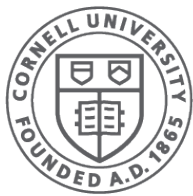


# Virtual Memory & Caching

(Chapter 12-17)

CS 4410  
Operating Systems



**Cornell CIS**  
COMPUTING AND INFORMATION SCIENCE

# Last Time: Address Translation

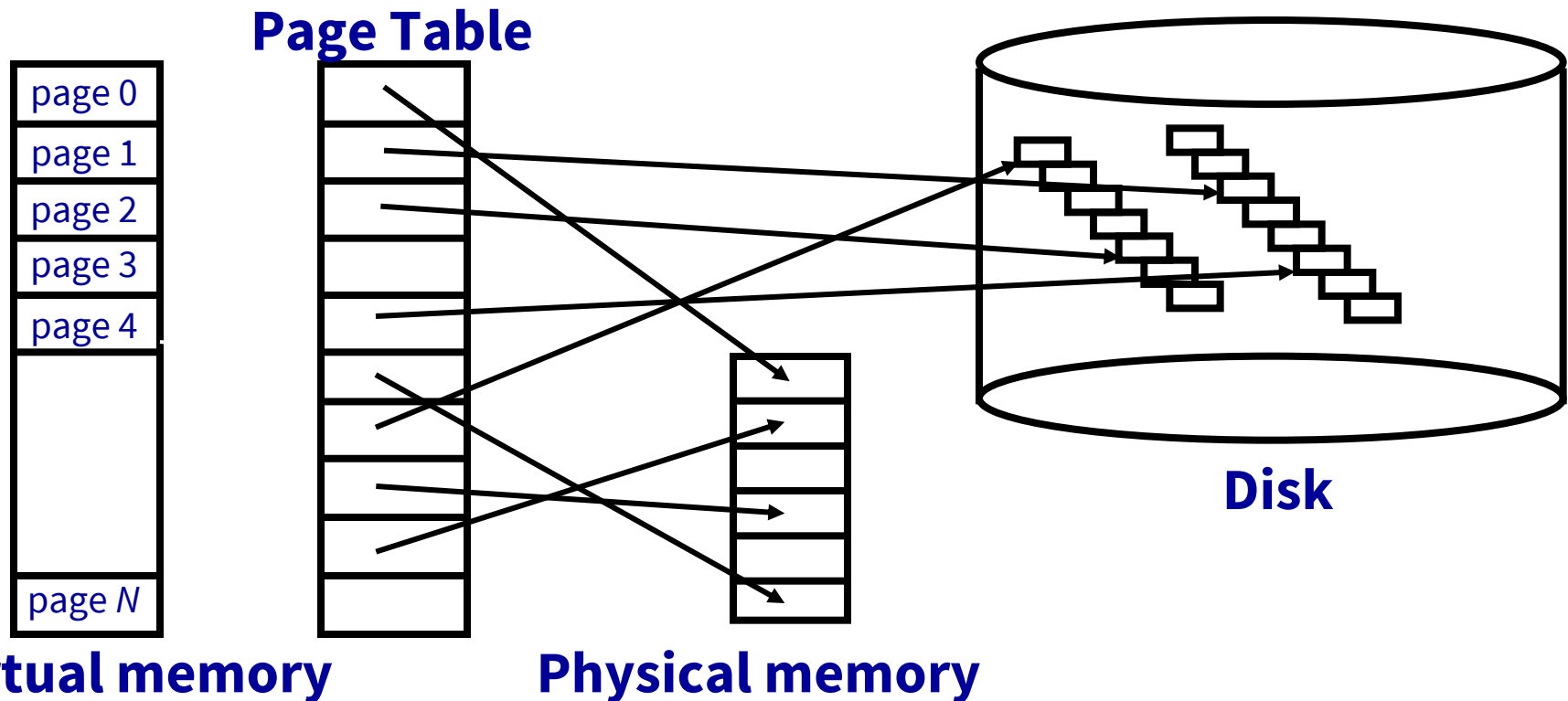
- Paged Translation
- Efficient Address Translation
  - Multi-Level Page Tables
  - Inverted Page Tables
  - TLBs

