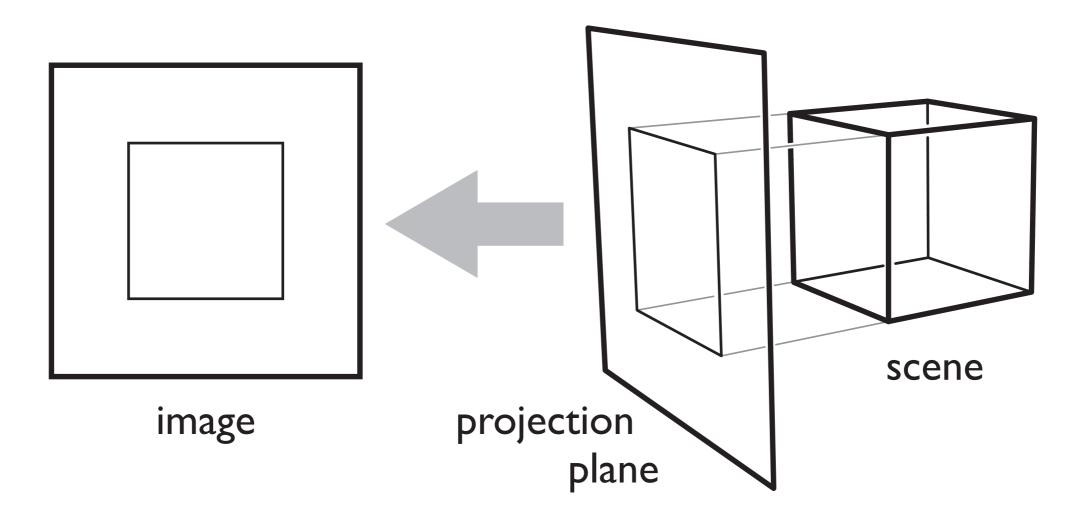
Perspective

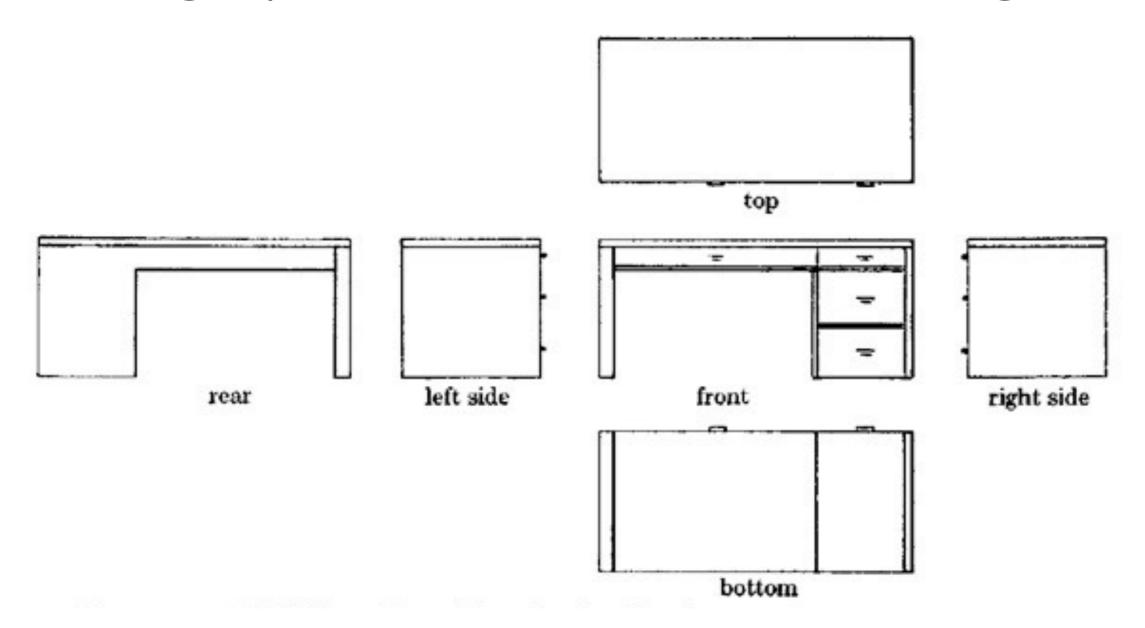
CS 4620 Lecture 5

Parallel projection

- To render an image of a 3D scene, we project it onto a plane
- Simplest kind of projection is parallel projection

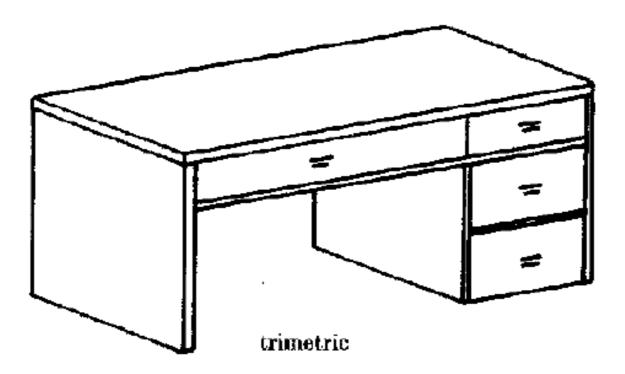


Orthographic in traditional drawing



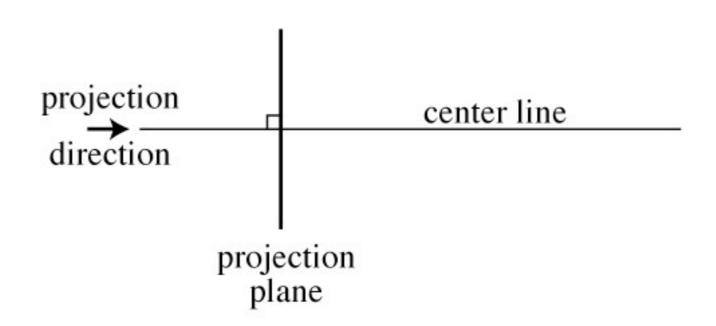
- projection plane parallel to a coordinate plane
- projection direction perpendicular to projection plane

