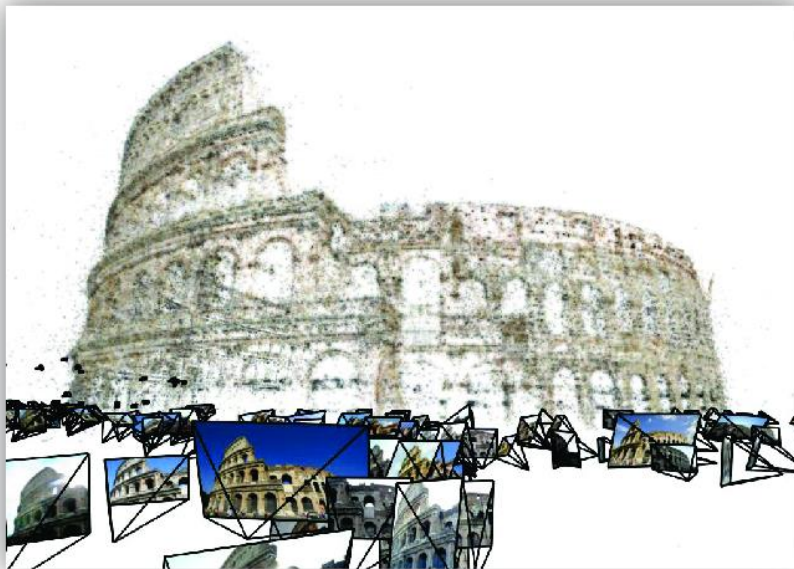


# CS5670: Computer Vision

Noah Snavely

## Multi-view stereo



# Announcements

- Project 4 due April 22, 2019, by 11:59pm
- Final quiz in-class next Wednesday, April 24
- In-class final exam, May 6

# Recommended Reading

- Szeliski Chapter 11.6
- *Multi-View Stereo: A Tutorial*, Furukawa and Hernandez, 2015
  - [http://carlos-hernandez.org/papers/fnt\\_mvs\\_2015.pdf](http://carlos-hernandez.org/papers/fnt_mvs_2015.pdf)

# Multi-view Stereo

**Problem formulation:** given several images of the same object or scene, compute a representation of its 3D shape



Stereo



Multi-view stereo

# Multi-view Stereo



[Point Grey](#)'s Bumblebee XB3



[Point Grey](#)'s ProFusion 25

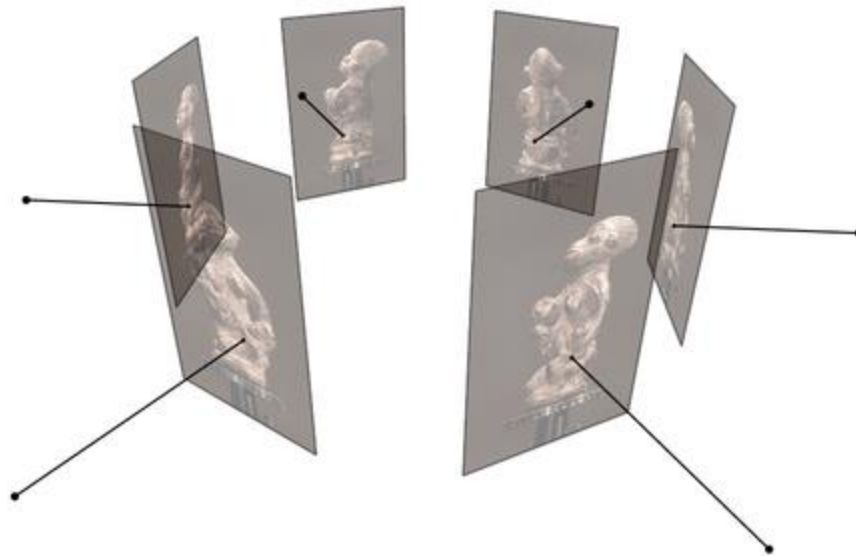


CMU's [3D Room](#)

# Multi-view Stereo

**Input:** calibrated images from several viewpoints (known intrinsics and extrinsics)

**Output:** 3D object model



Figures by Carlos Hernandez

# Applications



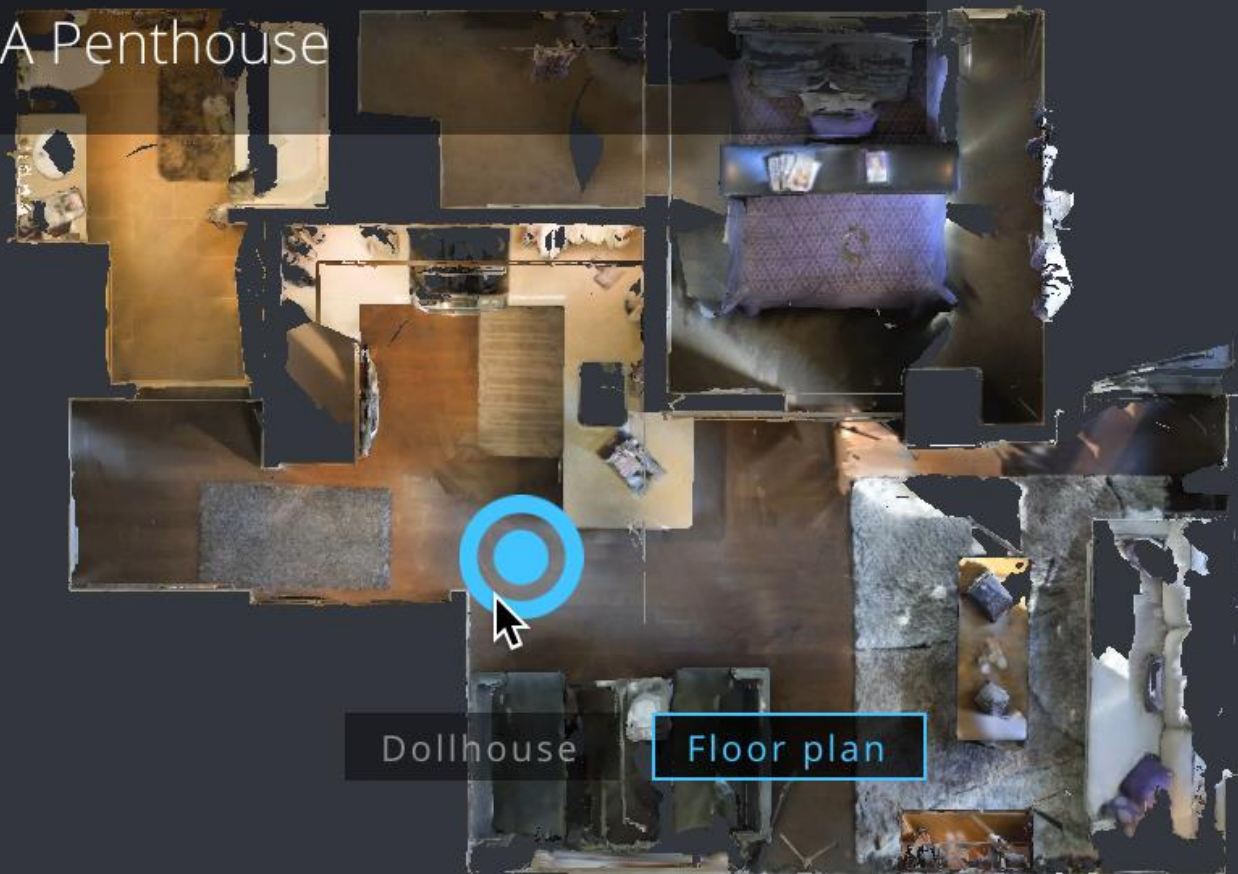
Data SIO, NOAA, U.S. Navy, NGA, GEBCO

Google earth



< 1BR, 1BA Penthouse

[Terms](#)



