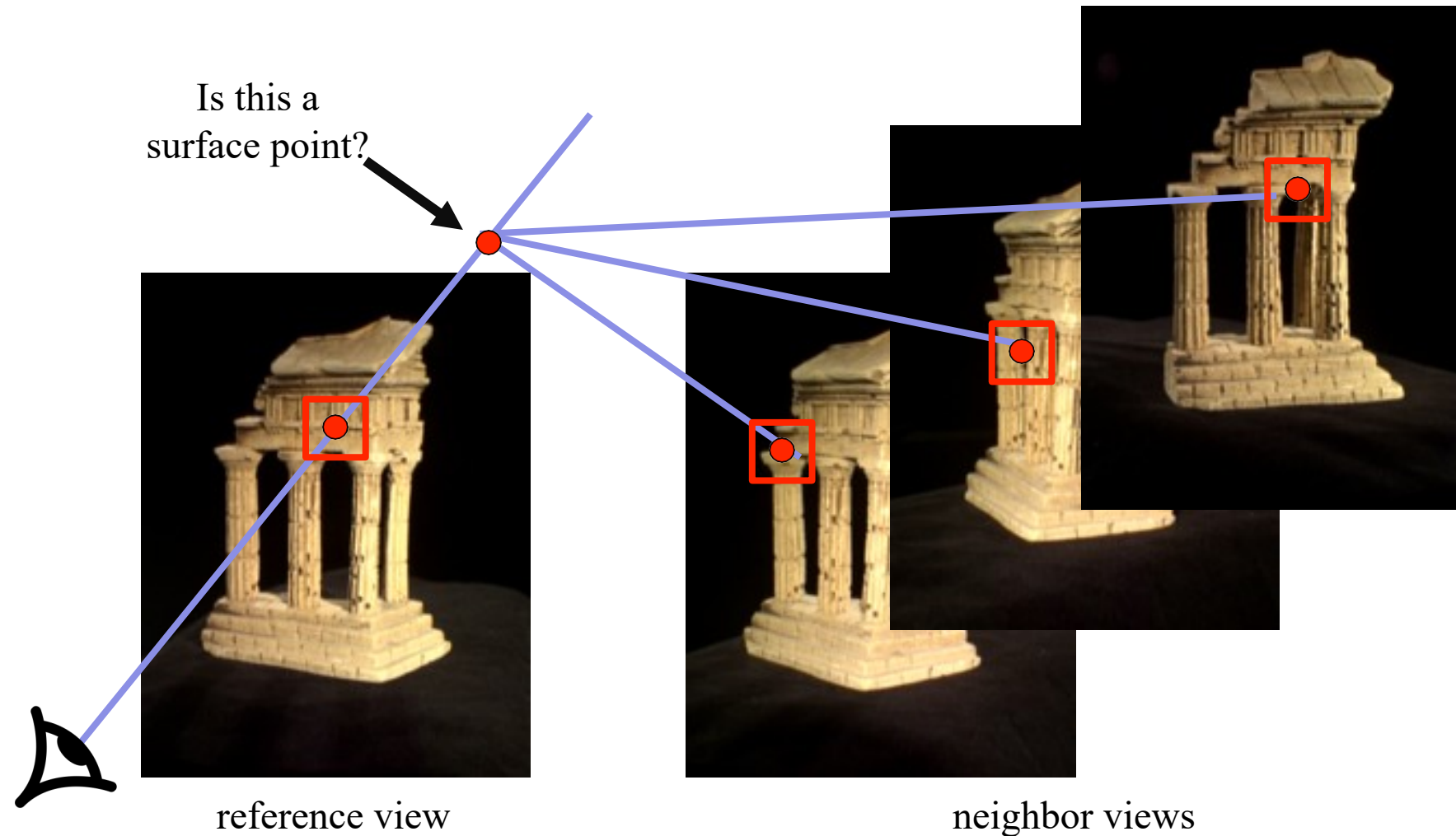




[https://code.facebook.com/posts/1755691291326688/introducing-facebook-surround-360-an-open-high-quality-3d-360-video-capture-system?hc\\_location=ufi](https://code.facebook.com/posts/1755691291326688/introducing-facebook-surround-360-an-open-high-quality-3d-360-video-capture-system?hc_location=ufi)



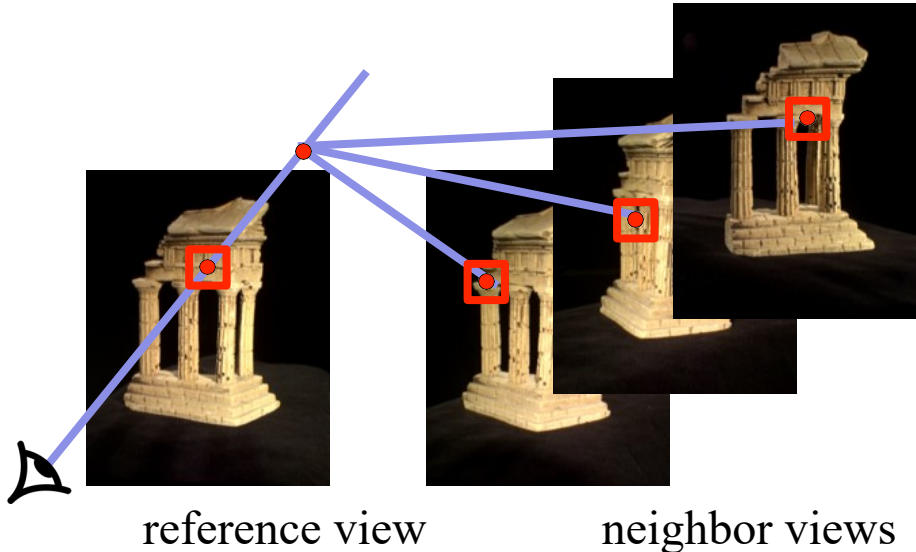
# Multi-view stereo: Basic idea



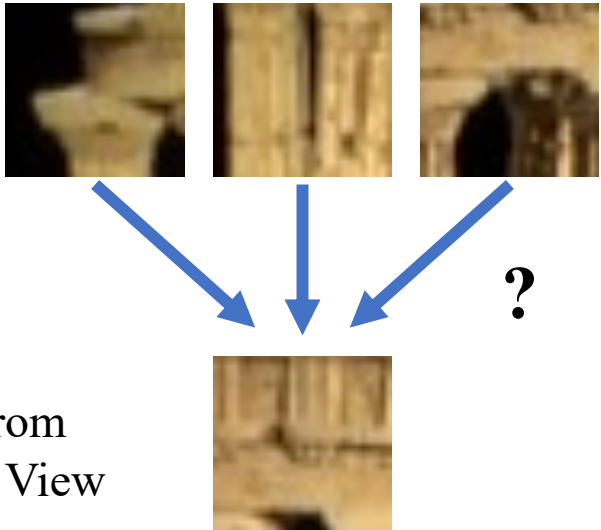


# Multi-view stereo: Basic idea

Evaluate the likelihood of geometry at a particular depth for a particular reference patch:

