

Sequence Model

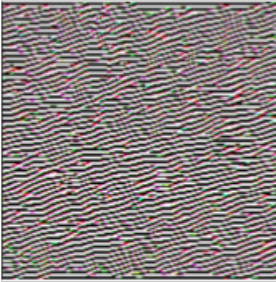
Announcements

1. Makeup exam Dec 11
2. We will release the last reading quiz today

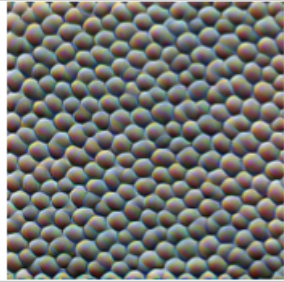
Recap on Convolutional neural network

Learned feature representations in CNN

Edges



Textures



Patterns



Parts



Objects



Objective today

Understanding neural network structures that are suitable for natural language (i.e., sequences of words)

Outline today

1. Word-2-Vec embedding and positional embedding

2. Attention model

3. Putting things together: the Transformer model

Example: autocompletion

e.g., I went to the climbing gym and I ____

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$$y_1 \sim P(Y = \cdot \mid x_1, \dots, x_n) \in \mathbb{R}^{100k}$$

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$$y_2 \sim P(Y = \cdot \mid x_1, \dots, x_n, y_1)$$

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A Language model is a conditional probability model:

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$$y_2 \sim P(Y = \cdot \mid x_1, \dots, x_n, y_1)$$

$$y_m \sim P(Y = \cdot \mid x_1, \dots, x_n, y_1, \dots, y_{m-1})$$

Word to Vector Embedding

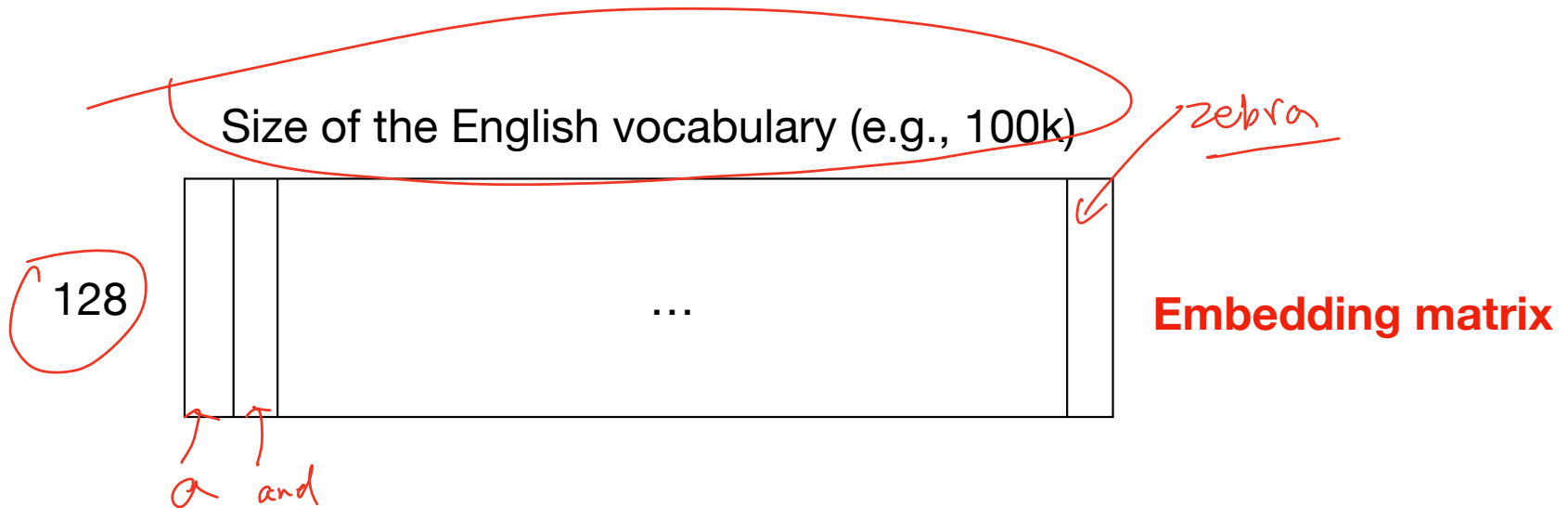
ML models only take vectors of real numbers as inputs...

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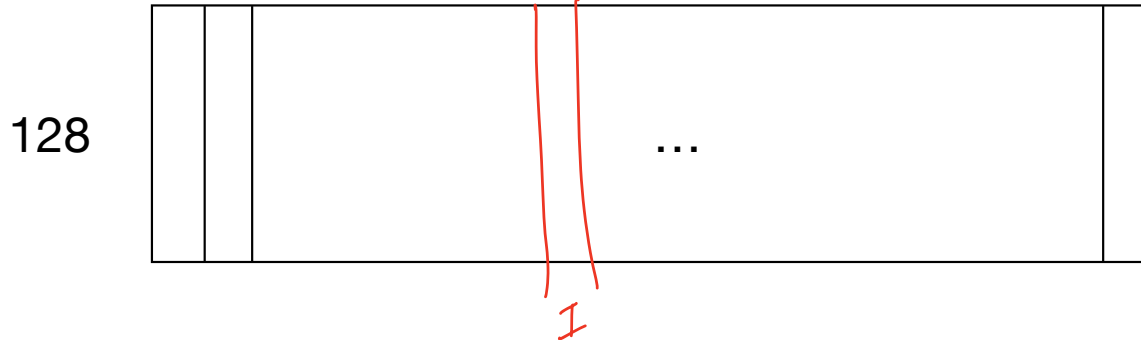
Word to Vector Embedding

ML models only take vectors of real numbers as inputs...

e.g., I went to the climbing gym and I

$$u_I \in \mathbb{R}^{128}$$

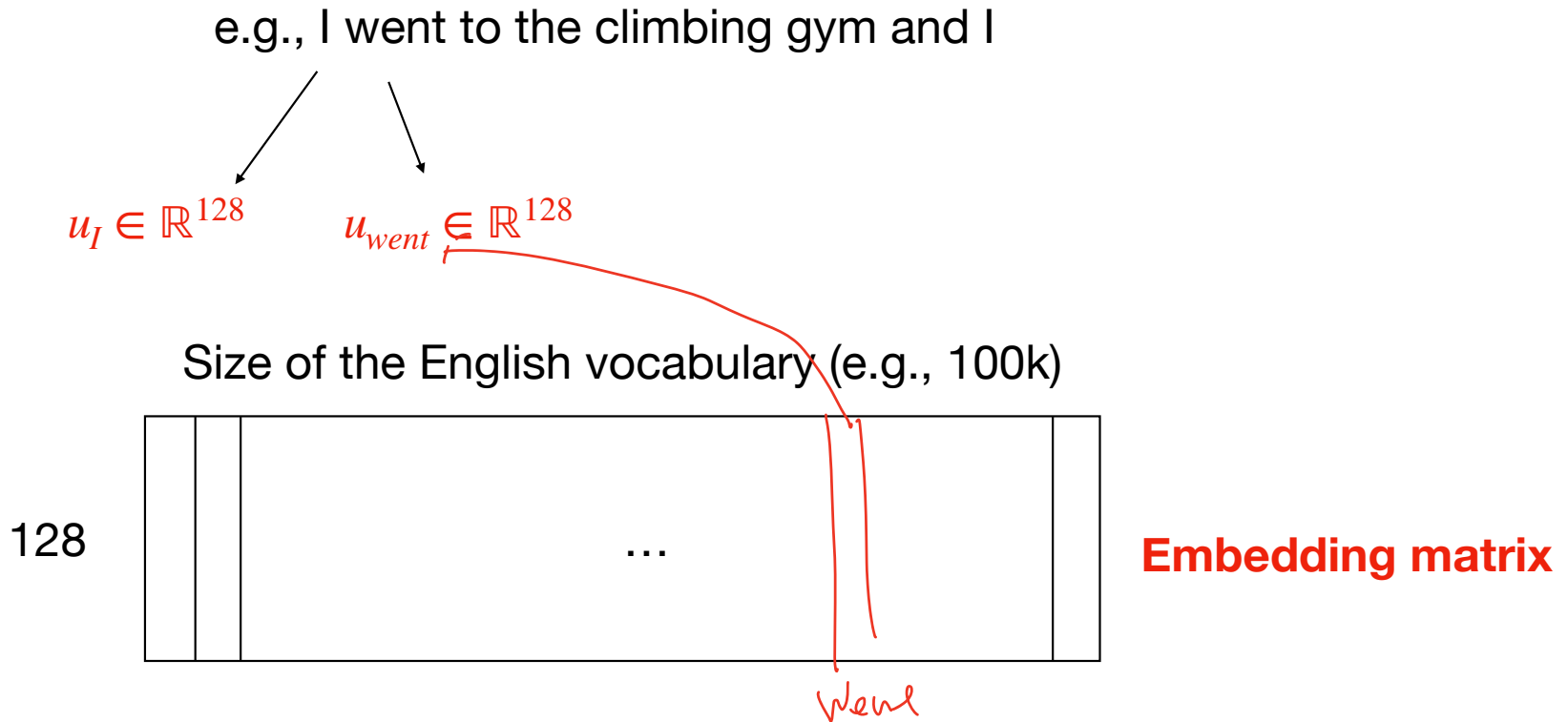
Size of the English vocabulary (e.g., 100k)



Embedding matrix

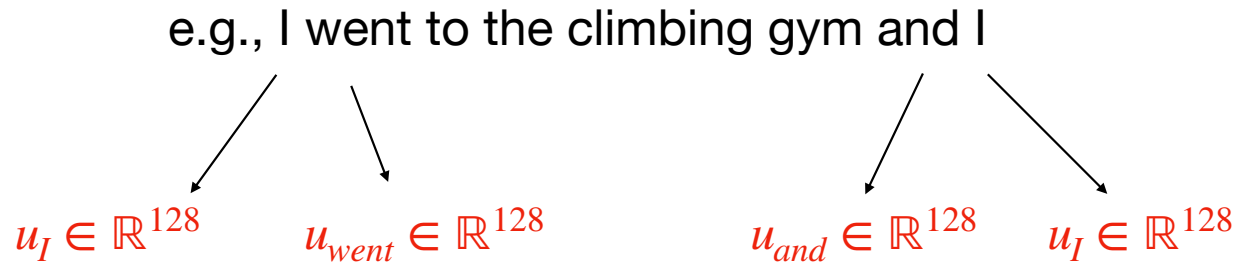
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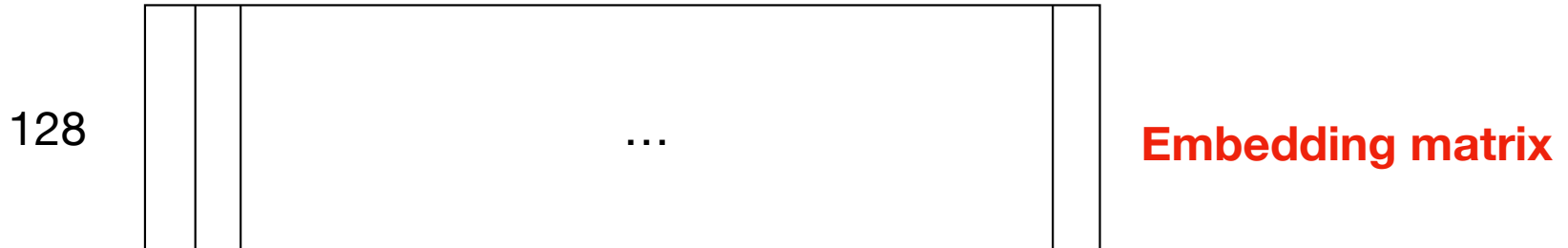


Word to Vector Embedding

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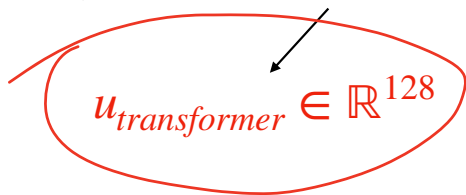
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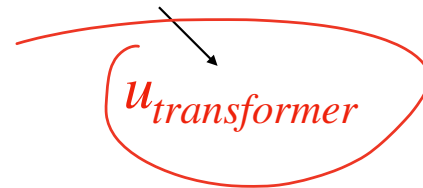
Positional embedding

Order of the words and their positions matter...

e.g., When I say Transformer in ML, I do not mean the transformer in the movies



$u_{\text{transformer}} \in \mathbb{R}^{128}$



$u_{\text{transformer}}$

Positional embedding

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$$\begin{array}{ccc} \swarrow & \downarrow & \swarrow \\ u_{\text{transformer}} \in \mathbb{R}^{128} & u_{\text{mean}} & u_{\text{transformer}} + p_{13} \in \mathbb{R}^{128} \\ + p_4 \in \mathbb{R}^{128} & + p_{11} & \end{array}$$

Positional embedding

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$$u_{transformer} \in \mathbb{R}^{128}$$
$$+ p_4 \in \mathbb{R}^{128}$$

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Create positional embedding using sin functions

Positional embedding

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$$u_{\text{transformer}} \in \mathbb{R}^{128} \\ + p_4 \in \mathbb{R}^{128}$$

$$u_{\text{transformer}} + p_{13} \in \mathbb{R}^{128}$$

Create positional embedding using sin functions

$t \in \{1, \dots, N\}$
 t_i position

$$p_t = \begin{bmatrix} \sin(t/c_1) \\ \sin(t/c_2) \\ \dots \\ \sin(t/c_{128}) \end{bmatrix}$$

c_1 small

c_{128} big

Positional embedding

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$u_{\text{transformer}} \in \mathbb{R}^{128}$
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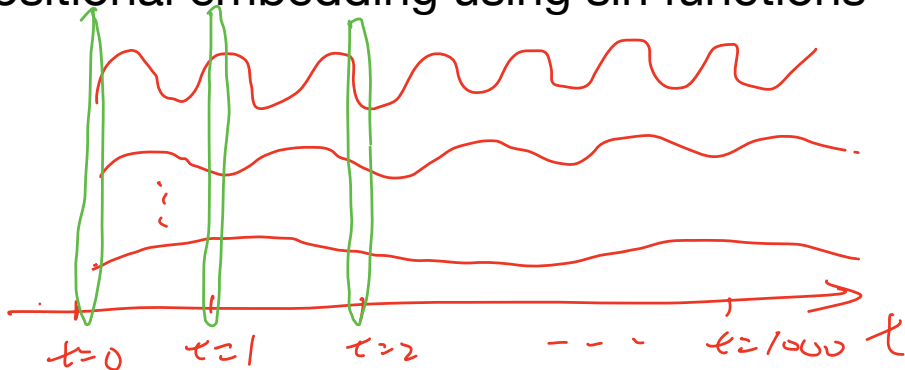
$u_{\text{transformer}} + p_{13} \in \mathbb{R}^{128}$

High frequency

$$p_t = \begin{bmatrix} \sin(t/c_1) \\ \sin(t/c_2) \\ \vdots \\ \sin(t/c_{128}) \end{bmatrix}$$

Low frequency

Create positional embedding using sin functions



Summary so far

We turn words into vectors of real numbers

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$$u_{transformer} + p_4$$


$$u_{transformer} + p_{13} \in \mathbb{R}^{128}$$

Summary so far

We turn words into vectors of real numbers

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$$u_{\text{transformer}} + p_4$$

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Feature of the word + feature of the position

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Motivation

e.g., When I say Transformer in ML, I do not mean the transformer in the movies

e.g., When I say Transformer, I literally mean the transformer in the movies

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Contextual feature: feature of a word should depend on the context around it

Self-attention

I went to the climbing gym

Word-2-vec + positional

x_1

x_2

x_3

x_4

x_5

x_6

$\in \mathbb{R}^{128}$

Self-attention

I went to the climbing gym

Word-2-vec + positional

x_1

x_2

x_3

x_4

x_5

x_6

$R^{128 \times 128}$
 $R^{128 \times 128}$
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Attention head:
three matrices:
 W_q, W_k, W_v

x

Self-attention

I went to the climbing gym

Word-2-vec + positional

x_1

x_2

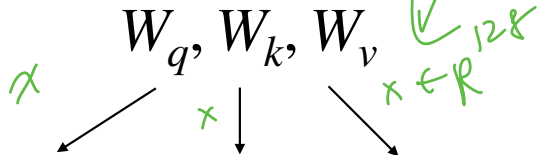
x_3

x_4

x_5

x_6

Attention head:
three matrices:

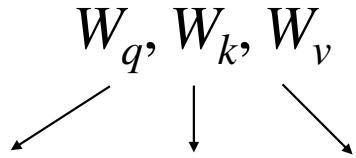


$$q = W_q x \quad k = W_k x \quad v = W_v x$$

Query key value

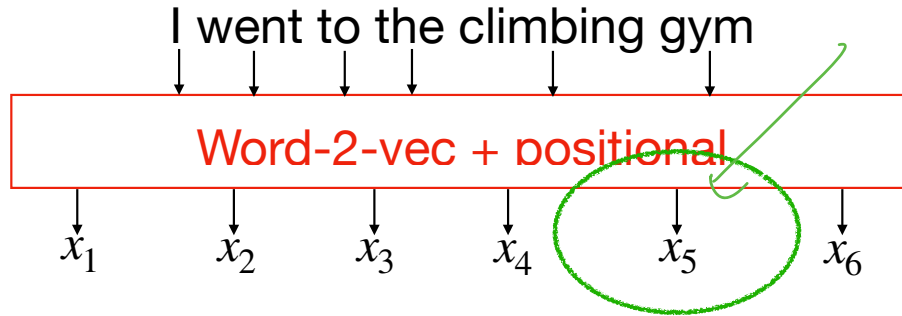
Self-attention

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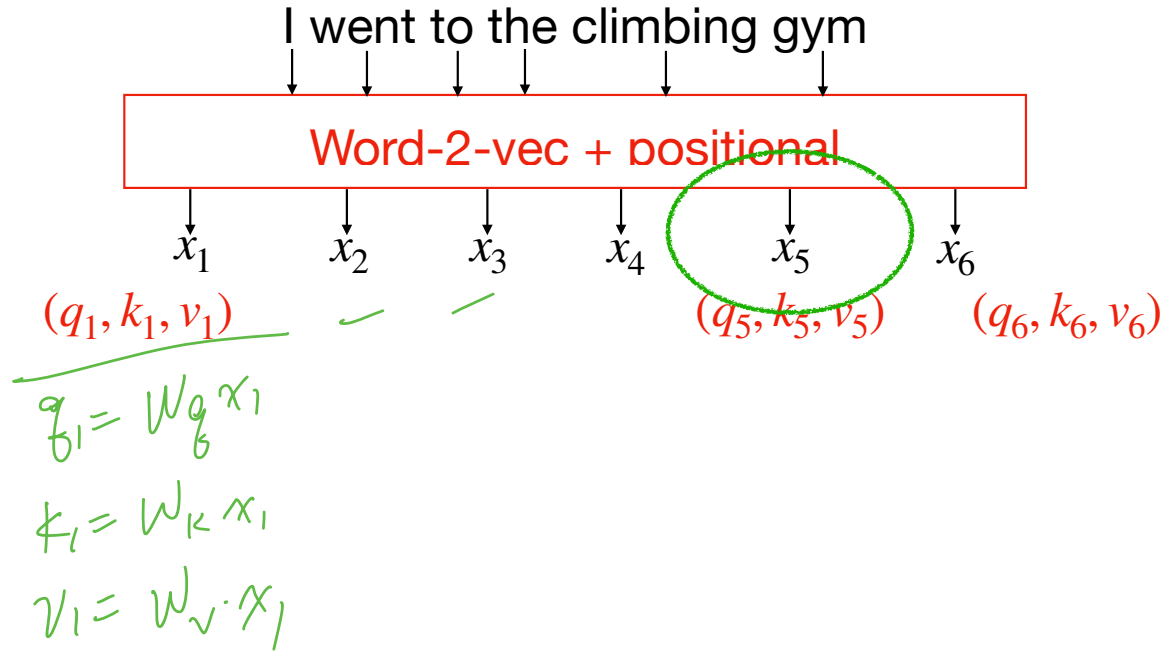
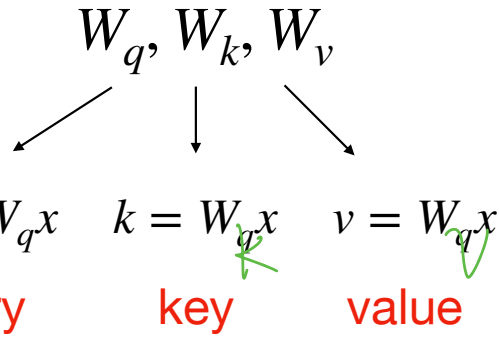
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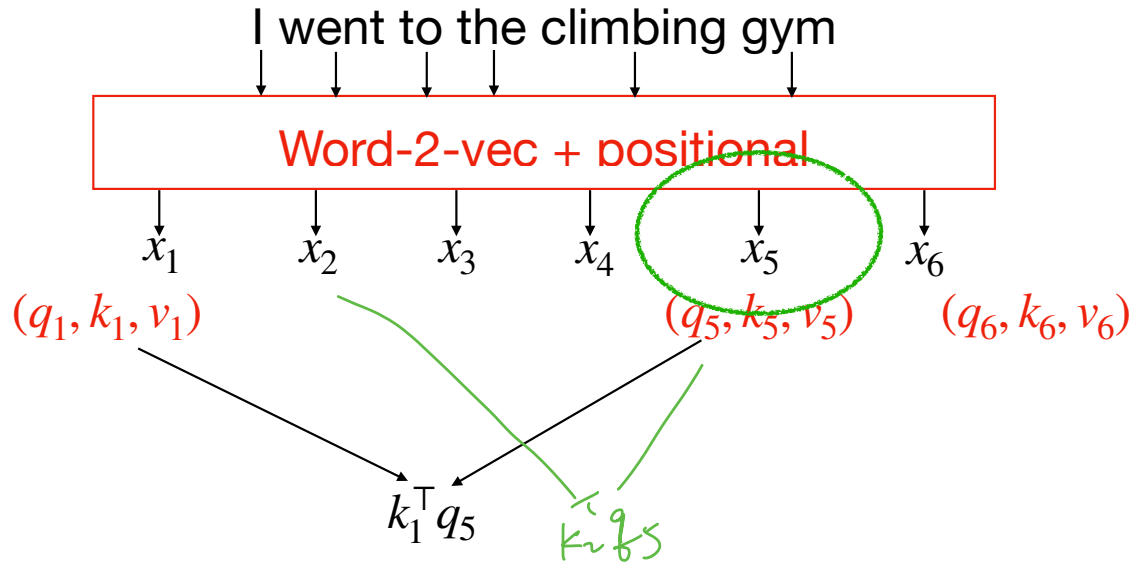
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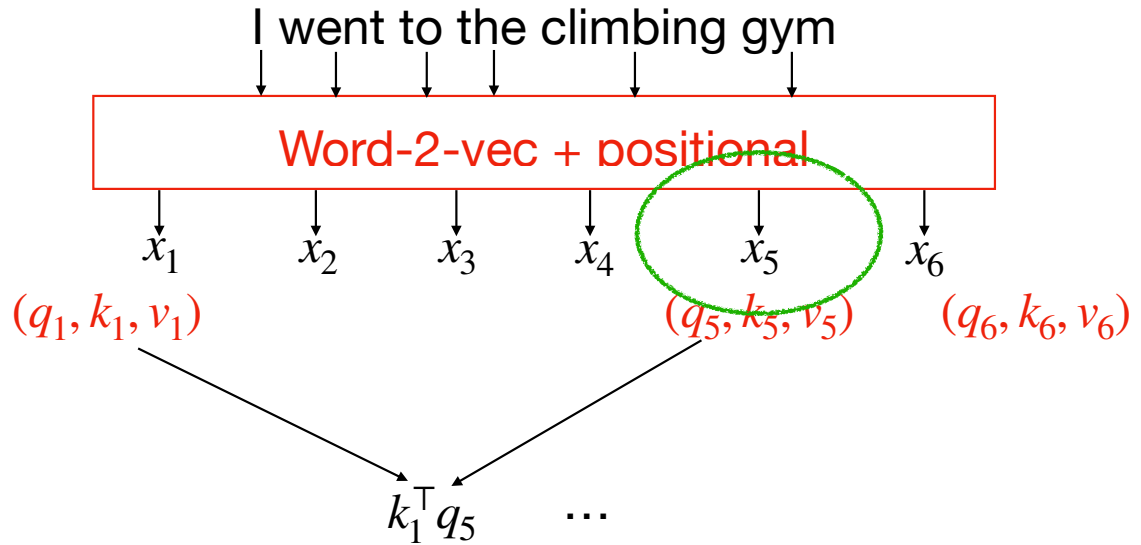


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Query

key

value



Self-attention

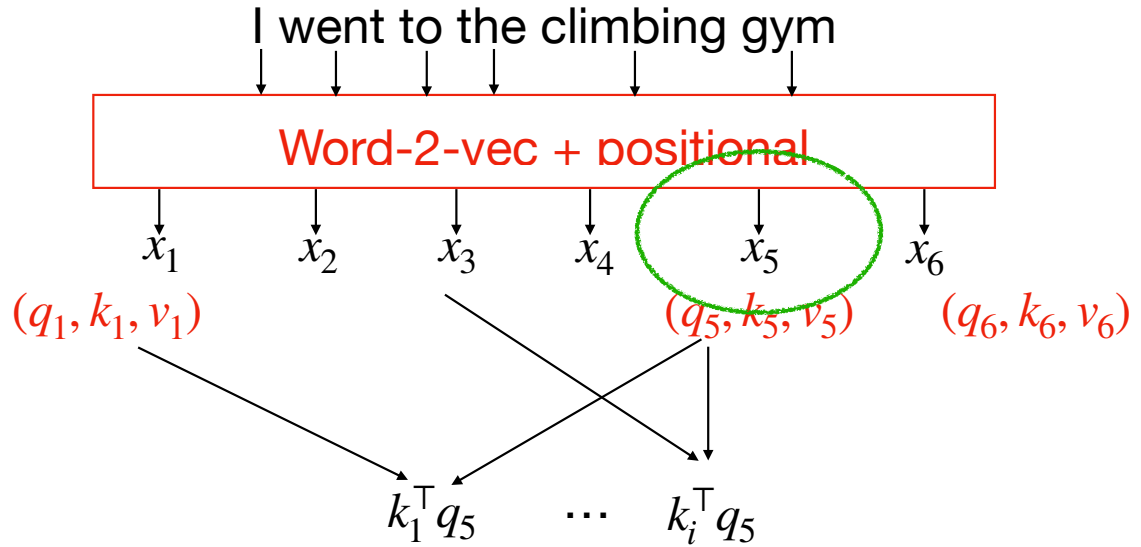
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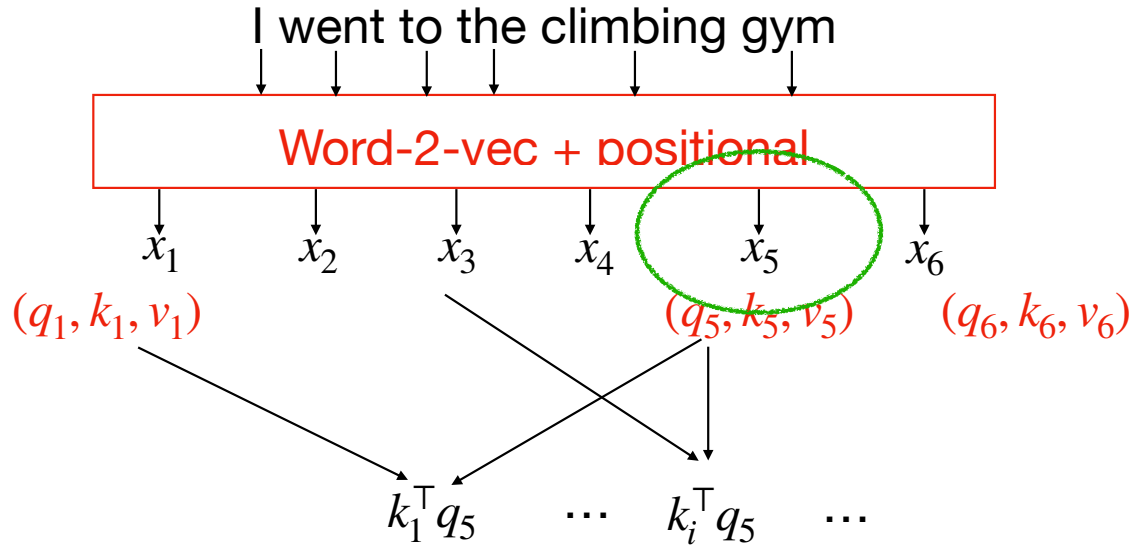
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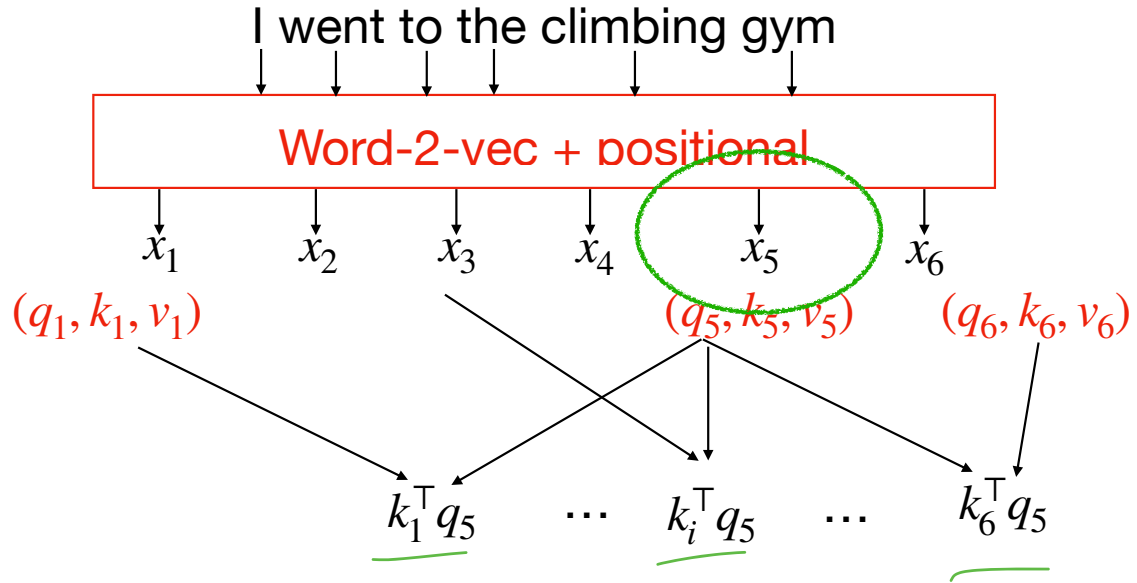
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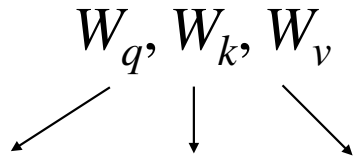
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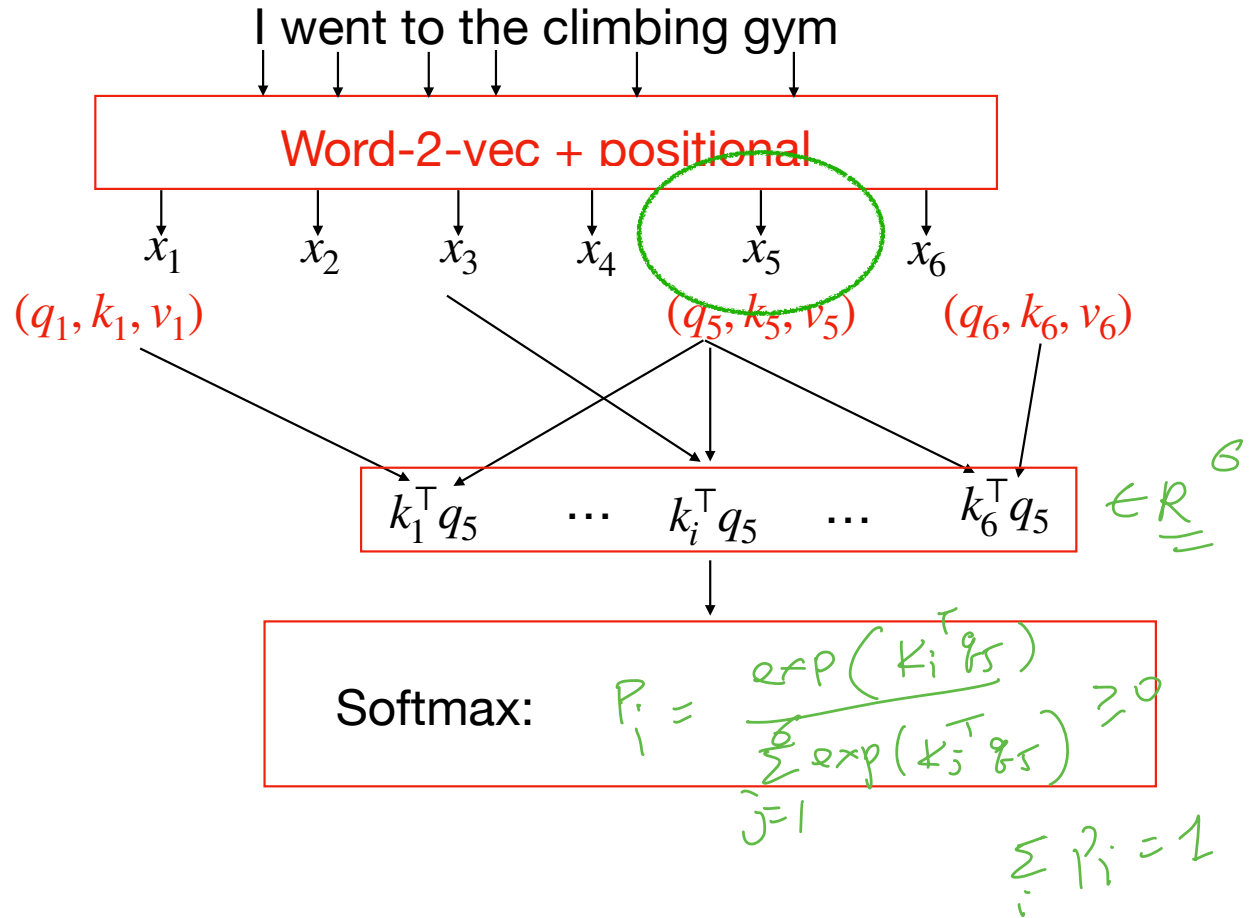
Self-attention