Dollhouse

Floor plan



# Whistle in the Form of Female Figure 600 AD - 900 AD



Details

Los Angeles County Museum of Art



Los Angeles County Museum of Art



Sculpture



Mexico

Share



Compare



Saved <sup>0</sup>



Discover



Google



THE RENDERPEOPLE MISSION

# ***IMPROVING THE QUALITY***

***TY  
LE***

<https://renderpeople.com/about-us/>





JUMP

Google



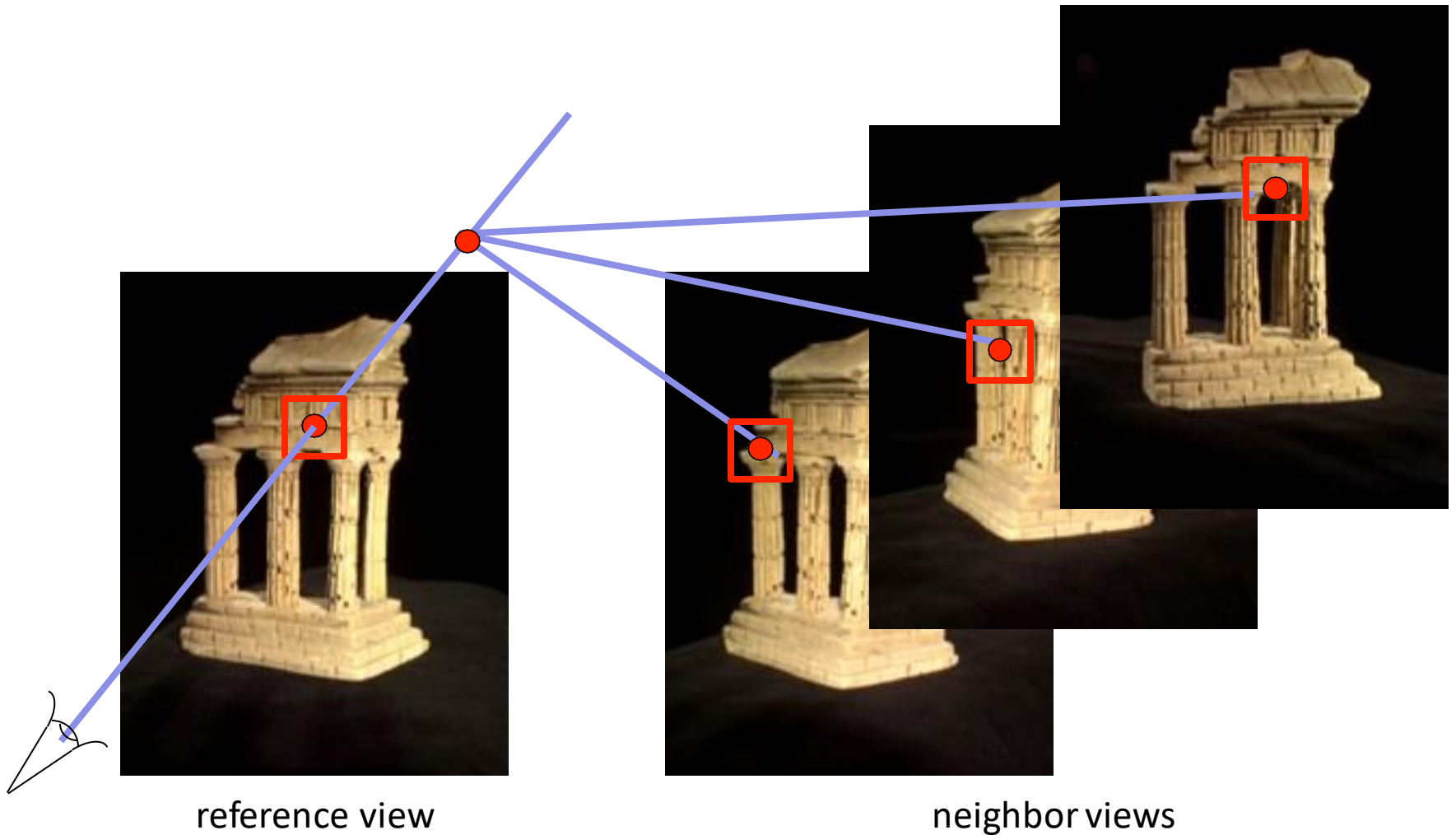




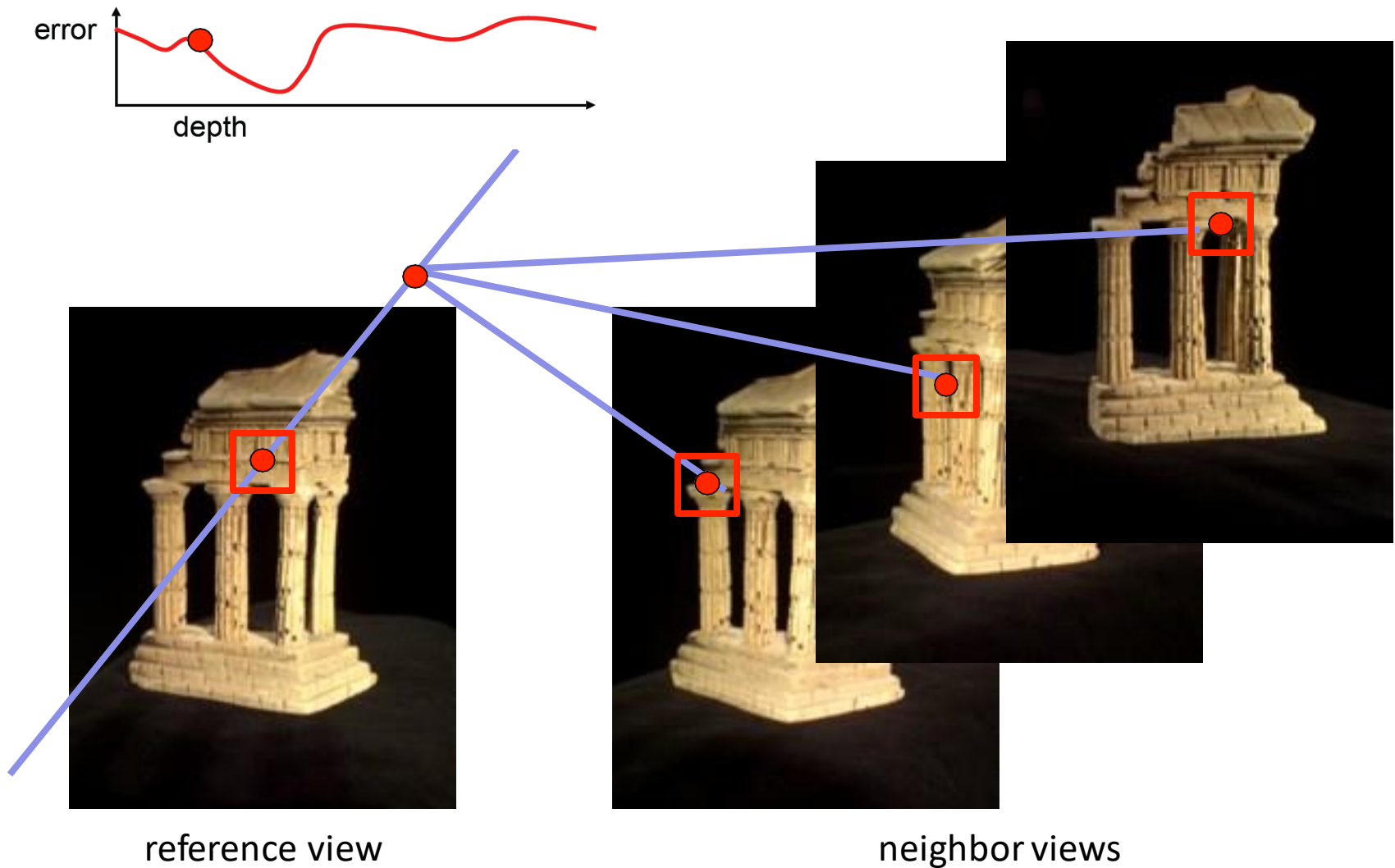
[https://code.facebook.com/posts/1755691291326688/introducing-facebook-surround-360-an-open-high-quality-3d-360-video-capture-system?hc\\_location=ufi](https://code.facebook.com/posts/1755691291326688/introducing-facebook-surround-360-an-open-high-quality-3d-360-video-capture-system?hc_location=ufi)



