

## CS 4120 Introduction to Compilers

Andrew Myers  
Cornell University

Lecture 21: Live Variable Analysis  
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## Problem

- Abstract assembly contains arbitrarily many registers  $t_i$
- Want to replace all such nodes with register nodes for  $e[a-d]x$ ,  $e[sd]i$ ,  $(ebp)$
- Local variables allocated to TEMP's too
- Only 6-7 usable registers: need to allocate multiple  $t_i$  to each register
- For each statement, need to know which variables are *live* to reuse registers

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## Using scope

- Observation: temporaries, variables have bounded scope in program
- Simple idea: use information about program scope to decide which variables are live
- Problem: overestimates liveness

```
{ int b = a + 2; ← b is live
  int c = b*b; ← c is live, b is not
  int d = c + 1; ← what is live here?
  return d; }
```

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## Live variable analysis

- Goal: for each statement, identify which temporaries are live
- Analysis will be *conservative* (may overestimate liveness, will never underestimate)

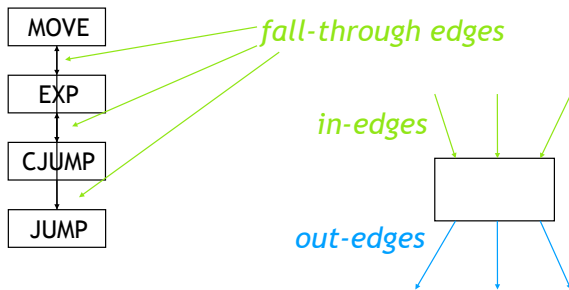
But more *precise* than simple scope analysis  
(will estimate fewer live temporaries)

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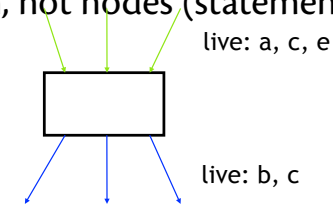
## Control Flow Graph

- Canonical IR forms *control flow graph (CFG)*: statements are nodes; jumps, fall-throughs are edges



## Liveness

- Liveness is associated with *edges* of control flow graph, not nodes (statements)



- Same register can be used for different temporaries manipulated by one stmt

## Example

$a = b + 1$



MOVE(TEMP(ta), TEMP(tb) + 1)



mov ta, tb

add ta, 1

Live: tb  
mov ta, tb  
add ta, 1  
Live: ta (maybe)

Register allocation: ta  $\Rightarrow$  eax, tb  $\Rightarrow$  eax

~~mov eax, eax~~  
add eax, 1

## Use/Def

- Every statement *uses* some set of variables (reads from them) and *defines* some set of variables (writes to them)
- For statement  $s$  define:
  - $use[s]$ : set of variables used by  $s$
  - $def[s]$ : set of variables defined by  $s$
- Example:

$a = b + c$

$use = b, c$      $def = a$

$a = a + 1$

$use = a$      $def = a$

## Liveness

Variable  $v$  is *live* on edge  $e$  if:

There is

- a node  $n$  in the CFG that uses it *and*
- a directed path from  $e$  to  $n$  passing through no *def*

How to compute efficiently?

How to use?

## Simple algorithm: Backtracing

“variable  $v$  is *live* on edge  $e$  if there is a node  $n$  in CFG that uses it *and* a directed path from  $e$  to  $n$  passing through no *def*”

(*Slow*) algorithm: Try all paths from each *use* of a variable, tracing *backward* in the control flow graph until a *def* node or previously visited node is reached. Mark variable live on each edge traversed.

## Dataflow Analysis

- *Idea*: compute liveness for all variables simultaneously
- Approach: define *equations* that must be satisfied by any liveness determination
- Solve equations by iteratively converging on solution
- Instance of general technique for computing program properties: *dataflow analysis*

## Dataflow values

$use[n]$  : set of variables used by  $n$

$def[n]$  : set of variables defined by  $n$

$in[n]$  : variables live on entry to  $n$

$out[n]$  : variables live on exit from  $n$

Clearly:  $in[n] \supseteq use[n]$

What other constraints are there?