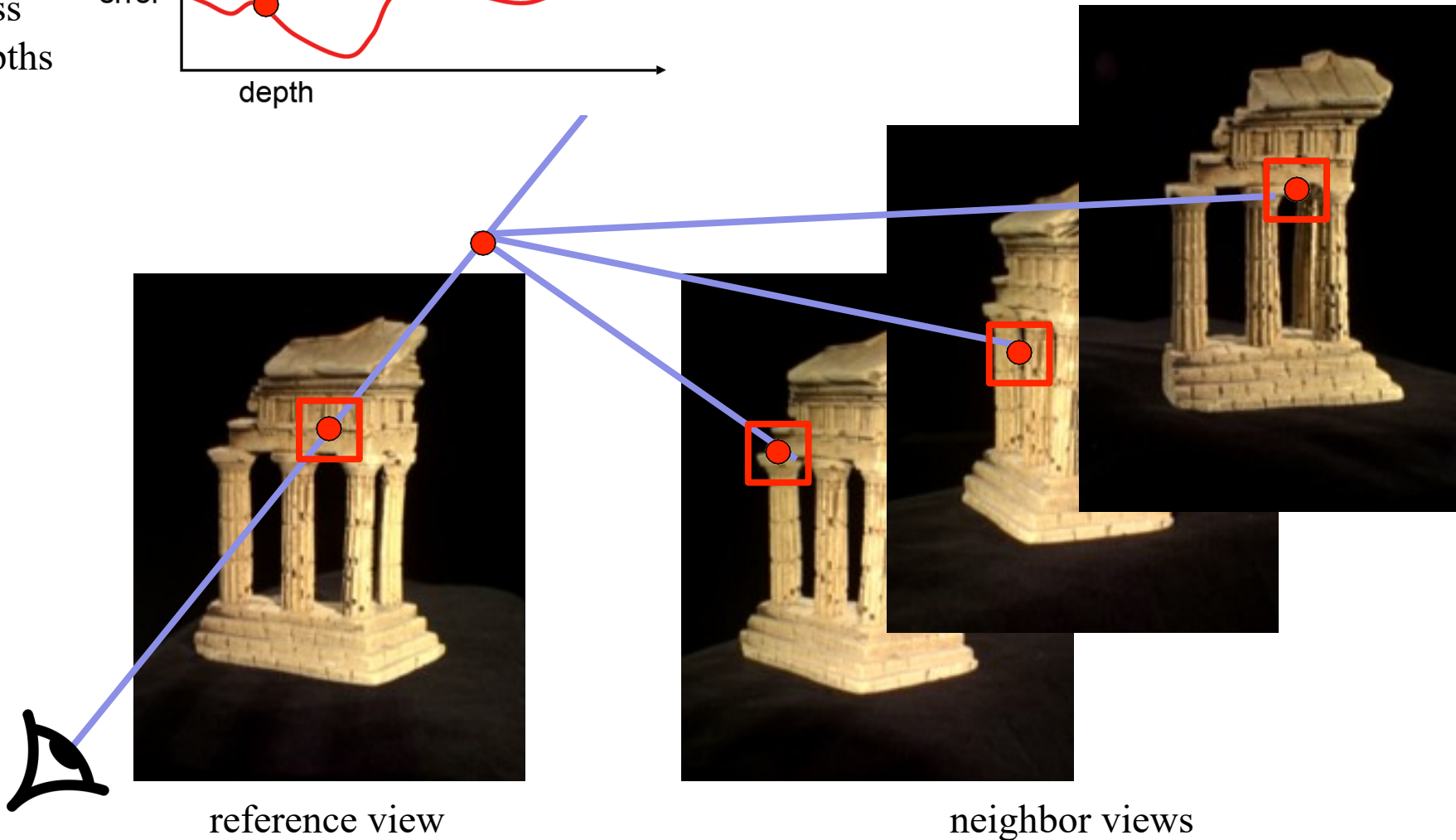
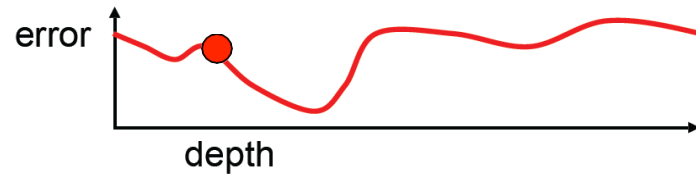


Corresponding patches at depth guess in other views



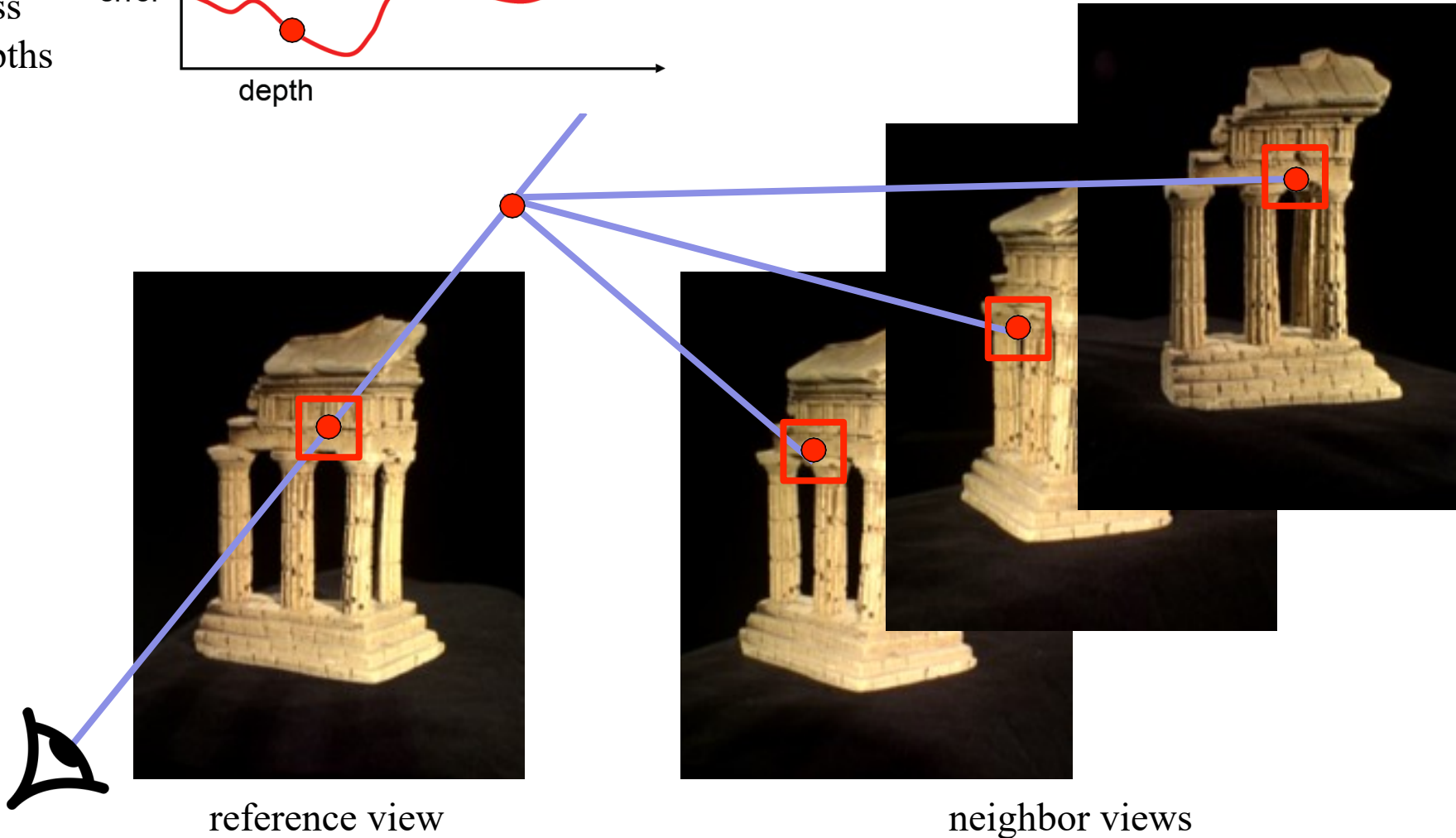
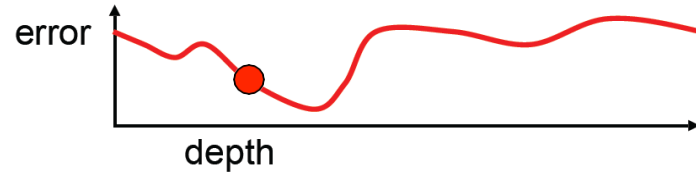
# Multi-view stereo: Basic idea