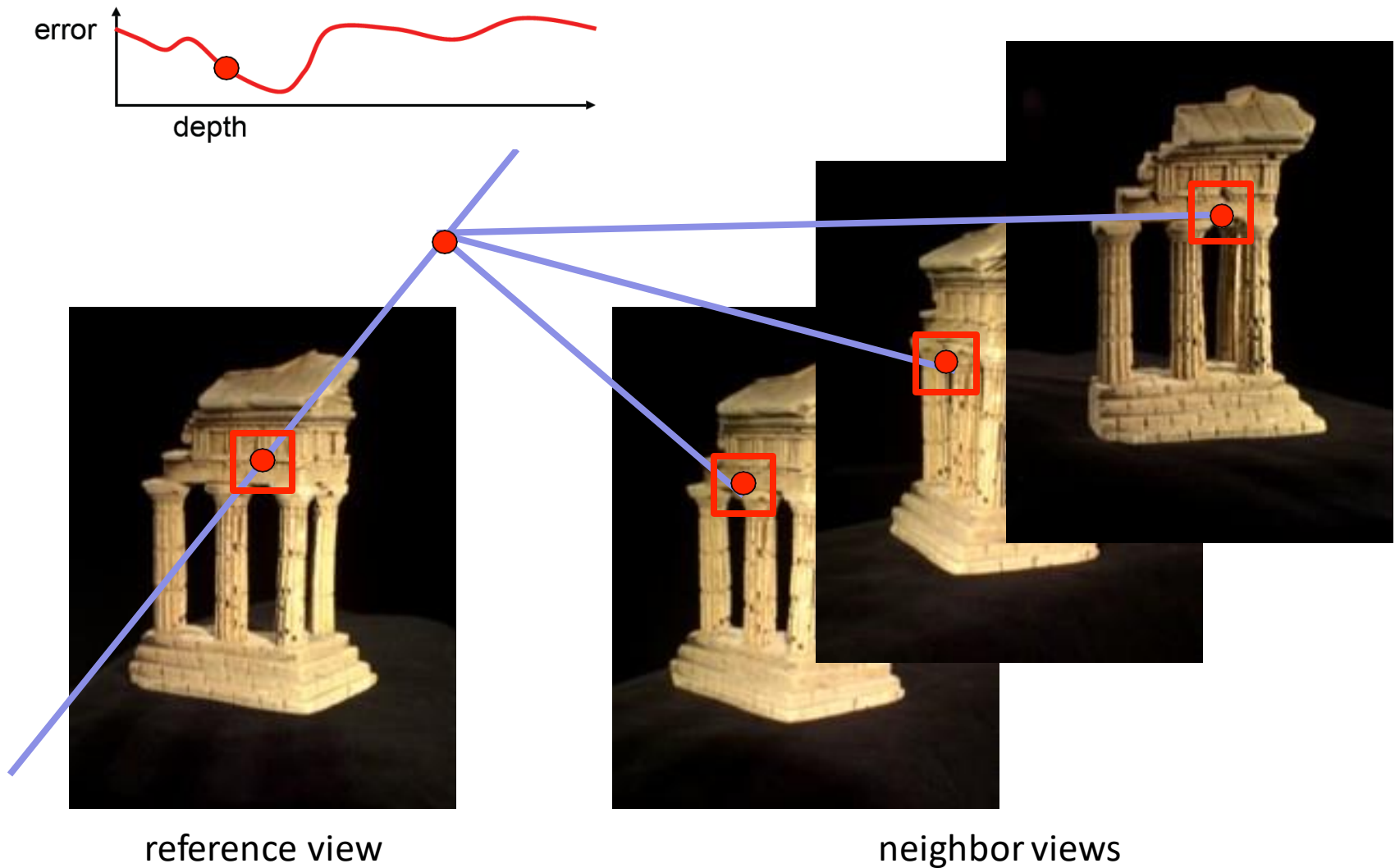
# Multi-view stereo: Basic idea



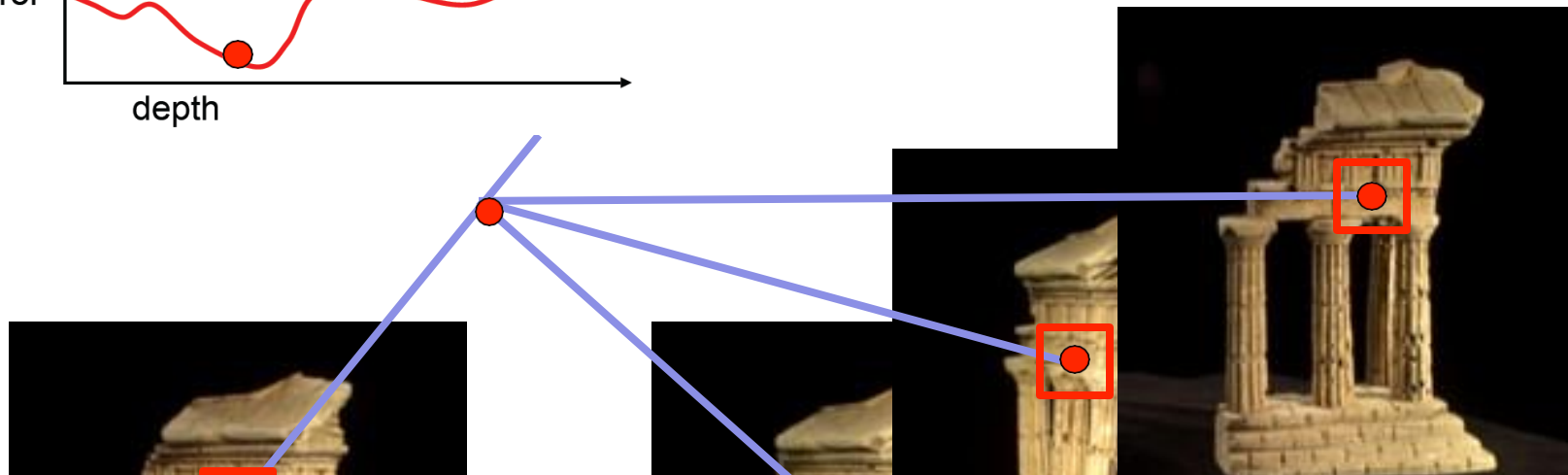
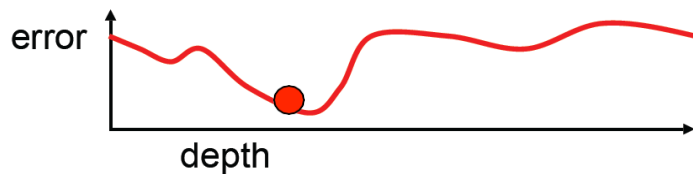
# Multi-view stereo: Basic idea