Attention head:
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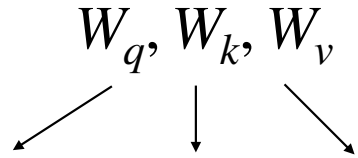
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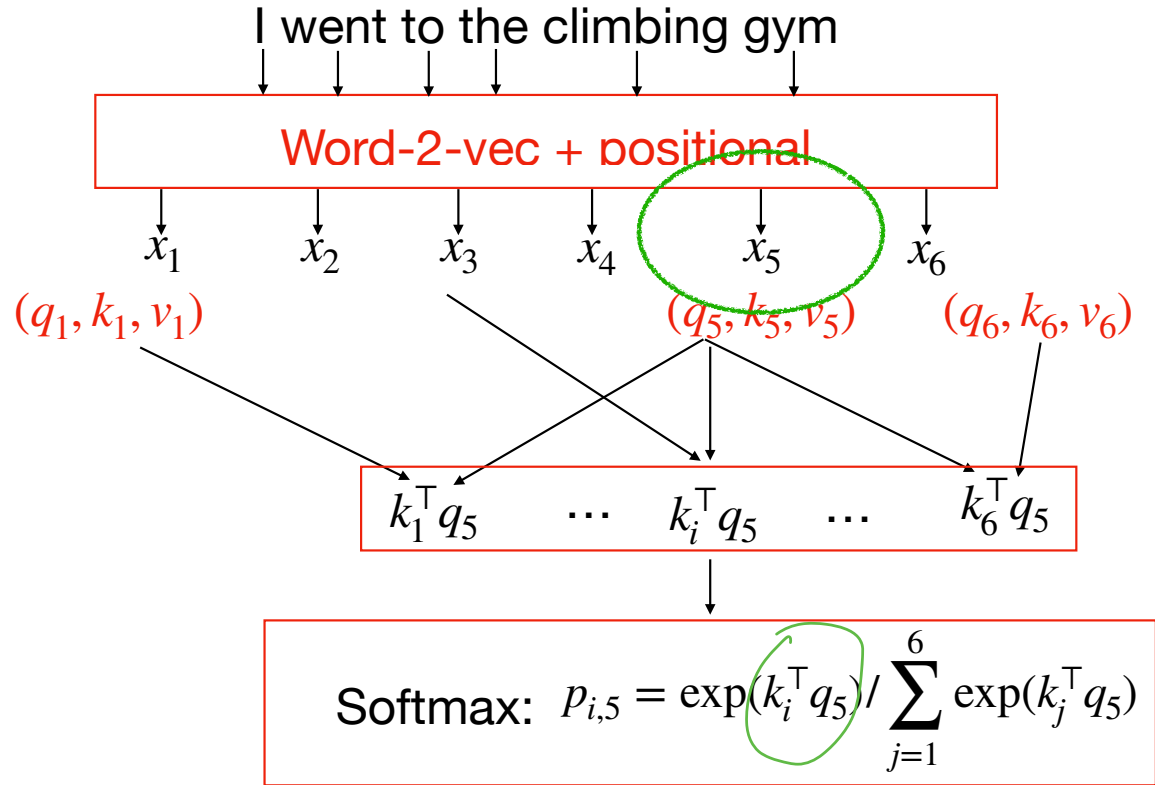
Self-attention

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Query key value



$$k_i^T q_5 \rightarrow \infty$$

$$p_{i,5} \rightarrow 1$$

Self-attention

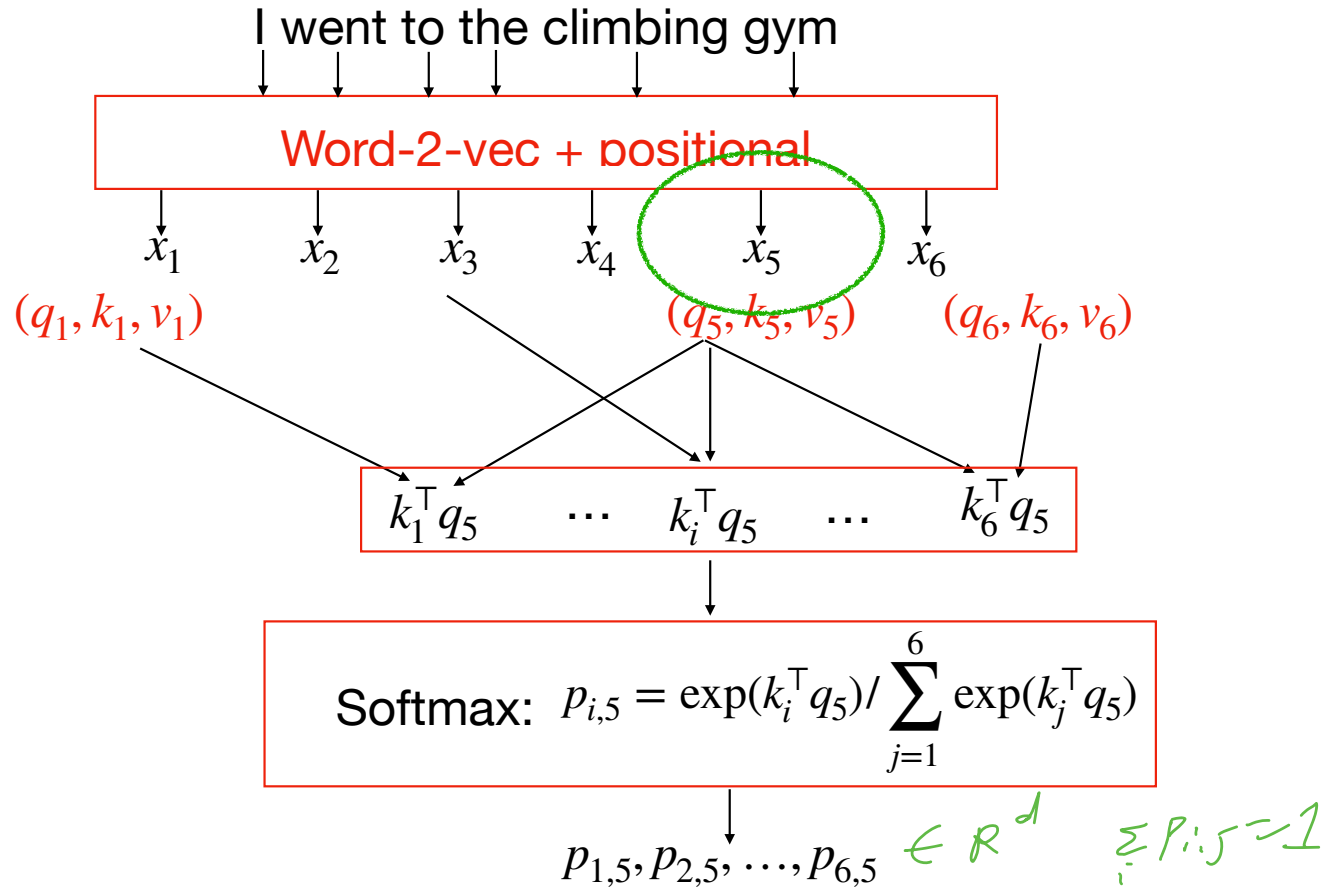
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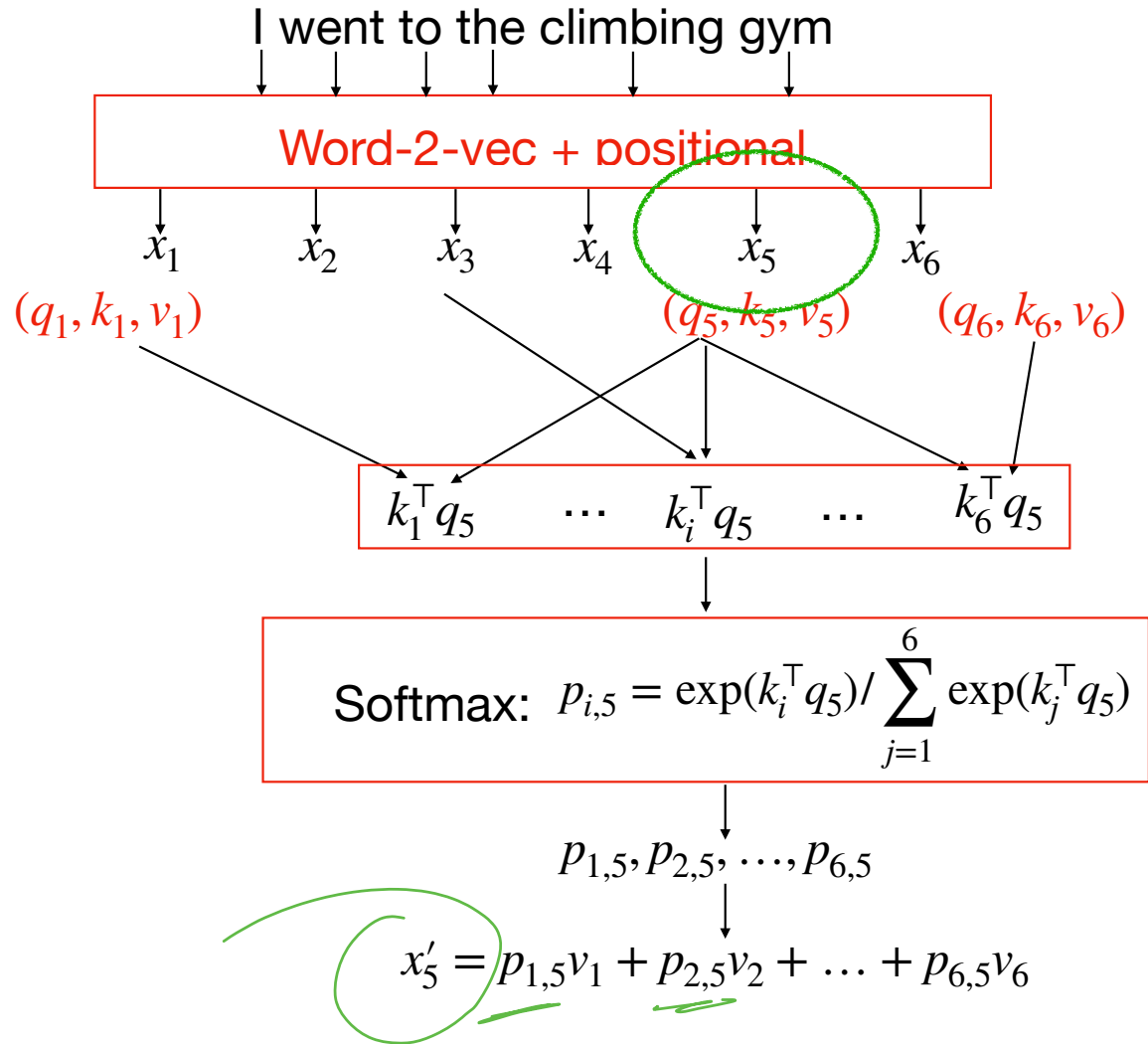
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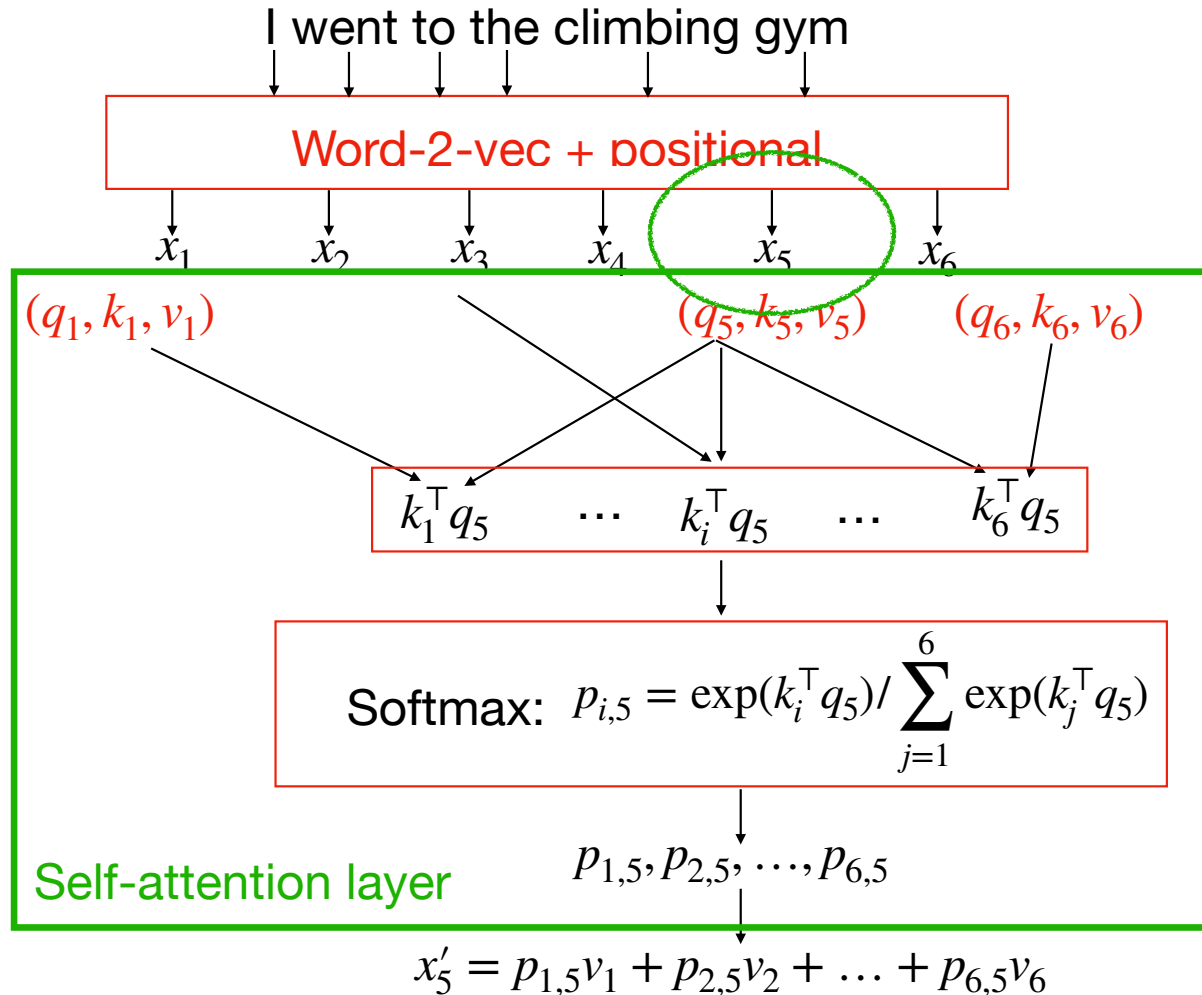
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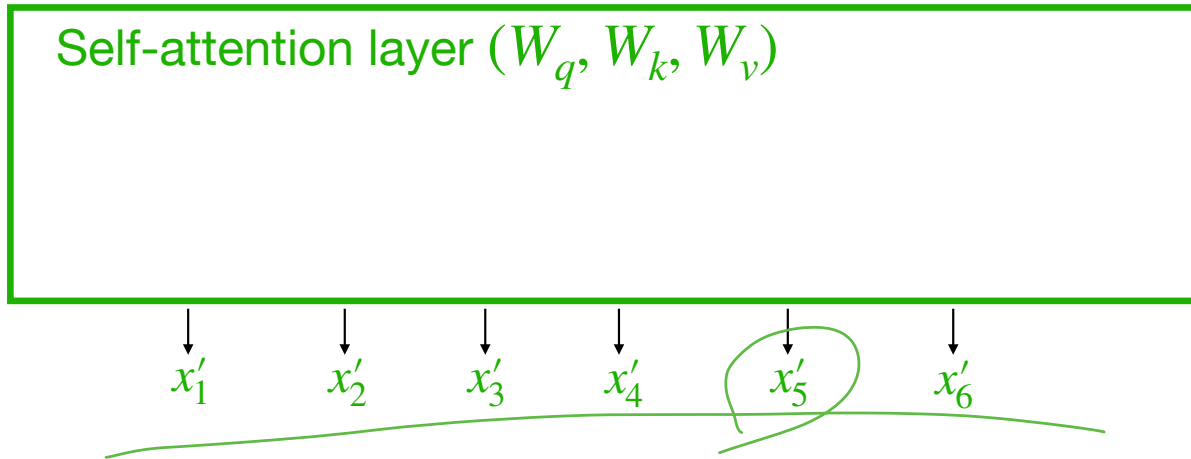
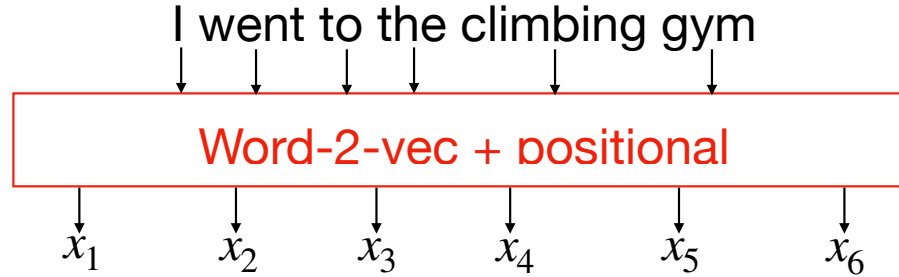
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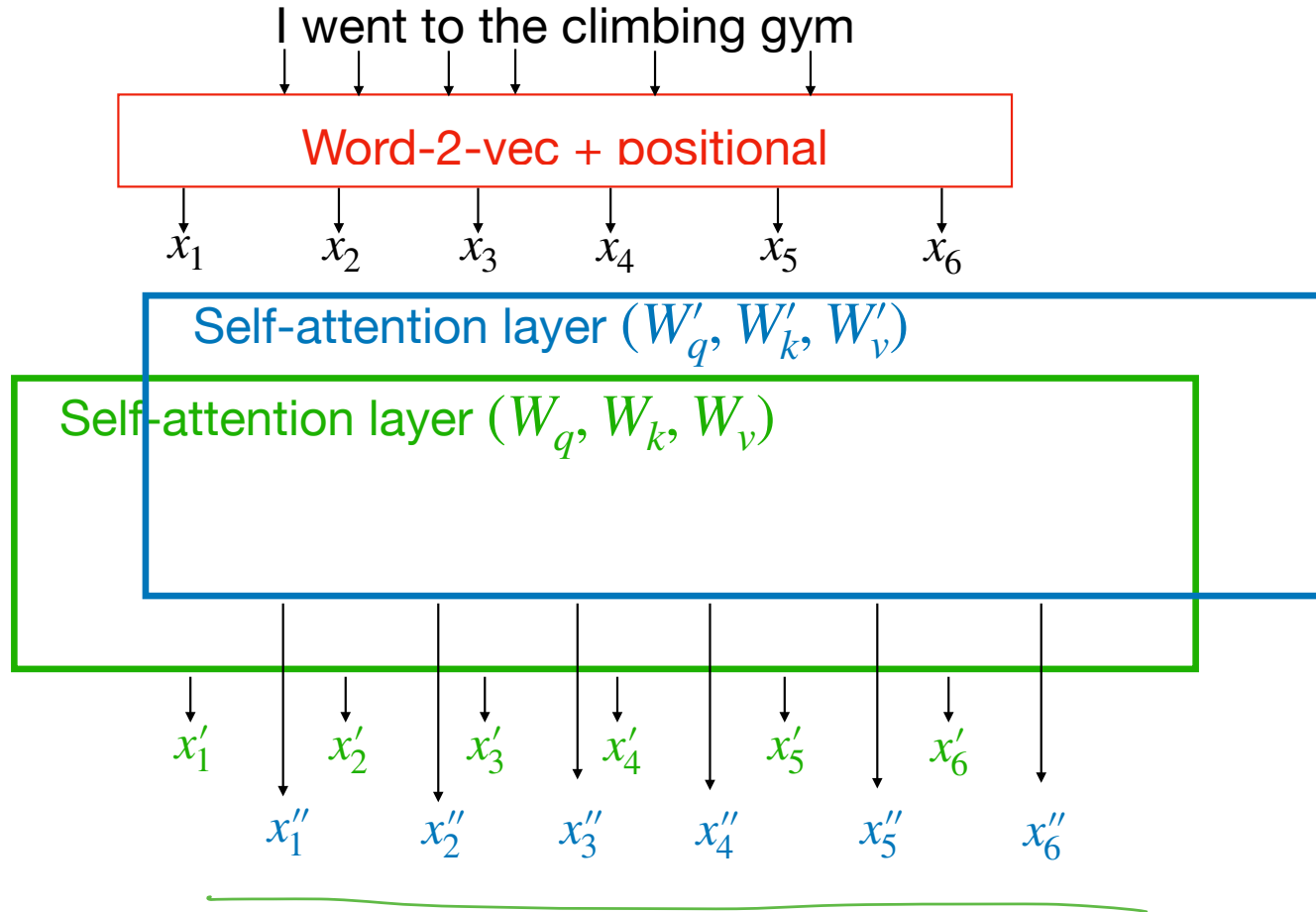
Query key value