Photometric error across different depths



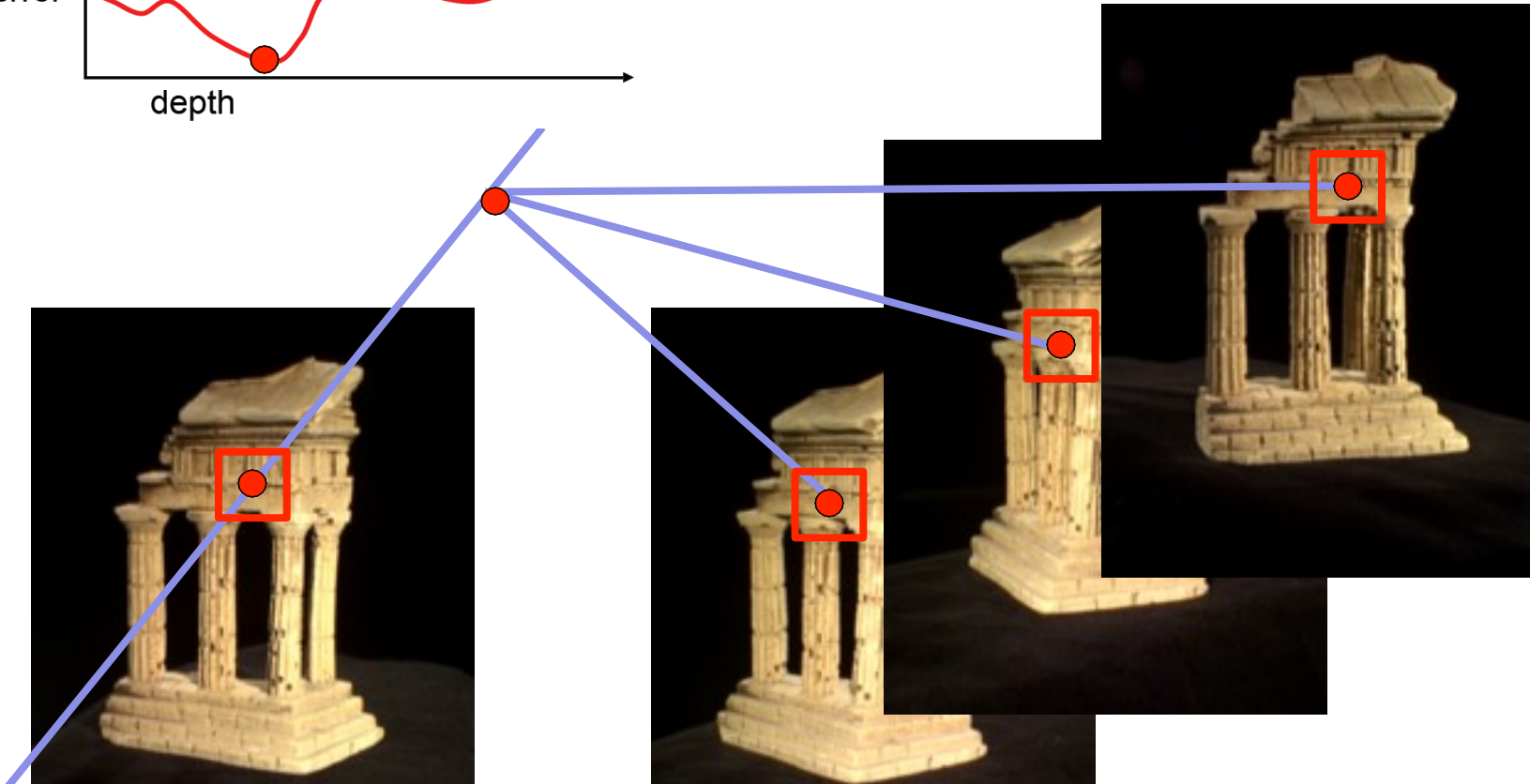
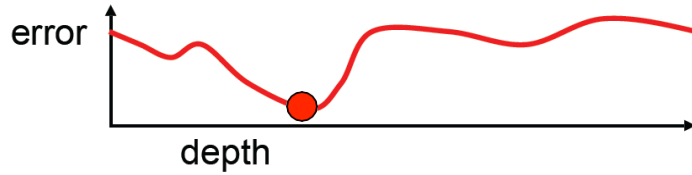
# Multi-view stereo: Basic idea

Photometric error across different depths



# Multi-view stereo: Basic idea

Photometric error across different depths

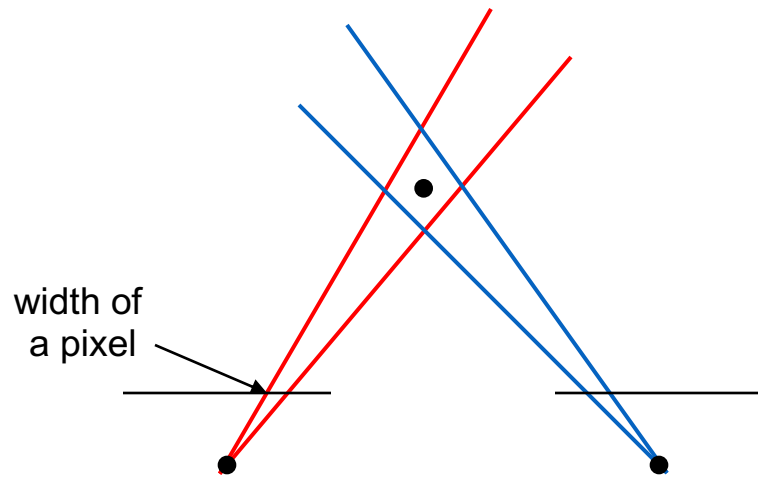


**In this manner, solve for a depth map over the whole reference view**

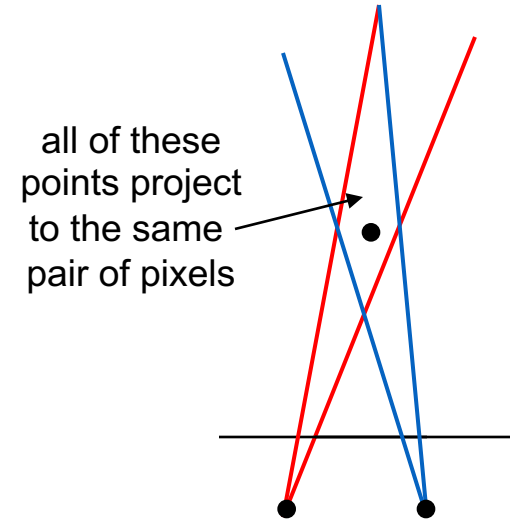
# Multi-view stereo: advantages

- Can match windows using more than 1 neighbor, giving a **stronger match signal**
- If you have lots of potential neighbors, can **choose the best subset** of neighbors to match per reference image
- Can reconstruct a depth map for each reference frame, and then merge into a **complete 3D model**