Other parallel in traditional drawing

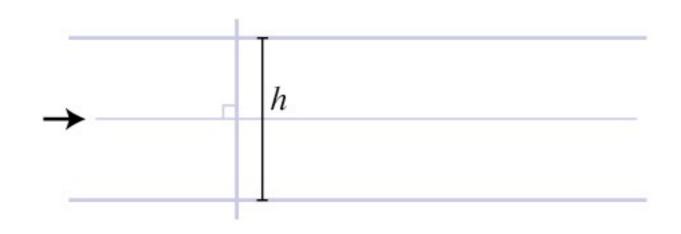


axonometric: projection plane perpendicular to projection direction but not parallel to coordinate planes

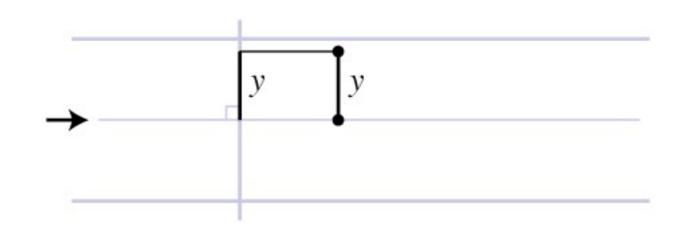
- In graphics usually we lump axonometric with orthographic
 - projection plane perpendicular to projection direction
 - image height determines size of objects in image



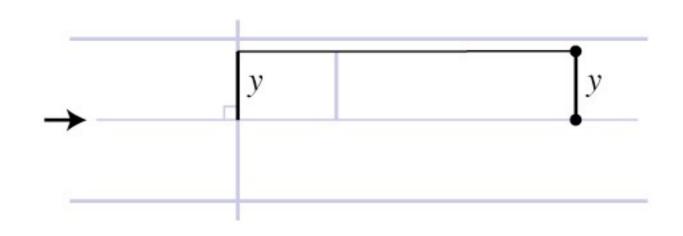
- In graphics usually we lump axonometric with orthographic
 - projection plane
 perpendicular to
 projection direction
 - image height
 determines size
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- In graphics usually we lump axonometric with orthographic
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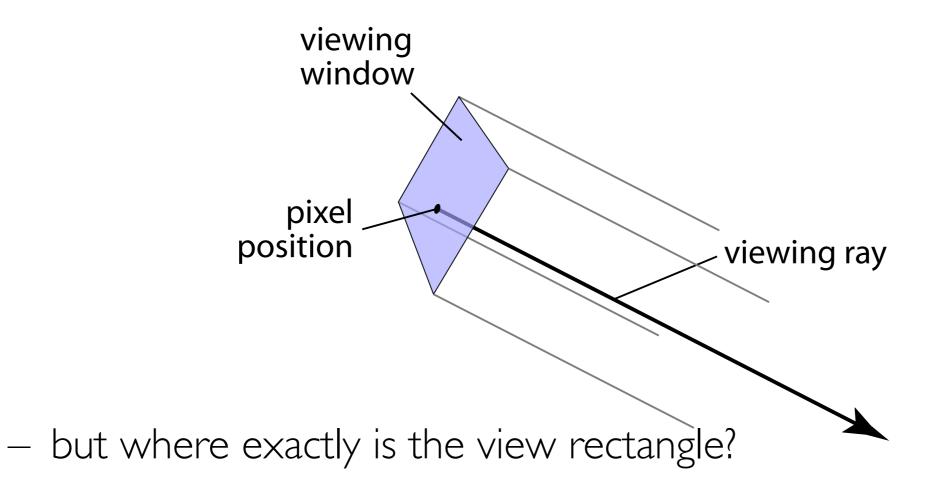


- In graphics usually we lump axonometric with orthographic
 - projection plane
 perpendicular to
 projection direction
 - image height
 determines size
 of objects in image



Generating eye rays—orthographic

- Ray origin (varying): pixel position on viewing window
- Ray direction (constant): view direction



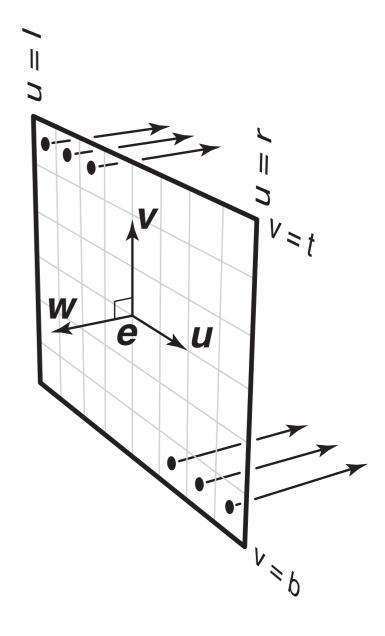
Generating eye rays—orthographic

Positioning the view rectangle

- establish three vectors to be camera basis: u, v, w
- view rectangle is in **u**-**v** plane, specified by l, r, t, b (often l = -r and b = -t)

Generating rays

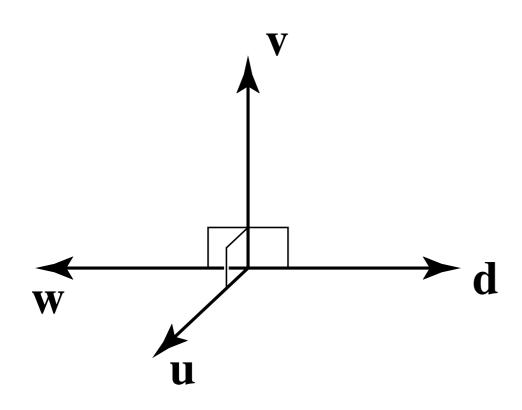
- for (u, v) in $[l, r] \times [b, t]$
- ray.origin = $\mathbf{e} + u \mathbf{u} + v \mathbf{v}$
- ray.direction = -**w**



