

Introduction

- ❖ As for any index, 3 alternatives for data entries **k***:
 - 9 Data record with key value \mathbf{k}

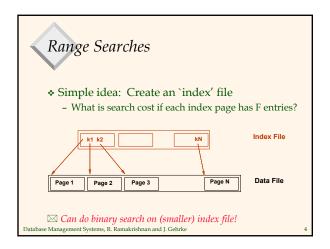
 - (1) <k, list of rids of data records with search key k>
- Choice is orthogonal to the *indexing technique* used to locate data entries k*.
- * Tree-structured indexing techniques support both *range searches* and *equality searches*.
- * <u>ISAM</u>: static structure; <u>B+ tree</u>: dynamic, adjusts gracefully under inserts and deletes.

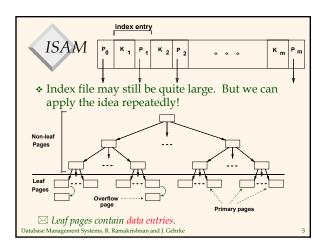
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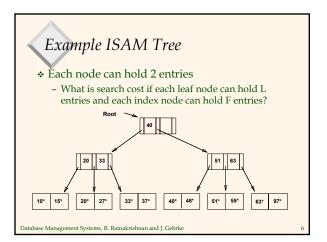
Range Searches

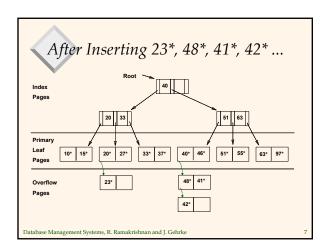
- ❖ ``Find all students with gpa > 3.0''
 - If data *entries* are sorted, do binary search to find first such student, then scan to find others.
- * Problem?

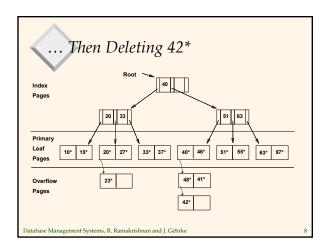
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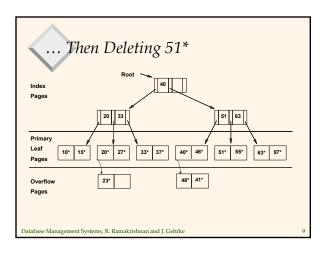


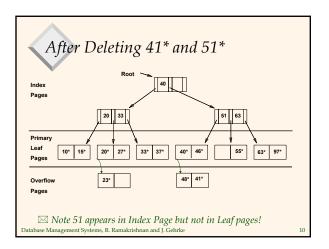






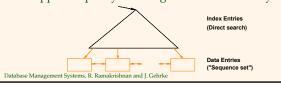






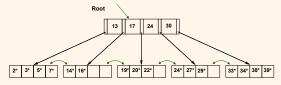
B+ Tree: The Most Widely Used Index

- Insert/delete at log F N cost; keep tree heightbalanced. (F = fanout, N = # leaf pages)
- Minimum 50% occupancy (except for root). Each node contains d <= m <= 2d entries. The parameter d is called the *order* of the tree.
- * Supports equality and range-searches efficiently.



Example B+ Tree

- Search begins at root, and key comparisons direct it to a leaf (as in ISAM).
- ❖ Search for 5*, 15*, all data entries >= 24* ...



☑ Based on the search for 15*, we know it is not in the tree!

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B+-tree Search Performance

- ❖ Assume leaf pages can hold L data entries
- * Assume B+-tree has order d
- ❖ Assume the tree has to index N data entries
- * What is the best-case search performance (measured in number of I/Os)?
- ❖ What is the worst-case search performance

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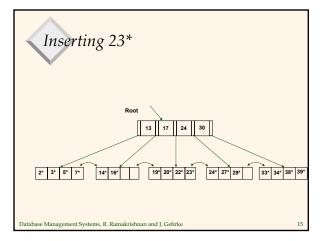
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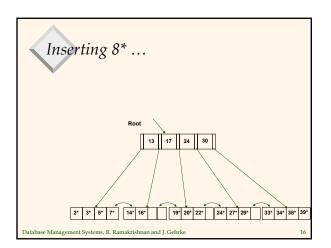
B+ Trees in Practice

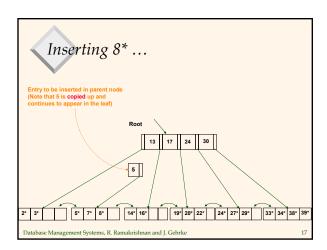
- * Typical order: 100. Typical fill-factor: 67%.
 - average fanout = 133
- * Typical capacities:
 - Height 4: 133⁴ = 312,900,700 records
 - Height 3: 133^3 = 2,352,637 records
- Can often hold top levels in buffer pool:
 - Level 1 = 1 page = 8 Kbytes
 - Level 2 = 133 pages = 1 Mbyte
 - Level 3 = 17,689 pages = 133 MBytes

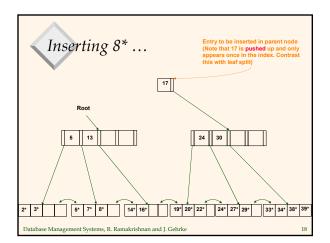
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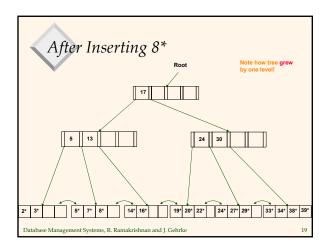
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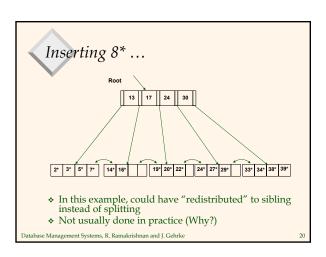