This time: **Virtual Memory & Caching**

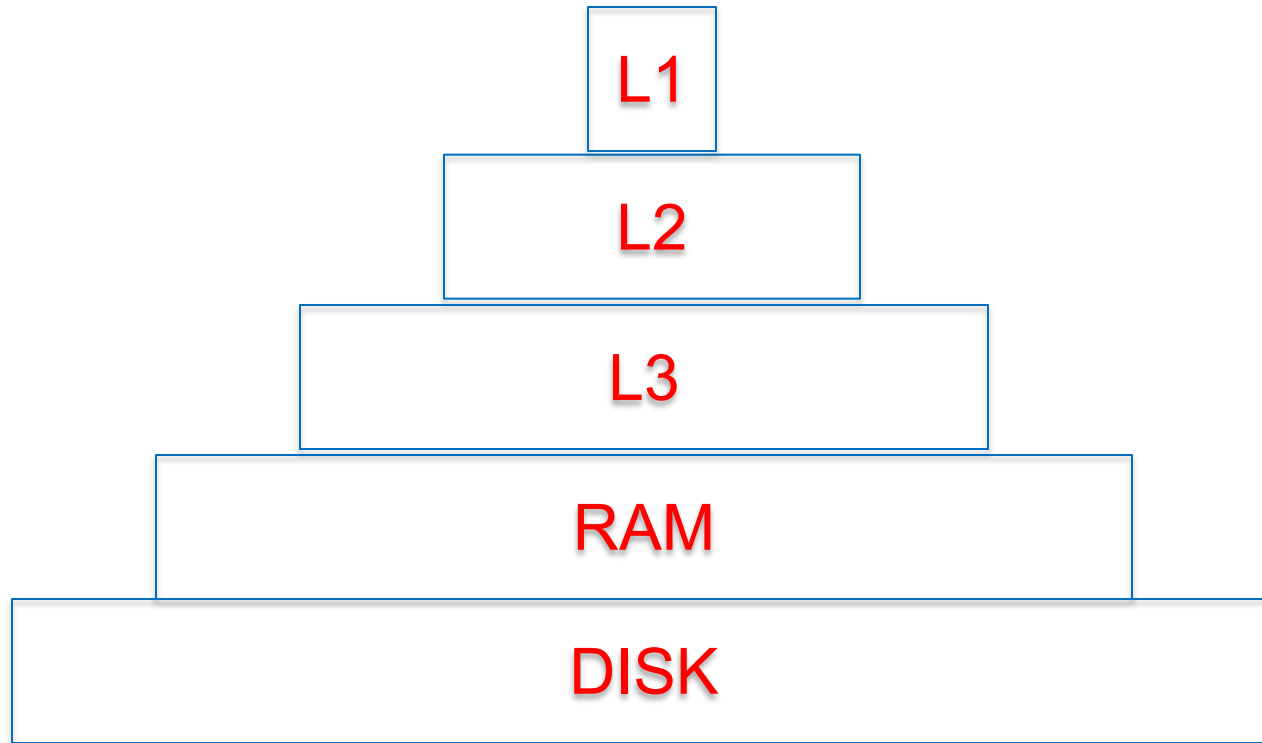
- 
- An abstract graphic on the left side of the slide. It features a dense, orange background with a complex network of thin, red lines crisscrossing it. Overlaid on this are several thick, diagonal blue lines. Scattered throughout the orange area are numerous small, white, oval-shaped dots, some of which are aligned along the blue lines.
- **Virtual Memory**
  - Caching

# What is Virtual Memory?

- Each process has illusion of large address space
  - $2^x$  bytes for x-bit addressing
- However, physical memory is usually much smaller
- How do we give this illusion to multiple processes?
  - Virtual Memory: some addresses reside in disk



# Process executes from disk!



RAM is really just another layer of cache

# Swapping vs. Paging

## Swapping

- Loads entire process in memory
- “Swap in” (from disk) or “Swap out” (to disk) a process
- Slow (for large processes)
- Wasteful (might not require everything)
- Does not support sharing of code segments
- Virtual memory limited by size of physical memory

## Paging

- Runs all processes concurrently
- A few pages from each process live in memory
- Finer granularity, higher performance
- Large virtual mem supported by small physical mem
- Certain pages (read-only ones, for example) can be shared among processes

# (the contents of) **A Virtual Page Can Be**

## ***Mapped***

- to a physical frame

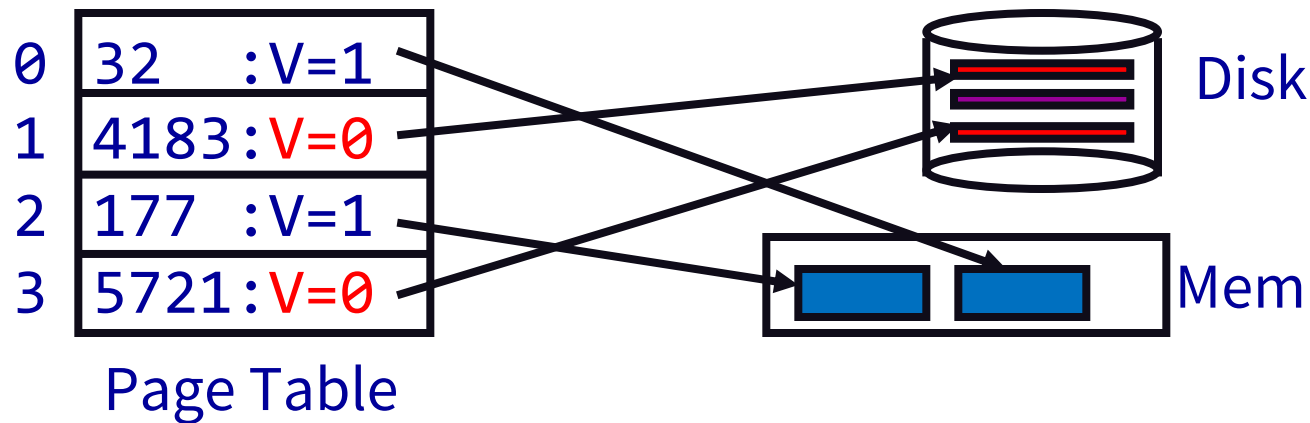
## ***Not Mapped (→ Page Fault)***

- in a physical frame, but not currently mapped
- or still in the original program file
- or zero-filled (heap/BSS, stack)
- or on backing store (“paged or swapped out”)
- or illegal: not part of a segment  
→ Segmentation Fault

# Supporting Virtual Memory

Modify Page Tables with a valid bit (= “present bit”)

- Page in memory  $\rightarrow$  *valid* = 1
- Page not in memory  $\rightarrow$  PT lookup triggers **page fault**





# Handling a Page Fault

Identify page and reason (r/w/x)

- access inconsistent w/ segment access rights
  - terminate process
- access a page that is kept on disk:
  - does frame with the code/data already exist?  
No? Allocate a frame & bring page in (next slide)
- access of zero-initialized data (BSS) or stack
  - Allocate a frame, fill page with zero bytes
- access of COW page
  - Allocate a frame and copy