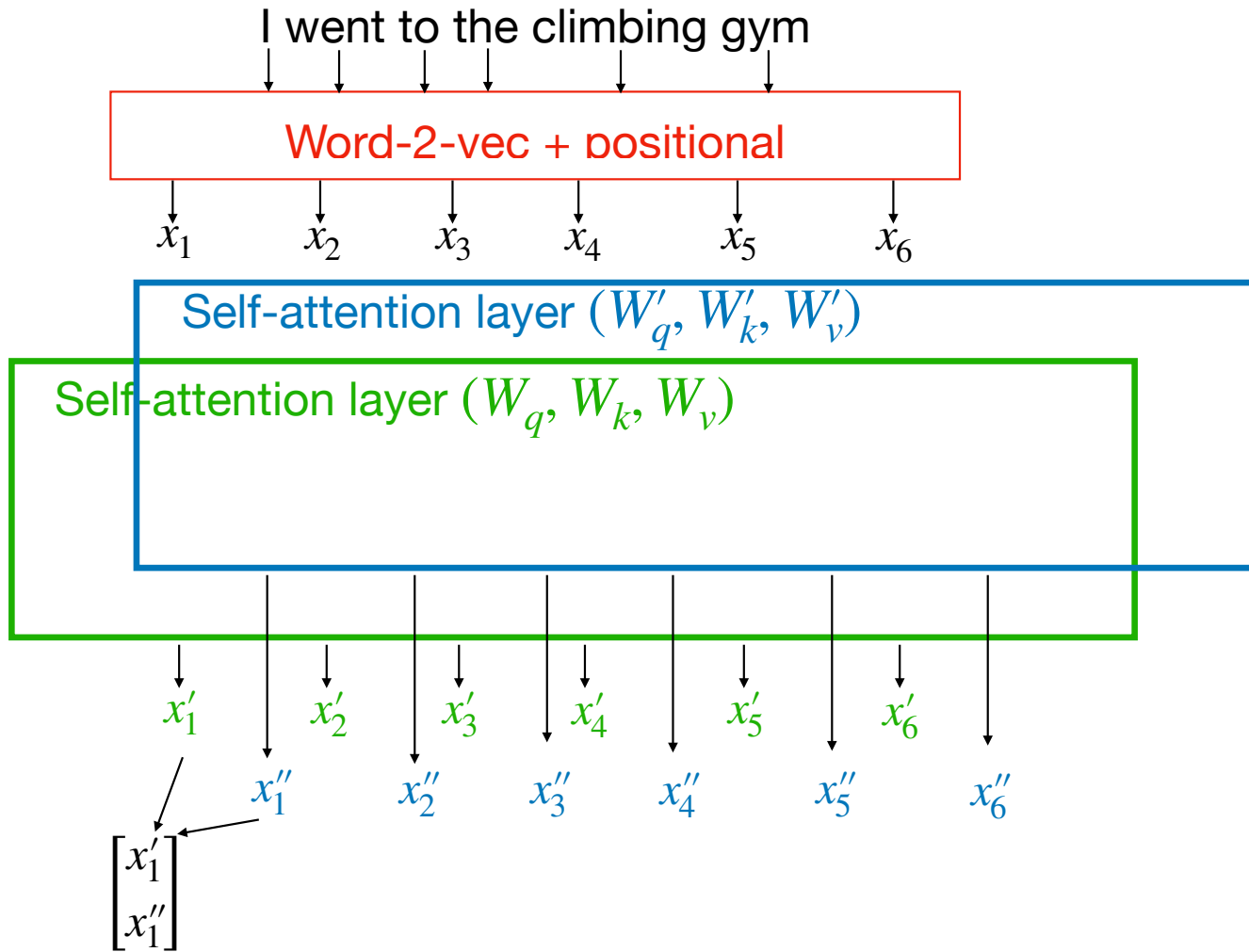
Multi-head self-attention



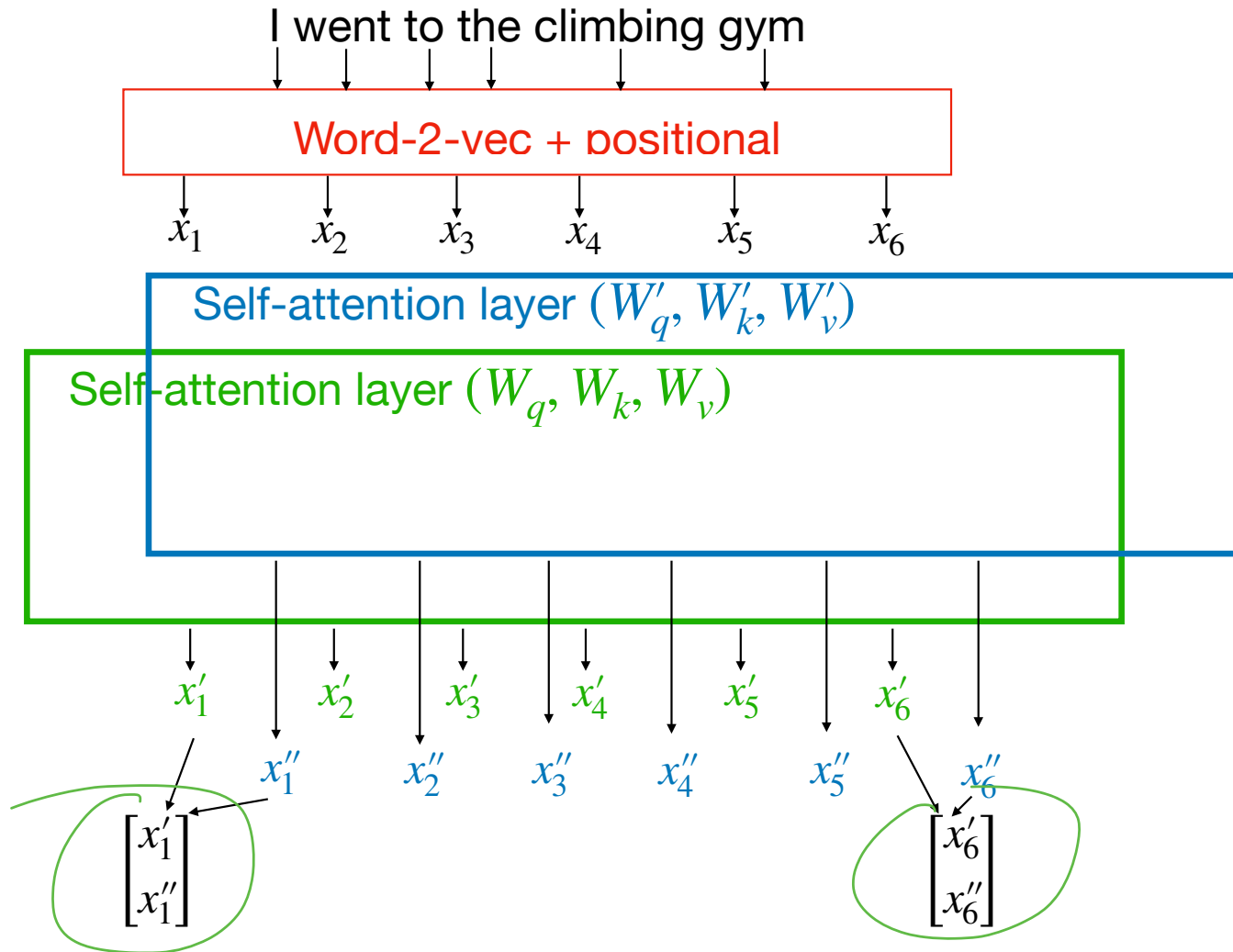
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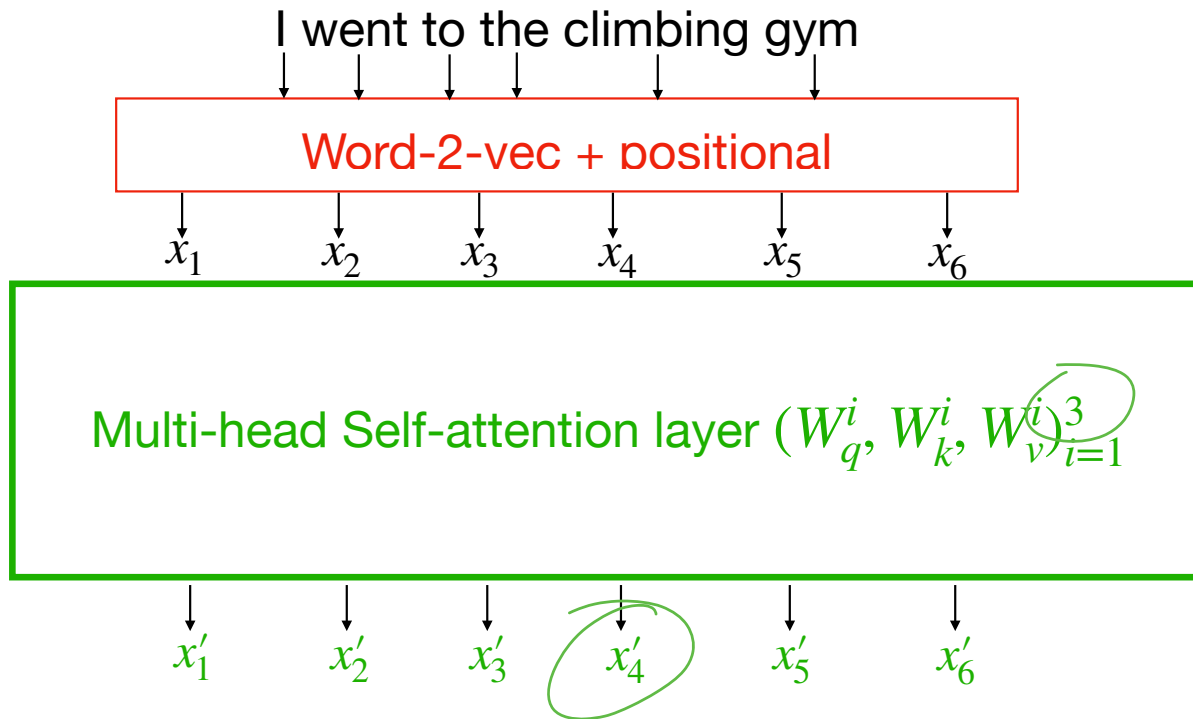
Multi-head self-attention