# Choosing the stereo baseline



**Large Baseline**

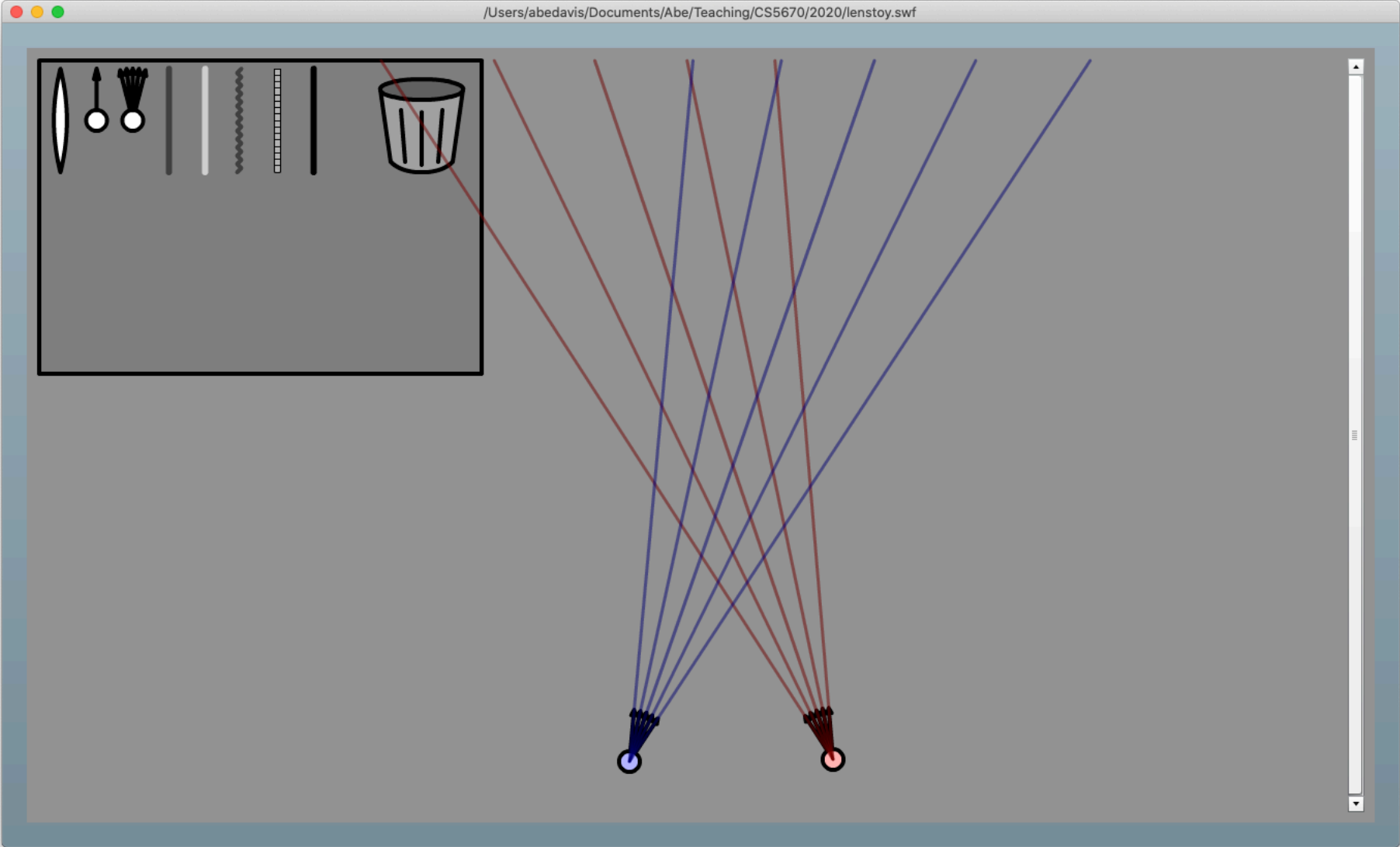


**Small Baseline**

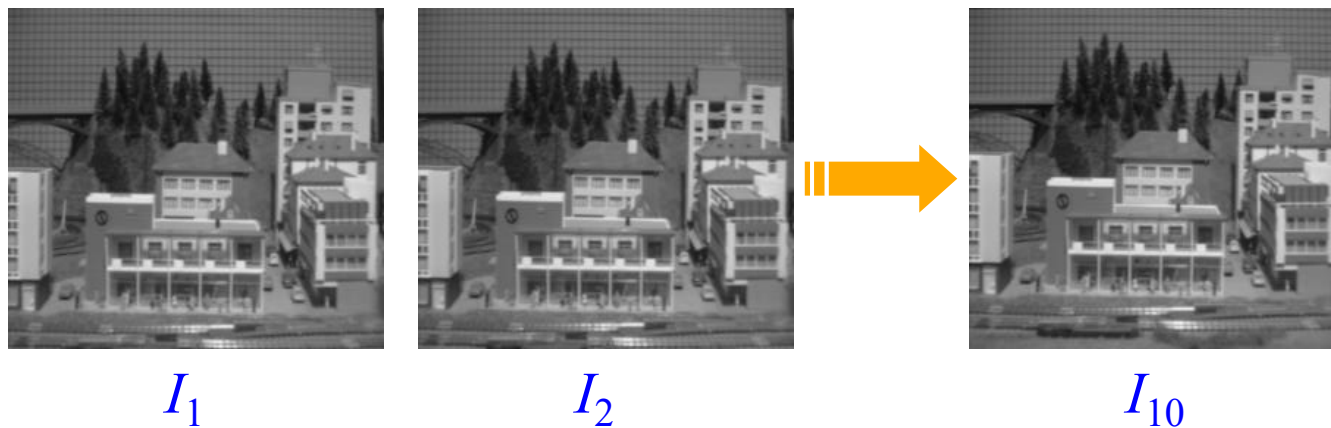
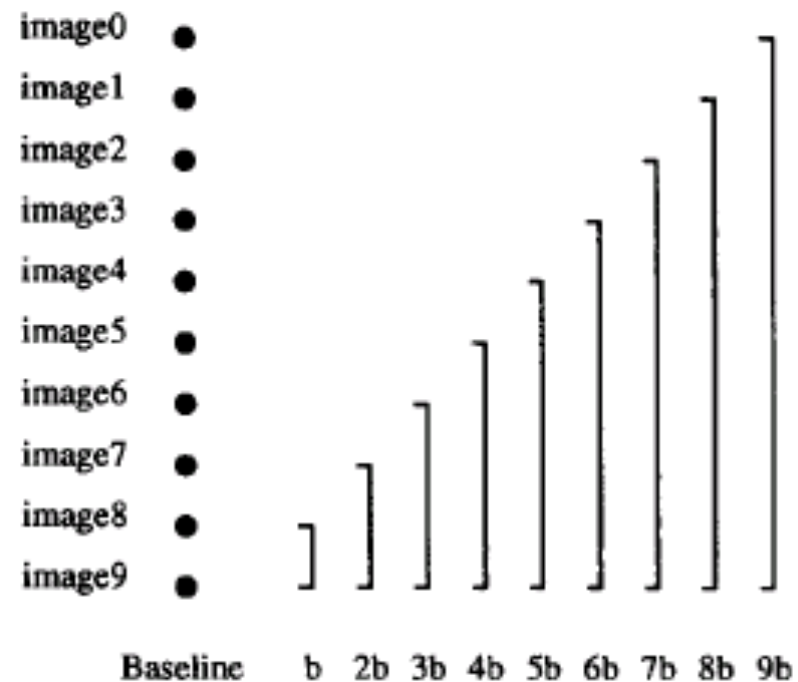
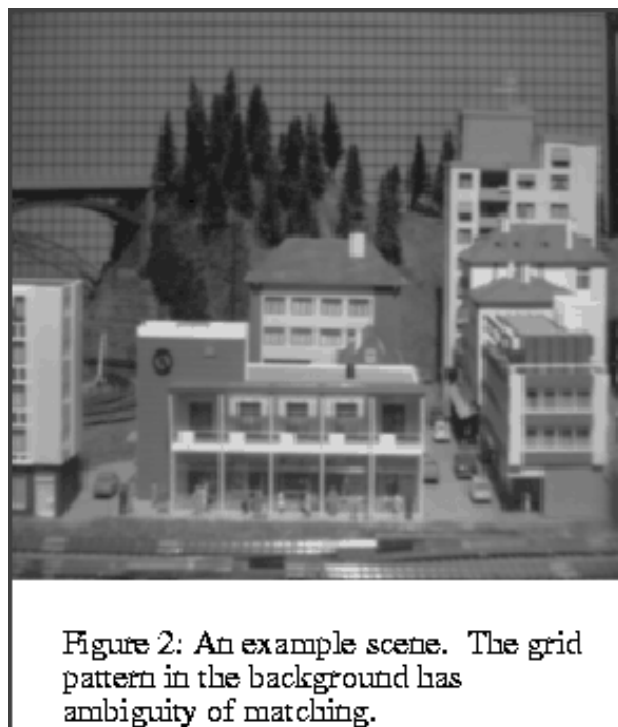
What's the optimal baseline?

- Too small: large depth error
- Too large: difficult search problem

# Demo

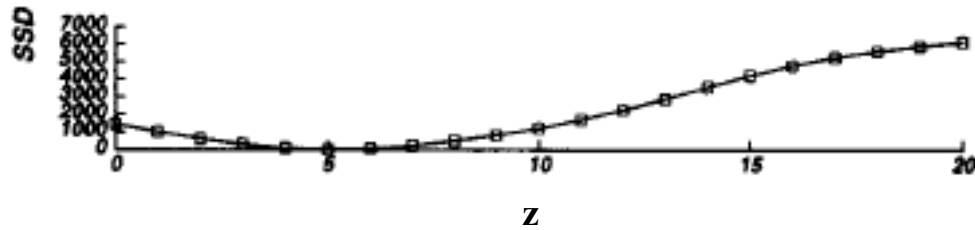


# The Effect of Baseline on Depth Estimation



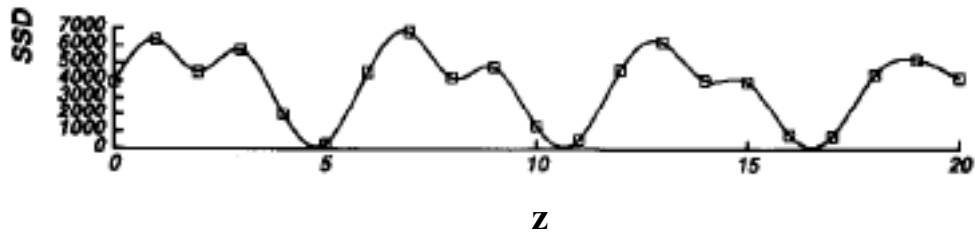
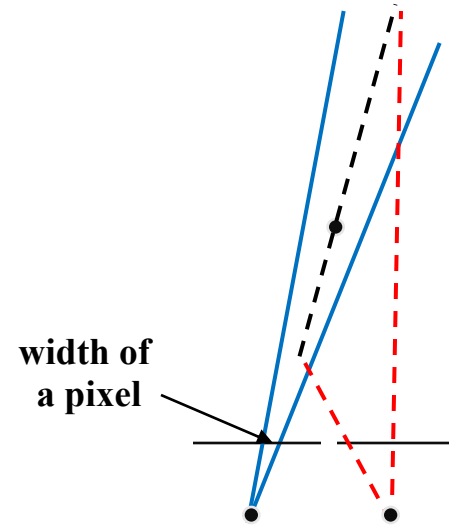


# Multiple-baseline stereo

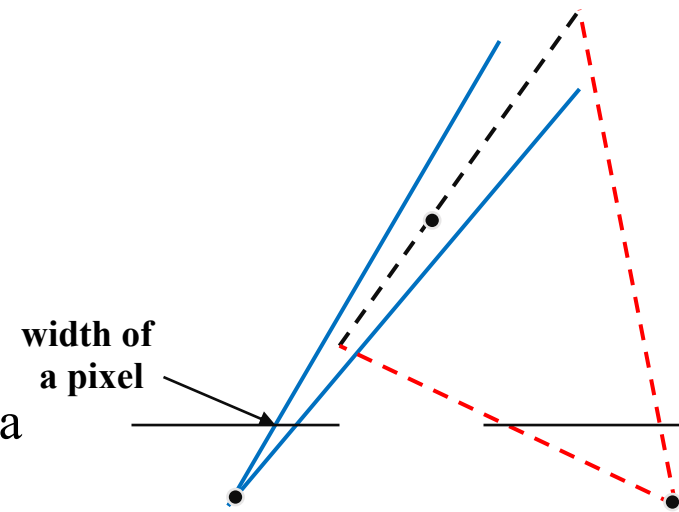


pixel matching score

- For short baselines, estimated depth will be less precise due to narrow triangulation