# When a page needs to be brought in...

- Find a free frame
  - evict one if there are no free frames
- Issue disk request to fetch data for page
- Block current process
- Context switch to new process
- When disk completes, update PTE
  - frame number, valid bit, RWX bits
- Put current process in ready queue

# When a page is swapped out...


- Find all page table entries that refer to old page
  - Frame might be shared
  - Core Map (frames → pages)
- Set each page table entry to invalid
- Remove any TLB entries
  - “TLB Shutdown”
- Write changes on page back to disk, if needed
  - Dirty/Modified bit in PTE indicates need
  - Text segments are (still) on program image on disk

# Demand Paging, MIPS style

1. TLB miss
2. Trap to kernel
3. Page table walk
4. Find page is invalid
5. Convert virtual address to disk block number
6. Allocate frame
  - evict if needed
7. Initiate disk block read into frame
8. Disk interrupt when DMA complete
9. Mark page valid
10. Update TLB
11. Resume process at faulting instruction
12. Execute instruction

Software handling page fault between arrows

# Demand Paging, x86 style

1. TLB miss
2. Page table walk
3. Page fault (find page is invalid)
-  4. Trap to kernel
5. Convert virtual address to disk block number
6. Allocate frame
  - evict if needed
7. Initiate disk block read into frame
8. Disk interrupt when DMA complete
9. Mark page valid
10. Resume process at faulting instruction
11. TLB miss
12. Page table walk to fetch translation
13. Execute instruction

# Updated Context Switch

- Save current process' registers in PCB
  - Also Page Table Base Register (PTBR)
- ***Flush TLB*** (*unless TLB is tagged*)
- Restore registers and PTBR of next process to run
- “Return from Interrupt”

# OS Support for Paging

## Process Creation

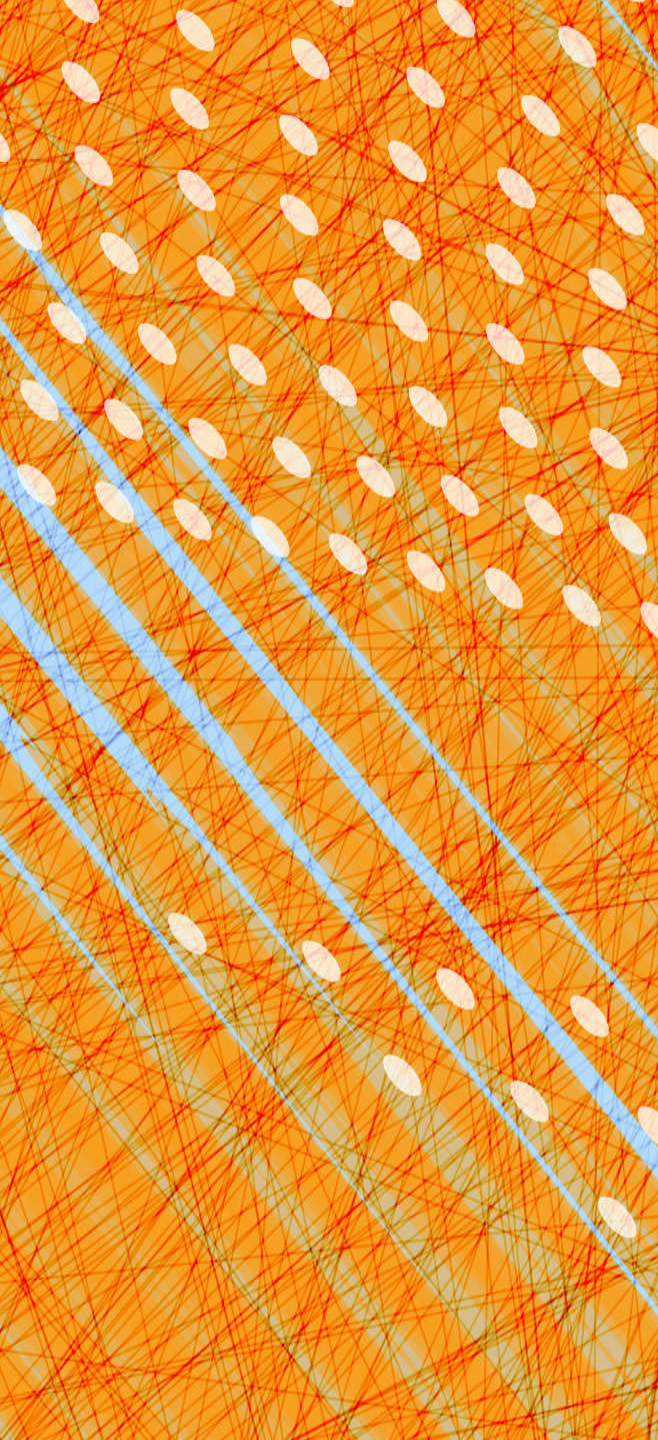
- Allocate frames, create & initialize page table & PCB

## Process Execution

- Reset MMU (PTBR) for new process
- Context switch: flush TLB (or TLB has pids)
- Handle page faults

## Process Termination

- Release pages



- Virtual Memory
- **Caching**



# What are some examples of caching?

- TLBs
- hardware caches
- internet naming
- web content
- incremental compilation
- just in time translation
- virtual memory
- file systems
- branch prediction



