Antialiasing & Compositing

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Pixel coverage

- Antialiasing and compositing both deal with questions of pixels that contain unresolved detail
- Antialiasing: how to carefully throw away the detail
- Compositing: how to account for the detail when combining images

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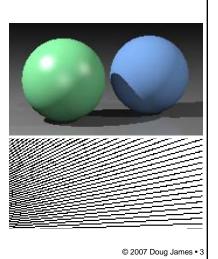
Aliasing

point sampling a continuous image:

continuous image defined by ray tracing procedure

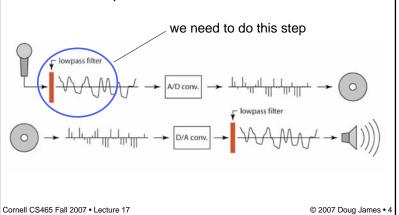
continuous image defined by a bunch of black rectangles

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Signal processing view

• Recall this picture:

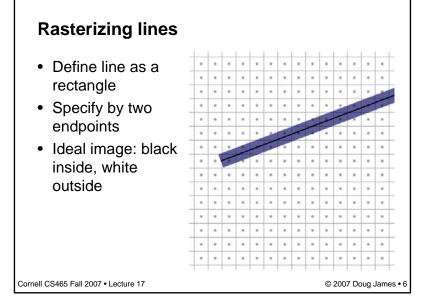


Antialiasing

- A name for techniques to prevent aliasing
- In image generation, we need to lowpass filter
 - Sampling the convolution of filter & image
 - Boils down to averaging the image over an area
 - Weight by a filter
- Methods depend on source of image
 - Rasterization (lines and polygons)
 - Point sampling (e.g. raytracing)
 - Texture mapping (to be discussed in 467)

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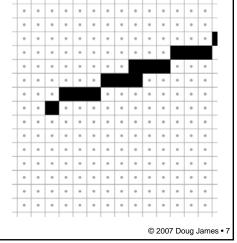


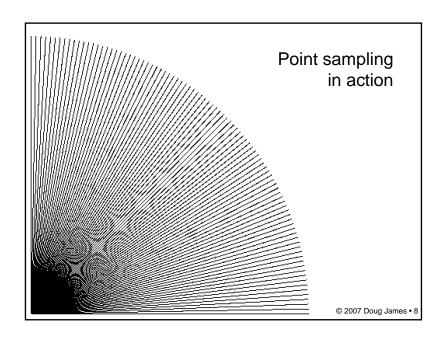
Point sampling

- Approximate rectangle by drawing all pixels whose centers fall within the line
- Problem: all-ornothing leads to jaggies

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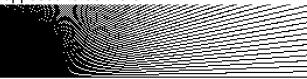
 this is sampling with no filter (aka. point sampling)





Aliasing

- Point sampling is fast and simple
- But the lines have stair steps and variations in width
- This is an aliasing phenomenon
 - Sharp edges of line contain high frequencies
- Introduces features to image that are not supposed to be there!



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Antialiasing

- Point sampling makes an all-or-nothing choice in each pixel
 - therefore steps are inevitable when the choice changes
 - yet another example where discontinuities are bad
- On bitmap devices this is necessary
 - hence high resolutions required
 - 600+ dpi in laser printers to make aliasing invisible
- On continuous-tone devices we can do better

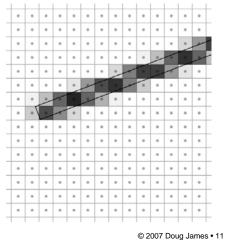
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Antialiasing

- Basic idea: replace "is the image black at the pixel center?" with "how much is pixel covered by black?"
- Replace yes/no question with quantitative question.