- For larger baselines, must search larger area in second image



# Multiple-baseline stereo

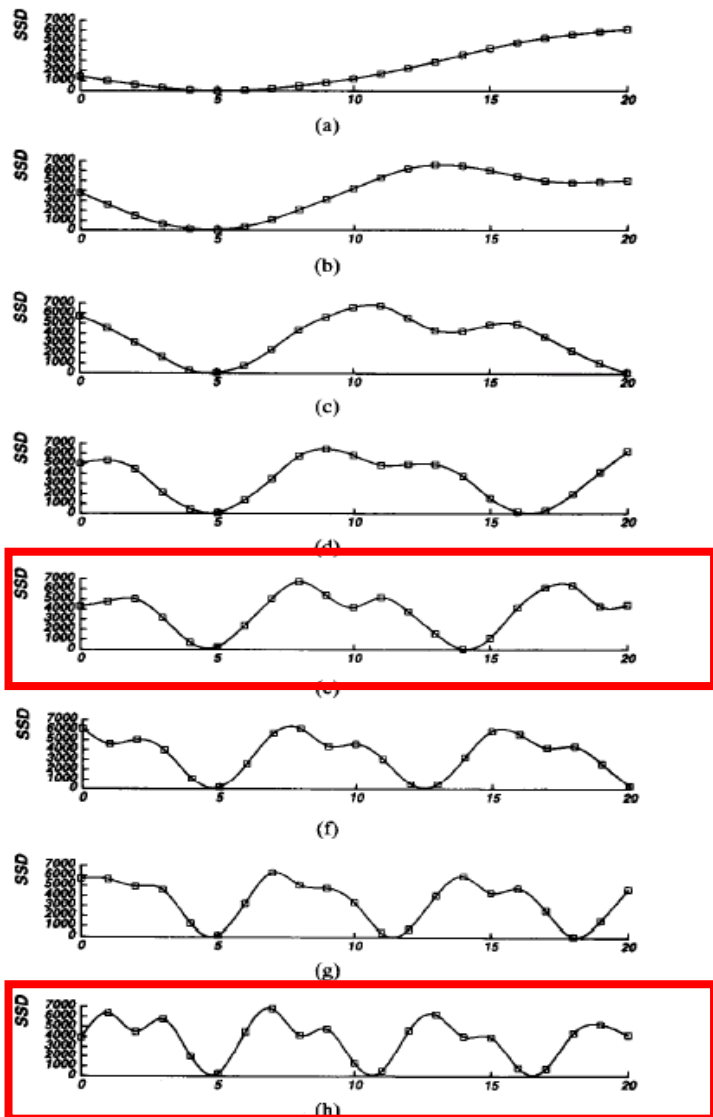


Fig. 5. SSD values versus inverse distance: (a)  $B = b$ ; (b)  $B = 2b$ ; (c)  $B = 3b$ ; (d)  $B = 4b$ ; (e)  $B = 5b$ ; (f)  $B = 6b$ ; (g)  $B = 7b$ ; (h)  $B = 8b$ . The horizontal axis is normalized such that  $8bF = 1$ .

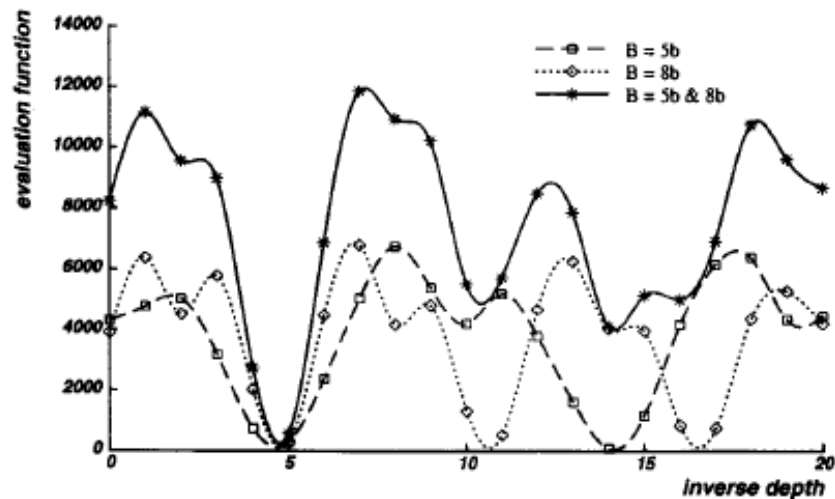


Fig. 6. Combining two stereo pairs with different baselines.

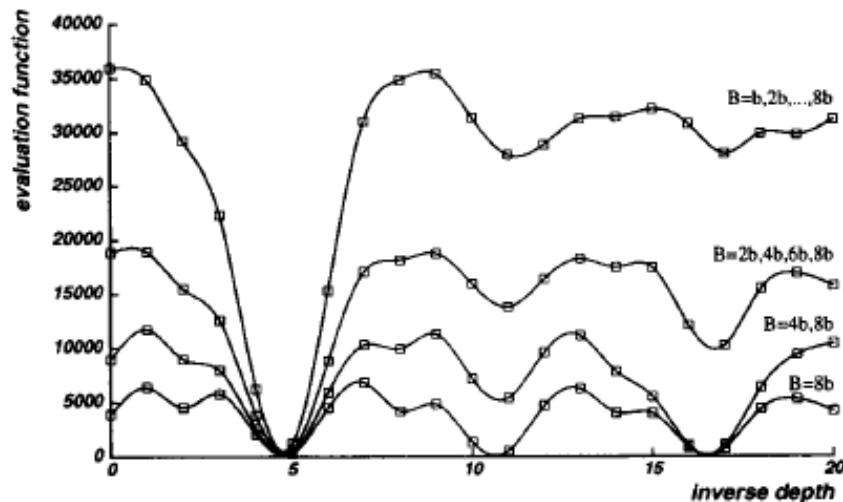
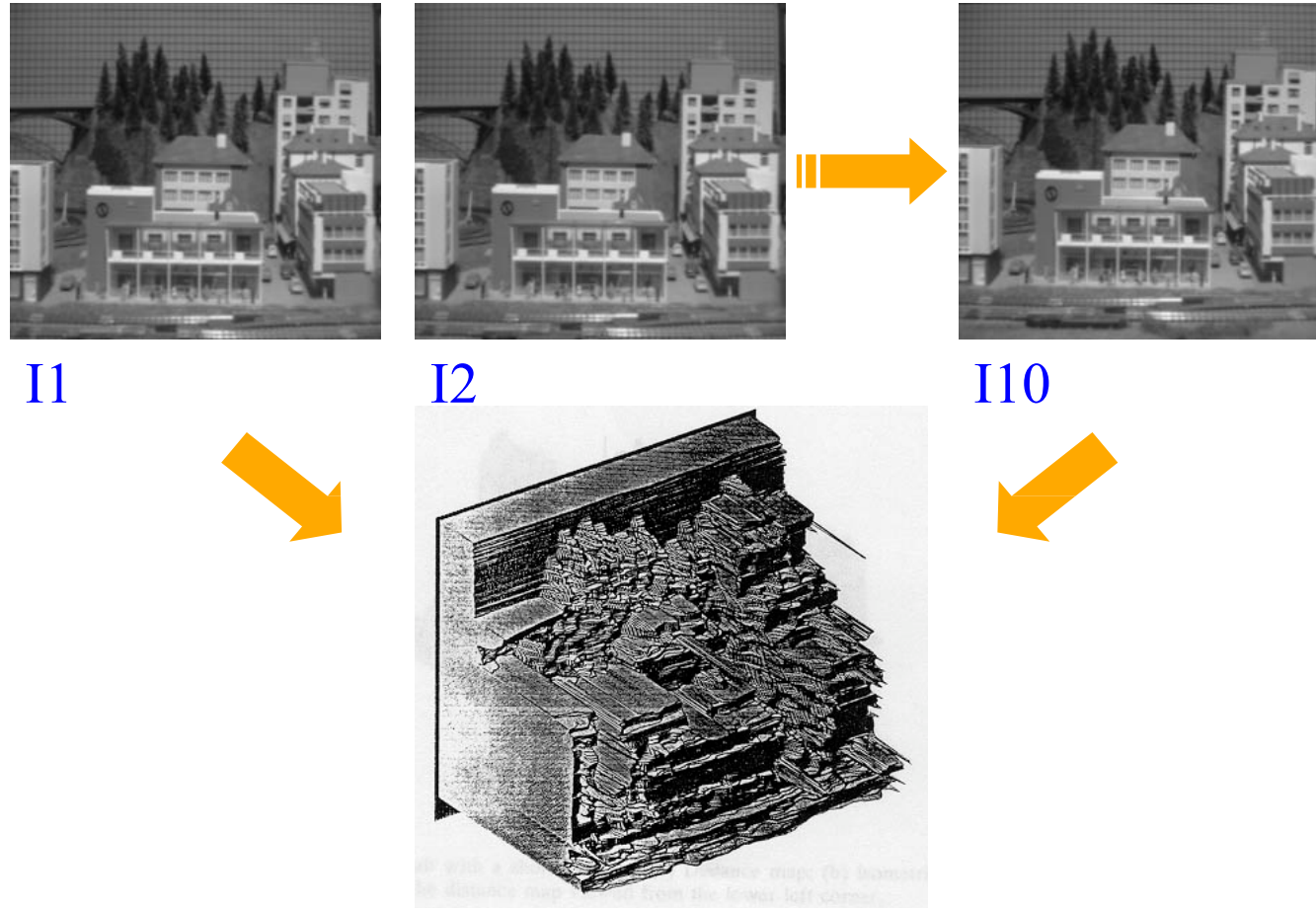


Fig. 7. Combining multiple baseline stereo pairs.