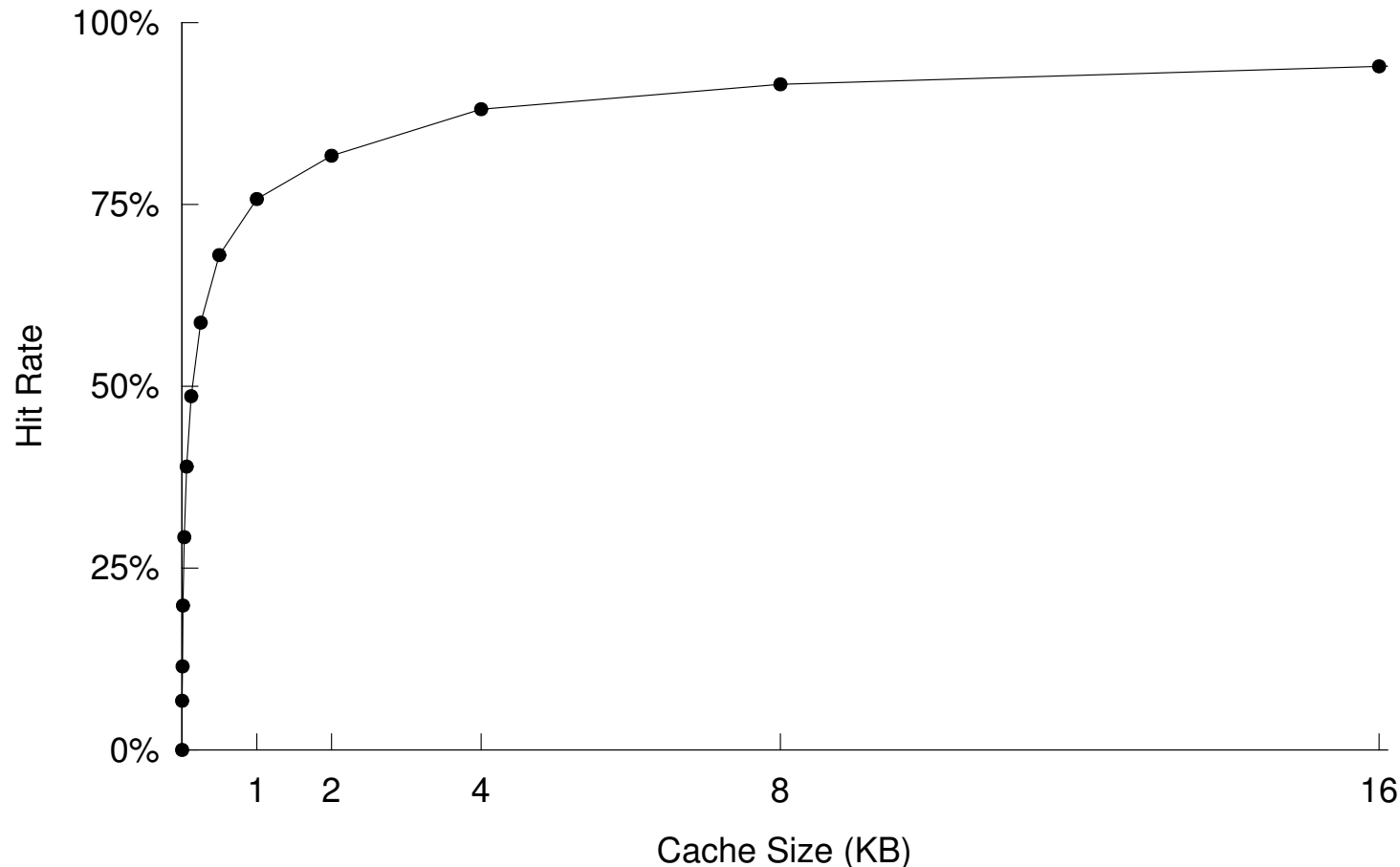
# Memory Hierarchy

Cache	Hit Cost	Size
1st level cache / 1st level TLB	1 ns	64 KB
2nd level cache / 2nd level TLB	4 ns	256 KB
3rd level cache	12 ns	2 MB
Memory (DRAM)	100 ns	10 GB
Data center memory (DRAM)	100 $\mu$ s	100 TB
Local non-volatile memory	100 $\mu$ s	100 GB
Local disk	10 ms	1 TB
Data center disk	10 ms	100 PB
Remote data center disk	200 ms	1 XB

Every layer is a cache for the layer below it.

# Working Set

1. Collection of a process' most recently used pages  
(The Working Set Model for Program Behavior, Denning, '68)
2. Pages referenced by process in last  $\Delta$  time-units