# Multi-view stereo: Basic idea



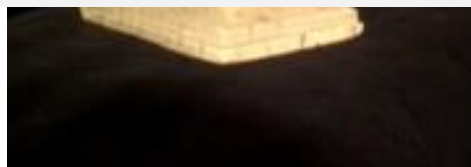
# Multi-view stereo: Basic idea



**In this manner, solve for a depth map  
over the whole reference view**



reference view

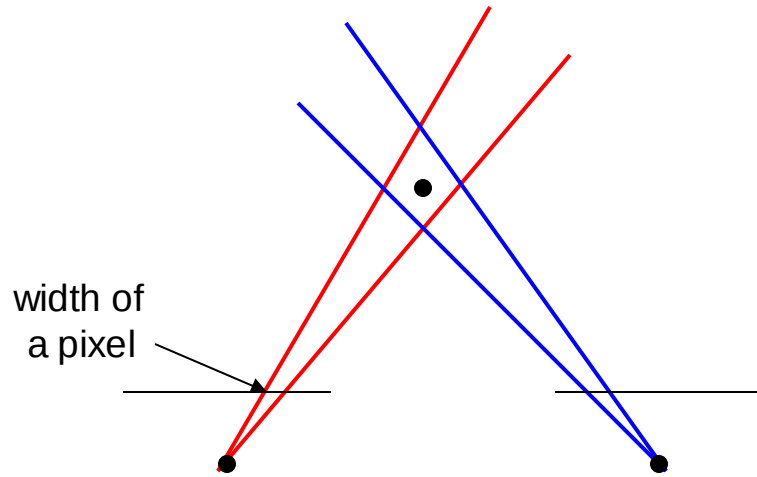


neighbor views

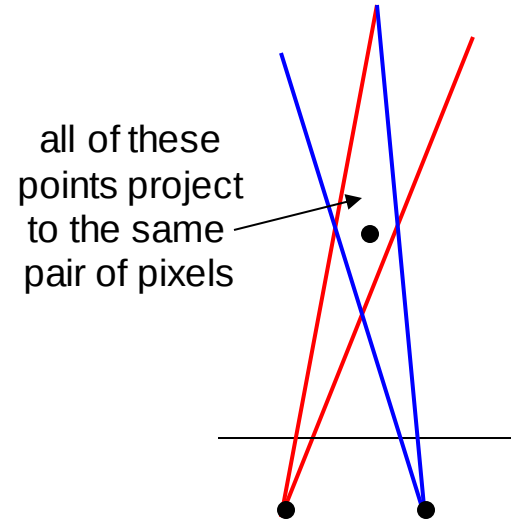
# Multi-view stereo: advantages

- Can match windows using more than 1 neighbor, giving a **stronger match signal**
- If you have lots of potential neighbors, can **choose the best subset** of neighbors to match per reference image
- Can reconstruct a depth map for each reference frame, and then merge into a **complete 3D model**

# Choosing the stereo baseline



**Large Baseline**



**Small Baseline**

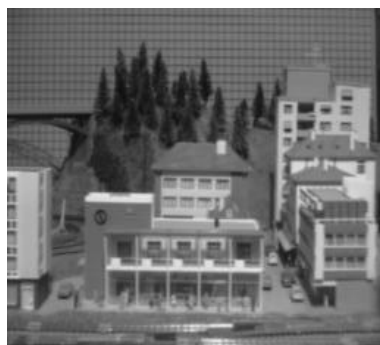
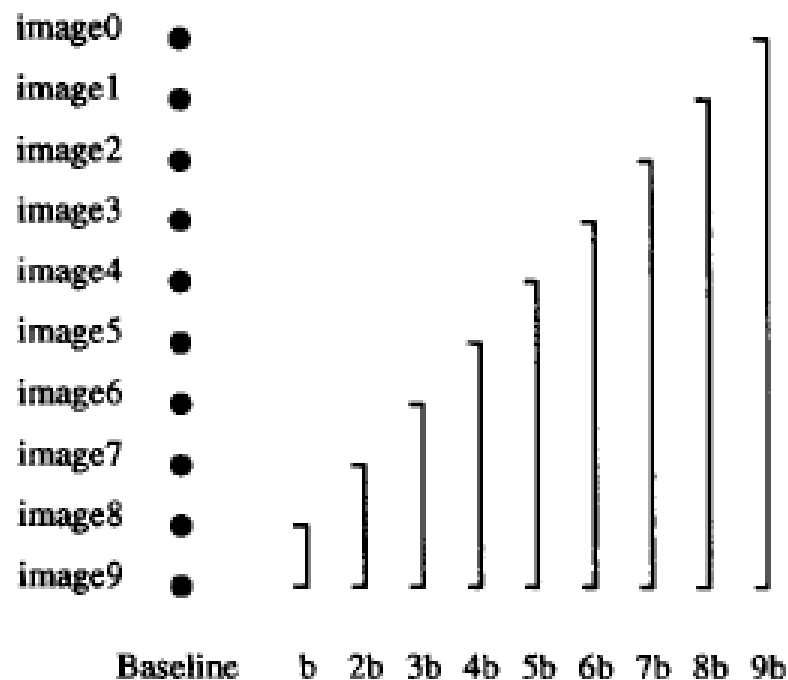
What's the optimal baseline?

- Too small: large depth error
- Too large: difficult search problem

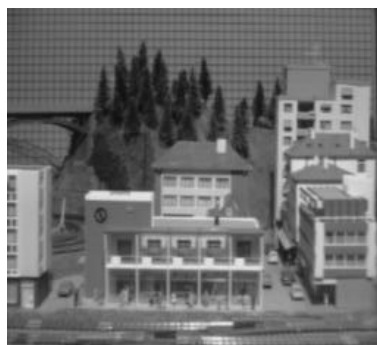
# The Effect of Baseline on Depth Estimation



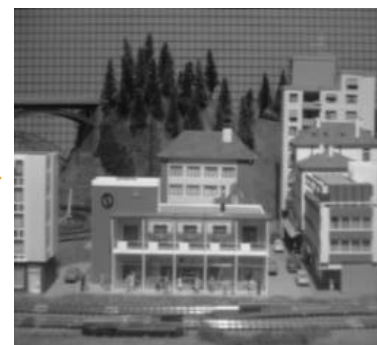
Figure 2: An example scene. The grid pattern in the background has ambiguity of matching.



$I_1$

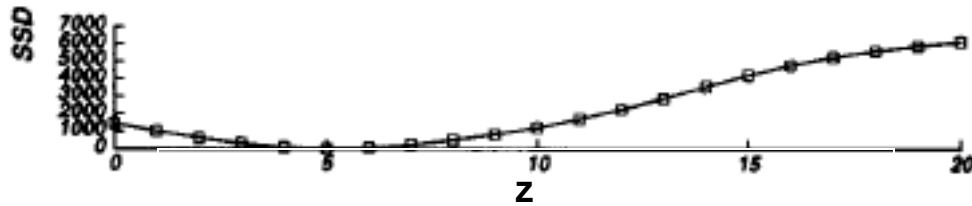


$I_2$

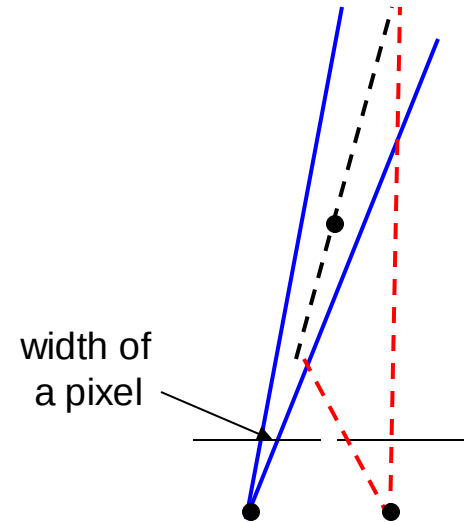


$I_{10}$

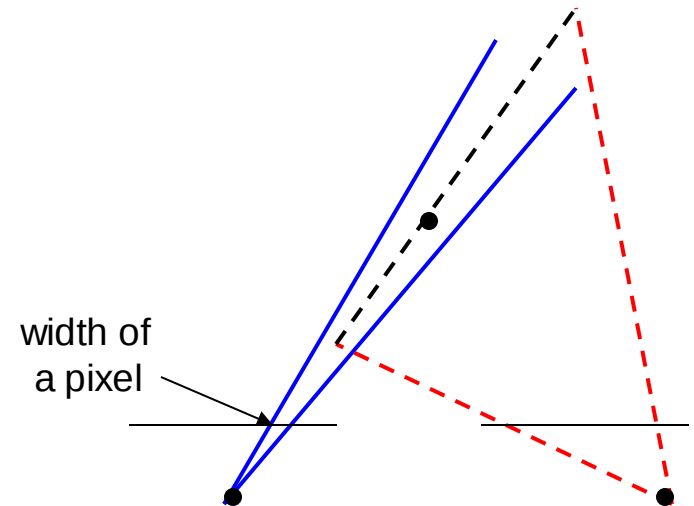
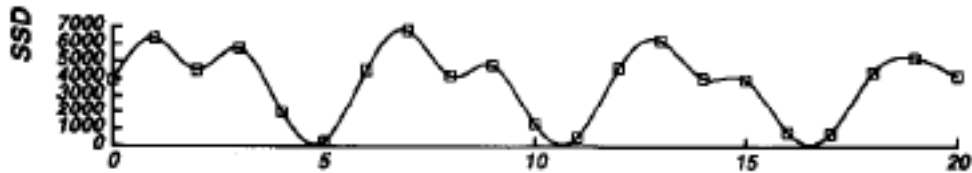
# Multiple-baseline stereo