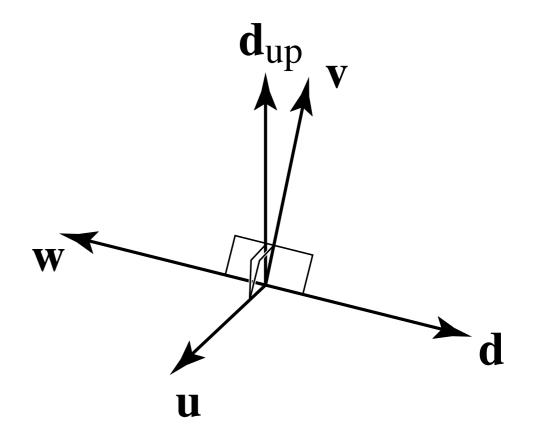
Establishing the camera basis

- Could require user to provide e, u, v, and w
 - but this is error prone and unintuitive
- Instead, calculate basis from things the user cares about
 - viewpoint: where the camera is \rightarrow **e**
 - view direction: which way the camera is looking → d
 - view plane normal (normally same as view direction)
 - up vector: how the camera is oriented
- This is enough to calculate u, v, and w
 - set w parallel to v.p. normal, facing away from d
 - set u perpendicular to w and perpendicular to up-vector
 - set v perpendicular to w and u to form a right-handed ONB

Camera basis



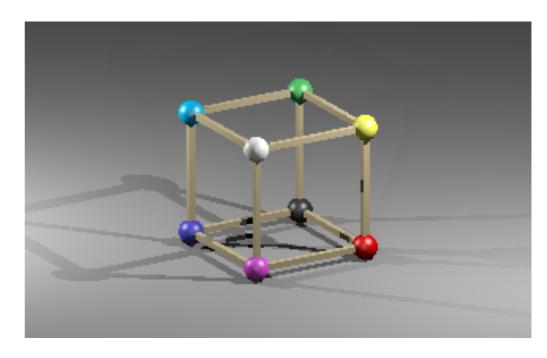
forming the basis with **d** and **v** given



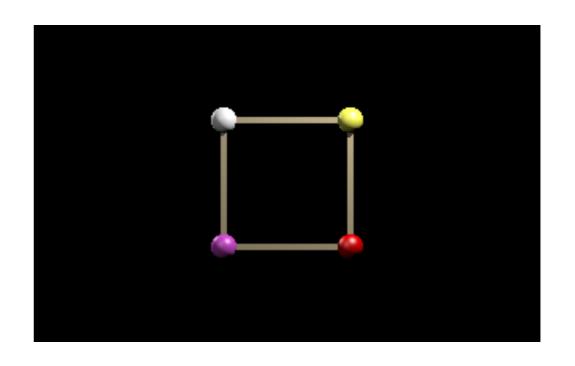
forming the basis with **d** and up vector given

Orthographic views in Ray I

```
<camera type="OrthographicCamera">
<viewPoint>10 4.2 6</viewPoint>
<viewDir>-5 -2.1 -3</viewDir>
<viewUp>0 1 0</viewUp>
<viewWidth>8</viewWidth>
<viewHeight>5</viewHeight>
</camera>
```



```
<camera type="OrthographicCamera">
<viewPoint>10 0 0</viewPoint>
 <viewDir>-1 0 0</viewDir>
 <viewUp>0 1 0</viewUp>
 <viewWidth>8</viewWidth>
 <viewHeight>5</viewHeight>
</camera>
```



History of projection

- Ancient times: Greeks wrote about laws of perspective
- Renaissance: perspective is adopted by artists



