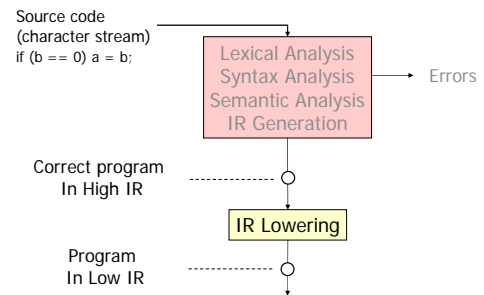


## CS412/CS413

Introduction to Compilers  
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Lecture 23: Introduction to Optimizations  
28 March 05

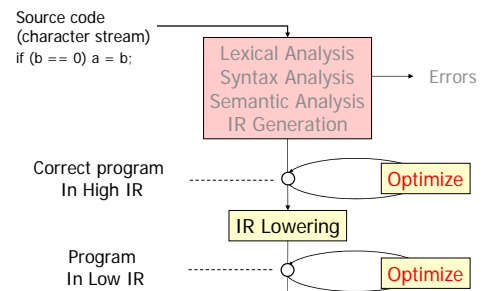
## Where We Are



## What Next?

- At this point we could generate assembly code from the low-level IR
- Better:
  - Optimize the program first
  - Then generate code
- If optimization performed at the IR level, then they apply to all target machines

## Optimizations



## What are Optimizations?

- **Optimizations** = code transformations that improve the program
- **Different kinds**
  - space optimizations: improve (reduce) memory use
  - time optimizations: improve (reduce) execution time
- Code transformations must be **safe!**
  - They must preserve the meaning of the program

## Why Optimize?

- Programmers don't always write optimal code – can recognize ways to improve code (e.g., avoid recomputing same expression)
- High-level language may make some optimizations inconvenient or impossible to express

$$a[i][j] = a[i][j] + 1$$

- High-level unoptimized code may be more readable: cleaner, modular

```
int square(x) { return x*x; }
```

## Where to Optimize?

- Usual goal: improve time performance
- Problem: many optimizations trade off space versus time
- Example: loop unrolling
  - Increases code space, speeds up one loop
  - Frequently executed code with long loops: space/time tradeoff is generally a win
  - Infrequently executed code: may want to optimize code space at expense of time
- Want to optimize program hot spots

## Many Possible Optimizations

- Many ways to optimize a program
- Some of the most common optimizations:
  - Function Inlining
  - Function Cloning
  - Constant folding
  - Constant propagation
  - Dead code elimination
  - Loop-invariant code motion
  - Common sub-expression elimination
  - Strength reduction
  - Constant folding & propagation
  - Branch prediction/optimization
  - Loop unrolling

## Constant Propagation

- If value of variable is known to be a constant, replace use of variable with constant
- Example:

```
n = 10
c = 2
for (i=0; i<n; i++) { s = s + i*c; }
```
- Replace n, c:

```
for (i=0; i<10; i++) { s = s + i*2; }
```
- Each variable must be replaced only when it has known constant value:
  - Forward from a constant assignment
  - Until next assignment of the variable

## Constant Folding

- Evaluate an expression if operands are known at compile time (i.e. they are constants)
  - Example:

```
x = 1.1 * 2;    =>    x = 2.2;
```
  - Performed at every stage of compilation
    - Constants created by translations or optimizations
- ```
int x = a[2] => t1 = 2*4
                t2 = a + t1
                x = *t2
```

## Algebraic Simplification

- More general form of constant folding: take advantage of usual simplification rules

```
a * 1  => a      a * 0  => 0
a / 1  => a      a + 0  => a
b || false => b   b && true => b
```
- Repeatedly apply the above rules

```
(y*1+0)/1 => y*1+0 => y*1 => y
```
- Must be careful with floating point!