pixel matching score



- For short baselines, estimated depth will be less precise due to narrow triangulation



- For larger baselines<sup>z</sup>, must search larger area in second image

# Multiple-baseline stereo

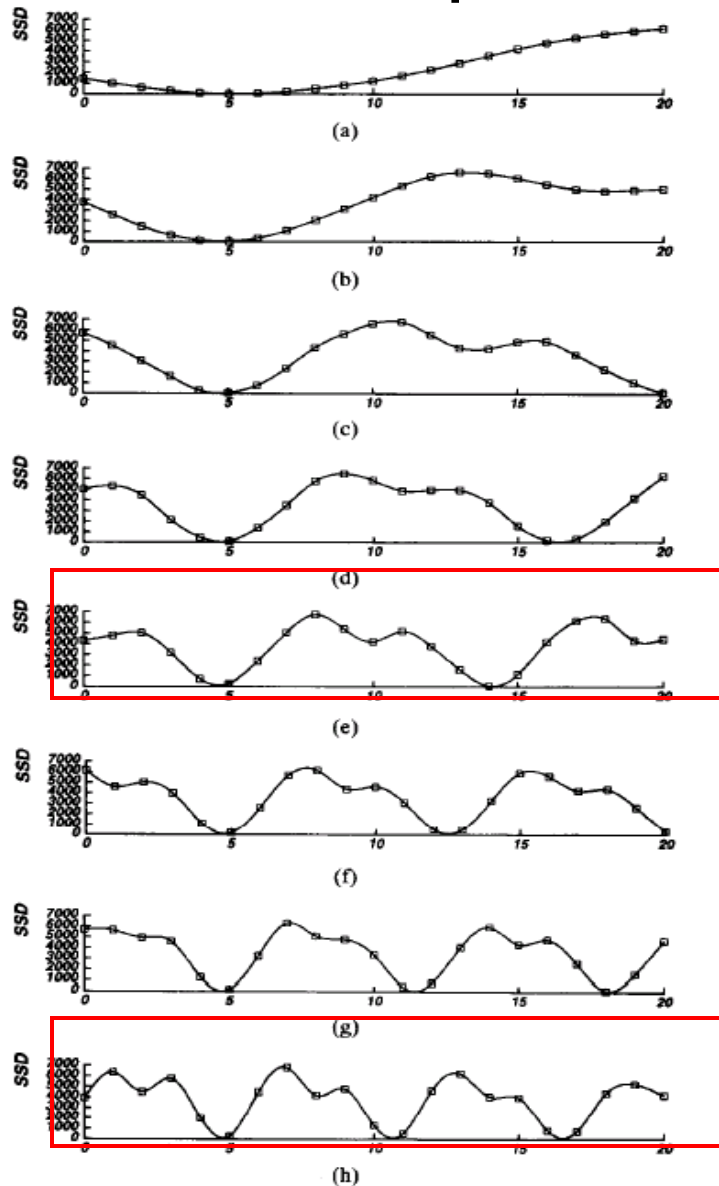


Fig. 5. SSD values versus inverse distance: (a)  $B = b$ ; (b)  $B = 2b$ ; (c)  $B = 3b$ ; (d)  $B = 4b$ ; (e)  $B = 5b$ ; (f)  $B = 6b$ ; (g)  $B = 7b$ ; (h)  $B = 8b$ . The horizontal axis is normalized such that  $8bF = 1$ .

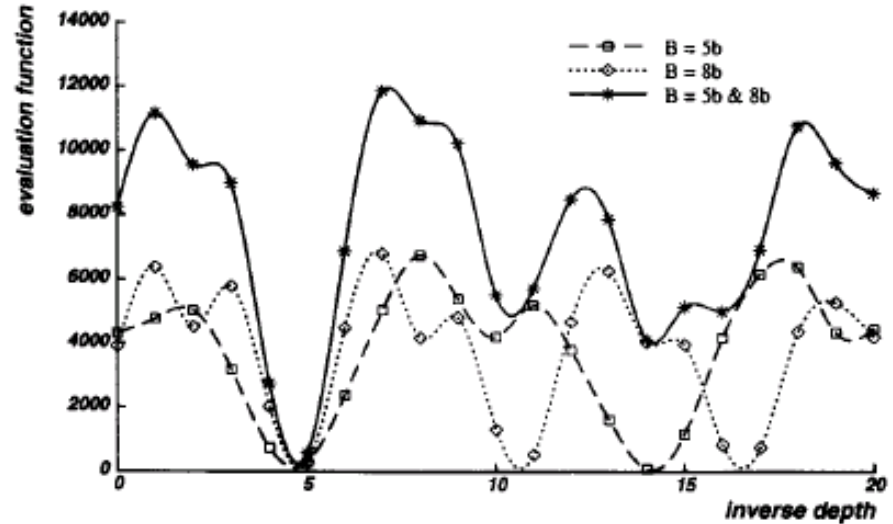


Fig. 6. Combining two stereo pairs with different baselines.

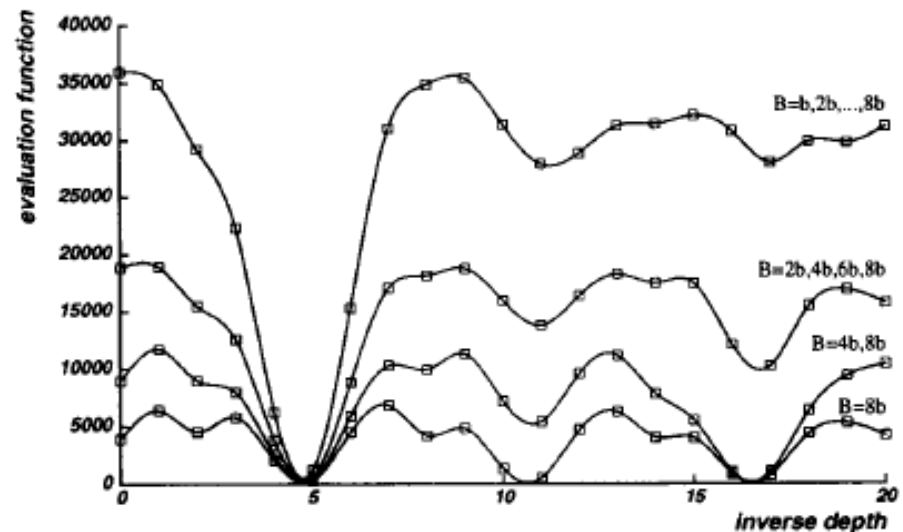
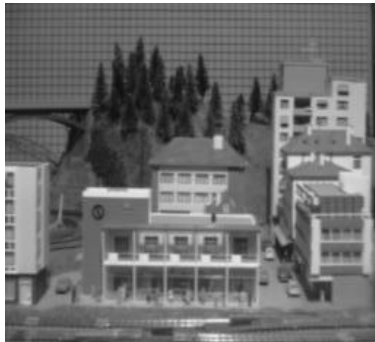
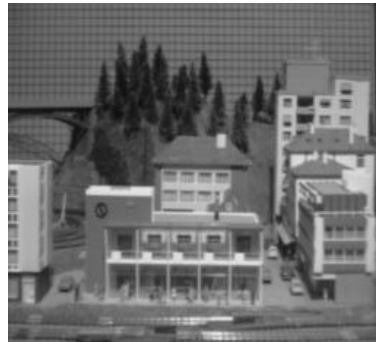


Fig. 7. Combining multiple baseline stereo pairs.