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Summary so far



Contextual features: e.g., x'_4 encodes information from all words

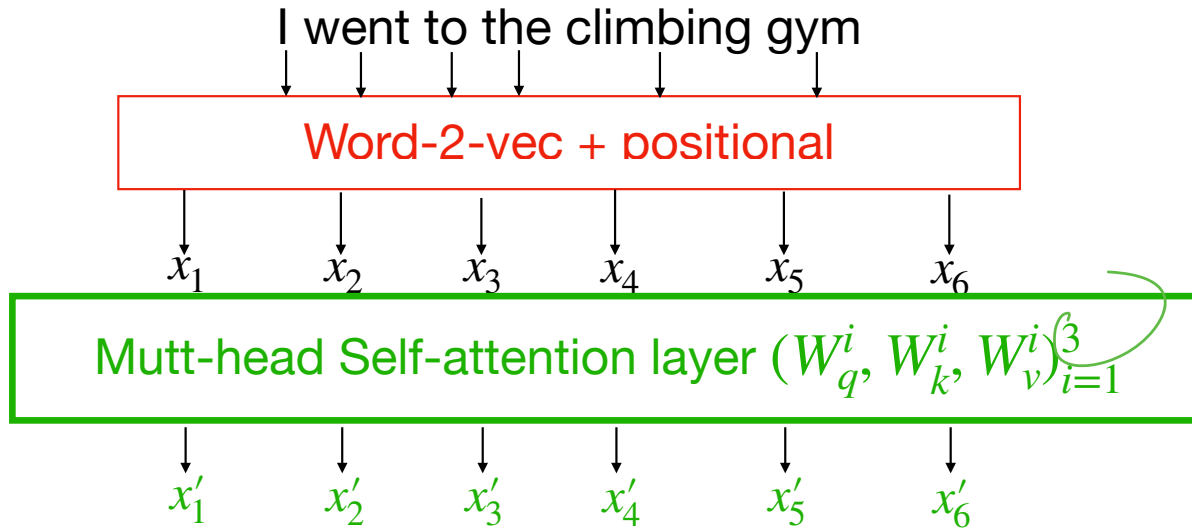
Outline today

1. Word-2-Vec embedding and positional embedding

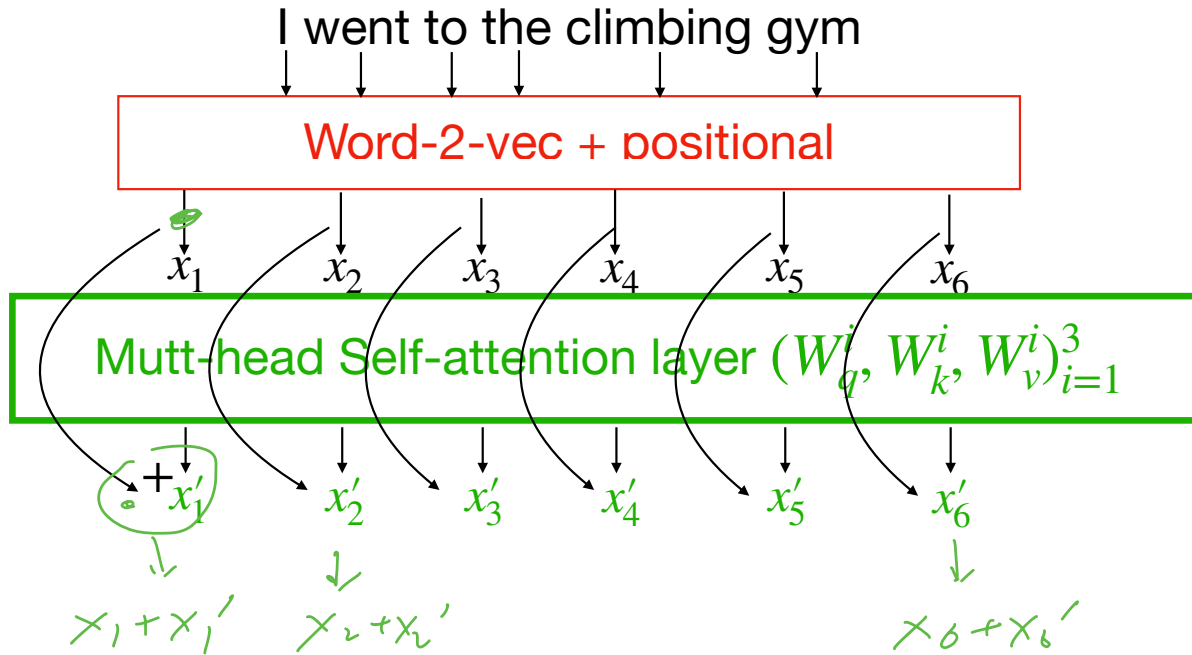
2. Attention model

3. Putting things together: the Transformer model

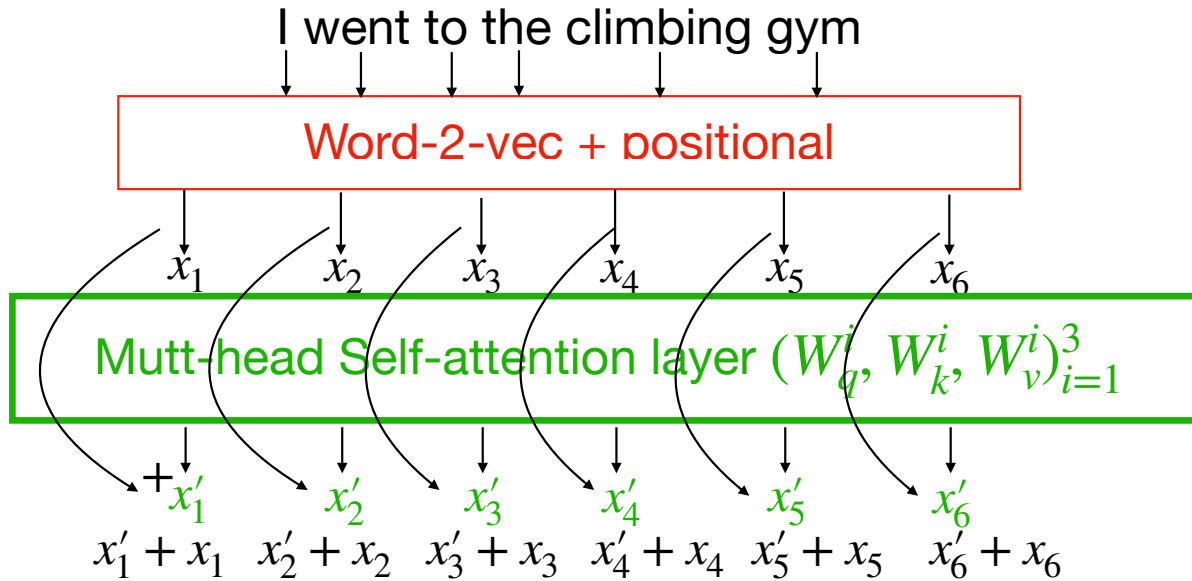
The Transformer model: encoder



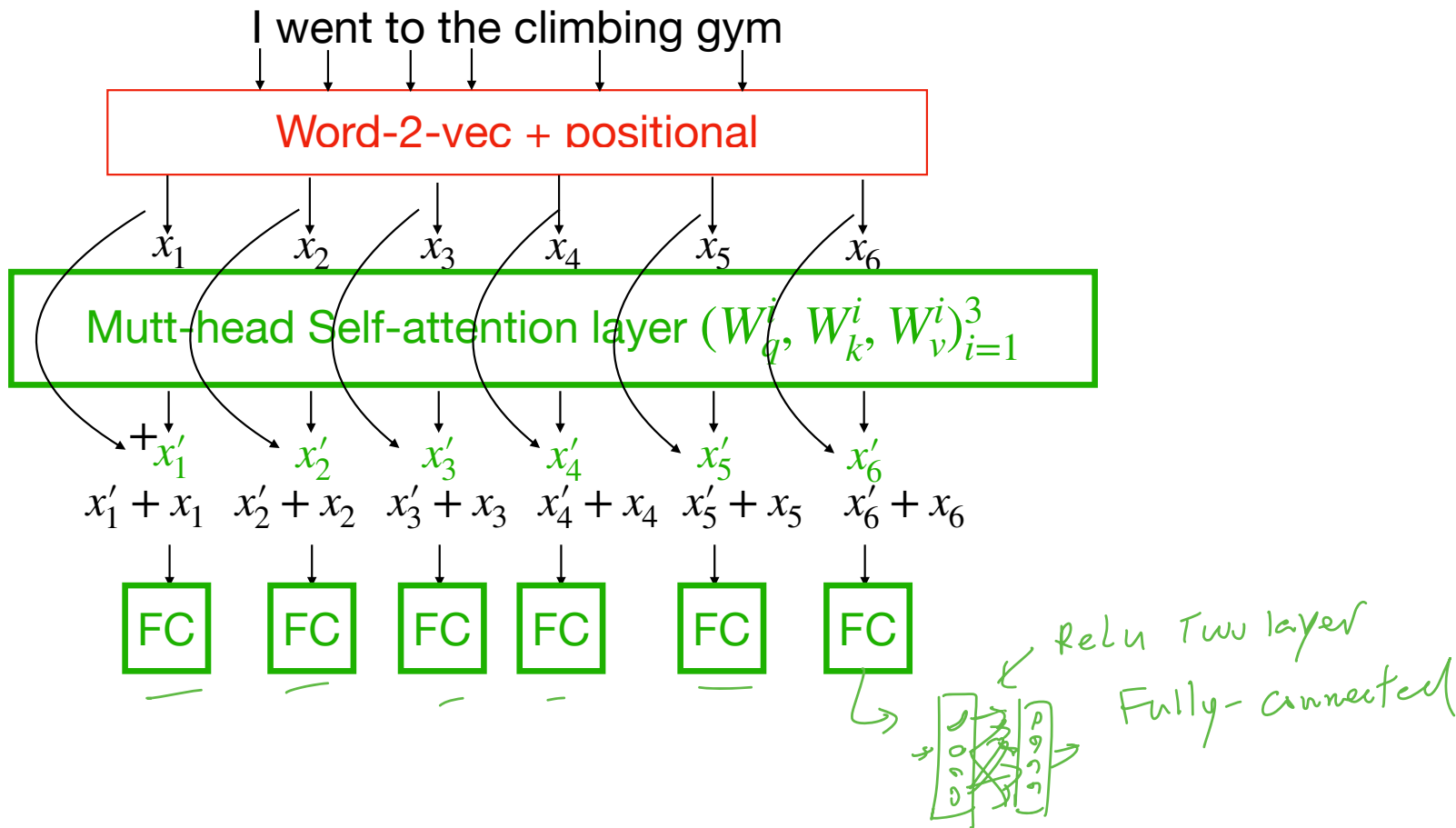
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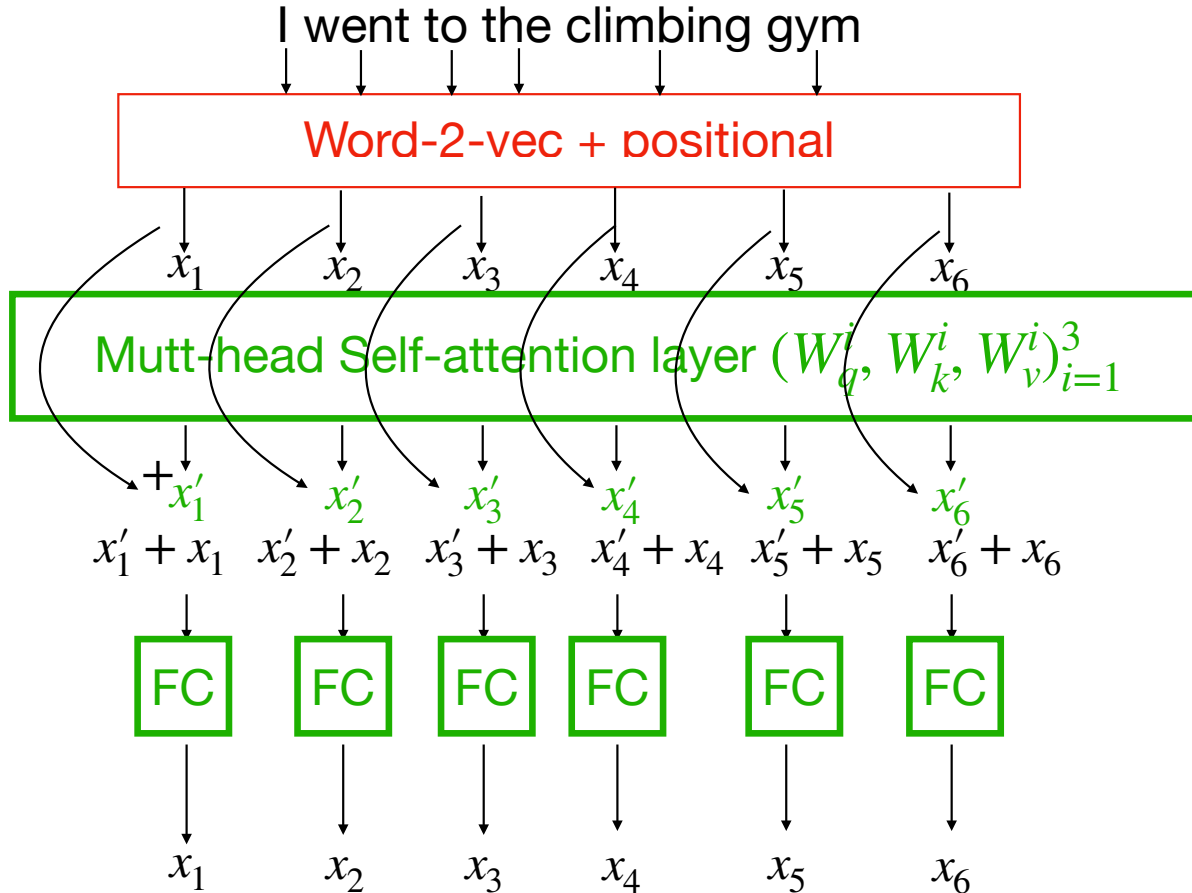
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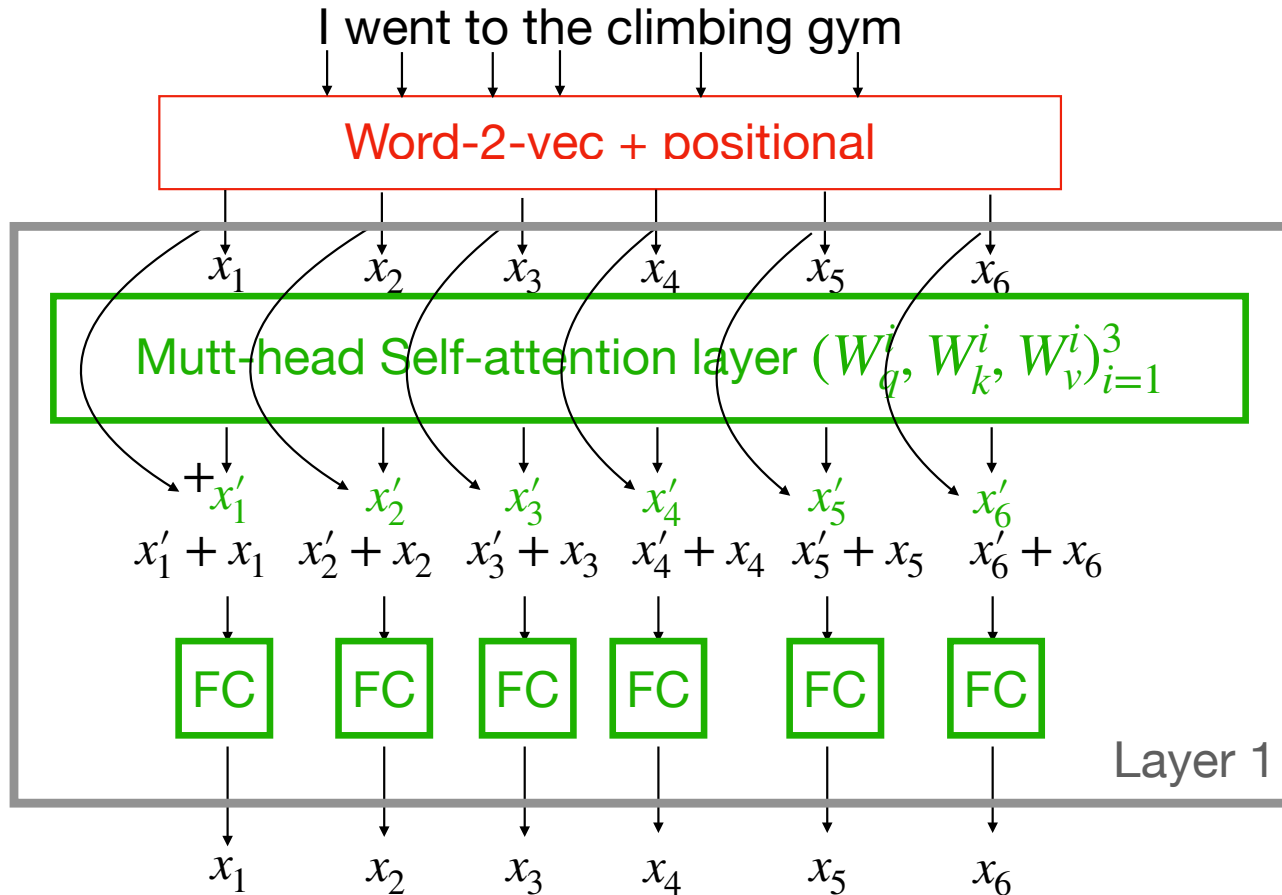
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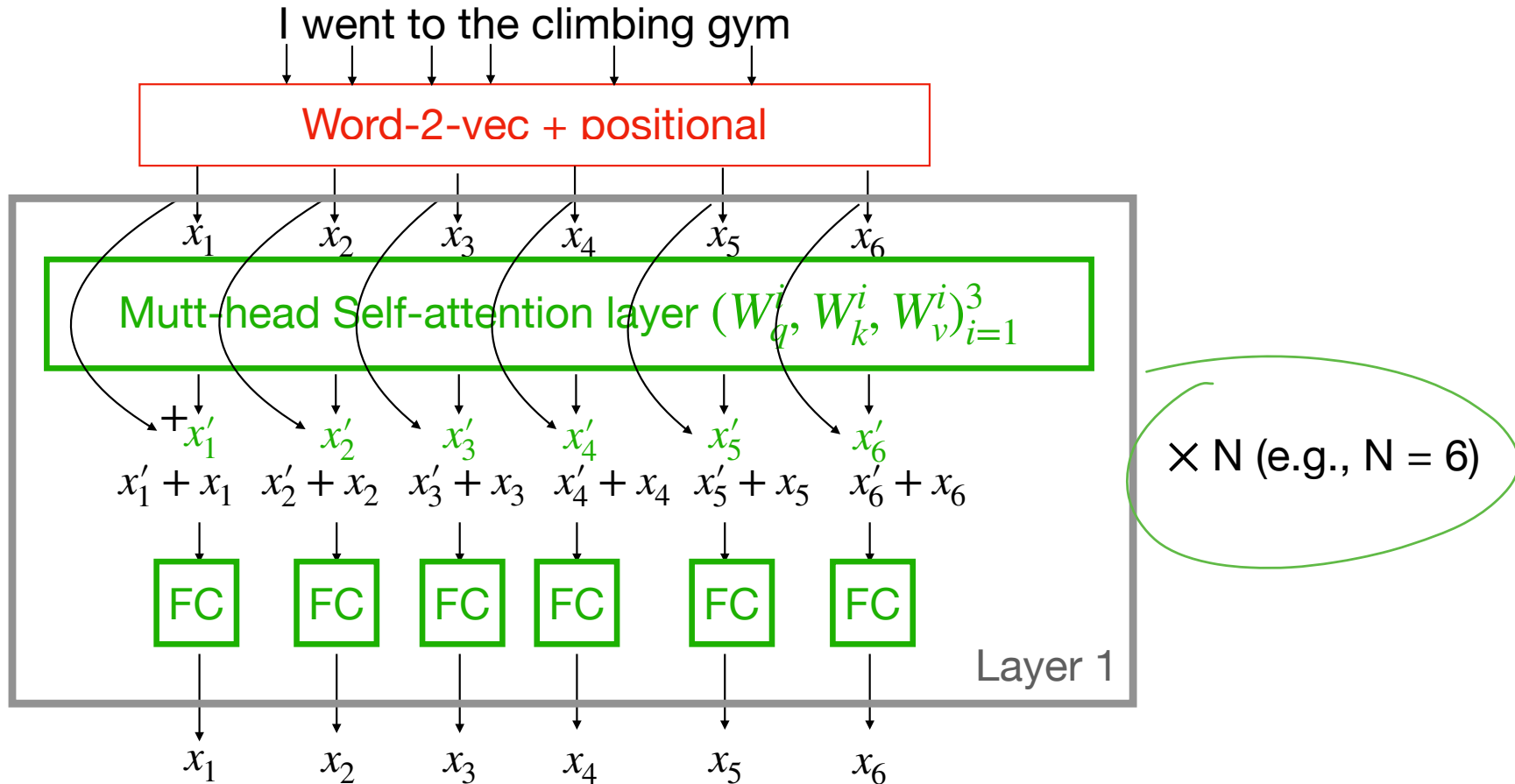
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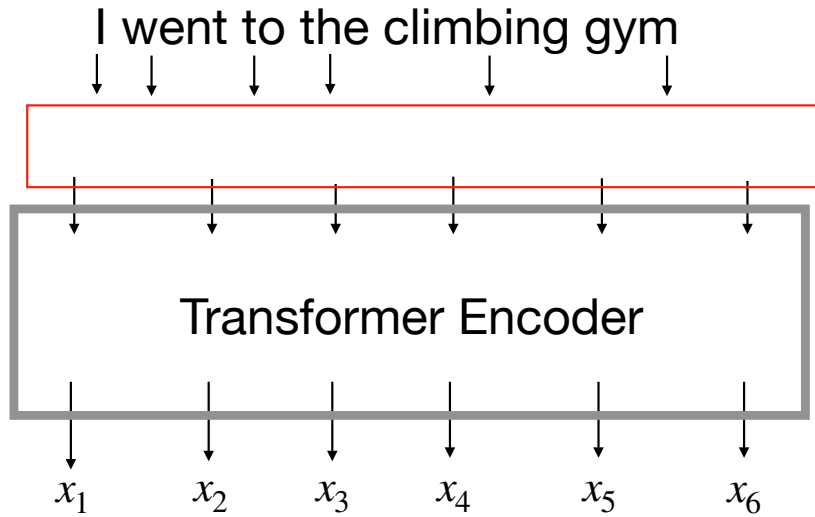
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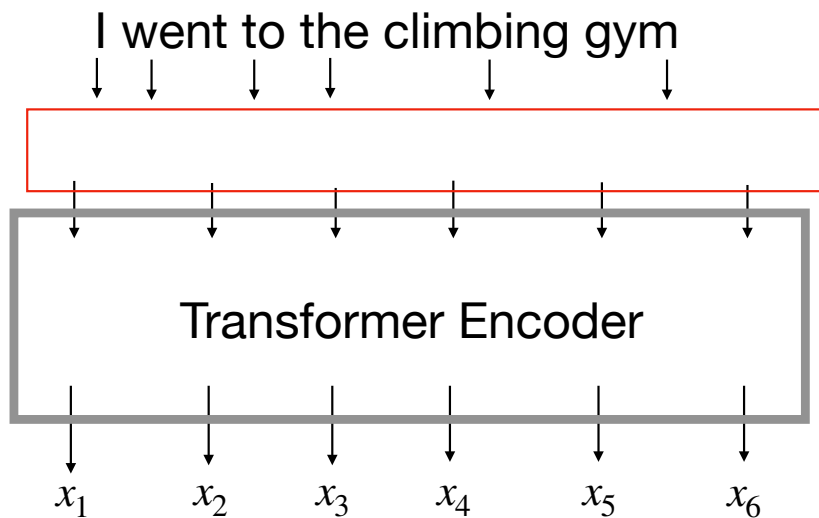
The Transformer model: encoder