## Dataflow constraints

$$in[n] \supseteq use[n]$$

- A variable must be live on entry to  $n$  if it is used by the statement itself

$$in[n] \supseteq out[n] - def[n]$$

- If a variable is live on output and the statement does not define it, it must be live on input too

$$out[n] \supseteq in[n'] \text{ if } n' \in succ[n]$$

- if live on input to  $n'$ , must be live on output from  $n$

## Iterative dataflow analysis

- Initial assignment to  $in[n]$ ,  $out[n]$  is empty set  $\emptyset$ : will not satisfy constraints

$$in[n] \supseteq use[n]$$

$$in[n] \supseteq out[n] - def[n]$$

$$out[n] \supseteq in[n'] \text{ if } n' \in succ[n]$$

- Idea: iteratively re-compute  $in[n]$ ,  $out[n]$  when forced to by constraints. Live variable sets will increase monotonically.
- Dataflow equations:

$$in'[n] = use[n] \cup (out[n] - def[n])$$

$$out'[n] = \bigcup_{n' \in succ[n]} in[n']$$

## Complete algorithm

for all  $n$ ,  $in[n] = out[n] = \emptyset$

repeat until no change

for all  $n$

$$out[n] = \bigcup_{n' \in succ[n]} in[n']$$

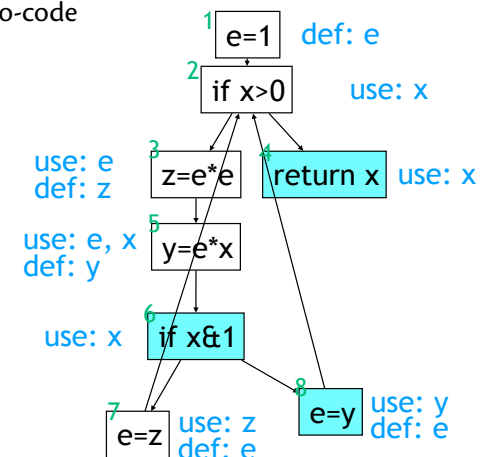
$$in[n] = use[n] \cup (out[n] - def)$$

$[n]$   
end  
end

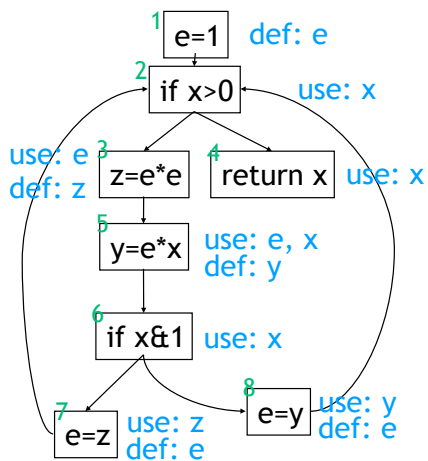
- Finds *fixed point* of  $in$ ,  $out$  equations
- Problem: does extra work recomputing  $in$ ,  $out$  values when no change can happen

## Example

- For simplicity: pseudo-code



## Example



2: in={x}  
 3: in={e}  
 4: in={x}  
 5: in={e,x}  
 6: in={x}  
 7: out={x}, in={x,z}  
 8: out={x}, in={x,y}  
 1: out={x}, in={x}  
 2: out={e,x}, in={e,x}  
 3: out={e,x}, in={e,x}  
 5: out={x}, in={e,x}  
 6: out={x,y,z}, in={x,y,z}  
 7: out={e,x}, in={x,z}  
 8: out={e,x}, in={x,y}  
 1: out={e,x}, in={x}  
 5: out={x,y,z}, in={e,x,z}  
 3: out={e,x,z}, in={e,x}  
 all equations satisfied

## Faster algorithm

- Information only propagates between nodes because of this equation:

$$\text{out}[n] = \bigcup_{n' \in \text{succ}[n]} \text{in}[n']$$

- Node is updated from its successors
  - If successors haven't changed, no need to apply equation for node
  - Should start with nodes at "end" and work backward

## Worklist algorithm

- Idea: keep track of nodes that might need to be updated in *worklist* : FIFO queue

for all  $n$ ,  $\text{in}[n] = \text{out}[n] = \emptyset$

$w = \{ \text{set of all nodes} \}$

repeat until  $w$  empty

$n = w.\text{pop}()$

$\text{out}[n] = \bigcup_{n' \in \text{succ}[n]} \text{in}[n']$

$\text{in}[n] = \text{use}[n] \cup (\text{out}[n] - \text{def}[n])$

if change to  $\text{in}[n]$ ,

for all predecessors  $m$  of  $n$ ,  $w.\text{push}(m)$

end