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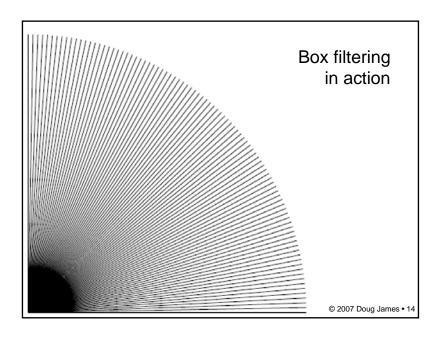
Box filtering

- Pixel intensity is proportional to area of overlap with square pixel area
- Also called "unweighted area averaging"

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Compute coverage fraction by counting subpixels Simple, accurate But slow Box filtering by supersampling 4/25 covered 20/25 covered 80% gray

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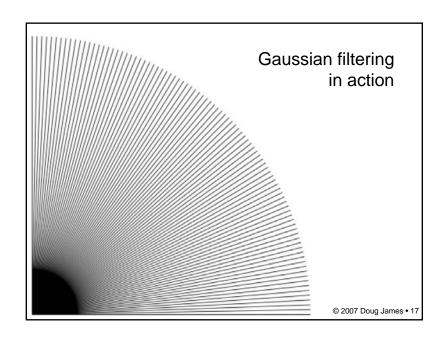
Weighted filtering

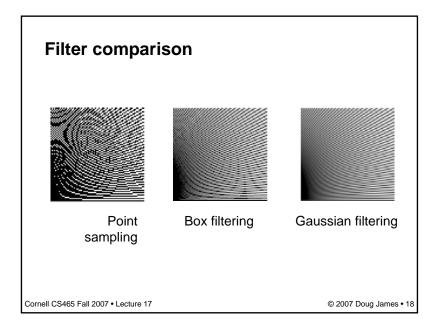
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- Box filtering problem: treats area near edge same as area near center
 - results in pixel turning on "too abruptly"
- Alternative: weight area by a smoother filter
 - unweighted averaging corresponds to using a box function
 - sharp edges mean high frequencies
 - so want a filter with good extinction for higher freqs.
 - a gaussian is a popular choice of smooth filter
 - important property: normalization (unit integral)

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Weighted filtering by supersampling • Compute filtering integral by summing filter values for covered subpixels • Simple, accurate • But really slow Cornell CS465 Fall 2007 • Lecture 17

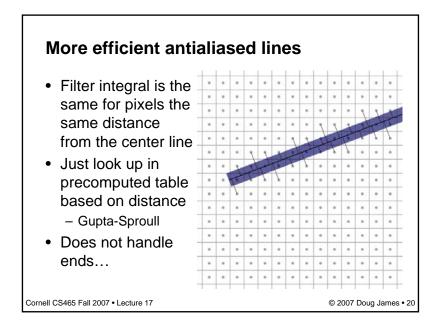


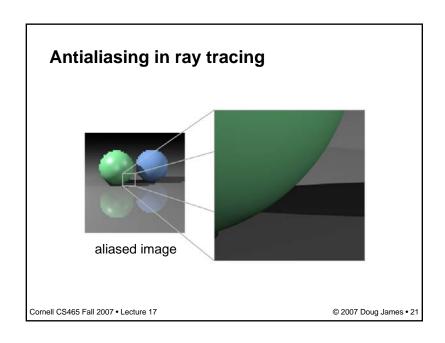


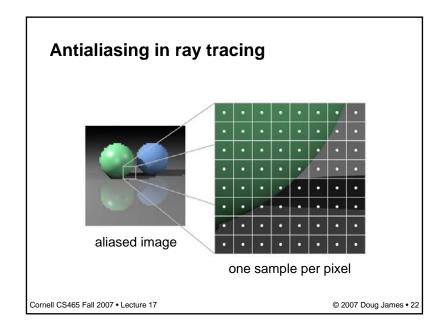
Antialiasing and resampling

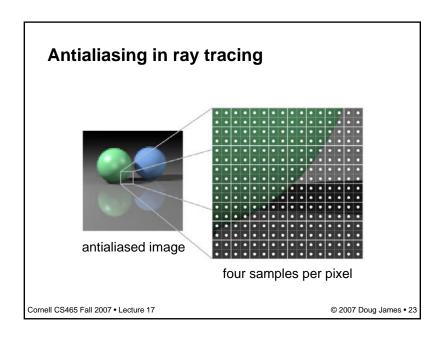
- Antialiasing by regular supersampling is the same as rendering a larger image and then resampling it to a smaller size
- Convolution of filter with high-res image produces an estimate of the area of the primitive in the pixel.
- So we can re-think this
 - one way: we're computing area of pixel covered by primitive
 - another way: we're computing average color of pixel
 - this way generalizes easily to arbitrary filters, arbitrary images