The Transformer model: decoder

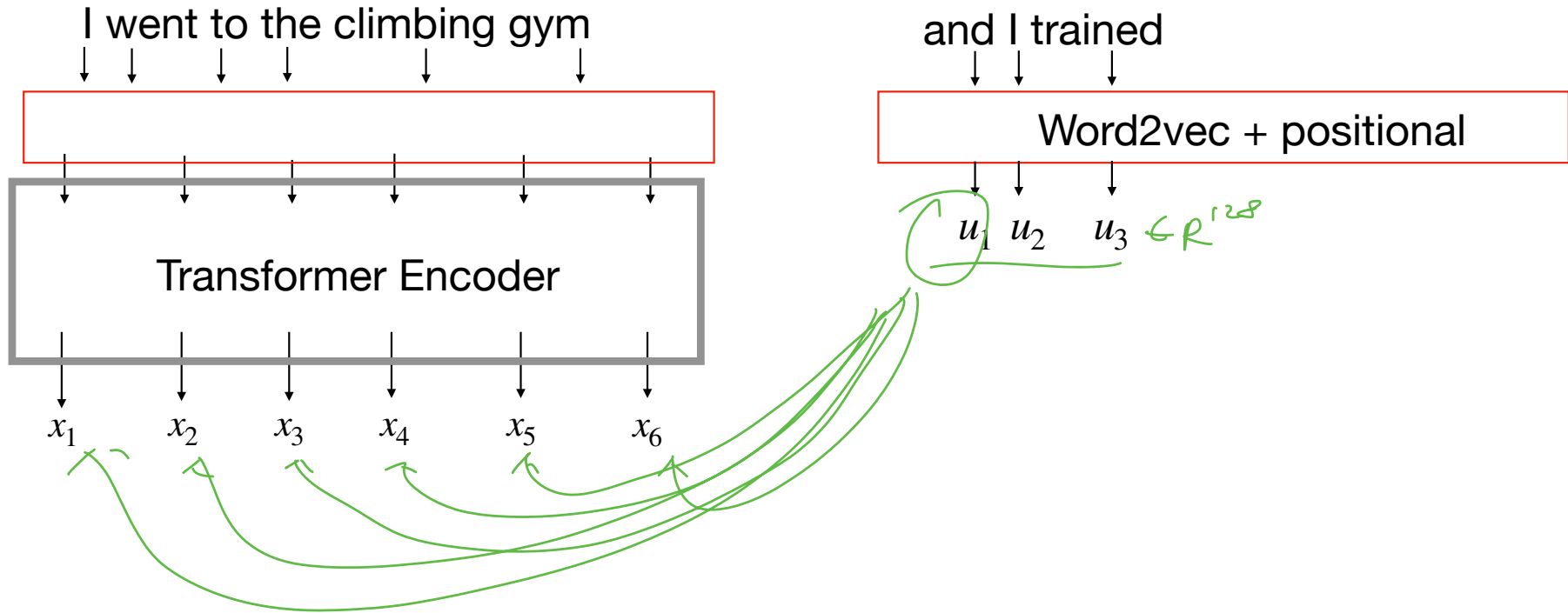


The Transformer model: decoder

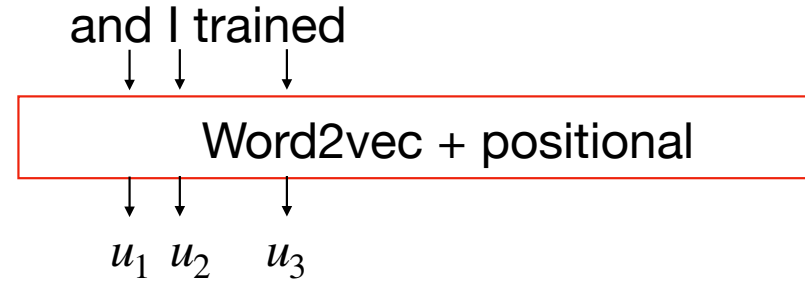
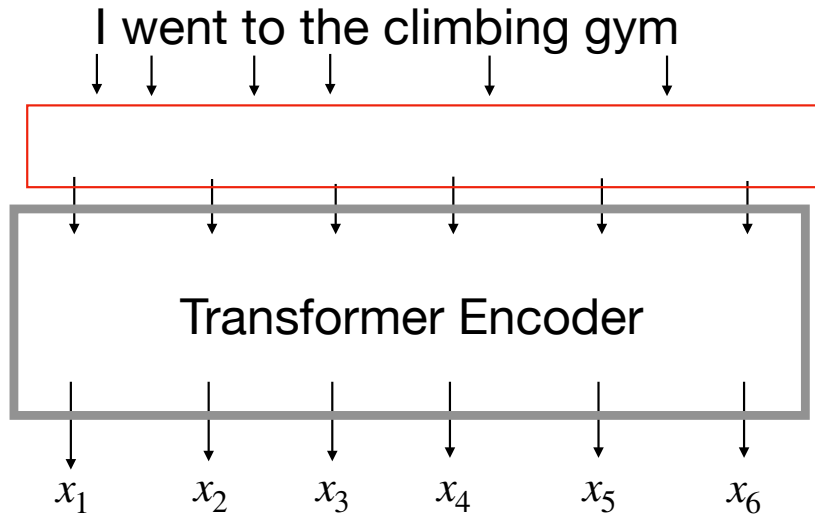


and I trained

The Transformer model: decoder

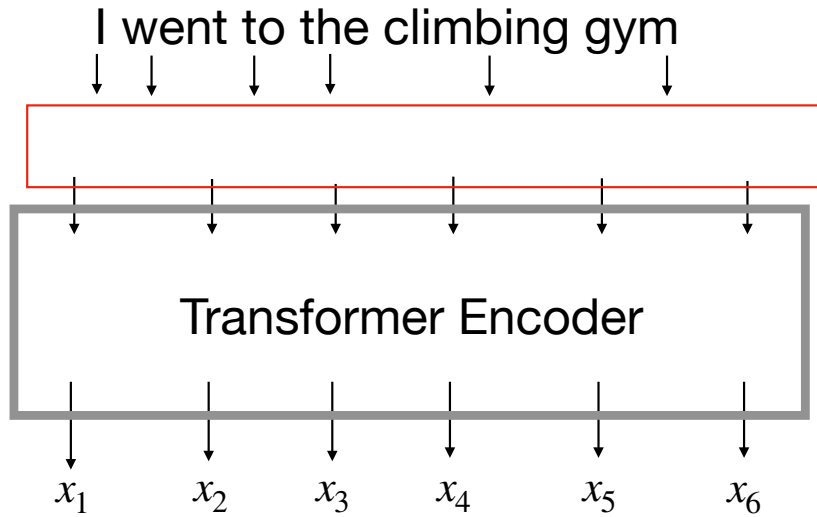


The Transformer model: decoder



cross-attention (W_q, W_k, W_v)

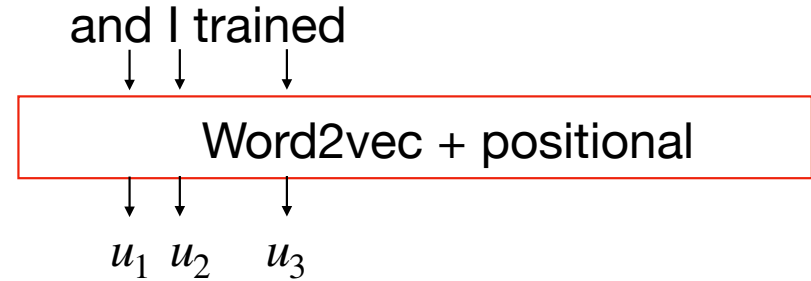
The Transformer model: decoder



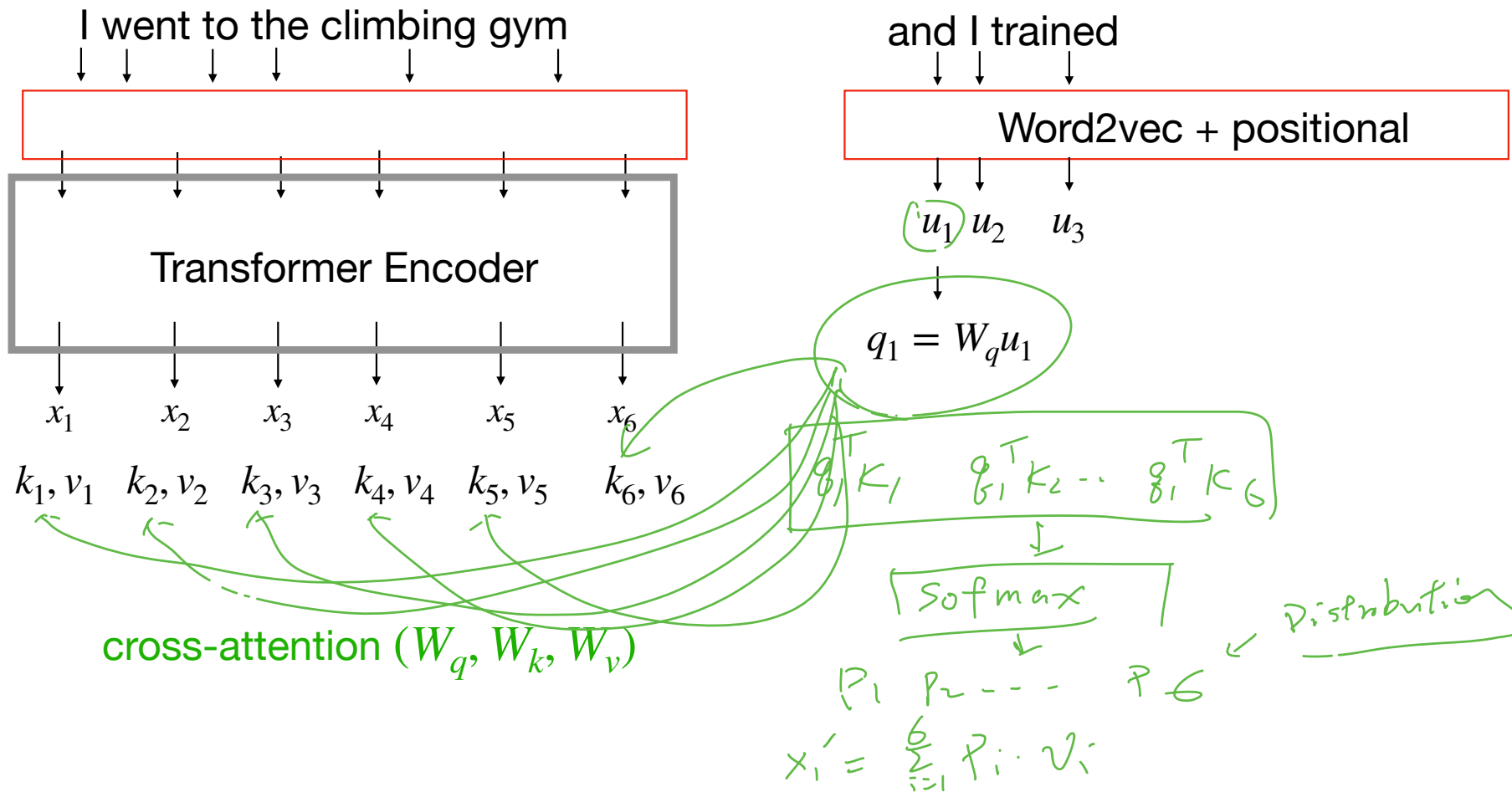
k_1, v_1 k_2, v_2 k_3, v_3 k_4, v_4 k_5, v_5 k_6, v_6

$$k_1 = W_k \cdot x_1 \quad v_1 = W_v \cdot x_1$$

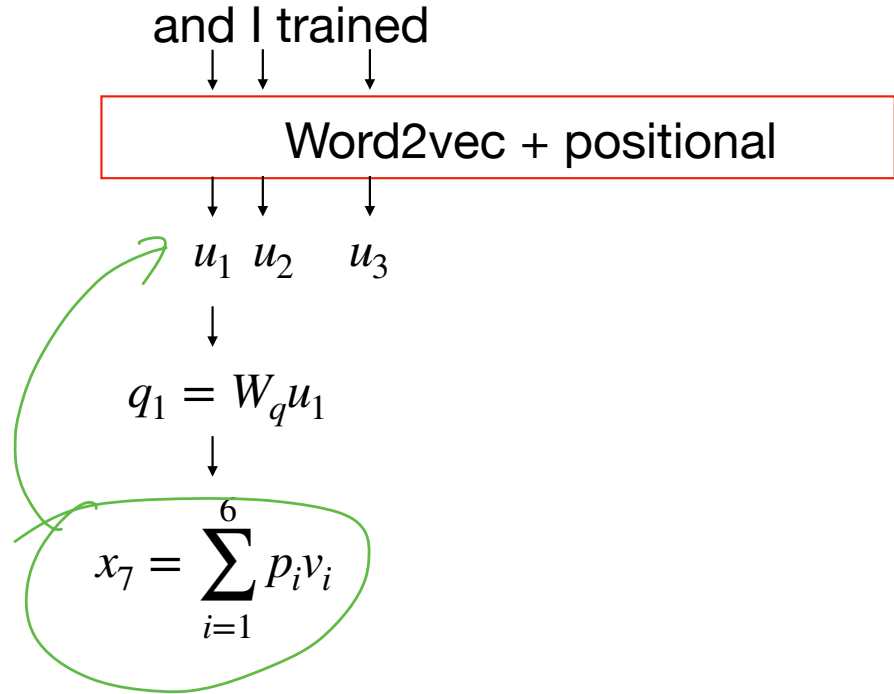
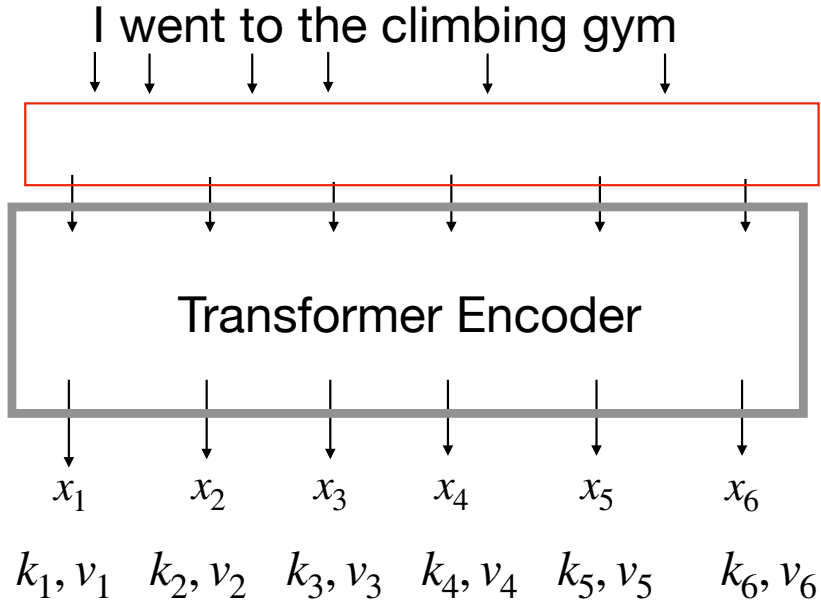
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The Transformer model: decoder

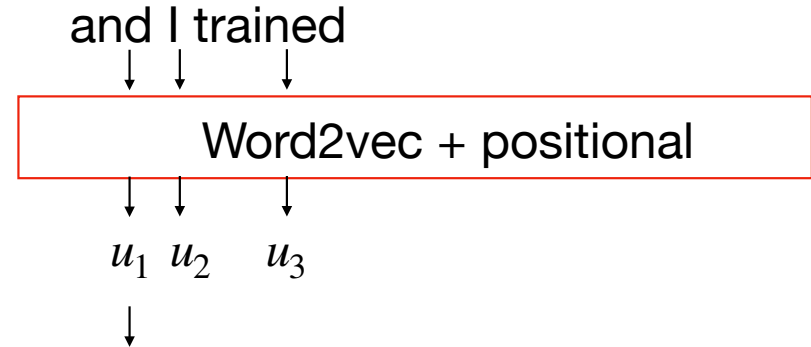
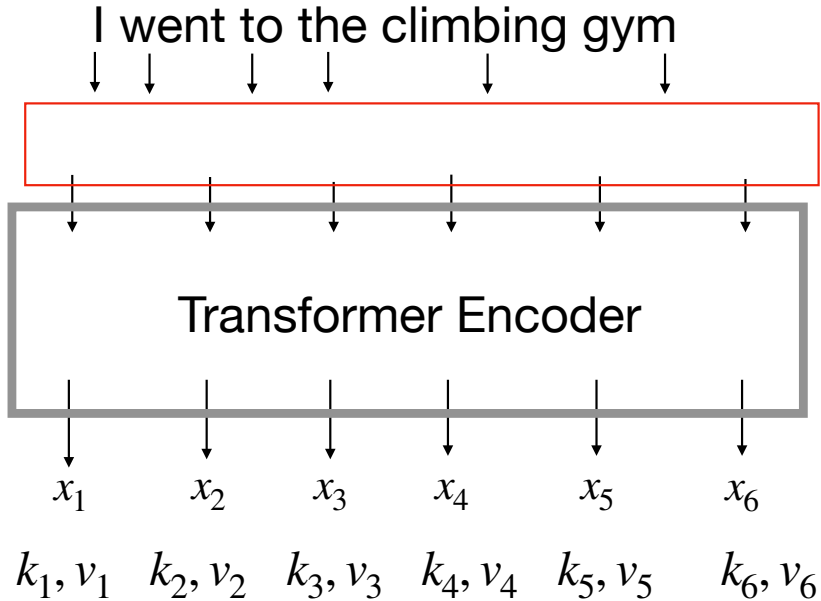


