

CS 465 Lecture 20

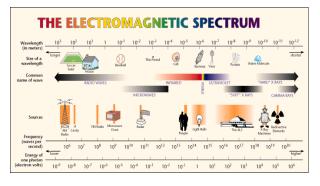
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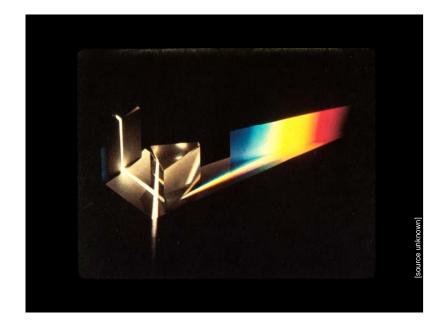
What light is

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- · Light is electromagnetic radiation
 - exists as oscillations of different frequency (or, wavelength)



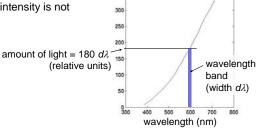
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Measuring light

- Salient property is the spectral power distribution (SPD)
 - the amount of light present at each wavelength
 - units: Watts per nanometer (tells you how much power you'll find in a narrow range of wavelengths)

 for color, often use "relative units" when overall intensity is not important



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What color is

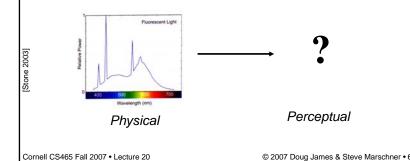
- Colors are the sensations that arise from light energy of different wavelengths
 - we are sensitive from about 380 to 760 nm—one "octave"
- Color is a phenomenon of human perception; it is **not** a universal property of light
- Roughly speaking, things appear "colored" when they depend on wavelength and "gray" when they do not.

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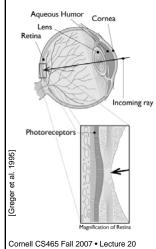
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The problem of color science

- Build a model for human color perception
- That is, map a Physical light description to a Perceptual color sensation



The eye as a measurement device



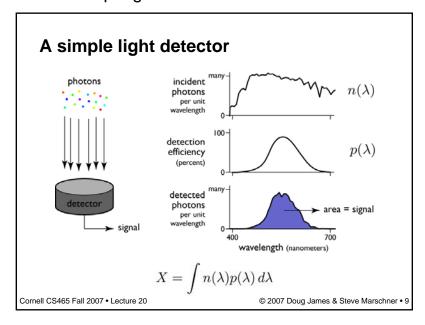
- We can model the low-level behavior of the eye by thinking of it as a light-measuring machine
 - its optics are much like a camera
 - its detection mechanism is also much like a camera
- Light is measured by the photoreceptors in the retina
 - they respond to visible light
 - different types respond to different wavelengths

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A simple light detector

- Produces a scalar value (a number) when photons land on
 - this value depends strictly on the number of photons detected
 - each photon has a probability of being detected that depends on the wavelength
 - there is no way to tell the difference between signals caused by light of different wavelengths: there is just a number
- This model works for many detectors:
 - based on semiconductors (such as in a digital camera)
 - based on visual photopigments (such as in human eyes)

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Light detection math

- Same math carries over to power distributions
 - spectrum entering the detector has its spectral power distribution (SPD), $s(\lambda)$
 - detector has its spectral sensitivity or spectral response, $r(\lambda)$

$$X = \int s(\lambda) r(\lambda) \, d\lambda$$
 measured signal detector's sensitivity input spectrum

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Light detection math

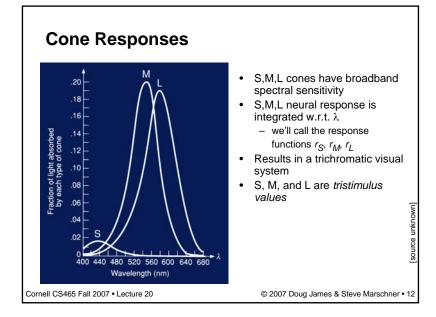
$$X = \int s(\lambda)r(\lambda) d\lambda$$
 or $X = s \cdot r$