# Multiple-baseline stereo results



M. Okutomi and T. Kanade, *A Multiple-Baseline Stereo System*, IEEE Trans. on Pattern Analysis and Machine Intelligence, 15(4):353-363 (1993).

# Multibaseline Stereo

## Basic Approach

- Choose a reference view
- Use your favorite stereo algorithm BUT
  - replace two-view SSD with **SSSD** over all baselines
  - **SSSD**: the SSD values are computed first for each pair of stereo images, and then add all together from multiple stereo pairs.

## Limitations

- Only gives a depth map (not an “object model”)
- Won't work for widely distributed views.

# Problem: *visibility*

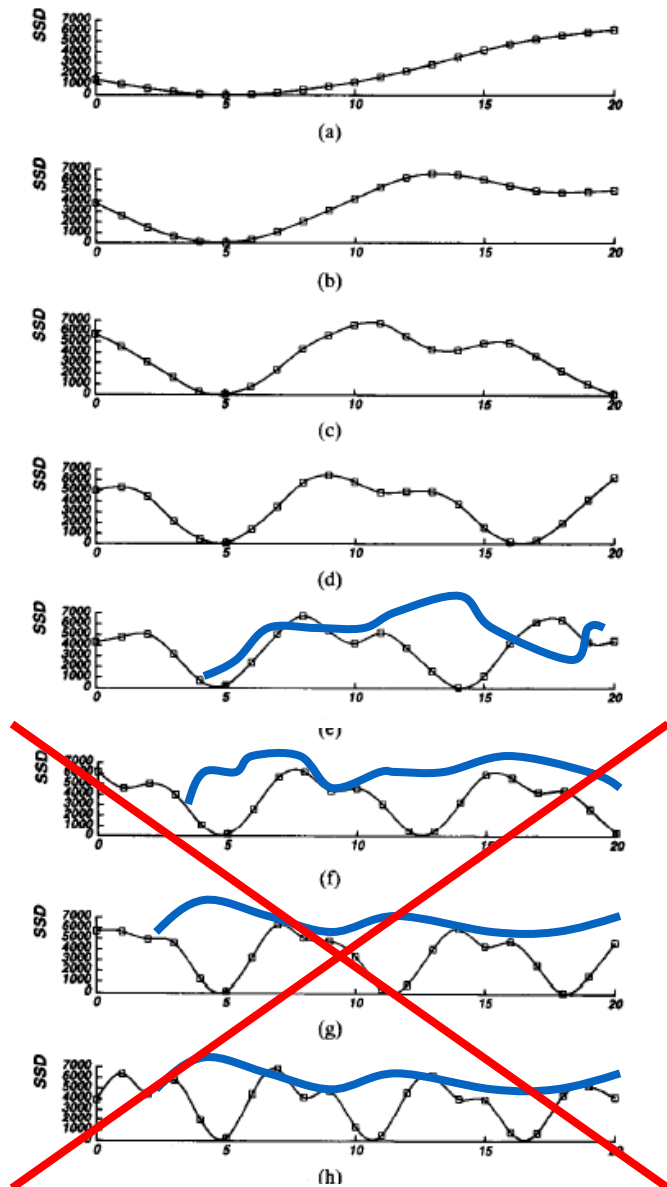


Fig. 5. SSD values versus inverse distance: (a)  $B = b$ ; (b)  $B = 2b$ ; (c)  $B = 3b$ ; (d)  $B = 4b$ ; (e)  $B = 5b$ ; (f)  $B = 6b$ ; (g)  $B = 7b$ ; (h)  $B = 8b$ . The horizontal axis is normalized such that  $8bF = 1$ .

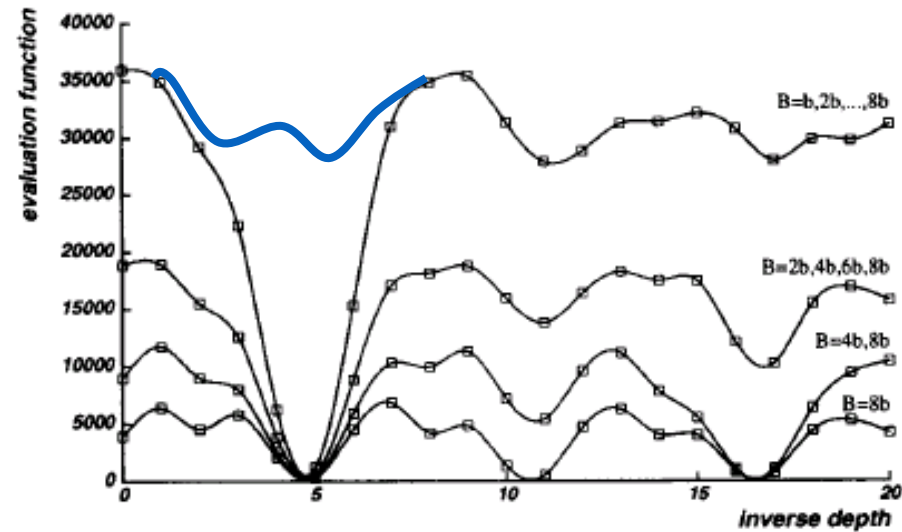


Fig. 7. Combining multiple baseline stereo pairs.

## Some Solutions

- Match only nearby photos [Narayanan 98]
- Use NCC instead of SSD, Ignore NCC values > threshold [Hernandez & Schmitt 03]

# Popular matching scores

- SSD (Sum Squared Distance)

$$\sum_{x,y} |W_1(x, y) - W_2(x, y)|^2$$

- SAD (Sum of Absolute Difference)  $\sum_{x,y} |W_1(x, y) - W_2(x, y)|$

- ZNCC (Zero-mean Normalized Cross Correlation)

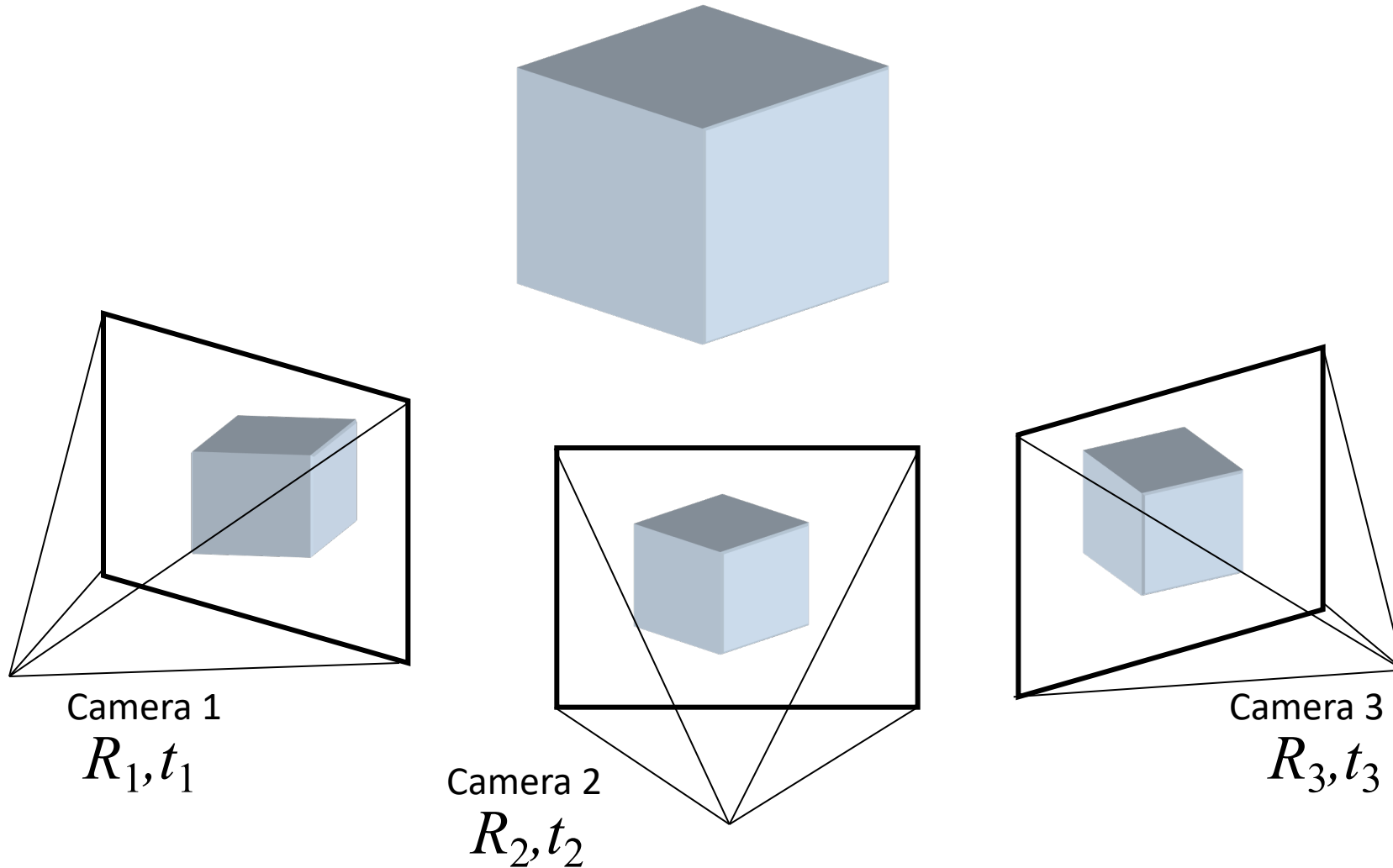
$$\frac{\sum_{x,y} (W_1(x, y) - \overline{W_1})(W_2(x, y) - \overline{W_2})}{\sigma_{W_1} \sigma_{W_2}}$$