Duccio c. 1308

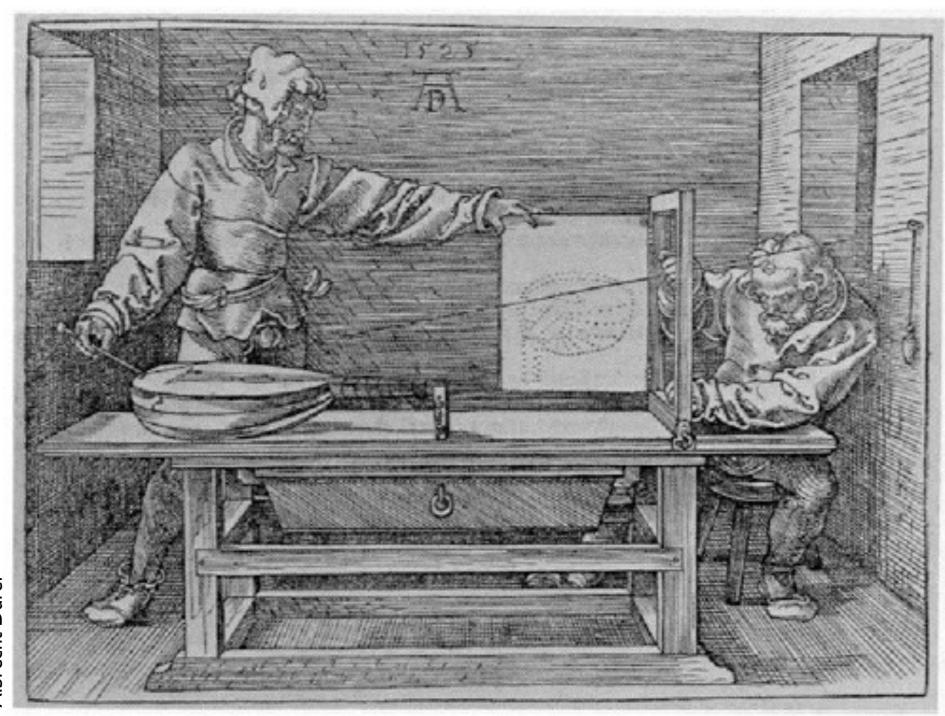
History of projection

Later Renaissance: perspective formalized precisely



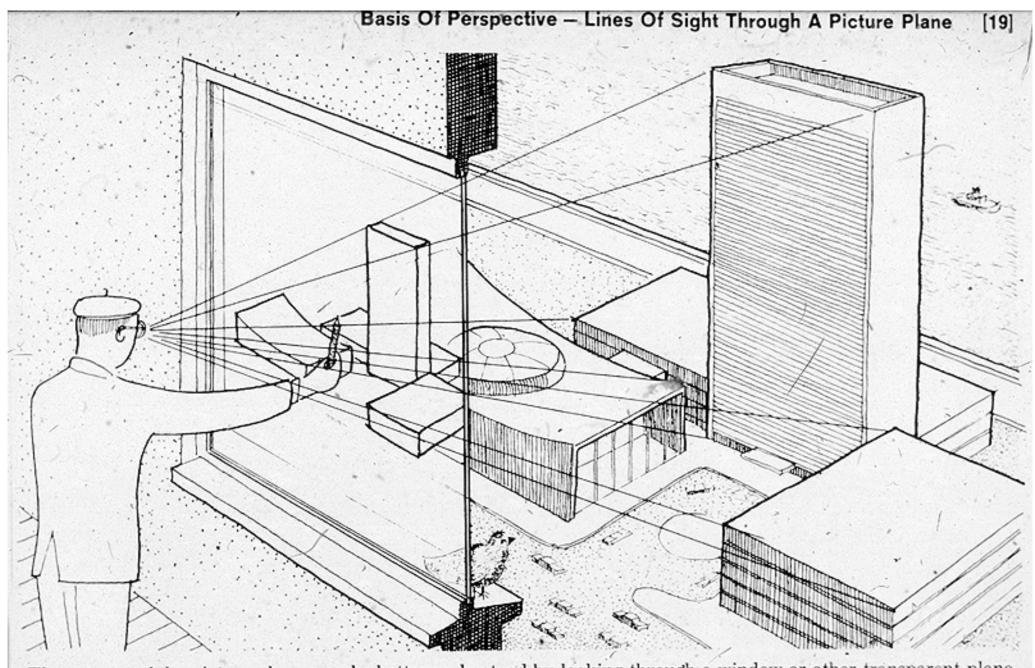
da Vinci c. 1498

Plane projection in drawing



Albrecht Dürer

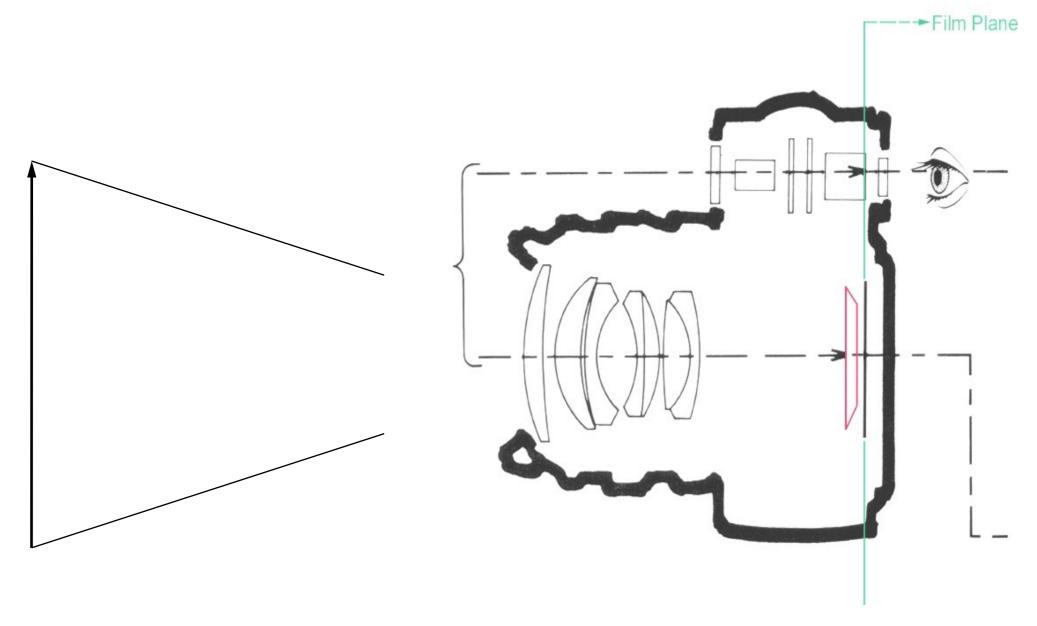
Plane projection in drawing



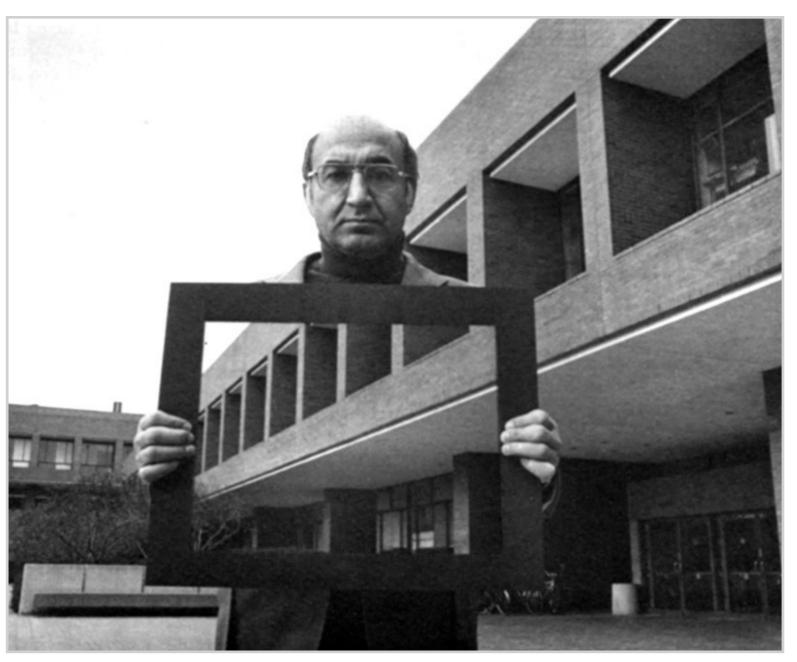
The concept of the picture plane may be better understood by looking through a window or other transparent plane from a fixed viewpoint. Your lines of sight, the multitude of straight lines leading from your eye to the subject, will all intersect this plane. Therefore, if you were to reach out with a grease pencil and draw the image of the subject on this plane you would be "tracing out" the infinite number of points of intersection of sight rays and plane. The result would be that you would have "transferred" a real three-dimensional object to a two-dimensional plane.