- If we think of s and r as vectors, this operation is a dot product (aka inner product)
 - in fact, the computation is done exactly this way, using sampled representations of the spectra.
 - let λ_i be regularly spaced sample points $\Delta \lambda$ apart; then:

$$\tilde{s}[i] = s(\lambda_i); \tilde{r}[i] = r(\lambda_i)$$
$$\int s(\lambda)r(\lambda) d\lambda \approx \sum_i \tilde{s}[i]\tilde{r}[i] \Delta\lambda$$

• this sum is very clearly a dot product

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Cone responses to a spectrum s

$$S = \int r_S(\lambda)s(\lambda) d\lambda = r_S \cdot s$$

$$M = \int r_M(\lambda)s(\lambda) d\lambda = r_M \cdot s$$

$$L = \int r_L(\lambda)s(\lambda) d\lambda = r_L \cdot s$$

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Basic fact of colorimetry

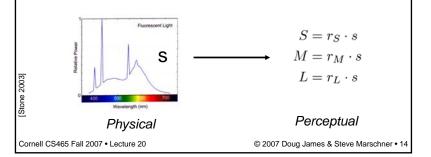
- Take a spectrum (which is a function)
- Eye produces three numbers
- This throws away a lot of information!
 - Quite possible to have two different spectra that have the same S,
 M, L tristimulus values
 - Two such spectra are *metamers*

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Colorimetry: an answer to the problem

- Wanted to map a *Physical light description* to a *Perceptual color sensation*
- Basic solution was known and standardized by 1930
 - Though not quite in this form-more on that in a bit



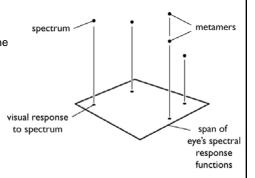
Pseudo-geometric interpretation

- A dot product is a projection
- We are projecting a high dimensional vector (a spectrum) onto three vectors
 - differences that are perpendicular to all 3 vectors are not detectable
- For intuition, we can imagine a 3D analog
 - 3D stands in for high-D vectors
 - 2D stands in for 3D
 - Then vision is just projection onto a plane

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Pseudo-geometric interpretation

- The information available to the visual system about a spectrum is three values
 - this amounts to a loss of information analogous to projection on a plane
- Two spectra that produce the same response are metamers



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Luminance, mathematically

• Y just has another response curve (like S, M, and L)

$$Y = r_{\mathbf{Y}} \cdot s$$

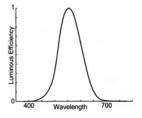
- r_Y is really called " V_{λ} "
- V_{λ} is a linear combination of S, M, and L
 - Has to be, since it's derived from cone outputs

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Basic colorimetric concepts

- Luminance
 - the overall magnitude of the the visual response to a spectrum (independent of its color)
 - corresponds to the everyday concept "brightness"
 - determined by product of SPD with the *luminous efficiency function* V_{λ} that describes the eye's overall ability to detect light at each wavelength
 - e.g. lamps are optimized to improve their luminous efficiency (tungsten vs. fluorescent vs. sodium vapor)



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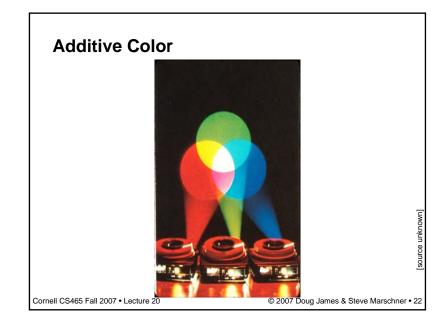
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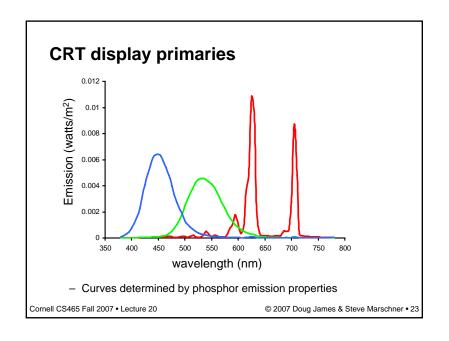
More basic colorimetric concepts