- where  $\overline{W_i} = \frac{1}{n} \sum_{x,y} W_i$   $\sigma_{W_i} = \sqrt{\frac{1}{n} \sum_{x,y} (W_i - \overline{W_i})^2}$

- what advantages might NCC have?

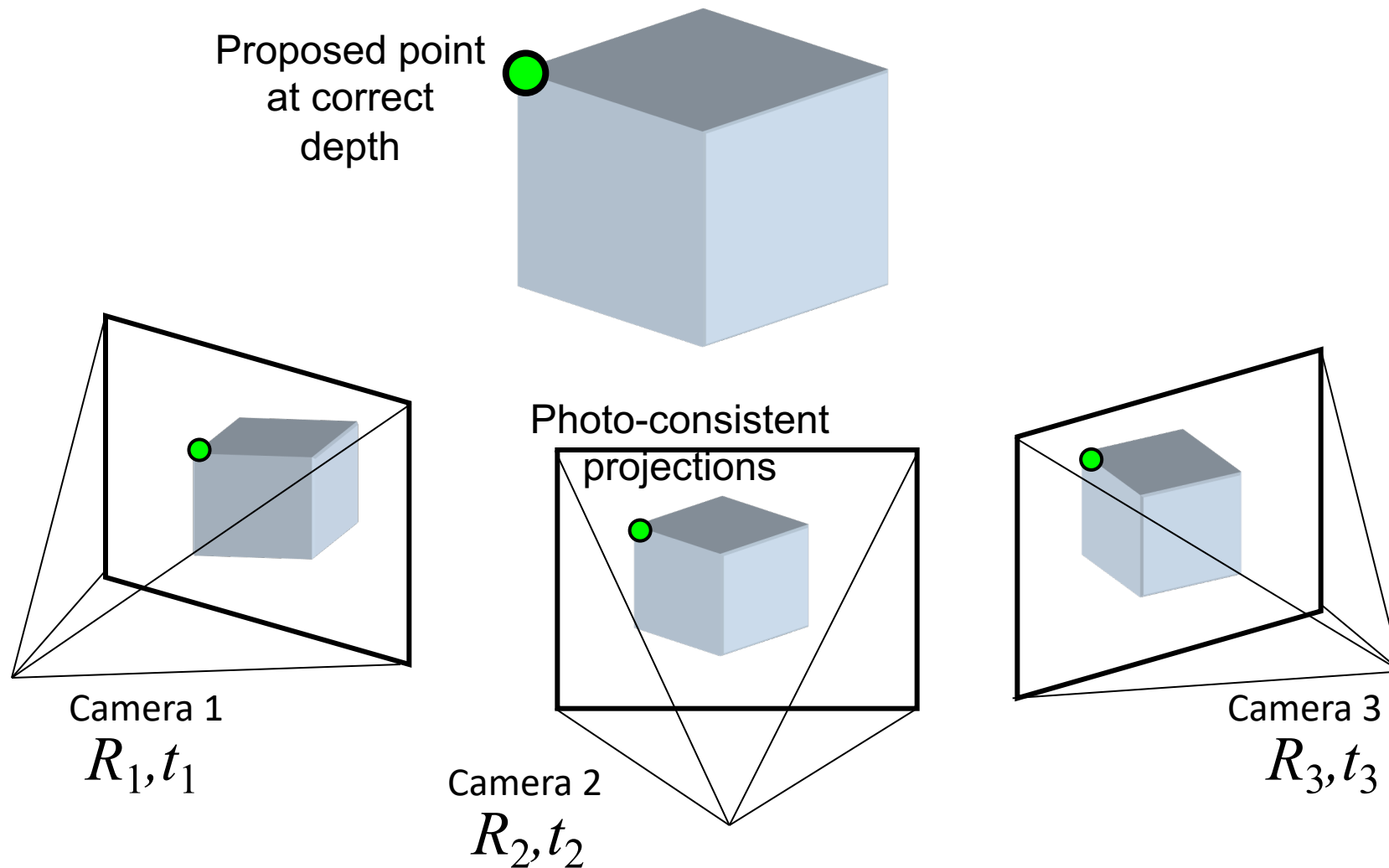
**Questions?**

# Plane-Sweep Stereo

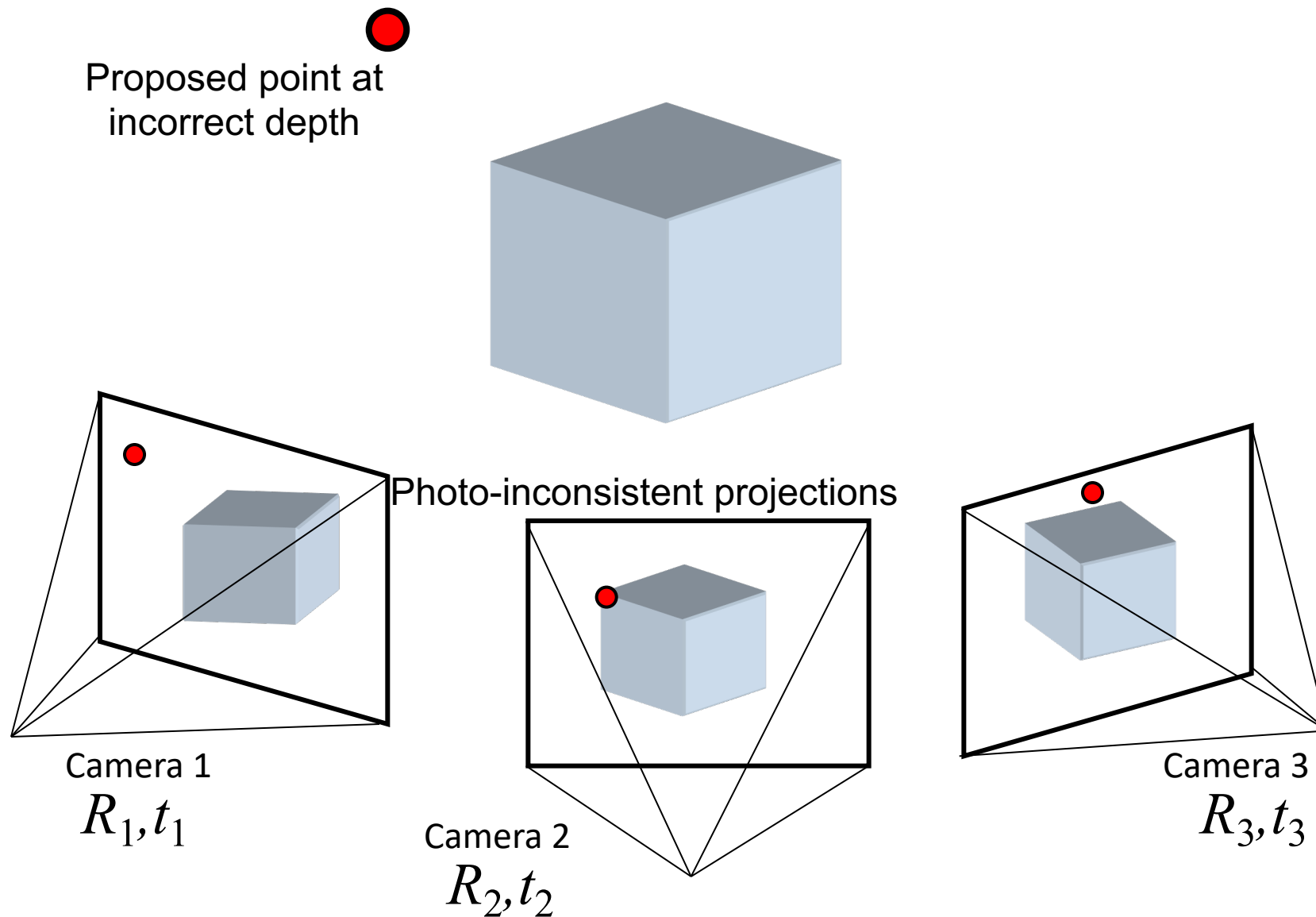




# Plane-Sweep Stereo

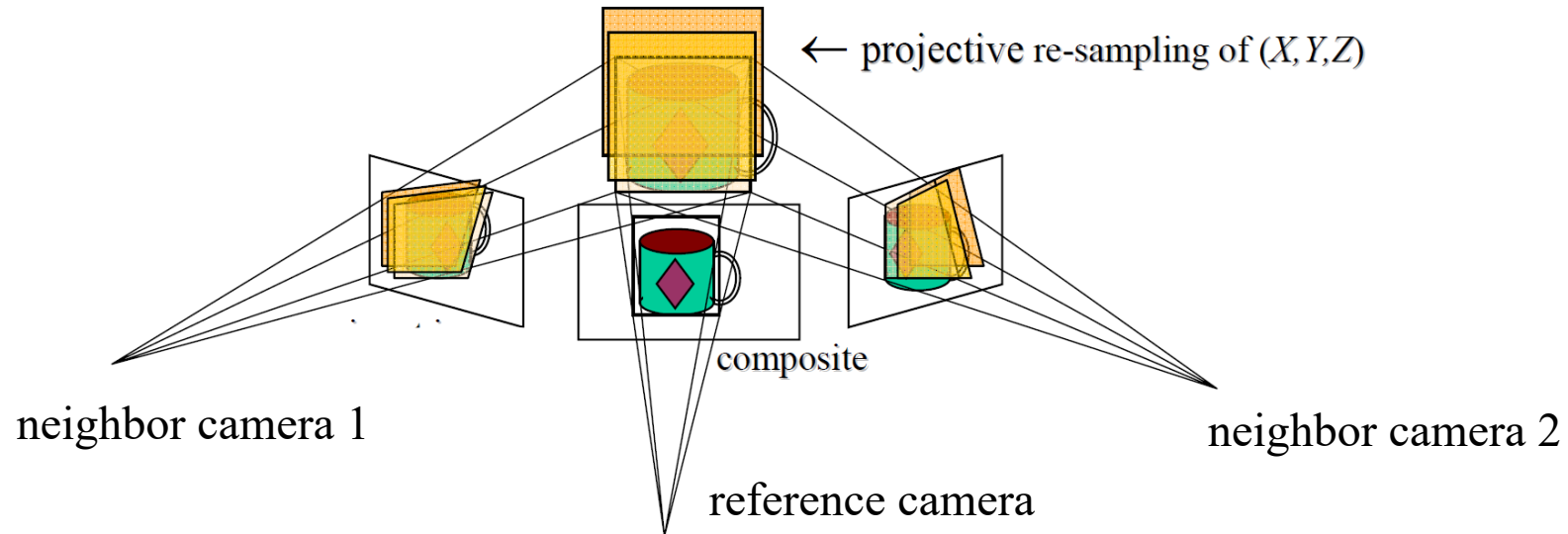


# Plane-Sweep Stereo



# Plane-Sweep Stereo

- Sweep family of planes parallel to the reference camera image plane
- Reproject neighbors onto each plane (via homography) and compare reprojections



# Plane-Sweep Stereo



Left neighbor