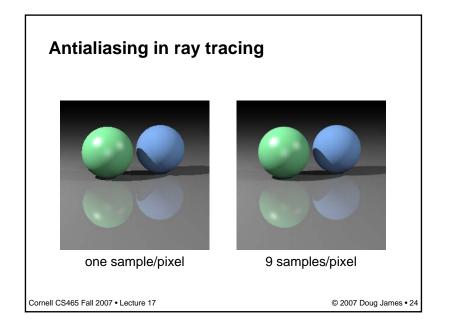
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Details of supersampling

• For image coordinates with integer pixel centers:

```
for iy = 0 to (ny-1) by 1

for ix = 0 to (nx-1) by 1 {

    ray = camera.getRay(ix, iy);

    image.set(ix, iy, trace(ray));

}
```

// one sample per pixel



```
// ns^2 samples per pixel
for iy = 0 to (ny-1) by 1
for ix = 0 to (nx-1) by 1 {
    Color sum = 0;
    for dx = -(ns-1)/2 to (ns-1)/2 by 1
        for dy = -(ns-1)/2 to (ns-1)/2 by 1 {
            x = ix + dx / ns;
            y = iy + dy / ns;
            ray = camera.getRay(x, y);
            sum += trace(ray);
        }
    image.set(ix, iy, sum / (ns*ns));
}
```

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Details of supersampling

For image coordinates in unit square

```
// one sample per pixel
for iy = 0 to (ny-1) by 1
for ix = 0 to (nx-1) by 1 {
    double x = (ix + 0.5) / nx;
    double y = (iy + 0.5) / ny;
    ray = camera.getRay(x, y);
    image.set(ix, iy, trace(ray));
}
```

```
// ns^2 samples per pixel
for iy = 0 to (ny-1) by 1
for ix = 0 to (nx-1) by 1 {
    Color sum = 0;
    for dx = 0 to (ns-1) by 1 {
        ror dy = 0 to (ns-1) by 1 {
            x = (ix + (dx + 0.5) / ns) / nx;
            y = (iy + (dy + 0.5) / ns) / ny;
            ray = camera.getRay(x, y);
            sum += trace(ray);
    }
    image.set(ix, iy, sum / (ns*ns));
}
```

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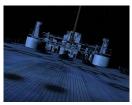
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Compositing











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Combining images

- Often useful combine elements of several images
- Trivial example: video crossfade
 - smooth transition from one scene to another







$$r_C = tr_A + (1 - t)r_B$$

 $g_C = tg_A + (1 - t)g_B$
 $b_C = tb_A + (1 - t)b_B$

- note: weights sum to 1.0
 - no unexpected brightening or darkening
 - no out-of-range results
- this is linear interpolation

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Foreground and background

- In many cases just adding is not enough
- Example: compositing in film production
 - shoot foreground and background separately
 - also include CG elements
 - this kind of thing has been done in analog for decades
 - how should we do it digitally?

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Foreground and background

• How we compute new image varies with position

use foreground-



use background

 Therefore, need to store some kind of tag to say what parts of the image are of interest

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Binary image mask

- First idea: store one bit per pixel
 - answers question "is this pixel part of the foreground?"





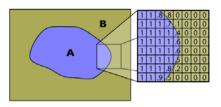
- causes jaggies similar to point-sampled rasterization
- same problem, same solution: intermediate values

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Partial pixel coverage

 The problem: pixels near boundary are not strictly foreground or background

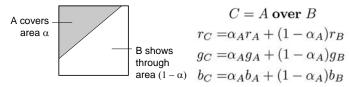


- how to represent this simply?
- interpolate boundary pixels between the fg. and bg.