# Multiple-baseline stereo results



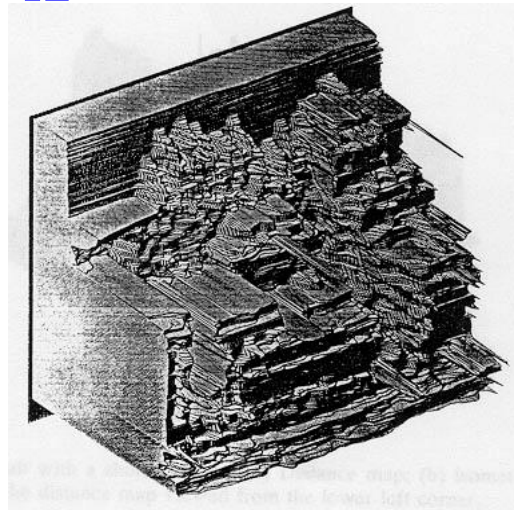
I1



I2



I10



M. Okutomi and T. Kanade, *A Multiple-Baseline Stereo System*, IEEE Trans. on Pattern Analysis and Machine Intelligence, 15(4):353-363 (1993).

# Multibaseline Stereo

## Basic Approach

- Choose a reference view
- Use your favorite stereo algorithm BUT
  - replace two-view SSD with **SSSD** over all baselines
  - **SSSD**: the SSD values are computed first for each pair of stereo images, and then add all together from multiple stereo pairs.

## Limitations

- Only gives a depth map (not an “object model”)
- Won't work for widely distributed views.

# Problem: *visibility*

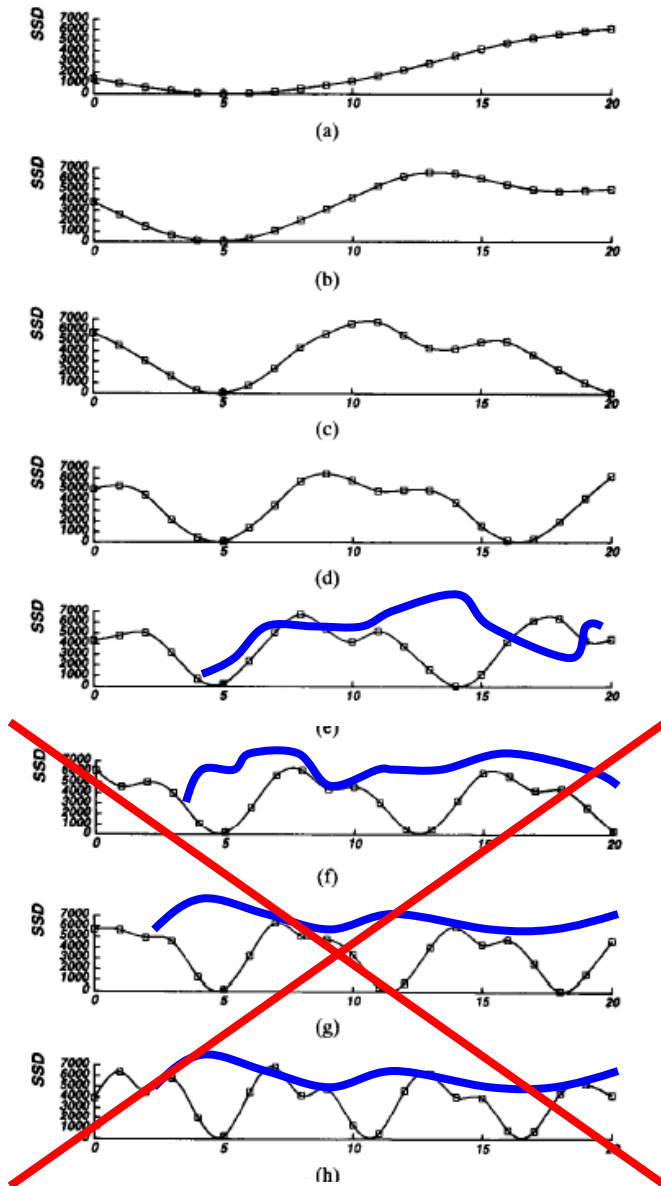


Fig. 5. SSD values versus inverse distance: (a)  $B = b$ ; (b)  $B = 2b$ ; (c)  $B = 3b$ ; (d)  $B = 4b$ ; (e)  $B = 5b$ ; (f)  $B = 6b$ ; (g)  $B = 7b$ ; (h)  $B = 8b$ . The horizontal axis is normalized such that  $8bF = 1$ .

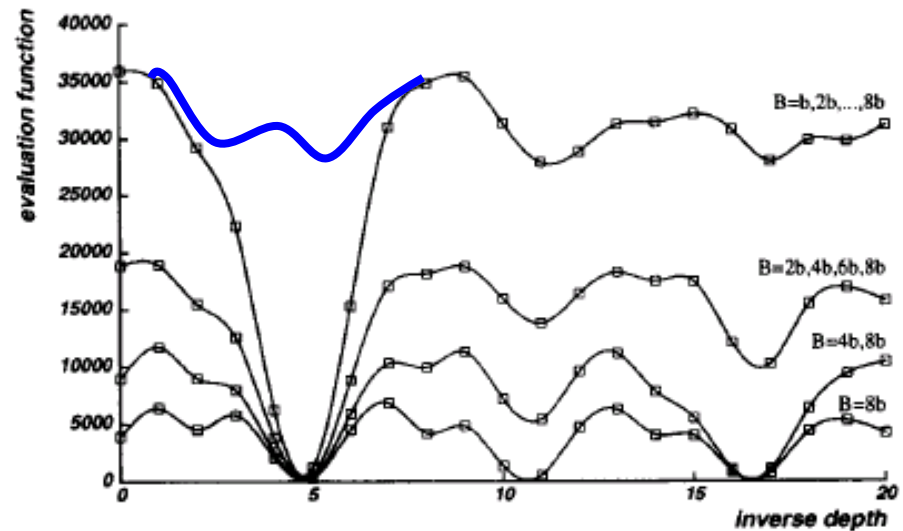


Fig. 7. Combining multiple baseline stereo pairs.