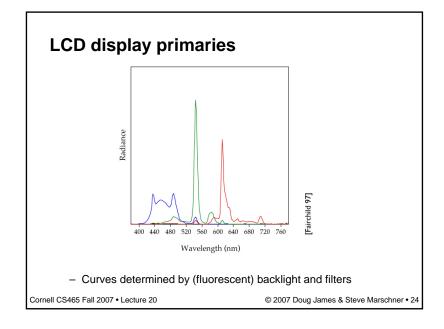
- Chromaticity
 - what's left after luminance is factored out (the color without regard for overall brightness)
 - scaling a spectrum up or down leaves chromaticity alone
- · Dominant wavelength
 - many colors can be matched by white plus a spectral color
 - correlates to everyday concept "hue"
- Purity
 - ratio of pure color to white in matching mixture
 - correlates to everyday concept "colorfulness" or "saturation"

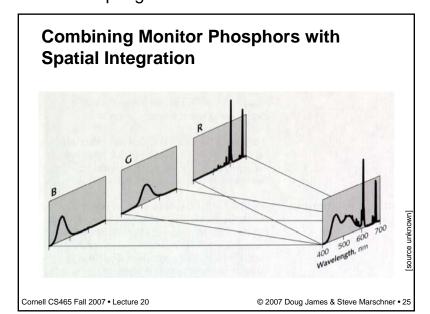
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Color reproduction • Have a spectrum s; want to match on RGB monitor - "match" means it looks the same - any spectrum that projects to the same point in the visual color space is a good reproduction • Must find a spectrum that the monitor can produce that is a metamer of s R, G, B? Cornell CS465 Fall 2007 • Lecture 20 © 2007 Doug James & Steve Marschner • 21









Color reproduction

- Say we have a spectrum s we want to match on an RGB monitor
 - "match" means it looks the same
 - any spectrum that projects to the same point in the visual color space is a good reproduction
- So, we want to find a spectrum that the monitor can produce that matches s
 - that is, we want to display a metamer of s on the screen

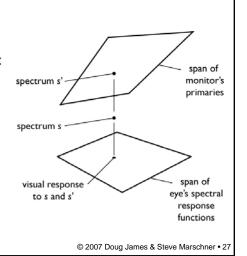
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Color reproduction

 We want to compute the combination of r, g, b that will project to the same visual response as s.

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Color reproduction as linear algebra

• The projection onto the three response functions can be written in matrix form:

$$\begin{bmatrix} S \\ M \\ L \end{bmatrix} = \begin{bmatrix} -r_S - \\ -r_M - \\ -r_L - \end{bmatrix} \begin{bmatrix} | \\ s \\ | \end{bmatrix}$$

or,

$$V = M_{SML} \, s.$$

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Color reproduction as linear algebra

• The spectrum that is produced by the monitor for the color signals R, G, and B is:

$$s_a(\lambda) = Rs_r(\lambda) + Gs_g(\lambda) + Bs_b(\lambda).$$

• Again the discrete form can be written as a matrix:

$$\begin{bmatrix} | \\ | \\ | \\ | \end{bmatrix} = \begin{bmatrix} | & | & | \\ | & | & | \\ | & | & | \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

or

$$s_a = M_{RGB} C.$$

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Color reproduction as linear algebra

 Goal of reproduction: visual response to s and s_a is the same:

$$M_{SML}\,\tilde{s}=M_{SML}\,\tilde{s_a}.$$

• Substituting in the expression for s_a,

$$M_{SML} \tilde{s} = M_{SML} M_{RGB} C$$

 $C = (M_{SML} M_{RGB})^{-1} M_{SML} \tilde{s}$

color matching matrix for RGB

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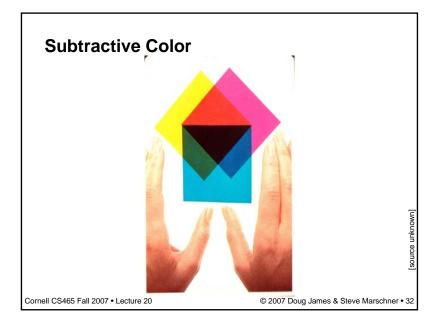
Color reproduction as linear algebra