# Thrashing

Excessive rate of paging

Cache lines evicted before they can be reused

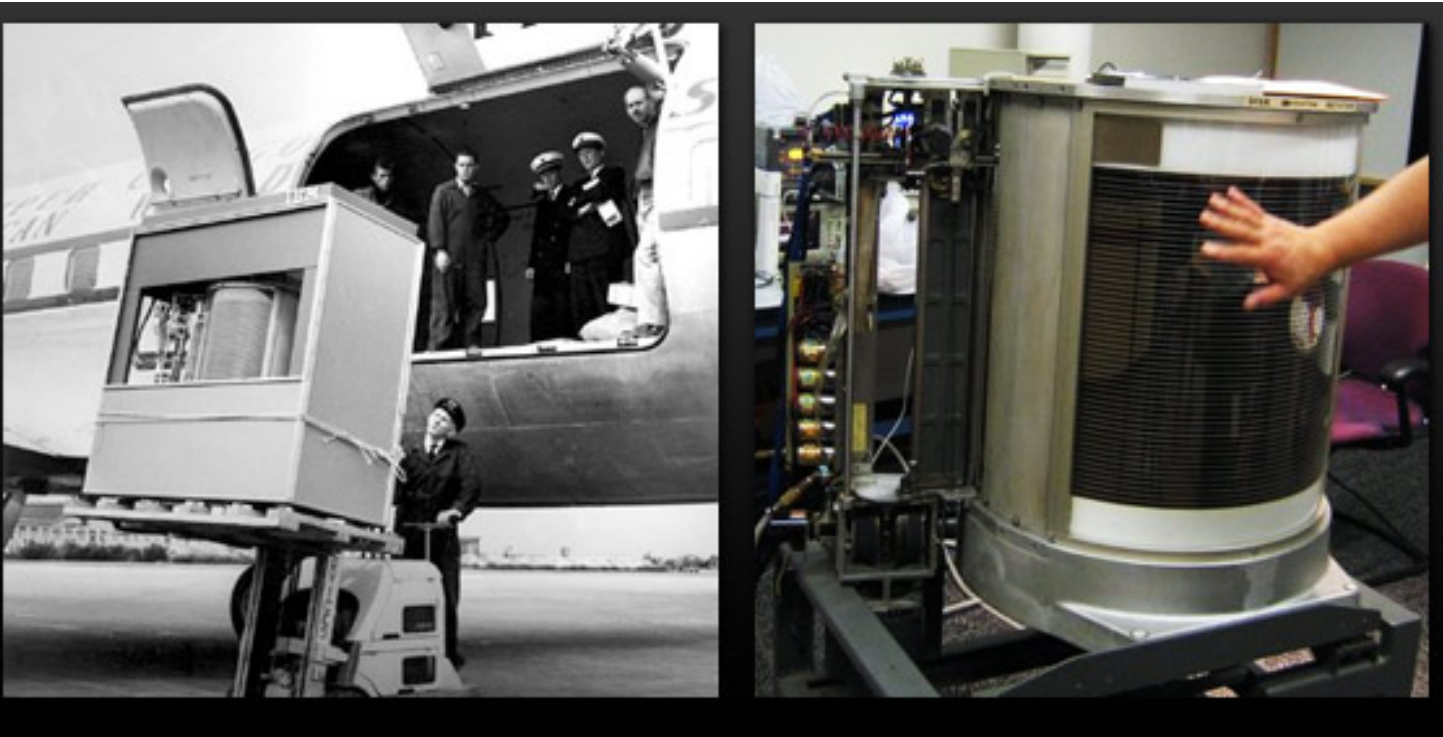
## **Causes:**

- Too many processes in the system
- Cache not big enough to fit working set
- Bad luck (conflicts)
- Bad eviction policies (later)

## **Prevention:**

- Restructure code to reduce working set
- Increase cache size
- Improve caching policies

# Why “thrashing”?



The first hard disk drive—the IBM Model 350 Disk File (came w/IBM 305 RAMAC, 1956).

Total storage = 5 million characters (just under 5 MB).

<http://royal.pingdom.com/2008/04/08/the-history-of-computer-data-storage-in-pictures/>

“Thrash” dates from the 1960’s, when disk drives were as large as washing machines. If a program’s working set did not fit in memory, the system would need to shuffle memory pages back and forth to disk. This burst of activity would violently shake the disk drive.

# Caching

- *Assignment*: where do you put the data?
- *Replacement*: who do you kick out?

# Address Translation Problem

- Adding a layer of indirection disrupts the spatial locality of caching
- CPU cache is usually physically indexed
- Adjacent pages may end up sharing the same CPU cache lines