## Some Solutions

- Match only nearby photos [Narayanan 98]
- Use NCC instead of SSD, Ignore NCC values > threshold [Hernandez & Schmitt 03]

# Popular matching scores

- SSD (Sum Squared Distance)

$$\sum_{x,y} |W_1(x, y) - W_2(x, y)|^2$$

- SAD (Sum of Absolute Difference)  $\sum_{x,y} |W_1(x, y) - W_2(x, y)|$
- ZNCC (Zero-mean Normalized Cross Correlation)

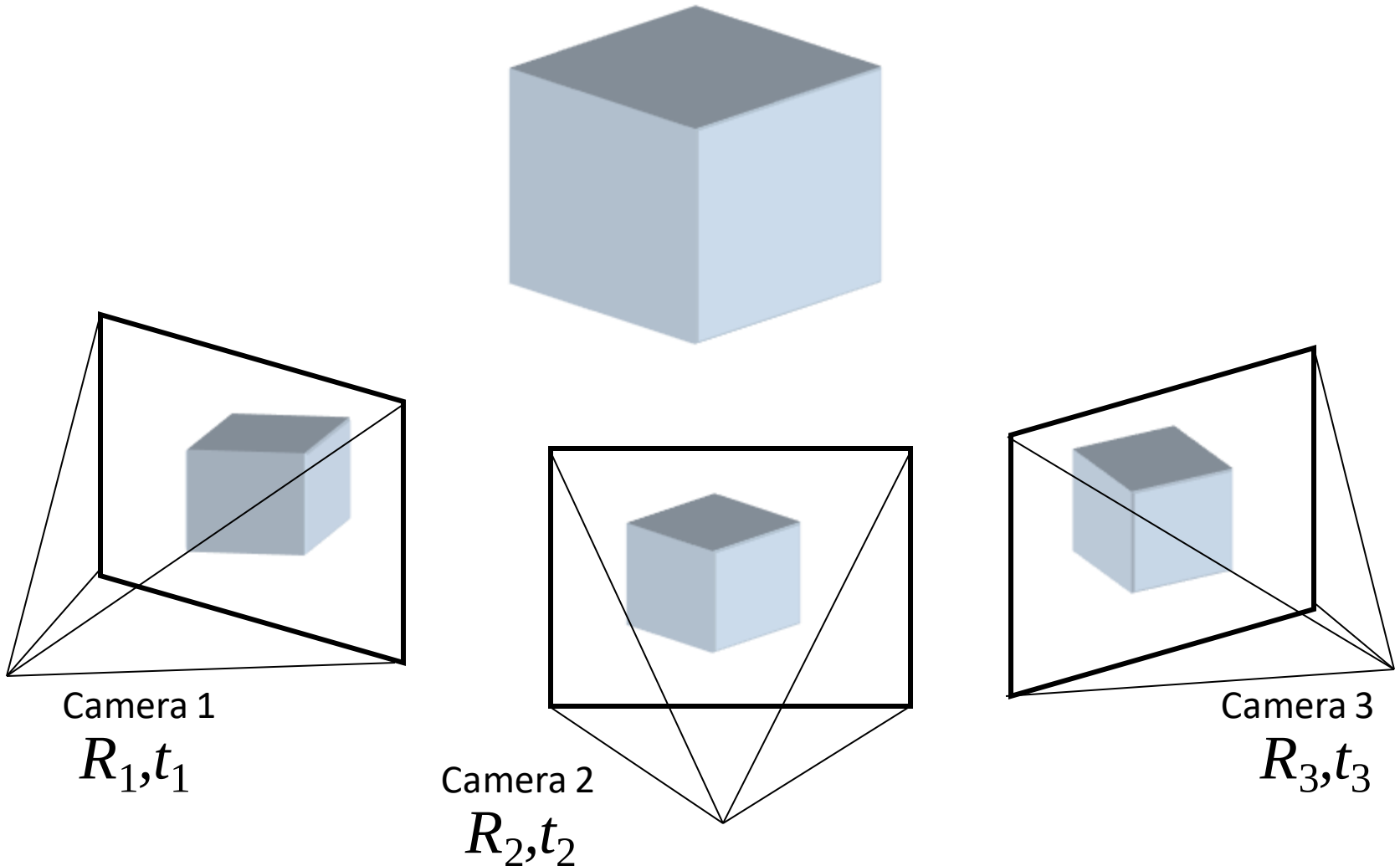
$$\frac{\sum_{x,y} (W_1(x, y) - \overline{W_1})(W_2(x, y) - \overline{W_2})}{\sigma_{W_1} \sigma_{W_2}}$$

– where  $\overline{W_i} = \frac{1}{n} \sum_{x,y} W_i$      $\sigma_{W_i} = \sqrt{\frac{1}{n} \sum_{x,y} (W_i - \overline{W_i})^2}$

– what advantages might NCC have?

# Questions?

# Plane-Sweep Stereo



# Plane-Sweep Stereo

Proposed point  
at correct depth

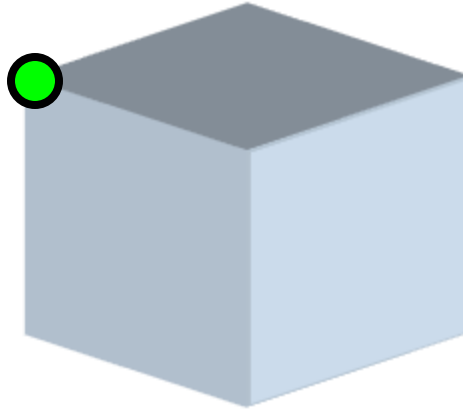
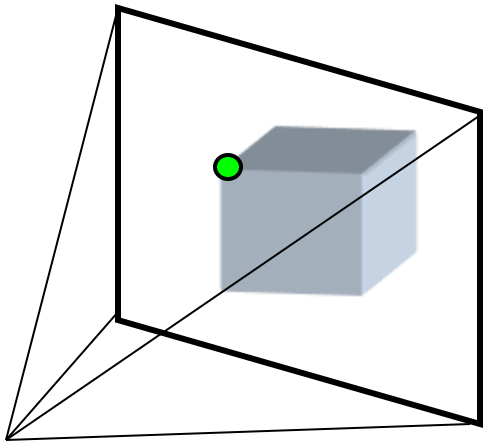
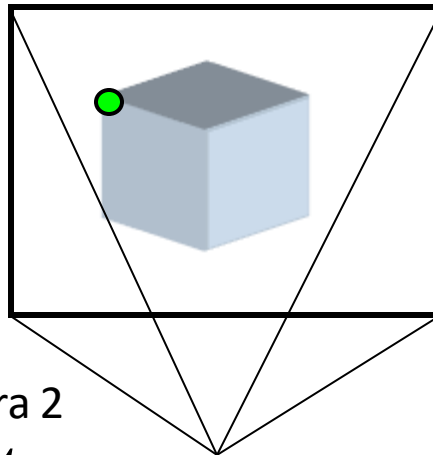


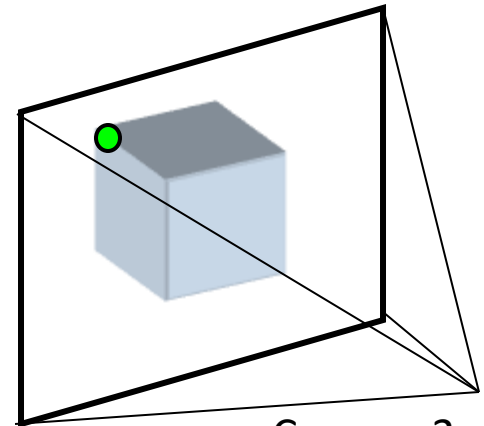
Photo-consistent projections



Camera 1  
 $R_1, t_1$



Camera 2  
 $R_2, t_2$



Camera 3  
 $R_3, t_3$

# Plane-Sweep Stereo



Proposed point at  
incorrect depth

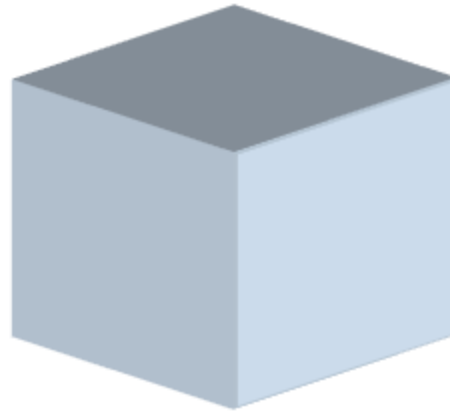
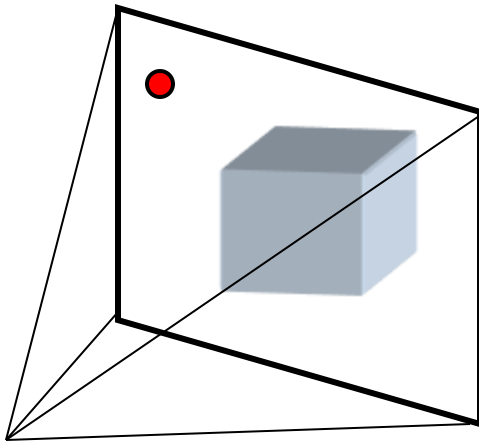
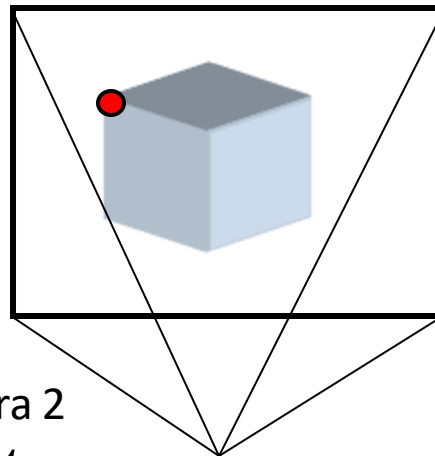