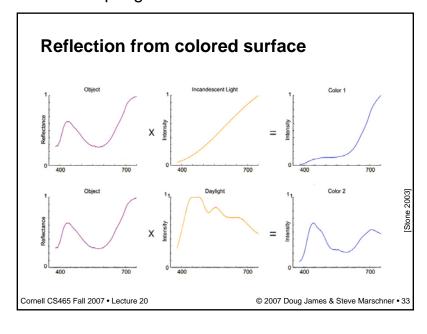
- What color do we see when we look at the display?
 - Feed C to display
 - Display produces s_a
 - Eye looks at sa and produces V

$$V = M_{SML} M_{RGB} C$$

$$\begin{bmatrix} S \\ M \\ L \end{bmatrix} = \begin{bmatrix} r_S \cdot s_R & r_S \cdot s_G & r_S \cdot s_B \\ r_M \cdot s_R & r_M \cdot s_G & r_M \cdot s_B \\ r_L \cdot s_R & r_L \cdot s_G & r_L \cdot s_B \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

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Subtractive color

- Produce desired spectrum by *subtracting* from white light (usually via absorption by pigments)
- Photographic media (slides, prints) work this way
- Leads to C, M, Y as primaries
- Approximately, 1-R, 1-G, 1-B

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Color spaces

- Need three numbers to specify a color
 - but what three numbers?
 - a color space is an answer to this question
- Common example: monitor RGB
 - define colors by what R, G, B signals will produce them on your monitor

(in math, s = RR + GG + BB for some spectra **R**, **G**, **B**)

- device dependent (depends on gamma, phosphors, gains, ...)
 - therefore if I choose RGB by looking at my monitor and send it to you, you may not see the same color
- also leaves out some colors (limited gamut), e.g. vivid yellow

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Standard color spaces

- Standardized RGB (sRGB)
 - makes a particular monitor RGB standard
 - other color devices simulate that monitor by calibration
 - sRGB is usable as an interchange space; widely adopted today
 - gamut is still limited

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A universal color space: XYZ

- Standardized by CIE (*Commission Internationale de l'Eclairage*, the standards organization for color science)
- Based on three "imaginary" primaries X, Y, and Z (in math, s = XX + YY + ZZ)
 - imaginary = only realizable by spectra that are negative at some wavelengths
 - key properties
 - any stimulus can be matched with positive X, Y, and Z
 - separates out luminance: X, Z have zero luminance, so Y tells you the luminance by itself

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Separating luminance, chromaticity

· Luminance: Y

• Chromaticity: x, y, z, defined as

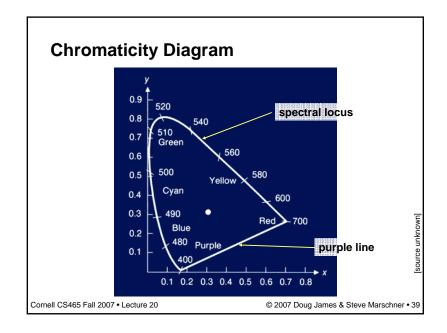
$$x = \frac{X}{X + Y + Z}$$

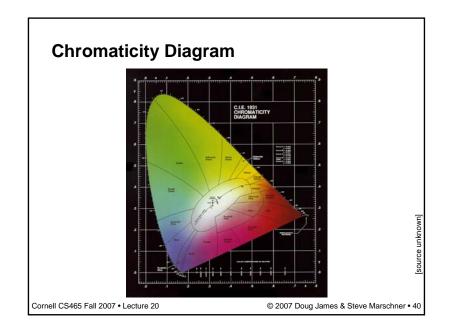
$$y = \frac{Y}{X + Y + Z}$$

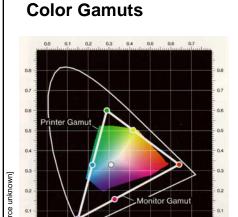
$$z = \frac{Z}{X + Y + Z}$$

- since x + y + z = 1, we only need to record two of the three
 - usually choose x and y, leading to (x, y, Y) coords

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Monitors/printers can't produce all visible colors

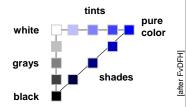
Reproduction is limited to a particular domain

For additive color (e.g. monitor) gamut is the triangle defined by the chromaticities of the three primaries.

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Perceptually organized color spaces

- Artists often refer to colors as tints, shades, and tones of pure pigments
 - tint: mixture with white
 - shade: mixture with black
 - tones: mixture with black and white
 - gray: no color at all (aka. neutral)



- This seems intuitive
 - tints and shades are inherently related to the pure color
 - "same" color but lighter, darker, paler, etc.