Plane projection in photography

- This is another model for what we are doing
 - applies more directly in realistic rendering

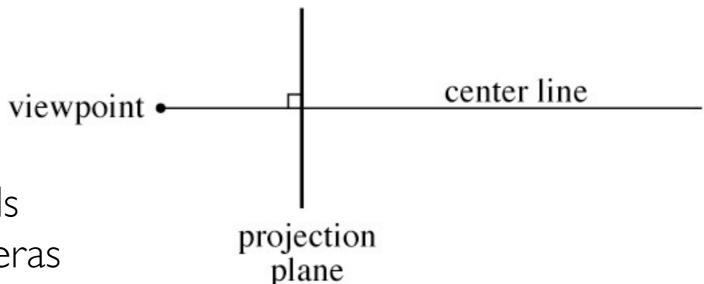


Plane projection in photography

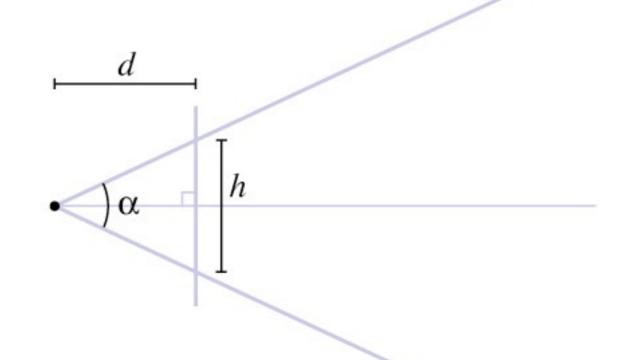


[Richard Zakia]

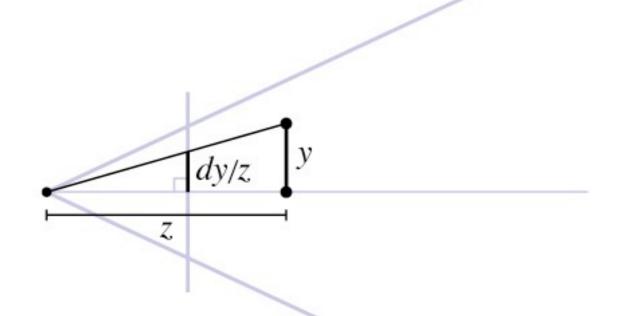
- Perspective is projection by lines through a point; "normal" = plane perpendicular to view direction
 - magnification determined by:
 - image height
 - object depth
 - image plane distance
 - f.o.v. $\alpha = 2 \operatorname{atan}(h/(2d))$
 - -y'=dy/z
 - "normal" case corresponds
 to common types of cameras



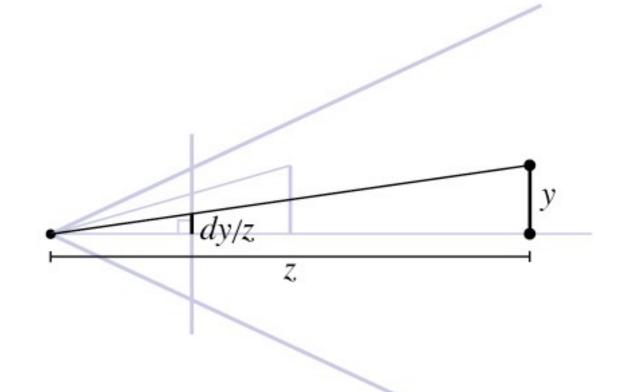
- Perspective is projection by lines through a point; "normal" = plane perpendicular to view direction
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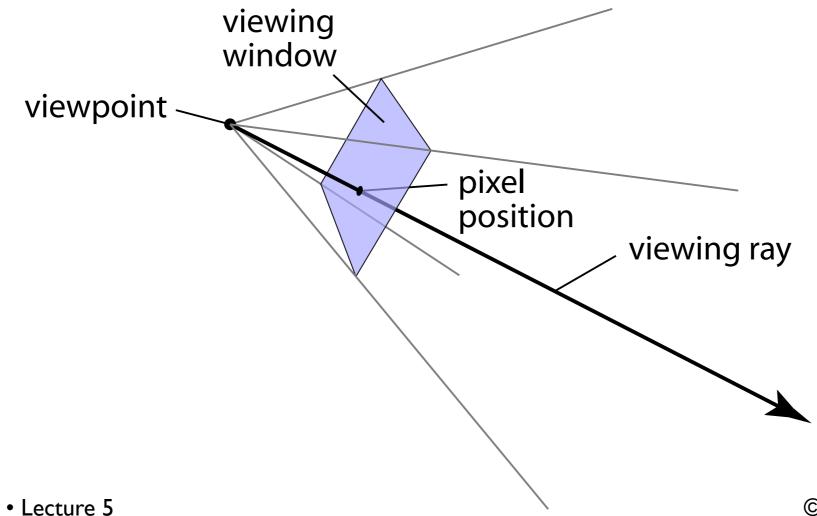


- Perspective is projection by lines through a point; "normal" = plane perpendicular to view direction
 - magnification determined by:
 - image height
 - object depth
 - image plane distance
 - f.o.v. $\alpha = 2 \operatorname{atan}(h/(2d))$
 - -y'=dy/z
 - "normal" case corresponds
 to common types of cameras



Generating eye rays—perspective

- Use window analogy directly
- Ray origin (constant): viewpoint
- Ray direction (varying): toward pixel position on viewing window



