

# **CS 4120**

## **Introduction to Compilers**

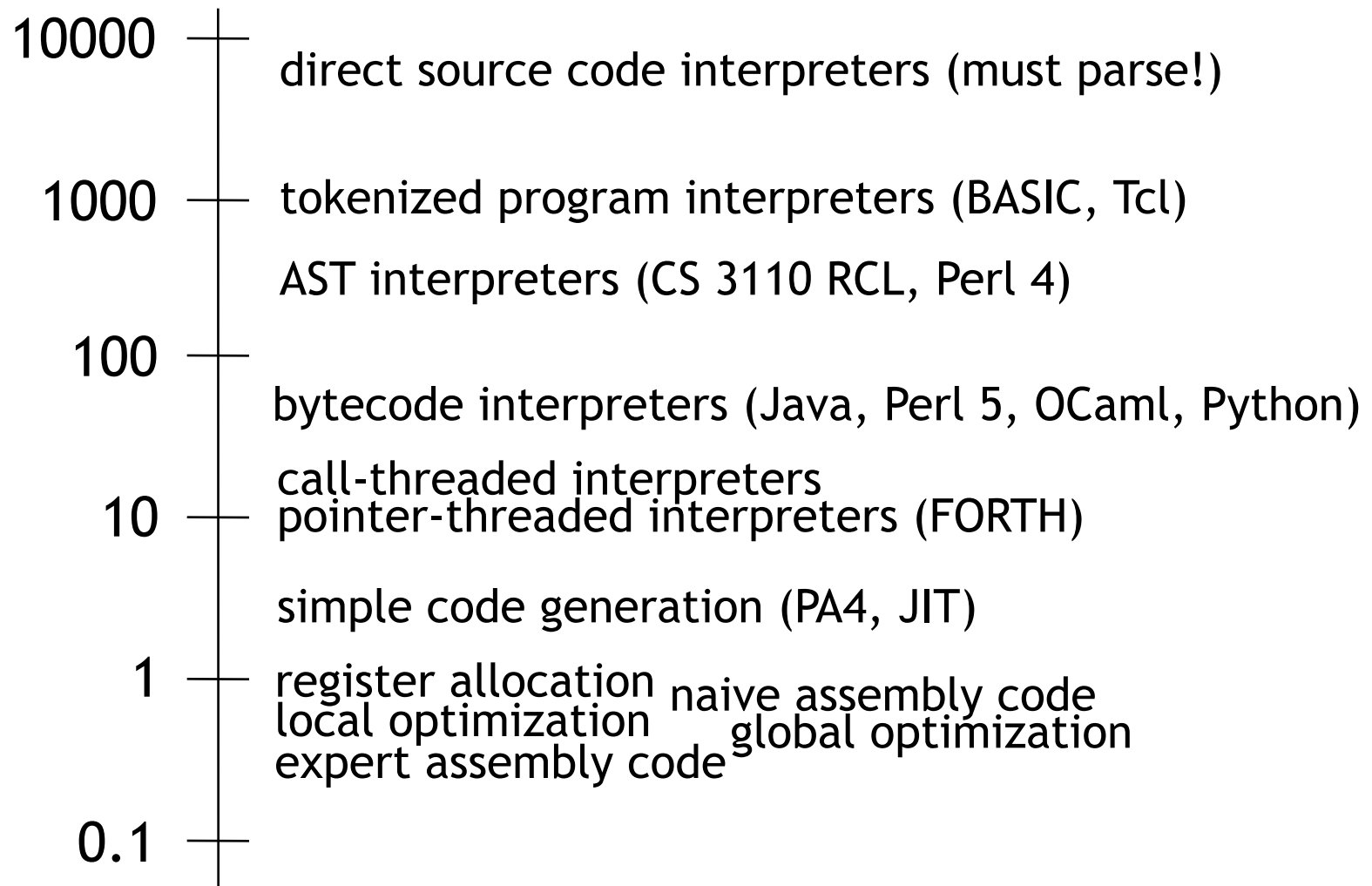
Andrew Myers  
Cornell University

Lecture 18: Introduction to Optimization  
9 March 16

# Optimization

- Next topic: how to generate better code through **optimization**.
- This course covers the most valuable and straightforward optimizations – much more to learn!
  - Other sources:
    - Muchnick has 10 chapters of optimization techniques
    - Cooper and Torczon also cover optimization

# How fast can you go?



# Goal of optimization

- Help programmers
  - clean, modular, high-level source code
  - but compile to assembly-code performance
- Optimizations are code transformations
  - can't change meaning of program to behavior not allowed by source.
- Different kinds of optimization:
  - space optimization: reduce memory use
  - time optimization: reduce execution time
  - power optimization: reduce power usage

# Why do we need optimization?

- Programmers may write suboptimal code to make it clearer.
- High-level language may make it inconvenient or impossible to avoid redundant computation

$$a[i][j] = a[i][j] + 1$$

- Architectural independence.
- Modern architectures assume optimization—hard to optimize by hand.