The Transformer model: decoder



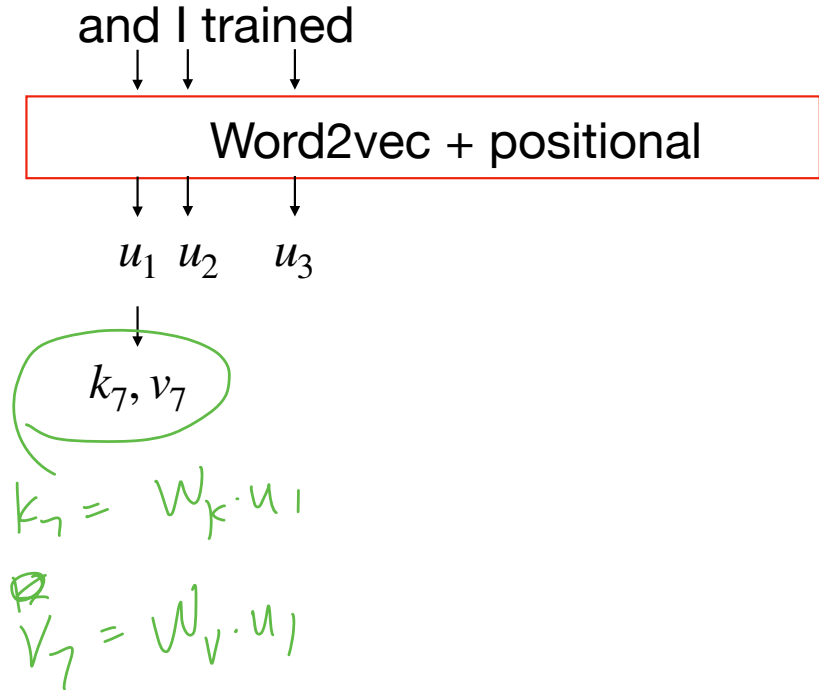
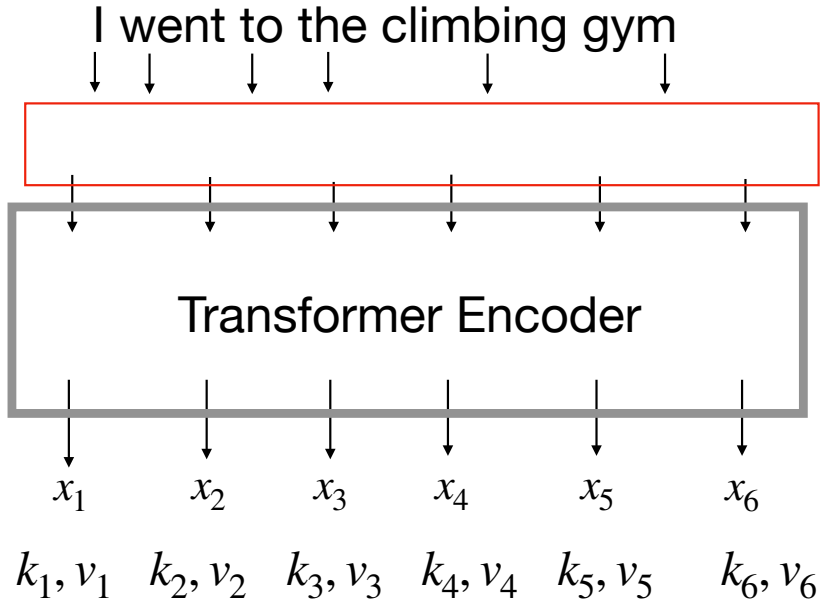
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The Transformer model: decoder



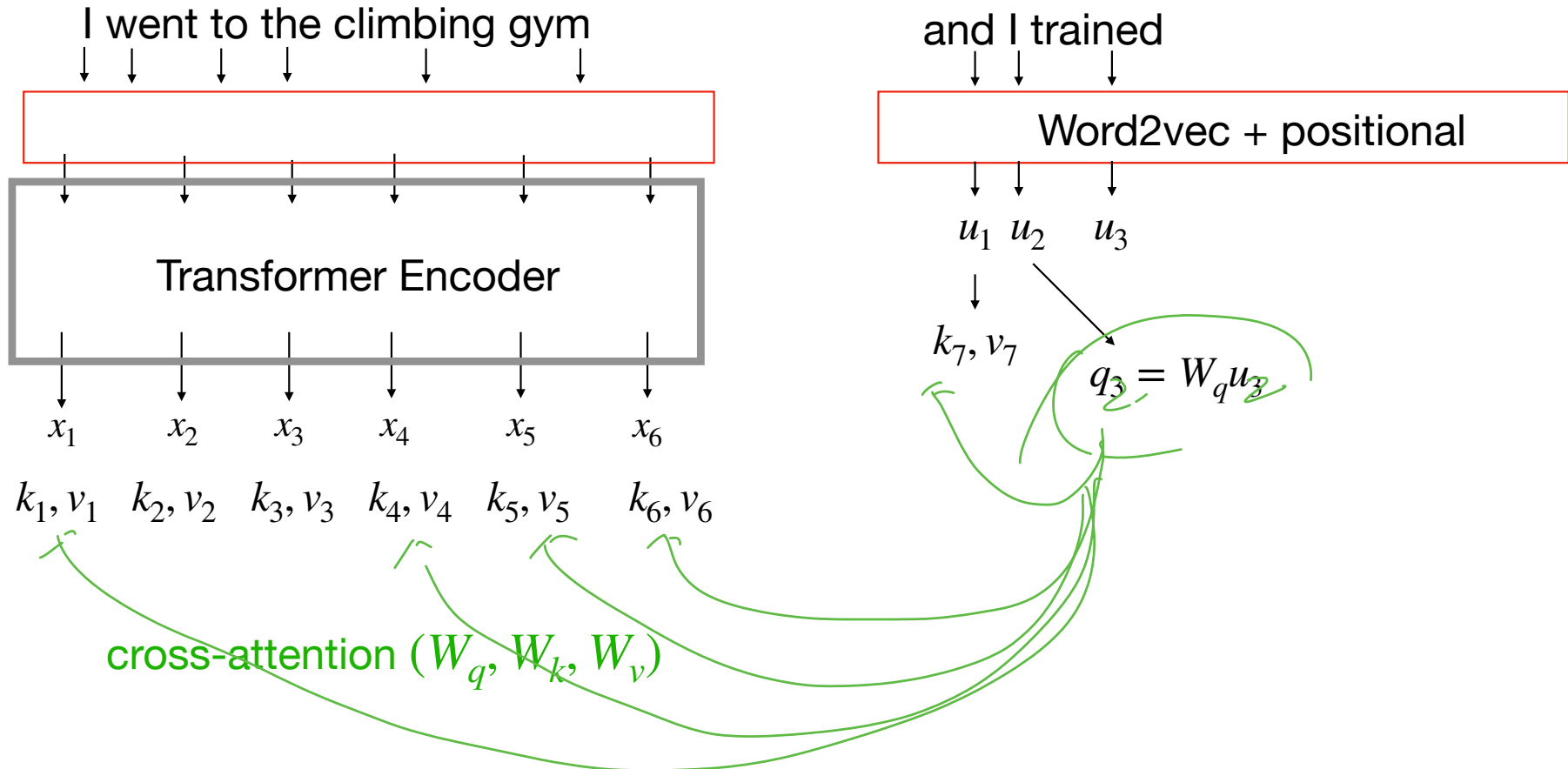
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The Transformer model: decoder

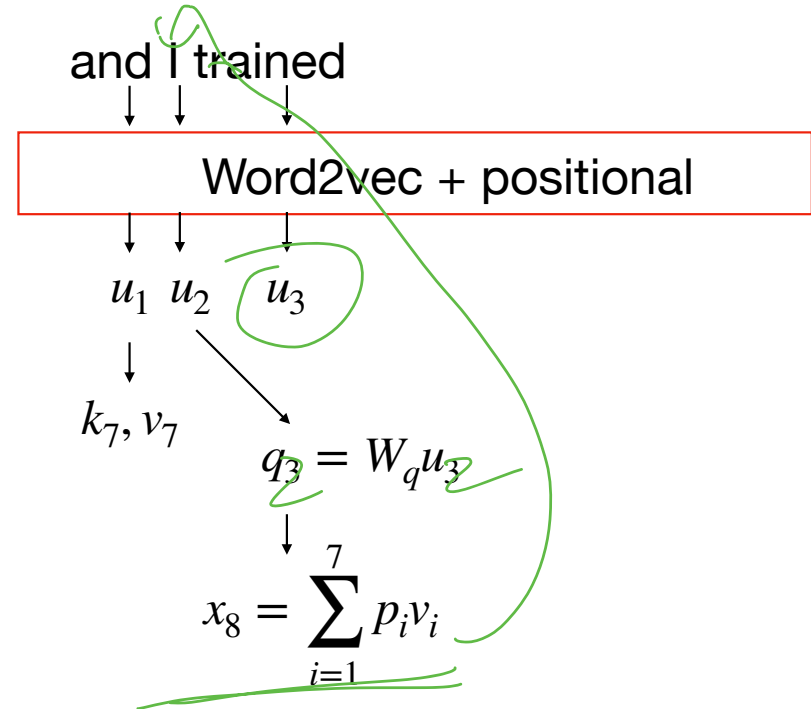
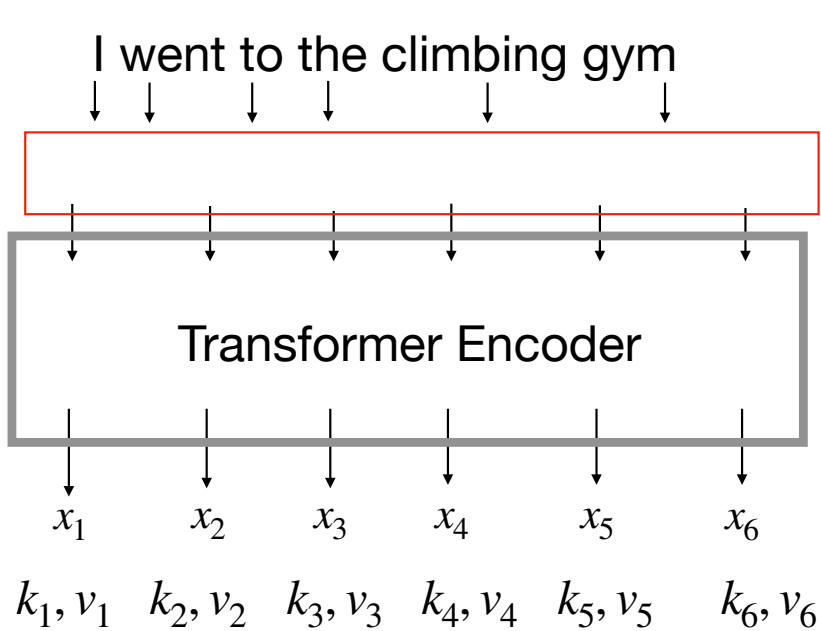


cross-attention (W_q, W_k, W_v)

The Transformer model: decoder

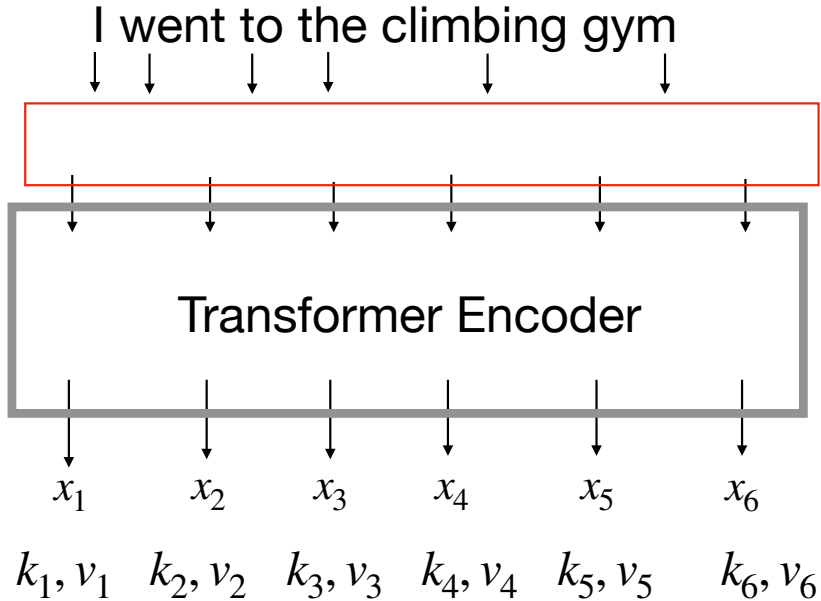


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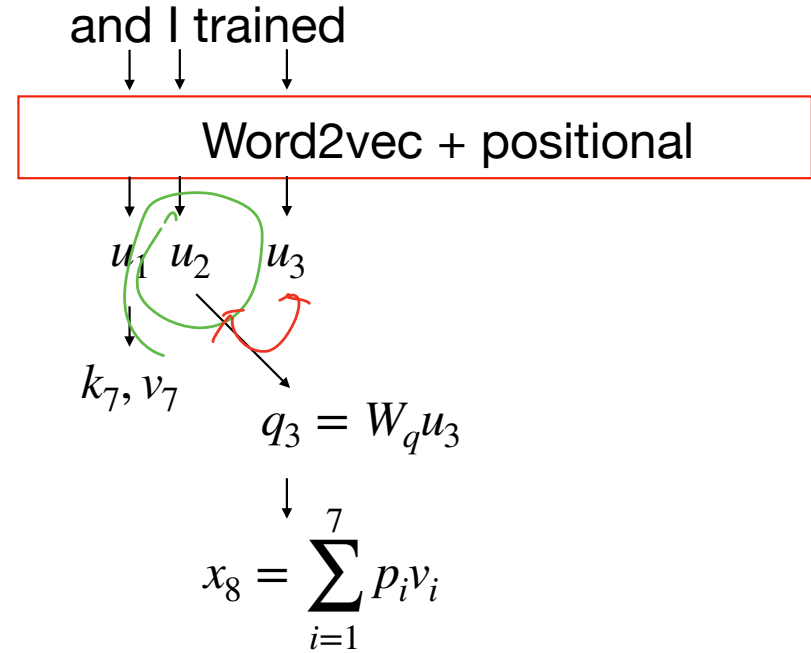


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The Transformer model: decoder

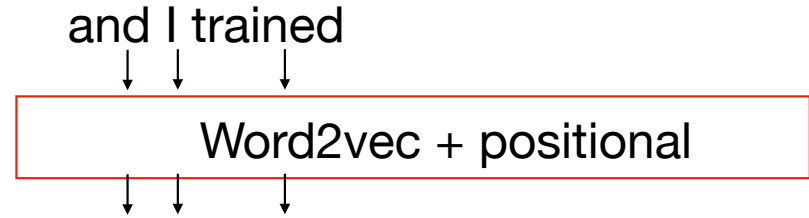
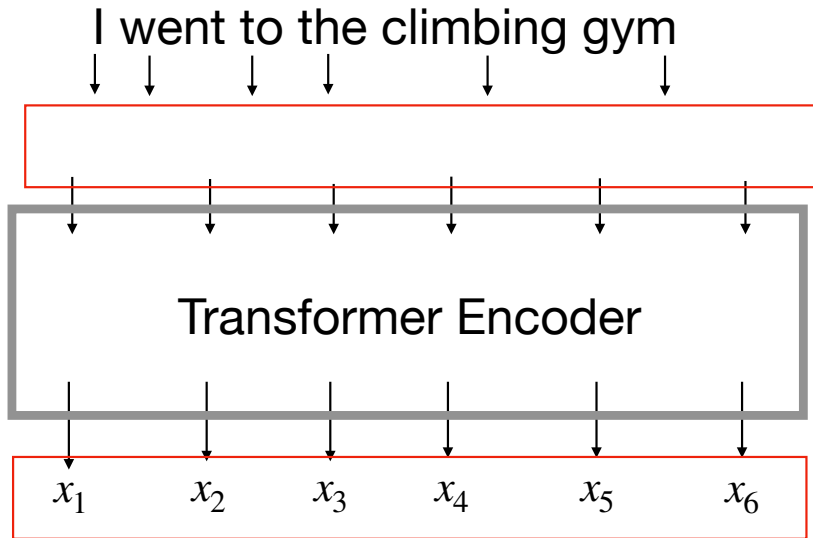


cross-attention (W_q, W_k, W_v)