→ **BIG PROBLEM:**

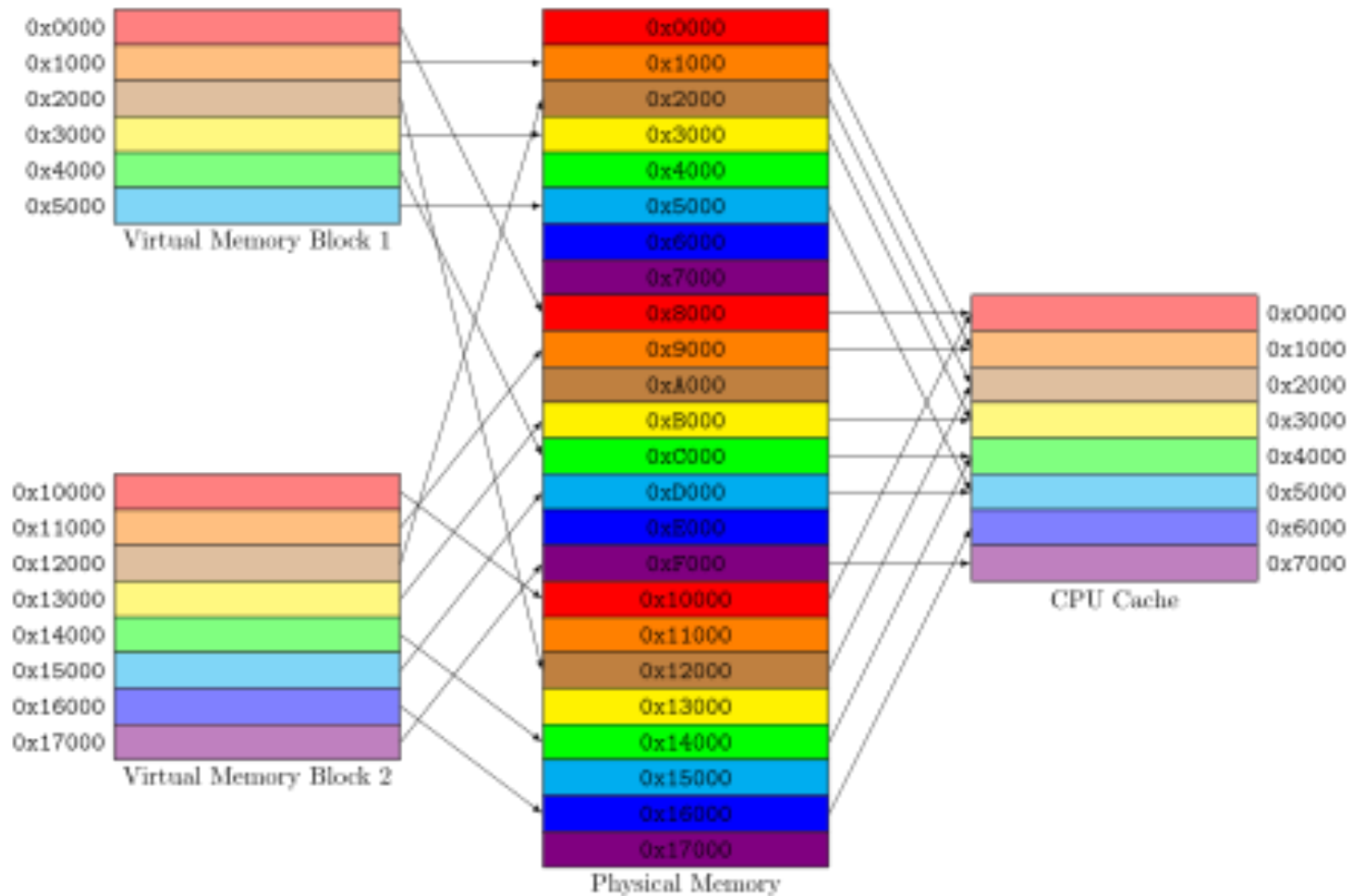
cache effectively smaller

## Solution: Cache Coloring (Page Coloring)

1. Color frames according to cache configuration.
2. Spread each process' pages across as many colors as possible.



# Cache Coloring Example



# Caching

- Assignment: where do you put the data?
- **Replacement: who do you kick out?**

**What do you do when memory is full?**

# Page Replacement Algorithms

- **Random:** Pick any page to eject at random
  - Used mainly for comparison
- **FIFO:** The page brought in earliest is evicted
  - Ignores usage
- **OPT:** Belady's algorithm
  - Select page not used for longest time
- **LRU:** Evict page that hasn't been used for the longest
  - Assumes past is a good predictor of the future
- **MRU:** Evict the most recently used page
- **LFU:** Evict least frequently used page
- And many approximation algorithms

# First-In-First-Out (FIFO) Algorithm

- *Reference string*: 1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5
- **3 frames** (3 pages in memory at a time per process):

frames      reference

			1
		1	2
	2	1	3
3	2	1	4
3	2	4	1
3	1	4	2
2	1	4	5
2	1	5	1
2	1	5	2
2	1	5	3
2	3	5	4
4	3	5	5
4	3	5	

← contents of frames at time of reference

page fault

hit

4

marks arrival time

9 page faults

# First-In-First-Out (FIFO) Algorithm

- *Reference string*: 1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5
- **4 frames** (4 pages in memory at a time per process):

frames      reference

				1
			1	2
		2	1	3
	3	2	1	4
4	3	2	1	1
4	3	2	1	2
4	3	2	1	5
4	3	2	5	1
4	3	1	5	2
4	2	1	5	3
3	2	1	5	4
3	2	3	4	5
3	2	5	4	

← contents of frames at time of reference

page fault

hit

4

marks arrival time

10 page faults

more frames → more page faults?

Belady's Anomaly

# Optimal Algorithm (OPT)

- Replace frame that will not be used for the longest
- 4 frames example

				1
			1	2
		2	1	3
	3	2	1	4
4	3	2	1	1
4	3	2	1	2
4	3	2	1	5
5	3	2	1	1
5	3	2	1	2
5	3	2	1	3
5	3	2	1	4
5	3	2	4	5
5	3	2	4	

6 page faults

Question: How do we tell the future?  
Answer: We can't

OPT used as upper-bound in measuring  
how well your algorithm performs

# OPT Approximation

In real life, we do not have access to the future page request stream of a program

→ Need to make a guess at which pages will not be used for the longest time

# Least Recently Used (LRU) Algorithm

Reference string: 1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5

				1
			1	2
		2	1	3
	3	2	1	4
4	3	2	1	1
4	3	2	1	2
4	3	2	1	5
4	5	2	1	1
4	5	2	1	2
4	5	2	1	3
3	5	2	1	4
3	4	2	1	5
3	4	2	5	

page fault

hit

4 marks most recent use

8 page faults



# Implementing LRU

- On reference: Timestamp each page
- On eviction: Scan for oldest page

Problems:

- Large page lists
- Timestamps are costly

Solution: **approximate LRU**

- Note: LRU is already an approximation
- Exploit *use* (REF) bit in PTE

# Not Recently Used

- Periodically (say, each clock tick), clear all *use* (aka REF) bits in PTEs
  - Ideally done in hardware
- When evicting a frame, scan for a frame that hasn't recently been referenced
  - *use* bit is clear in PTE
  - may require a scan of all frames, so keep track of last evicted frame
- If no such frame exists, select any

# Working Set Algorithm (WS)

- Maintain for each frame the approximate time the frame was last used
- At each clock tick
  - Update this time to the current time for all frames that were referenced since the last clock tick
    - i.e., the ones with *use* (REF) bits set
  - Clear all *use* bits
  - Put all frames that have not been used for some time  $\Delta$  (working set parameter) on the free list
- When a frame is needed, use free list
  - If empty, pick any frame