# Where to optimize?

- Usual goal: improve time performance
- But: many optimizations trade off space vs time.
- Example: loop unrolling replaces a loop body with N copies.
  - Increasing code space slows program down a little, speeds up one loop
  - Frequently executed code with long loops: space/time tradeoff is generally a win
  - Infrequently executed code: optimize code space at expense of time, saving instruction cache space
  - Complex optimizations may never pay off!
- Focus of optimization: program **hot spots**

# Safety

- Possible opportunity for **loop-invariant code motion**:

```
while (b) {  
    z = y/x; // x, y not assigned in loop  
    ...  
}
```

- Transformation: invariant code out of loop:

```
z = y/x;  
while (b) {  
    ...  
}
```

Preserves meaning?  
Faster?

Three aspects of an optimization:

1. the code transformation
2. safety of transformation
3. performance improvement

# Writing fast programs in practice

1. Pick the right algorithms and data structures: design for locality and few operations
2. Turn on optimization and **profile** to figure out program hot spots.
3. Evaluate whether design works; if so...
4. Tweak source code until optimizer does “the right thing” to machine code
  - understanding optimizers helps!



# Structure of an optimization

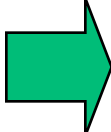
- Optimization is a code transformation
- Applied at some stage of compiler (HIR, MIR, LIR)
- In general requires some analysis:
  - safety analysis to determine where transformation does not change meaning (e.g. live variable analysis)
  - cost analysis to determine where it ought to speed up code (e.g., which variable to spill)

# When to apply optimization

HIR	AST	Inlining Specialization
	IR	Constant folding Constant propagation Value numbering
MIR	Canonical IR	Dead code elimination Loop-invariant code motion Common sub-expression elimination Strength reduction
	Abstract Assembly	Constant folding & propagation Branch prediction/optimization Register allocation
LIR	Assembly	Loop unrolling Cache optimization Peephole optimizations

# Register allocation

- Goal: convert abstract assembly (infinite no. of registers) into real assembly (6 registers)

<code>mov t1, t2</code>		<code>mov rax, rbx</code>
<code>add t1, -8(rbp)</code>		<code>add rax, -8(rbp)</code>
<code>mov t3, -16(rbp)</code>		<code>mov rbx, -16(rbp)</code>
<code>mov t4, t3</code>		
<code>cmp t1, t4</code>		<code>cmp rax, rbx</code>

Try to reuse registers aggressively (e.g., **rbx**)

- Coalesce registers (t3, t4) to eliminate **mov**'s
- May be impossible without **spilling** some temporaries to stack

# Constant folding

- Idea: if operands are known at compile time, evaluate at compile time when possible.

`int x = (2 + 3)*4*y;`     $\Rightarrow$     `int x = 5*4*y;`  
 $\Rightarrow$     `int x = 20*y;`

- Easy and useful at every stage of compilation
  - Constant expressions are created by translation and by optimization

`a[2]`  $\Rightarrow$  `MEM(MEM(a) + 2*4)`  
 $\Rightarrow$  `MEM(MEM(a) + 8)`

# Constant folding conditionals

$\text{if (true) } S \Rightarrow S$

$\text{if (false) } S \Rightarrow \{\}$

$\text{if (true) } S \text{ else } S' \Rightarrow S$

$\text{if (false) } S \text{ else } S' \Rightarrow S'$

$\text{while (false) } S \Rightarrow \{\}$

$\text{if (2 > 3) } S \Rightarrow \text{if (false) } S \Rightarrow \{\}$

# Algebraic simplification

- More general form of constant folding: take advantage of simplification rules

$$a * 1 \Rightarrow a$$

$$a * 0 \Rightarrow 0$$

$$a + 0 \Rightarrow a$$

**identities**

$$b \mid \text{false} \Rightarrow b$$

$$b \& \text{true} \Rightarrow b$$

$$(a + 1) + 2 \Rightarrow a + (1 + 2) \Rightarrow a + 3$$

**reassociation**

$$a * 4 \Rightarrow a \text{ shl } 2$$

$$a * 7 \Rightarrow (a \text{ shl } 3) - a$$

**strength reduction**

$$a / 32767 \Rightarrow a \text{ shr } 15 + a \text{ shr } 30 + a \text{ shr } 45 + a \text{ shr } 60$$

- Must be careful with floating point and with overflow - algebraic identities may give wrong or less precise answers.
  - E.g.,  $(a+b)+c \neq a+(b+c)$  in floating point if  $a, b$  small.

# Unreachable code elimination

- Basic blocks not contained by any trace leading from starting basic block are **unreachable** and can be eliminated
- Performed at canonical IR or assembly code levels
- Reductions in code size improve cache, TLB performance.