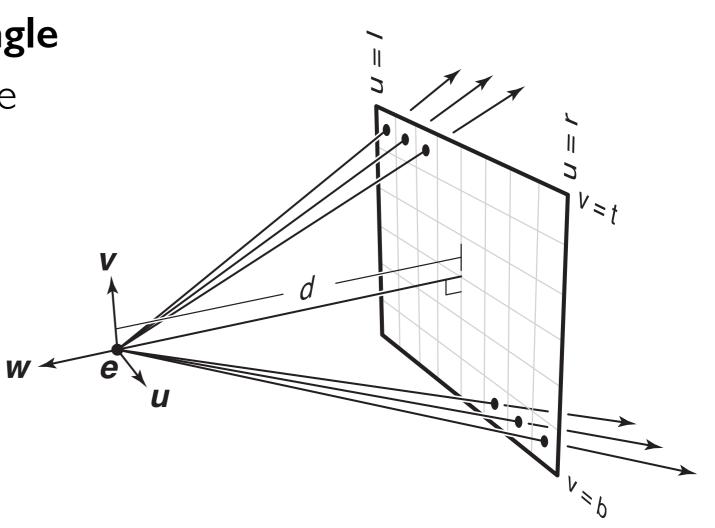
Generating eye rays—perspective

Positioning the view rectangle

- establish three vectors to becamera basis: u, v, w
- view rectangle is parallel to \mathbf{u} - \mathbf{v} plane, at w = -d, specified by l, r, t, b

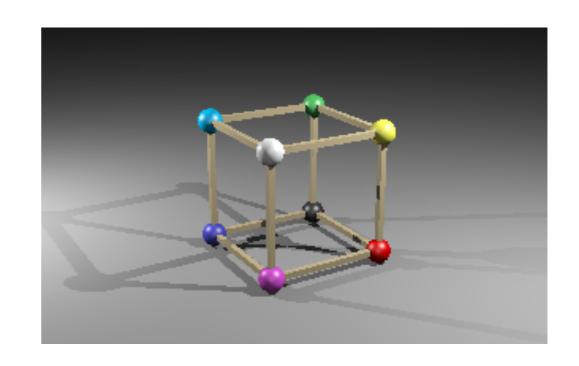
Generating rays

- for (u, v) in $[l, r] \times [b, t]$
- ray.origin = \mathbf{e}
- ray.direction = -d **w** + u **u** + v **v**

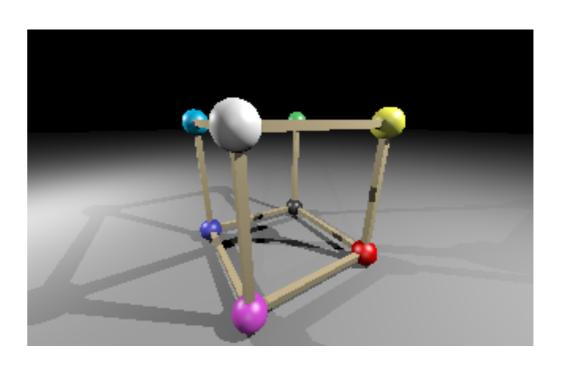


Perspective views in Ray I

```
<camera type="PerspectiveCamera">
      <viewPoint>10 4.2 6</viewPoint>
      <viewDir>-5 -2.1 -3</viewDir>
      <viewUp>0 1 0</viewUp>
      <projDistance>12</projDistance>
      <viewWidth>8</viewWidth>
      <viewHeight>5</viewHeight>
      </camera>
```



```
<camera type="PerspectiveCamera">
<viewPoint>2.5 1.05 1.5</viewPoint>
<viewDir>-5 -2.1 -3</viewDir>
<viewUp>0 1 0</viewUp>
<projDistance>3</projDistance>
<viewWidth>8</viewWidth>
<viewHeight>5</viewHeight>
</camera>
```



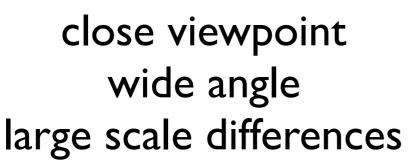
Field of view (or f.o.v.)

- The angle between the rays corresponding to opposite edges of a perspective image
 - simpler to compute for "normal" perspective
 - have to decide to measure vert., horiz., or diag.
- In cameras, determined by focal length
 - confusing because of many image sizes
 - for 35mm format (36mm by 24mm image)
 - -18mm = 67° v.f.o.v. super-wide angle
 - -28mm = 46° v.f.o.v. wide angle
 - -50mm = 27° v.f.o.v. "normal"
 - 100mm = 14° v.f.o.v. narrow angle ('telephoto')

Field of view

Determines "strength" of perspective effects







far viewpoint narrow angle small scale differences

Ken Perlin]

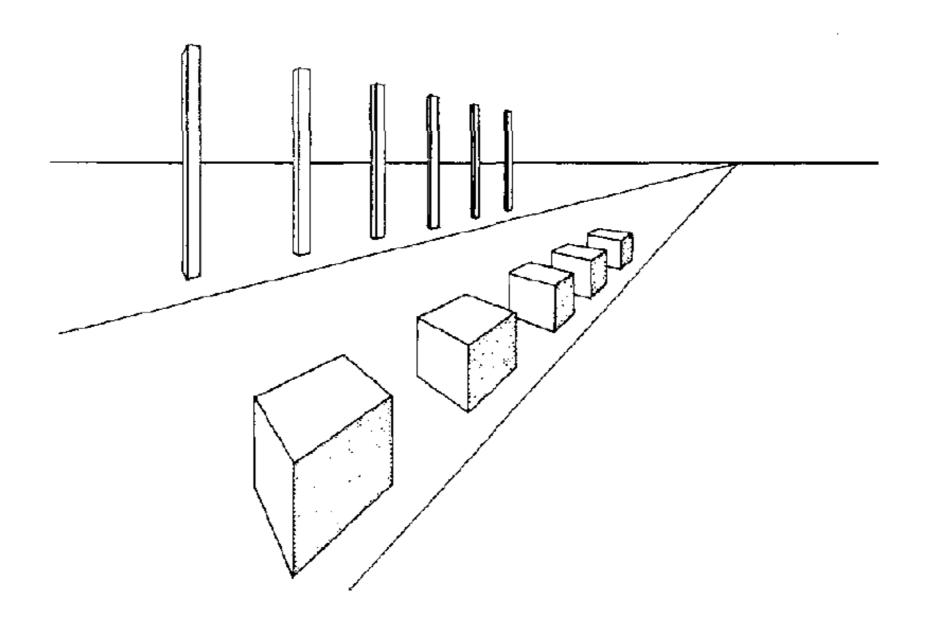
Choice of field of view

- In photography, wide angle lenses are specialty tools
 - "hard to work with"
 - easy to create weird-looking perspective effects
- In graphics, you can type in whatever f.o.v. you want
 - and people often type in big numbers!