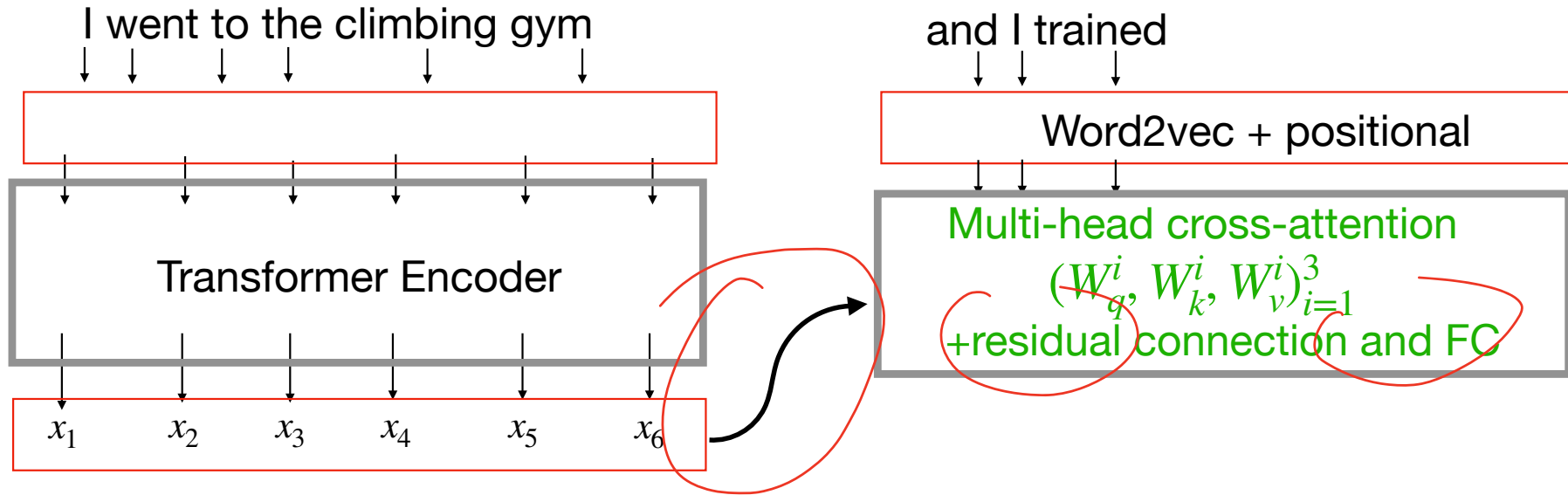


Note: we do not pay attention to future words

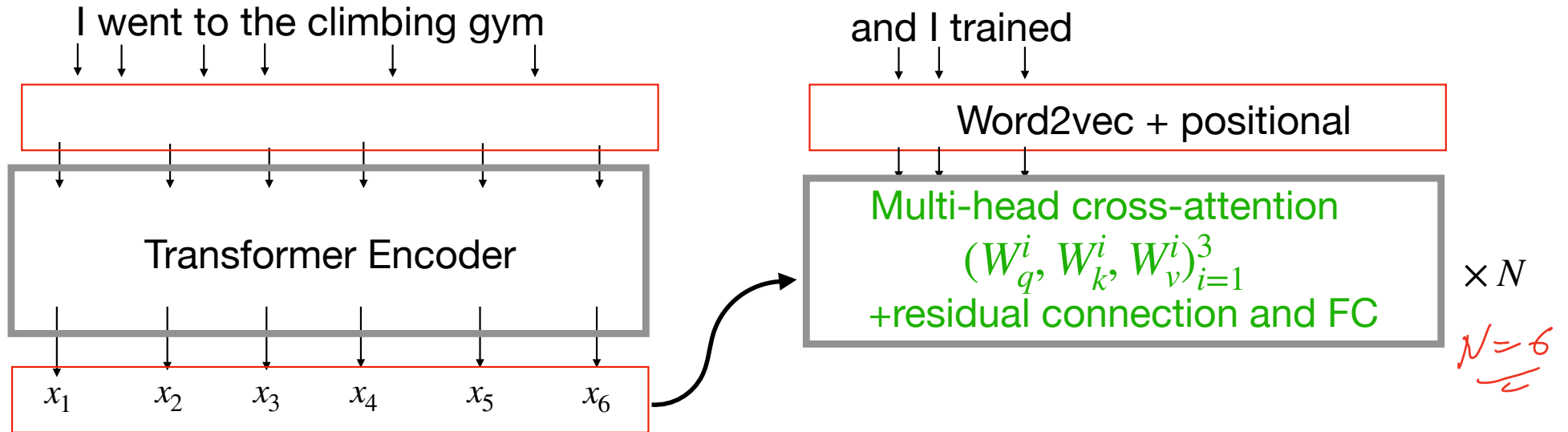
The Transformer model: decoder



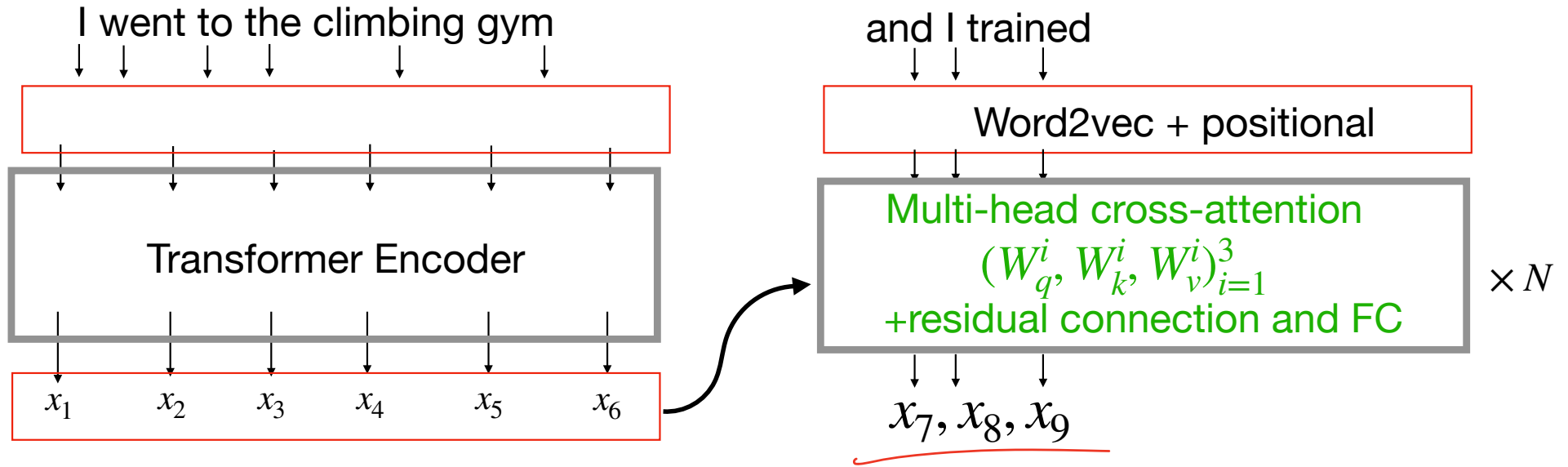
The Transformer model: decoder



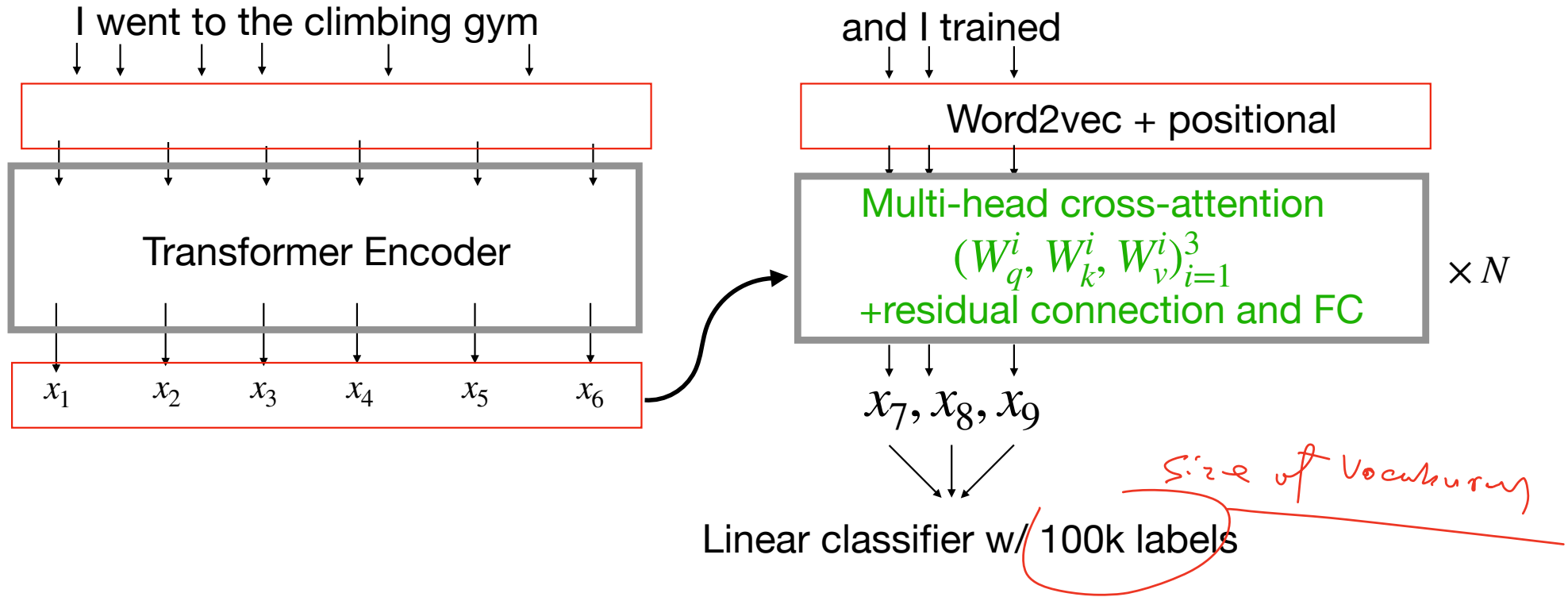
The Transformer model: decoder



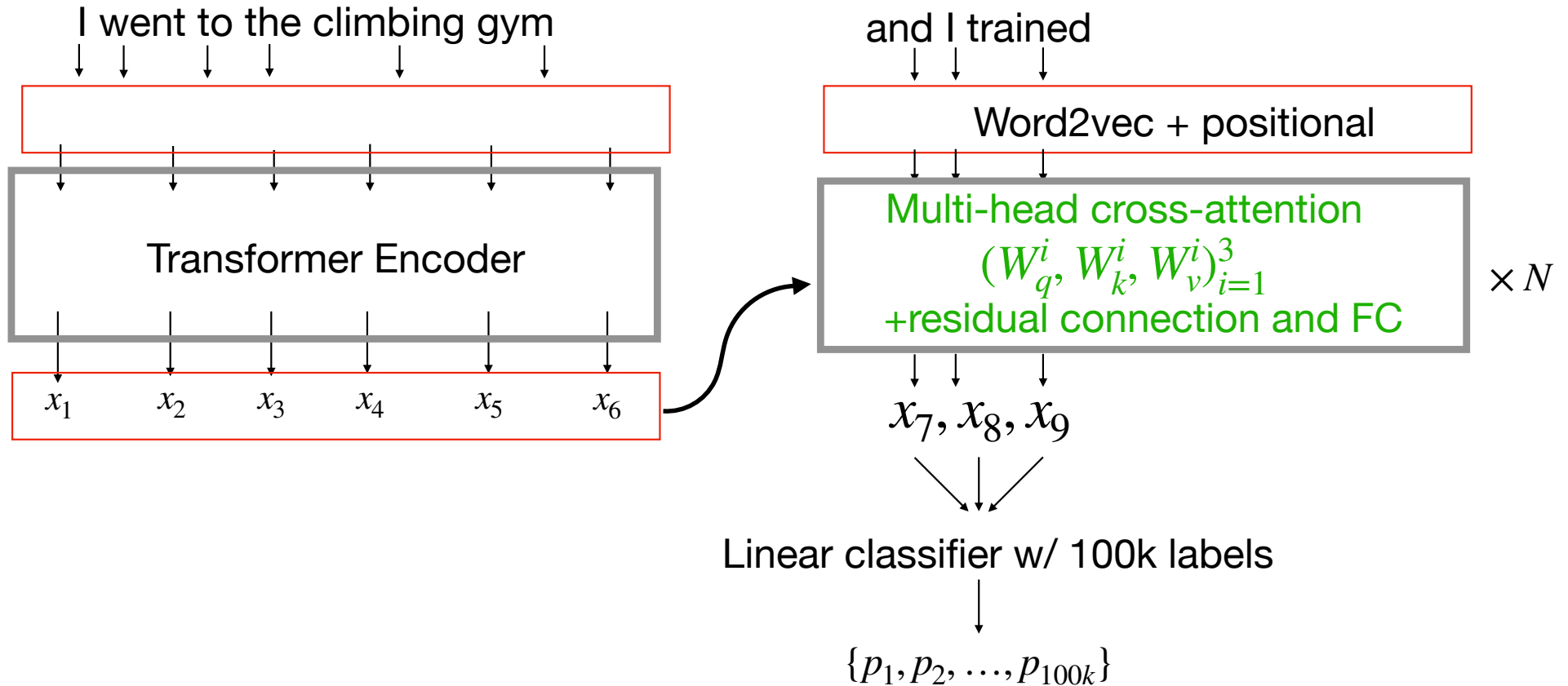
The Transformer model: decoder



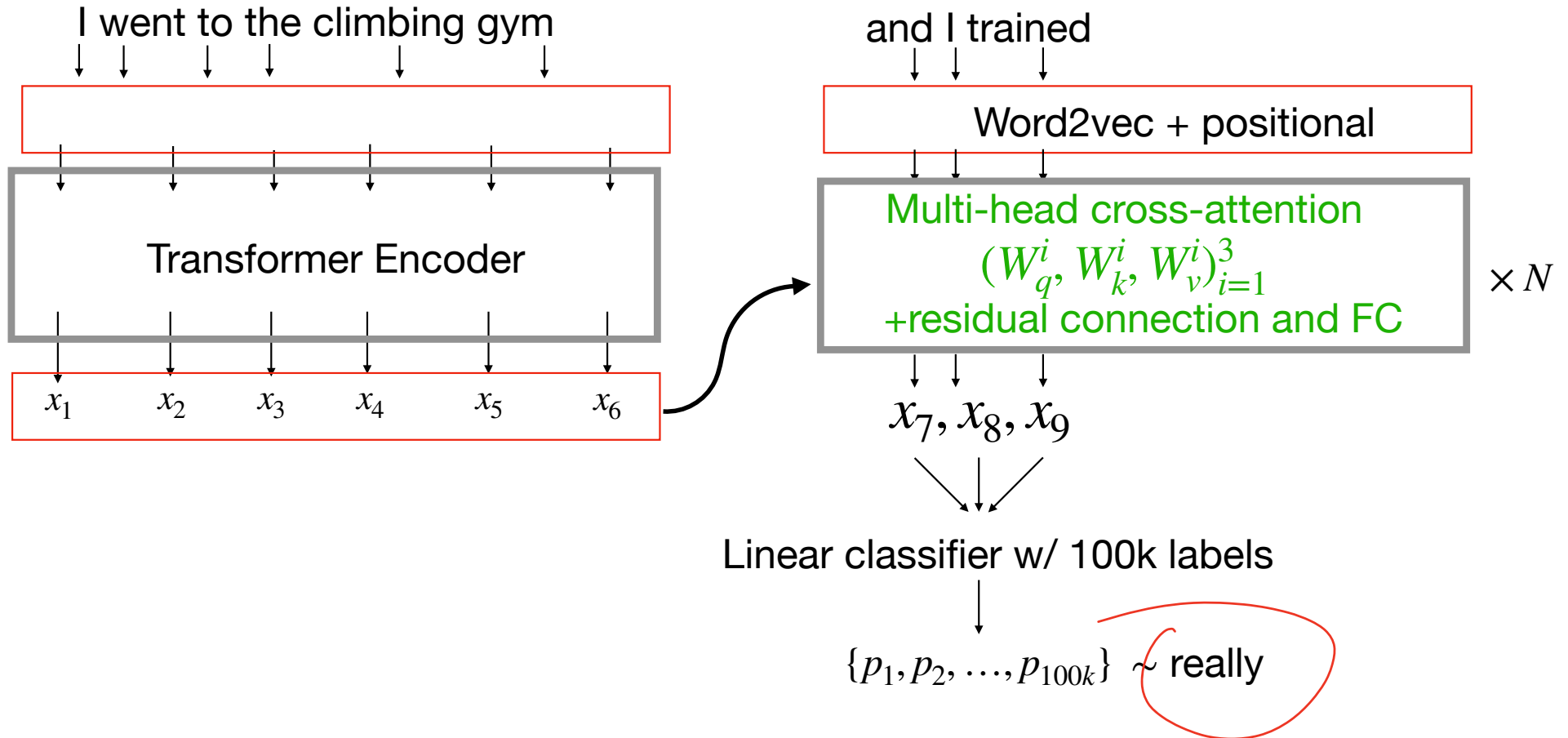
The Transformer model: decoder



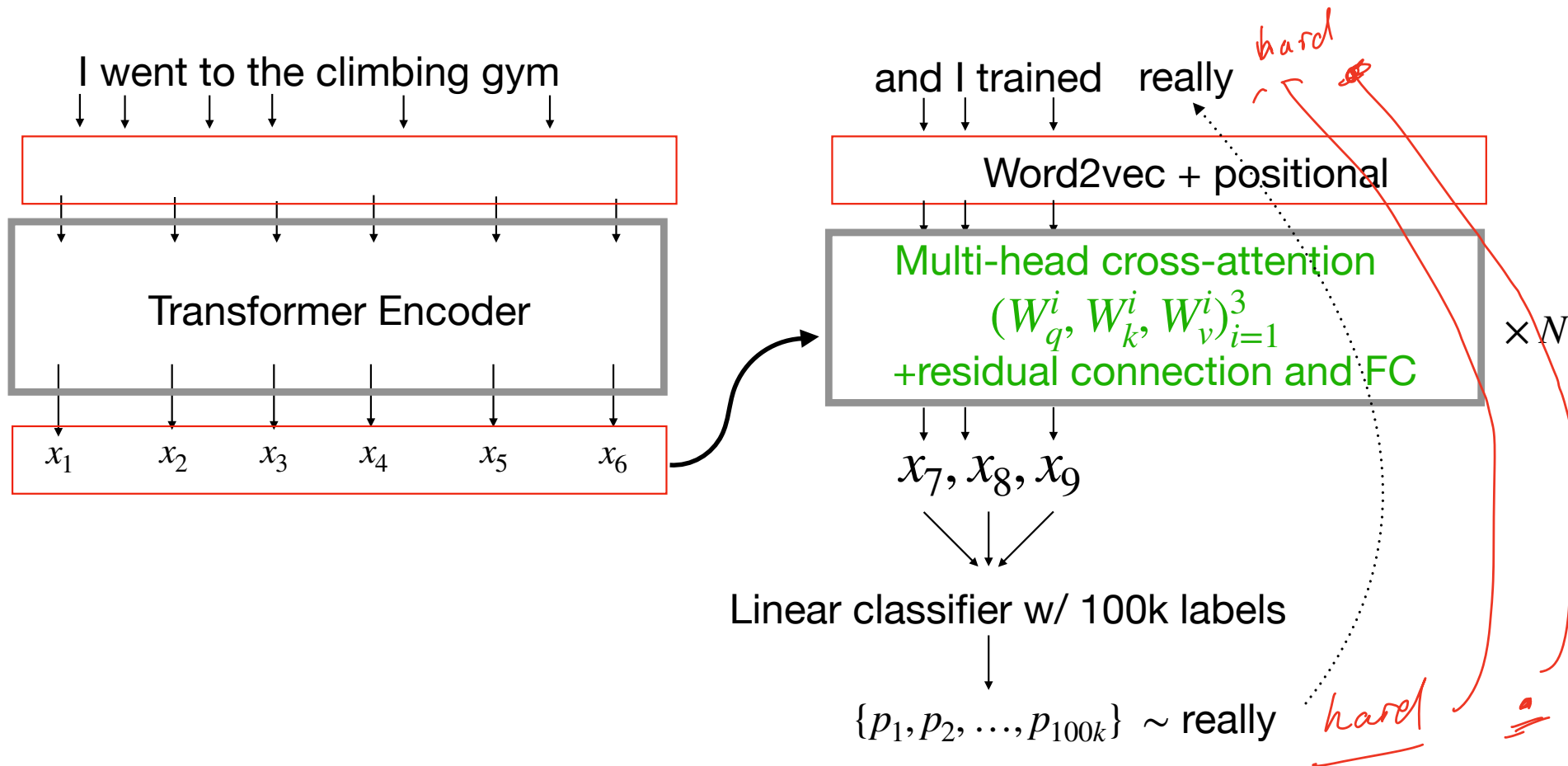
The Transformer model: decoder



The Transformer model: decoder



The Transformer model: decoder



Take home task:

Check out the the original paper (not too hard to read!)

Attention Is All You Need

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