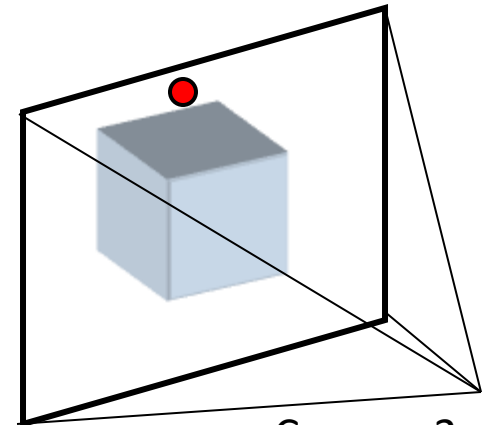
Photo-inconsistent projections



Camera 1  
 $R_1, t_1$



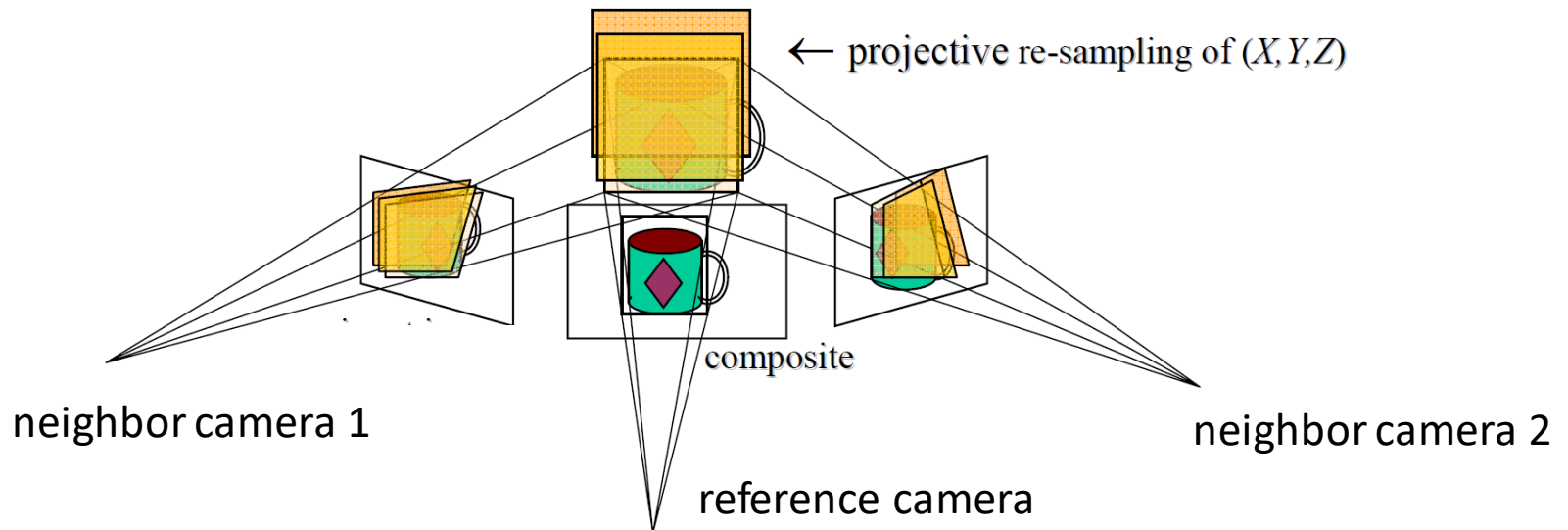
Camera 2  
 $R_2, t_2$



Camera 3  
 $R_3, t_3$

# Plane-Sweep Stereo

- Sweep family of planes parallel to the reference camera image plane
- Reproject neighbors onto each plane (via homography) and compare reprojections



# Plane-Sweep Stereo



Left neighbor



Reference image



Right neighbor



Left neighbor projected into  
reference image



Average images on each plane



Right neighbor projected into  
reference image

# Another example



Left neighbor



Reference image



Right neighbor

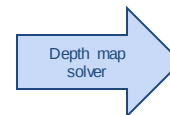
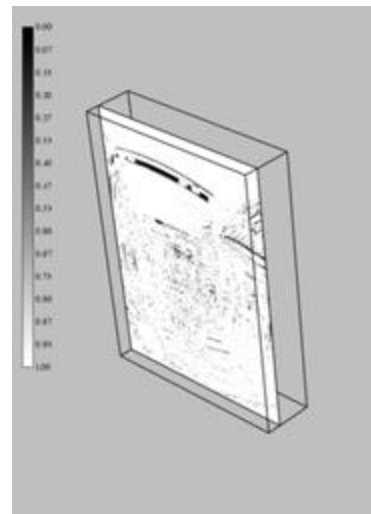
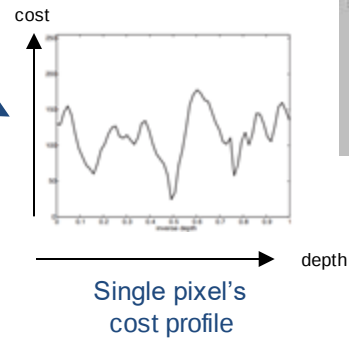


Planar image reprojections  
swept over depth (averaged)

# Cost Volumes -> Depth Maps



Reference image

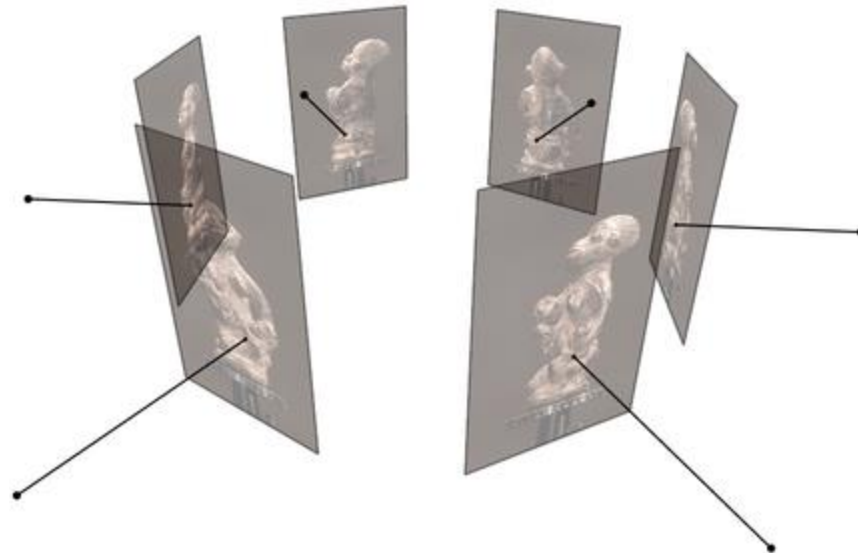


(Belief propagation,  
graph cuts, etc.)



# Fusing multiple depth maps

- Compute depth map per image
- Fuse the depth maps into a 3D model



Figures by Carlos Hernandez

# Questions?