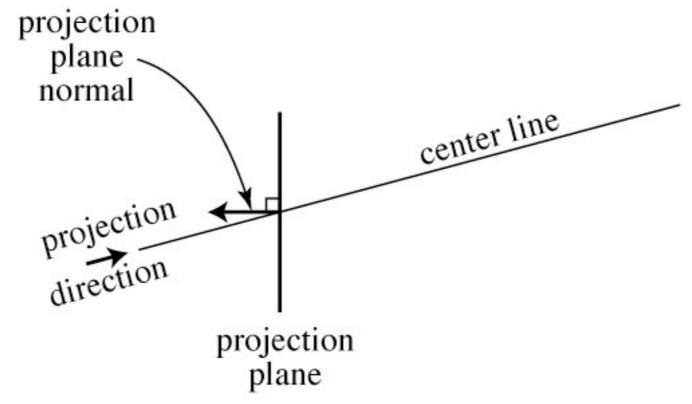


Perspective distortions

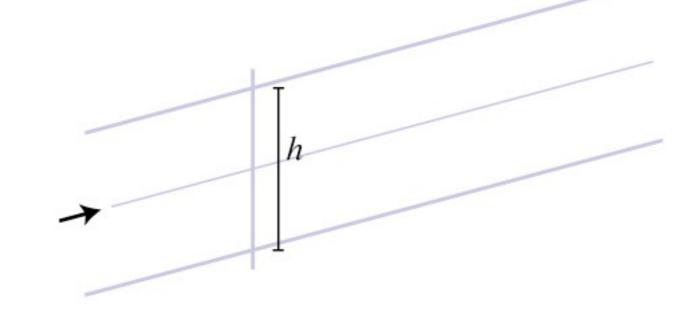
Lengths, length ratios



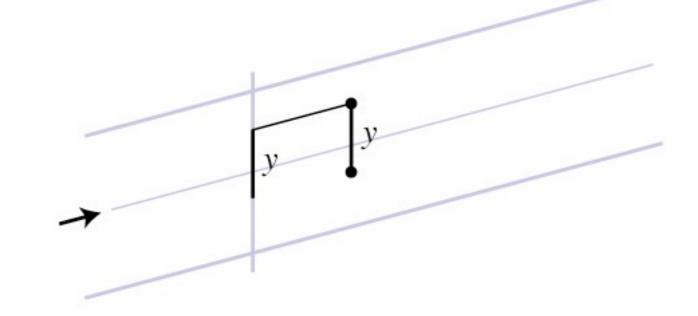
- View direction no longer coincides with projection plane normal (one more parameter)
 - objects at different distances still same size
 - objects are shifted
 in the image
 depending on their
 depth



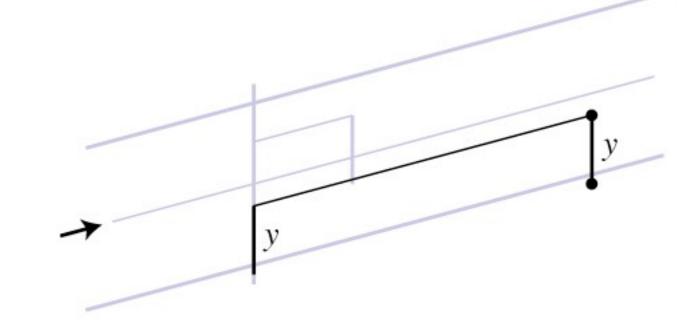
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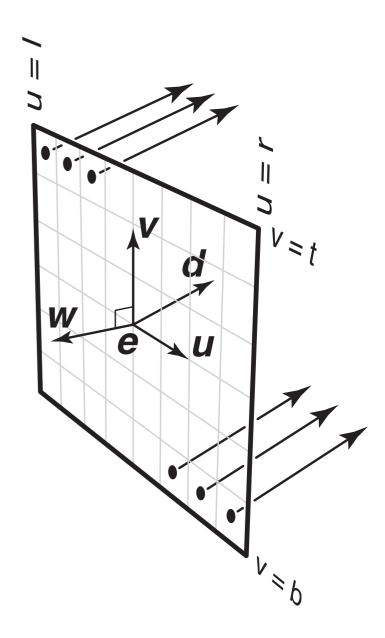
Oblique parallel views

View rectangle is the same

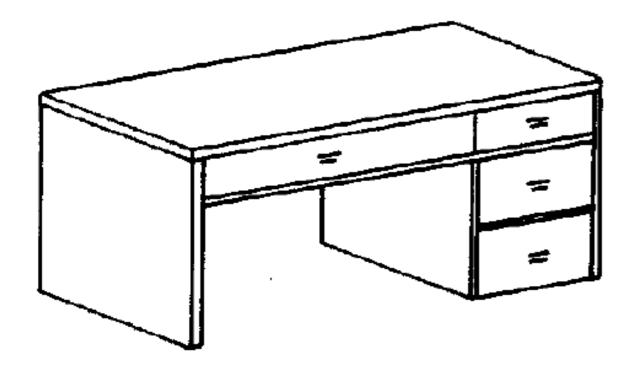
- ray origins identical to orthographic
- view direction d differs from -w