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Perceptual dimensions of color

- Hue
 - the "kind" of color, regardless of attributes
 - colorimetric correlate: dominant wavelength
 - artist's correlate: the chosen pigment color
- Saturation

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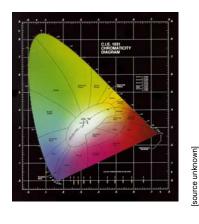
- the "colorfulness"
- colorimetric correlate: purity
- artist's correlate: fraction of paint from the colored tube
- Lightness (or value)
 - the overall amount of light
 - colorimetric correlate: luminance
 - artist's correlate: tints are lighter, shades are darker

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Perceptual dimensions: chromaticity

- In x, y, Y (or another luminance/chromaticity space), Y corresponds to lightness
- hue and saturation are then like polar coordinates for chromaticity (starting at white, which way did you go and how far?)

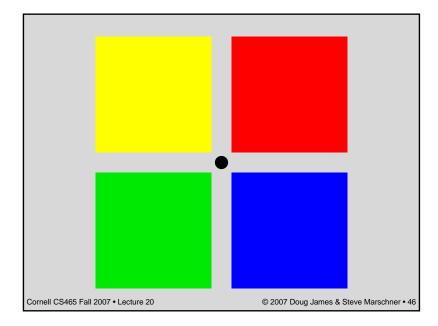


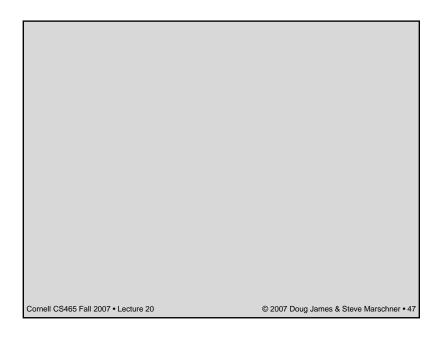
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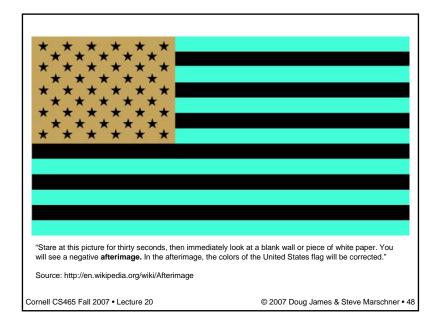
Perceptual dimensions of color

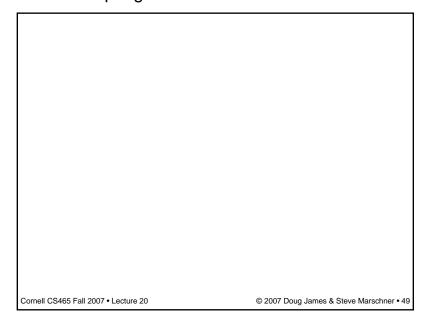
- There's good evidence ("opponent color theory") for a neurological basis for these dimensions
 - the brain seems to encode color early on using three axes:
 white black, red green, yellow blue
 - the white—black axis is lightness; the others determine hue and saturation
 - one piece of evidence: you can have a light green, a dark green, a yellow-green, or a blue-green, but you can't have a reddish green (just doesn't make sense)
 - thus red is the opponent to green
 - another piece of evidence: afterimages (next slide)

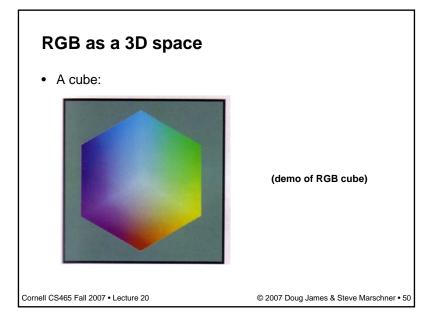
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Perceptual organization for RGB: HSV • Uses hue (an angle, 0 to 360), saturation (0 to 1), and value (0 to 1) as the three coordinates for a color - the brightest available RGB colors are those with one of R,G,B equal to 1 (top surface) - each horizontal slice is the surface of a sub-cube of the RGB cube (demo of HSV color pickers) (demo of HSV color pickers)

Perceptually uniform spaces

- Two major spaces standardized by CIE
 - designed so that equal differences in coordinates produce equally visible differences in color
 - LUV: earlier, simpler space; L*, u*, v*
 - LAB: more complex but more uniform: L*, a*, b*
 - both separate luminance from chromaticity
 - including a gamma-like nonlinear component is important

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