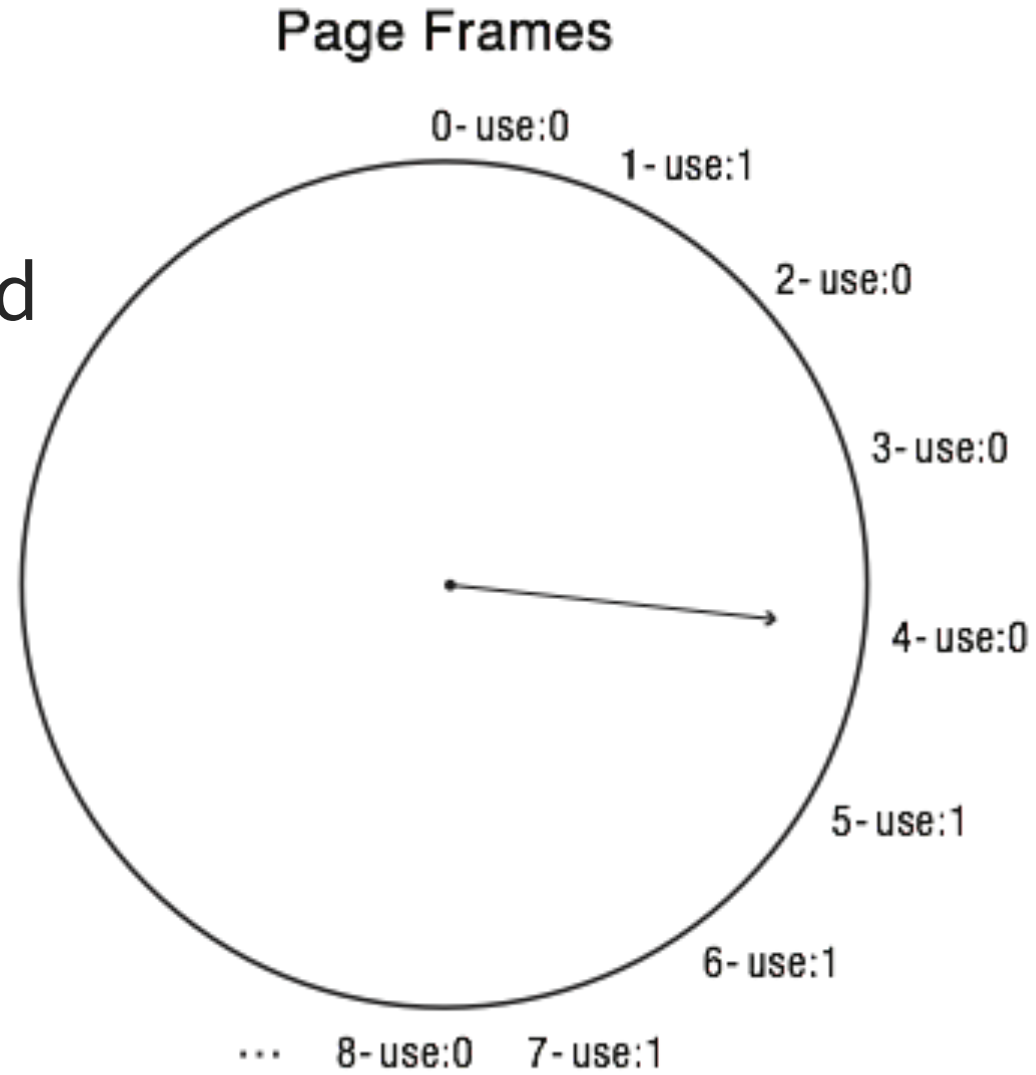
*Note: requires scan of all frames at each clock tick*

# Using virtual time or real time?

- Often, it is argued it would be more fair to use “virtual time” (the time that a process has the CPU) instead of “real time” in the WS algorithm and variants or processes that do not use the CPU much would be more likely to be paged out
- However, maybe processes that do not use the CPU also tend to use fewer pages per time unit
- And waiting processes do not age at all in virtual time, and do not use any pages

# Clock Algorithm

- To allocate a frame, inspect the *use* bit in the PTE at clock hand and advance clock hand
- Used? Clear *use* bit and repeat



# Two-Handed Clock

One-handed clock: What if memory is very large?