# Inlining

- Replace a function call with the body of the function:

```
f(a: int):int = { b:int=1;    n:int = 0
                while (n<a) {b = 2*b; return b }}
g(x: int):int  = { return 1 + f(x) }
⇒ g(x:int):int = { fx:int { a:int = x
                        { b:int=1; n:int=0;
                          while (n<a) { b = 2*b; fx=b }}
                        return 1 + fx; }
```

- Best done on HIR
- Can inline methods, but more difficult – there can be only one f.
- May need to rename variables to avoid **name capture**—what if f refers to a global variable x?



# Specialization

- Idea: create specialized versions of functions (or methods) that are called from different places w/ different args

```
class A implements I { m( ) {...} }  
class B implements I { m( ) {...} }  
f(x: I) { x.m( ); } // don't know which m  
a = new A(); f(a) // know A.m  
b = new B(); f(b) // know B.m
```

- Can inline methods when implementation is known
- Impl. known e.g. if only one implementing class
- Can specialize inherited methods (e.g., HotSpot JIT)

# Constant propagation

- If value of variable is known to be a constant, replace use of variable with constant
- Value of variable must be propagated forward from point of assignment

```
int x = 5;
```

```
int y = x*2;
```


```
int z = a[y]; // = MEM(MEM(a) + y*8)
```

- Interleave with constant folding!

# Dead code elimination

- If side effect of a statement can never be observed, can eliminate the statement


```
x = y*y;           // dead!  
...               // x unused    ...  
x = z*z;
```



```
x = z*z;
```

- **Dead variable:** if never read after defn. (exc to update other dead vars)

```
int i;  
while (m<n) { m++; i = i+1}
```



```
while (m<n) {m++}
```

- Other optimizations create dead statements, variables

# Copy propagation

- Given assignment  $X = y$ , replace subsequent uses of  $x$  with  $y$
- May make  $x$  a dead variable, result in dead code
- Need to determine where copies of  $y$  (definitely) propagate to

$x = y$

if ( $x > 1$ )

$x = x * f(x - 1)$



~~$x = y$~~

if ( $y > 1$ ) {

$x = y * f(y - 1)$

# Redundancy Elimination

- Common Subexpression Elimination (CSE) combines redundant computations

$$a[i] = a[i] + 1$$

$$\Rightarrow [[a]+i*8] = [[a]+i*8] + 1$$

$$\Rightarrow t1 = [a] + i*8; [t1] = [t1]+1$$

- Need to determine that expression always has same value in both places

$$b[j]=a[i]+1; c[k]=a[i] \Rightarrow t1=a[i]; b[j]=t1+1; c[k]=t1 \quad ?$$

# Loops

- Program *hot spots* are usually loops (exceptions: OS kernels, compilers)
- Most execution time in most programs is spent in loops: 90/10 is typical.
- Loop optimizations: important, effective, and numerous

# Loop-invariant code motion

- A form of redundancy elimination
- If result of a statement or expression does not change during loop, *and* it has no externally-visible side effect (!), can **hoist** before loop

```
for (i = 0; i < a.length; i++) {  
    // a not assigned in loop  
}  
  
t1 = a.length;  
for (i = 0; i < t1; i++) {  
    ...  
}
```

*hoisted loop-invariant expression*

# Loop-invariant code motion

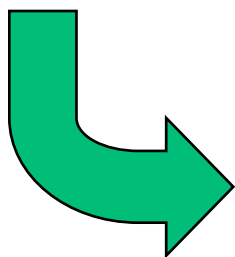
- Often useful for array element addressing computations – invariant code not visible at source level
- Requires analysis to identify loop-invariant expressions



# Strength reduction

- Replace expensive operations (\*,/) by cheap ones (+, -) via **dependent induction variable**

```
for (int i = 0; i < n; i++) {  
    a[i*3] = 1;  
}
```



```
int j = 0;  
for (int i = 0; i < n; i++) {  
    a[ j ] = 1; j = j+3;  
}
```

# Loop unrolling

- Branches are expensive; **unroll** loop to avoid them:

```
for (i = 0; i < n; i++) { S }
```



```
for (i = 0; i < n-3; i+=4) {S; S; S; S;}
```

```
for (      ; i < n; i++) { S }
```

- Eliminate  $\frac{3}{4}$  of conditional branches!
- Space-time tradeoff: not a good idea for large  $S$  or small  $n$ .

# Summary

- Many useful optimizations that can transform code to make it faster/smaller/...
- Whole is greater than sum of parts: optimizations should be applied together, sometimes more than once, at different levels.
- Problem: when are optimizations are safe and when are they effective?

⇒ **Dataflow analysis**

⇒ **Control flow analysis**

⇒ **Pointer analysis**