Generating rays

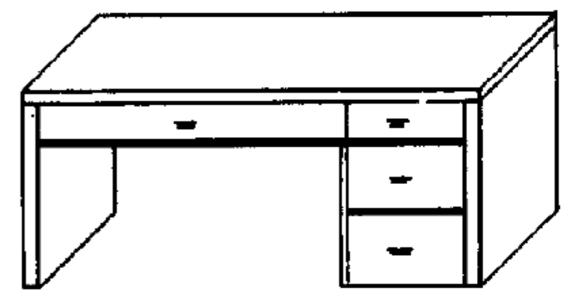
- for (u, v) in $[l, r] \times [b, t]$
- ray.origin = $\mathbf{e} + u \mathbf{u} + v \mathbf{v}$
- ray.direction = d



Off-axis parallel

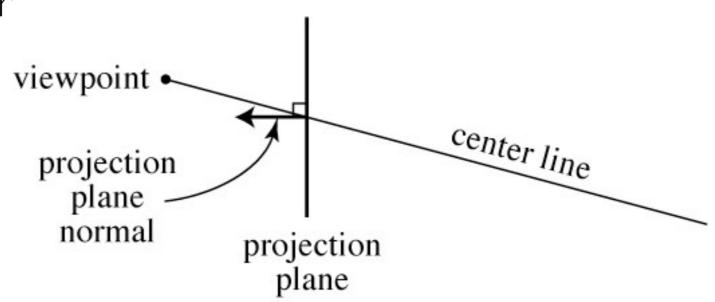


axonometric: projection plane perpendicular to projection direction but not parallel to coordinate planes

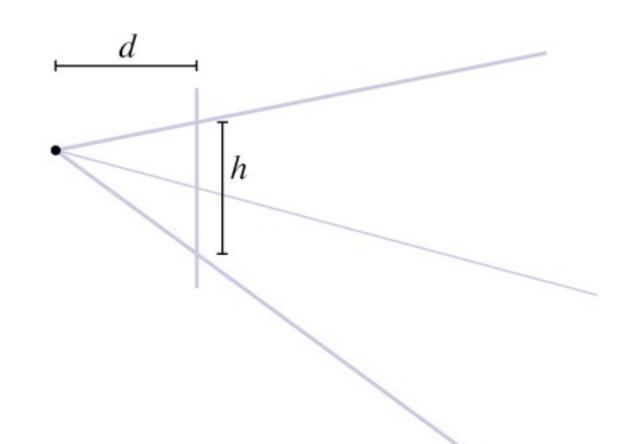


oblique: projection plane parallel to a coordinate plane but not perpendicular to projection direction.

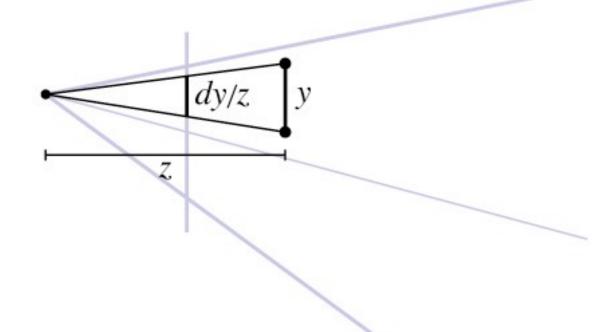
- Perspective but with projection plane not perpendicular to view direction
 - additional parameter:
 projection plane normal
 - exactly equivalent to cropping out an off-center rectangle from a larger "normal" perspective
 - corresponds to view camera in photography



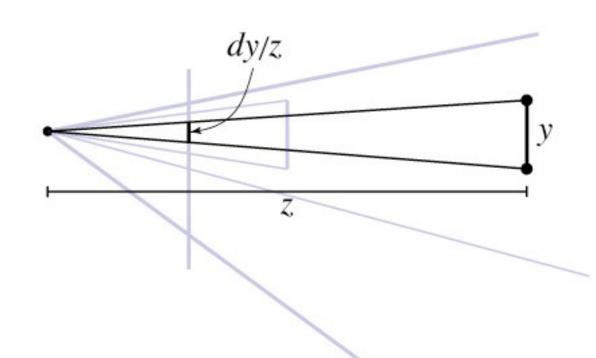
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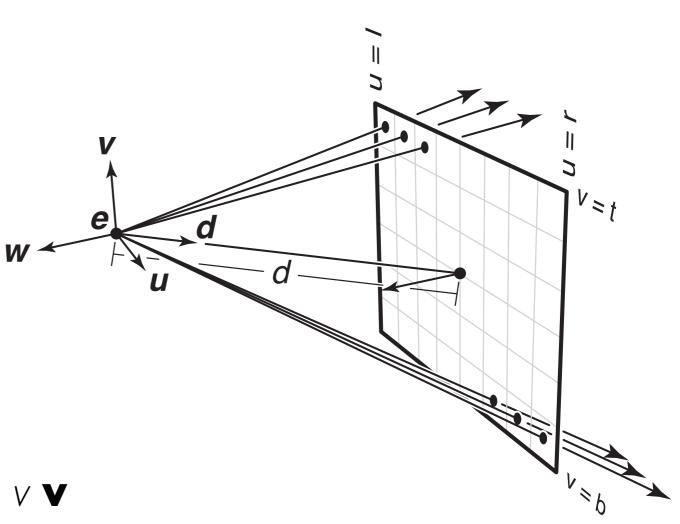
Oblique perspective views

Positioning the view rectangle

- establish three vectors to be
 camera basis: u, v, w
- view rectangle is the same,
 but shifted so that the
 center is in the
 direction d from e

Generating rays

- for (u, v) in $[l, r] \times [b, t]$
- ray.origin = \mathbf{e}
- ray.direction = d d + u u + v v



Why shifted perspective?

- Control convergence of parallel lines
- Standard example: architecture
 - buildings are taller than you, so you look up
 - top of building is farther away, so it looks smaller
- Solution: make projection plane parallel to facade
 - top of building is the same distance from the projection plane
- Same perspective effects can be achieved using postprocessing
 - (though not the focus effects)
 - choice of which rays vs. arrangement of rays in image



camera tilted up: converging vertical lines



lens shifted up: parallel vertical lines