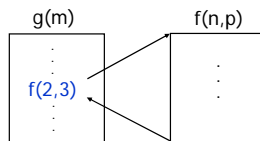


Dataflow Analysis

- Builds the CFG, iterate over basic blocks
- Compute information at each program point
 - E.g. constants, live variables, etc.
- Discussed: intra-procedural analysis
 - considers only the computation in the current procedure
- At function calls, assume worst case
 - Live variables: all globals/fields live before the call
 - Constant folding: globals/fields not constant after call

Inter-Procedural Analysis

- Precisely analyze interactions between functions/methods
- Same as dataflow analysis, but at each call analysis takes into account the computation in the invoked function
- Examples: inter-procedural constant folding, inter-procedural register allocation, etc.

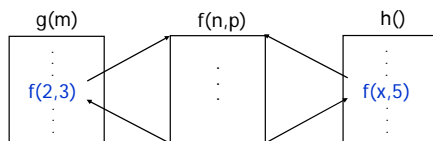


Issues

- Obtain a **stack of analyses** that corresponds to the execution stack of the program
- Analysis must **bind actual parameters to formals** before analyzing the callee
 - $n = 2; p = 3;$
- Another issue: different functions/methods have **different analysis domains**
 - E.g. for live variables, analysis domain includes set of variables local to the current function
 - Must change the analysis domain when analysis moves from caller to callee

Multiple Call Sites

- Another aspect: a function may be invoked from multiple call sites
- At different call sites, the analysis is different
 - **Input context** = analysis information at call site
- Hence, must re-analyze function in each context



Analysis Contexts

- The analysis of a function yields an **analysis context** which is a pair of:
 - an **input context**: the dataflow information at the entry (or exit) of the function
 - and a corresponding **analysis result**: the information at the exit (or entry) of the function, plus the return value
- Useful for **memoization**: whenever the information at a call site matches some input context, can reuse analysis result

Example

- Consider inter-procedural constant folding for the following program:

```
int a;          int f(int m, int n) {
void h() {      int t;
  int b;        t = a+m;
  scanf("%d", &b); a = a+n;
  a = 1;        return t;
  b = f(2,f(b,3));
}
```

- What are the contexts for function f?
- What is the value of b at the end of function h?

Recursion

- So far, analysis of recursive procedures doesn't terminate
- Analysis creates an unbounded number of analysis contexts
- Need a **fixed point algorithm**
 - Similar to analysis of loops in dataflow analysis
- Approach:** for each analysis context, keep a current best analysis result
 - Initialize current best to top
 - At recursive call sites use current result
 - At return: if result has changed, re-analyze function

Indirect Calls

- Problem:** calls for which the invoked function cannot be precisely determined at compile time
 - Function pointers in C/C++
 - Dynamically dispatched functions in Java/C++
- Approach:**
 - Analyze all possibly invoked functions
 - Then merge all of the results together
- To be precise, must accurately compute the possible targets of each indirect call
 - Function pointers: need points-to information
 - Virtual functions: need class hierarchy information

Exponential Blow-up

- Problem:** the number of procedure calls in a program may be exponential in the program size:

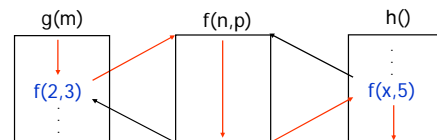
```
int f() { g(); g(); }
int g() { h(); h(); }
int h() { k(); k(); }
```
- Call graph** = graph describing the call structure
 - Nodes are functions, edges are call sites
 - Functions close to the leaves get executed many times
- Similarly, inter-procedural analysis may re-analyze functions many times; hence the analysis becomes expensive

Context-Insensitive Analysis

- So far: different analyses of a function for different input context (i.e., **context-sensitive** analysis)
- Alternative: **context-insensitive** analysis
 - Merge together all of the input contexts
 - Get a conservative input context
 - Analyze function for that input
 - Use analysis result for all of the call sites
- Less precise because it doesn't distinguish between different input contexts at different call sites
 - But more efficient: analyzes functions fewer times

Unrealizable Paths

- Source of imprecision:** information may flow from one call site to another
- The results models execution paths that don't follow the stack discipline, i.e. unrealizable paths



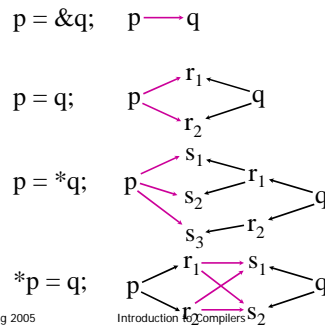
Flow-Sensitivity

- Dataflow analysis follows the control flow in the program to compute the result; hence, it is **flow-sensitive**
- Alternative: **flow-insensitive** analysis
 - Ignores the control flow!
 - Regards a program as a collection of statements
 - Assumes that statements can be executed multiple times, in any order
 - More efficient, less precise than flow-sensitive
- Similarity: **type information** is essentially flow insensitive
 - To check types of variables, just check assignments
 - Okay if assignments executed in a different order

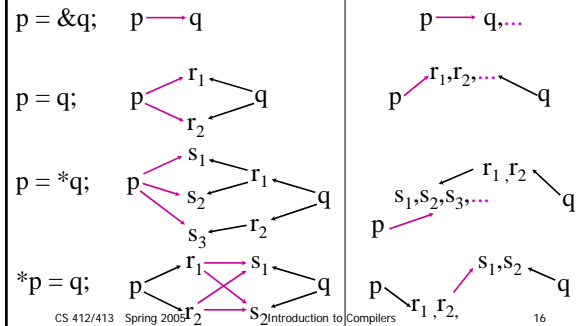
Flow-Insensitive Analysis

- Since the control flow is ignored, it is meaningless to compute a result per program point
- Instead, compute a single result valid for the whole program!
- General approach:
 - Derive constraints for each statement
 - Solve the system of constraints
- Example: points-to analysis -- for each pointer variable v , want to compute the set $\text{Ptr}(v)$ of possible targets of v

Flow-Insensitive Points-To Analysis [Andersen 94 --- $O(n^3)$]



Flow-Insensitive Points-To Analysis [Anderson 94 vs. Steensgaard 96 --- $\sim O(n)$]



Summary

- Inter-procedural analysis:
 - Context sensitive
 - Context insensitive
- Intra-procedural analysis:
 - Flow-sensitive (dataflow analysis)
 - Flow-insensitive
- Flow, context-sensitive: more precise, expensive
- Flow, context-insensitive: less precise, efficient