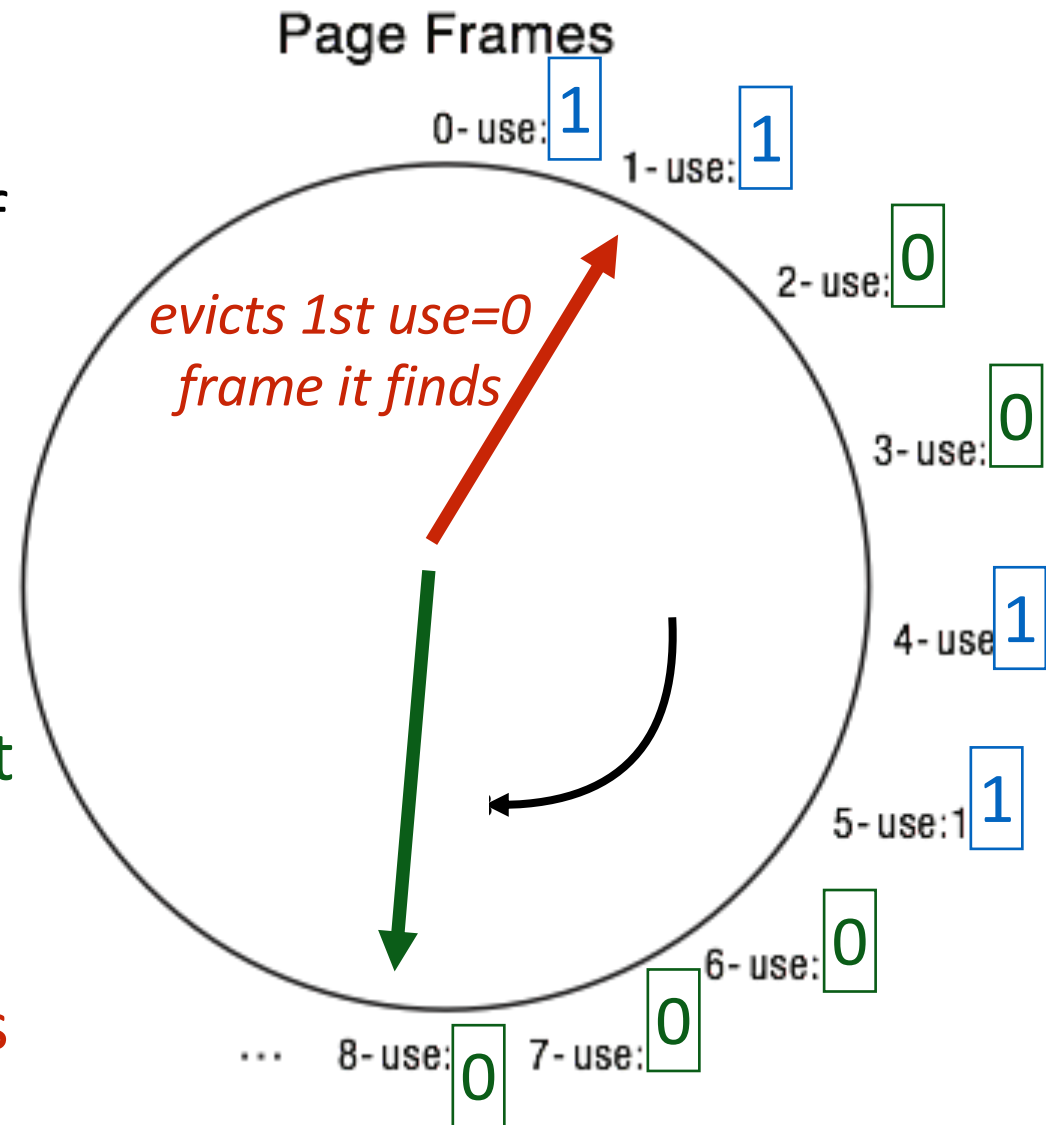
Use two hands!  
(at fixed angle)

Leading hand clears *use* bit

- slowly clears history
- finds victim candidates

Trailing hand evicts frames  
with *use* bit set to 0

Big angle? Small angle?



blue 1's were referenced after use bit  
was cleared by green hand

# WSCLOCK

- Merge WS and CLOCK algorithms
- Maintain *timestamp* for each frame
- When allocating a frame:
  - Inspect *use* bit of frame under hand
  - If set
    - Clear the *use* bit
    - Update the timestamp
    - Continue with next frame
  - If clear but  $now - timestamp < \Delta$ 
    - Continue with next frame (do not update timestamp)
  - Otherwise evict frame

*Note: can go into an infinite loop...*

# Stack Algorithms

- Let  $M(m, r)$  be the set the of virtual pages in physical memory given that there are  $m$  frames at reference string  $r$
- A page replacement algorithm is called a “stack algorithm” if for all #frames  $m$  and all reference strings  $r$ :

$M(m, r)$  is a subset of  $M(m + 1, r)$

i.e., a stack algorithm does *not* suffer from Belady’s anomaly:

more frames  $\rightarrow$  not more misses



# FIFO algorithm, $m = 3$ vs $m = 4$

			1					1
		1	2				1	2
	2	1	3				2	3
3	2	1	4				3	4
3	2	4	1				4	1
3	1	4	2				1	2
2	1	4	5				2	5
2	1	5	1				4	3
2	1	5	2				4	3
2	1	5	3				4	3
2	3	5	4				4	3
4	3	5	5				4	3
4	3	5					4	3

				1				1
			1	2				2
		2	1	3				3
	3	2	1	4				4
4	3	2	1	1				1
4	3	2	1	2				2
4	3	2	1	5				5
4	3	2	5	1				4
4	3	1	5	2				3
4	2	1	5	3				4
3	2	1	5	4				5
3	2	3	4	5				
3	2	5	4					

Stack algorithm  
“subset property”  
violated

# Theorem: LRU and MRU are stack algorithms

- By definition:
  - For LRU:  $M(m + 1, r)$  contains the  $m$  most frequently used frames, so  $M(m, r)$  is a subset of  $M(m + 1, r)$
  - Similar for MRU
  - Similar also for LFU (Least Frequently Used)

# Theorem: OPT is a stack algorithm

- Proof non-trivial. See paper that introduced the concept of stack algorithms:
  - R. L. Mattson, J. Gecsei, D. R. Slutz and I. L. Traiger, "Evaluation techniques for storage hierarchies," in IBM Systems Journal, vol. 9, no. 2, pp. 78-117, 1970.

# Local versus Global Replacement

- So far we have tacitly assumed that all frames are shared by all processes
  - This is called “global replacement”
- But is it fair?
  - Badly behaved processes can ruin the experience of processes with good locality
- Local replacement: divided the frames up evenly between the processes
  - Can lead to under-utilization