Reference image



Right neighbor



Left neighbor projected into reference image



Average images on each plane



Right neighbor projected into reference image

# Another example



Left neighbor



Reference image

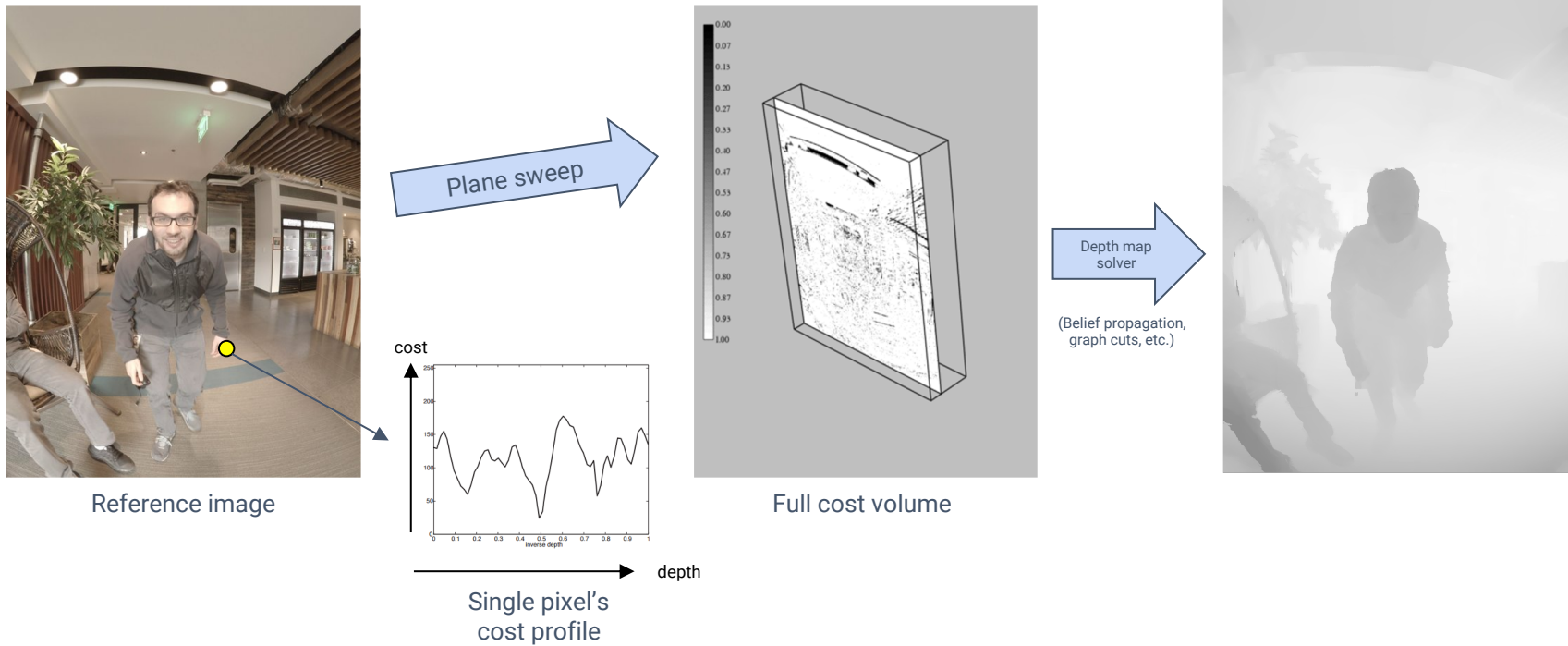


Right neighbor



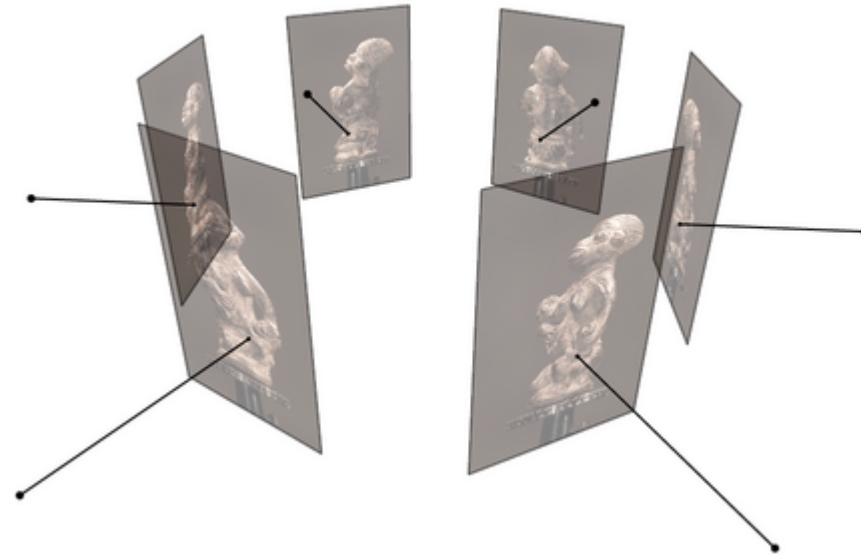
Planar image reprojections  
swept over depth (averaged)

# Cost Volumes -> Depth Maps



# Fusing multiple depth maps

- Compute depth map per image
- Fuse the depth maps into a 3D model



Figures by Carlos Hernandez

**Questions?**