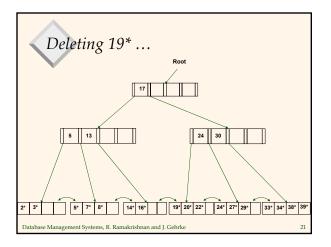


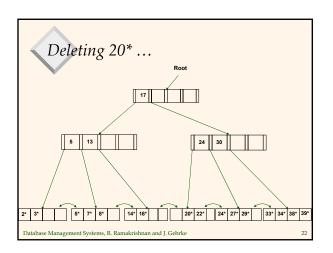


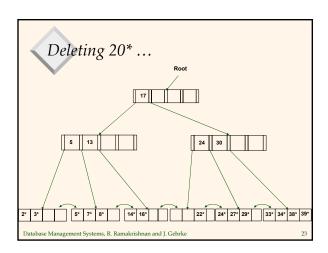


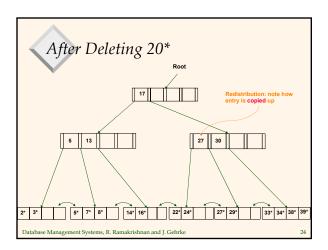


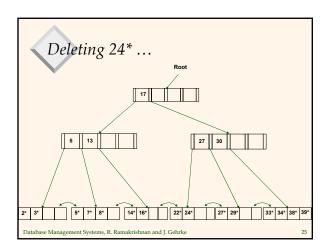


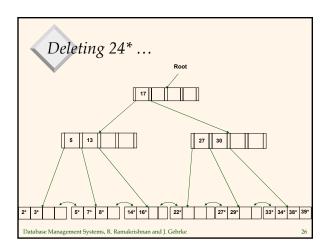


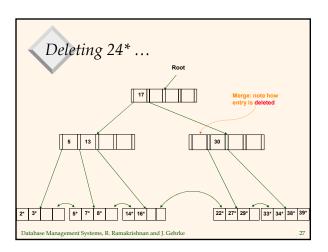


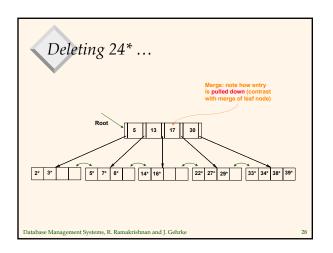




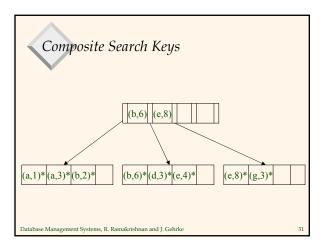








Example of Non-leaf Re-distribution During deletion of 24* In contrast to previous example, can re-distribute entry from left child of root to right child. Root 2 3 5 13 17 20 30 30 30 33 34 38 39 Database Management Systems, R. Ramakrishnan and J. Gehrke 29



Composite Search Keys

- * B+-tree index on (Age, Salary)
- * Which can you answer efficiently using a B+-tree?
 - Age = 20
 - Age > 20
 - Age = 20, Salary = 100000
 - Age > 20, Salary = 100000
 - Age = 20, Salary > 100000
 - Age > 20, Salary > 100000
- * Assume B+-tree index on (Age, Salary, Bonus); which can you answer efficiently?
 - Age = 20, Salary = 100000, Bonus > 5000
 - Age = 20, Salary > 100000, Bonus > 5000

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Prefix Key Compression

- Important to increase fan-out (Why?)
- Key values in index entries only `direct traffic'; can often compress them
 - E.g., adjacent index entries with search key values Dannon Yogurt, David Smith and Devarakonda Murthy
 - We can abbreviate *David Smith* to *Dav*. (The other keys can be compressed too ...)
- Is this correct?
 - Not quite! What if there is a data entry Davey Jones?
 - Compressed key should be greater than every entry in left sub-tree
 - Insert/delete modified appropriately

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A Note on 'Order'

- * Order (d) concept replaced by physical space criterion in practice (`at least half-full').
 - Index pages can typically hold many more entries than leaf pages.
 - Variable sized records and search keys mean different nodes will contain different numbers of entries.
 - Even with fixed length fields, multiple records with the same search key value (*duplicates*) can lead to variable-sized data entries (if we use Alternative (3)).

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Bulk Loading of a B+ Tree

- If we have a large collection of records, and we want to create a B+ tree on some field, doing so by repeatedly inserting records is very slow.
- * Bulk Loading can be done much more efficiently.
- Initialization: Sort all data entries, insert pointer to first (leaf) page in a new (root) page.



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Bulk Loading (Contd.) Index entries for leaf Data entry pages pages always entered into rightmost index page just above leaf level. When this fills up, it splits. (Split may go up right-most path to the root.) Data entry pages not yet in B+ tree Much faster than repeated inserts, especially when one considers locking! Database Management Systems, R. Ratinak visibnar and J. Centre 22 23 31 35 36

Summary of Bulk Loading

- * Option 1: multiple inserts.
 - Slow.
 - Does not give sequential storage of leaves.
- * Option 2: Bulk Loading
 - Has advantages for concurrency control.
 - Fewer I/Os during build.
 - Leaves will be stored sequentially (and linked, of course).
 - Can control "fill factor" on pages.

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