Colors
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Alpha compositing

- Formalized in 1984 by Porter & Duff
- Store fraction of pixel covered, called α



- exactly like a spatially varying crossfade
- Convenient implementation
 - 8 more bits makes 32
 - 2 multiplies + 1 add per pixel for compositing

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Alpha compositing—example





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Compositing composites

- so far we only considered single fg. over single bg.
- in real applications we have *n* layers
 - Titanic example
 - compositing foregrounds to create new foregrounds
 - what to do with α ?
- desirable property: associativity

$$A \text{ over } (B \text{ over } C) = (A \text{ over } B) \text{ over } C$$

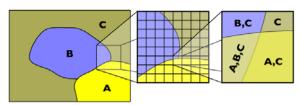
– to make this work we need to be careful about how $\boldsymbol{\alpha}$ is computed

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Compositing composites

• Some pixels are partly covered in more than one layer



- in D = A over (B over C) what will be the result?

$$c_D = \alpha_A c_A + (1 - \alpha_A)[\alpha_B c_B + (1 - \alpha_B)c_C]$$

= $\alpha_A c_A + (1 - \alpha_A)\alpha_B c_B + (1 - \alpha_A)(1 - \alpha_B)c_C$

Fraction covered by neither A nor B

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Associativity?

- What does this imply about (A over B)?
 - Coverage has to be

$$\alpha_{(A \text{ over } B)} = 1 - (1 - \alpha_A)(1 - \alpha_B)$$
$$= \alpha_A + (1 - \alpha_A)\alpha_B$$

...but the color values then don't come out nicely in D = (A over B) over C:

$$c_D = \alpha_A c_A + (1 - \alpha_A) \alpha_B c_B + (1 - \alpha_A) (1 - \alpha_B) c_C$$

= $\alpha_{(A \text{ over } B)}(\cdots) + (1 - \alpha_{(A \text{ over } B)}) c_C$

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An optimization

· Compositing equation again

$$c_C = \alpha_A c_A + (1 - \alpha_A) c_B$$

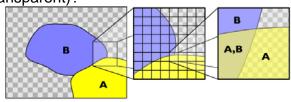
- Note c_A appears only in the product $\alpha_A c_A$
 - so why not do the multiplication ahead of time?
- Leads to premultiplied alpha:
 - store pixel value (r', g', b', α) where $c' = \alpha c$
 - C = A **over** B becomes $c'_C = c'_A + (1 \alpha_A)c'_B$
 - this turns out to be more than an optimization...
 - hint: so far the background has been opaque!

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Compositing composites

What about just C = A over B (with B transparent)?



- in premultiplied alpha, the result

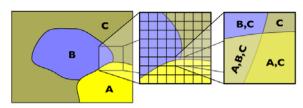
$$\alpha_C = \alpha_A + (1 - \alpha_A)\alpha_B$$

looks just like blending colors, and it leads to associativity.

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Associativity!



$$c_D = c'_A + (1 - \alpha_A)[c'_B + (1 - \alpha_B)c'_C]$$

= $[c'_A + (1 - \alpha_A)c'_B] + (1 - \alpha_A)(1 - \alpha_B)c'_C$
= $c'_{(A \text{ over } B)} + (1 - \alpha_{(A \text{ over } B)})c'_C$

- This is another good reason to premultiply

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Independent coverage assumption

- Why is it reasonable to blend α like a color?
- Simplifying assumption: covered areas are independent
 - that is, uncorrelated in the statistical sense



description	area
$\overline{A} \cap \overline{B}$	$(1-\alpha_A)(1-\alpha_B)$
$A \cap \overline{B}$	$\alpha_A(1-\alpha_B)$
$\overline{A} \cap B$	$(1-\alpha_A)\alpha_B$
$A \cap B$	$\alpha_A \alpha_B$

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Independent coverage assumption

· Holds in most but not all cases







- · This will cause artifacts
 - but we'll carry on anyway because it is simple and usually works...

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