## Copy Propagation

- After assignment  $x = y$ , replace uses of  $x$  with  $y$
- Replace until  $x$  is assigned again

```
x = y;
if (x > 1)
    s = x * f(x - 1);
```

```
x = y;
if (y > 1)
    s = y * f(y - 1);
```
- What if there was an assignment  $y = z$  before?
  - Transitivity apply replacements

## Common Subexpression Elimination

- If program computes same expression multiple time, can reuse the computed value
- Example:  

```
a = b+c;
c = b+c;
d = b+c;
⇒
a = b+c;
c = a;
d = b+c;
```
- Common subexpressions also occur in low-level code in address calculations for array accesses:  

```
a[i] = b[i] + 1;
```

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## Unreachable Code Elimination

- Eliminate code that is never executed
- Example:  

```
#define debug false
s = 1;
if (debug)
    print("state = ", s);
⇒
s = 1;
```
- Unreachable code may not be obvious in low IR (or in high-level languages with unstructured "goto" statements)

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## Unreachable Code Elimination

- Unreachable code in while/if statements when:
  - Loop condition is always false (loop never executed)
  - Condition of an if statement is always true or always false (only one branch executed)

```
if (false) S           ⇒ ;
if (true) S else S'    ⇒ S
if (false) S else S'   ⇒ S'
while (false) S        ⇒ ;
while (2>3) S          ⇒ ;
```

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## Dead Code Elimination

- If effect of a statement is never observed, eliminate the statement

```
x = y+1;
y = 1;
x = 2*z;
⇒
y = 1;
x = 2*z;
```

- Variable is dead if never used after definition
- Eliminate assignments to dead variables
- Other optimizations may create dead code

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## Loop Optimizations

- Program hot spots are usually loops (exceptions: OS kernels, compilers)
- Most execution time in most programs is spent in loops: 90/10 is typical
- Loop optimizations are important, effective, and numerous

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## Loop-invariant Code Motion

- If result of a statement or expression does not change during loop, and it has no externally-visible side-effect (!), can **hoist** its computation out of the loop
- Often useful for array element addressing computations – invariant code not visible at source level
- Requires analysis to identify loop-invariant expressions

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## Code Motion Example

- Identify invariant expression:

```
for(i=0; i<n; i++)
    a[i] = a[i] + (x*x)/(y*y);
```

- Hoist the expression out of the loop:

```
c = (x*x)/(y*y);
for(i=0; i<n; i++)
    a[i] = a[i] + c;
```

## Another Example

- Can also hoist statements out of loops
- Assume x not updated in the loop body:

```
...
while (...) {
    y = x*x;
    ...
}
...
⇒
...
y = x*x;
while (...) {
    ...
}
...
```

- ... Is it safe?

## Strength Reduction

- Replaces expensive operations (multiplies, divides) by cheap ones (adds, subtracts)
- Strength reduction more effective in loops
- Induction variable** = loop variable whose value depends linearly on the iteration number
- Apply strength reduction to induction variables

```
s = 0;
for (i = 0; i < n; i++) {
    v = 4*i;
    s = s + v;
}
⇒
s = 0; v = -4;
for (i = 0; i < n; i++) {
    v = v + 4;
    s = s + v;
}
```

## Strength Reduction

- Can apply strength reduction to computation other than induction variables:

```
x * 2    ⇒ x + x
i * 2c ⇒ i << c
i / 2c ⇒ i >> c
```

## Induction Variable Elimination

- If there are multiple induction variables in a loop, can eliminate the ones which are used only in the test condition
- Need to rewrite test using the other induction variables
- Usually applied after strength reduction

```
s = 0; v = -4;
for (i = 0; i < n; i++) {
    v = v + 4;
    s = s + v;
}
⇒
s = 0; v = -4;
for (; v < (4*n+4);) {
    v = v + 4;
    s = s + v;
}
```

## Loop Unrolling

- Execute loop body multiple times at each iteration
- Example:
 

```
for (i = 0; i < n; i++) { S }
```
- Unroll loop four times:
 

```
for (i = 0; i < n-3; i+=4) { S; S; S; S; }
for ( ; i < n; i++) S;
```
- Gets rid of ¾ of conditional branches!
- Space-time tradeoff: program size increases

## Function Inlining

- Replace a function call with the body of the function:

```
int g(int x) { return f(x)-1; }
int f(int n) { int b=1; while (n--) { b = 2*b }; return b; }
```

```
int g(int x) { int r;
              int n = x;
              { int b = 1; while (n--) { b = 2*b }; r = b }
              return r - 1; }
```

- Can inline methods, but more difficult
- ... how about recursive procedures?

## Function Cloning

- Create specialized versions of functions that are called from different call sites with different arguments

```
void f(int x[], int n, int m) {
    for(int i=0; i<n; i++) { x[i] = x[i] + i*m; }
}
```

- For a call `f(a, 10, 1)`, create a specialized version of `f`:

```
void f1(int x[]) {
    for(int i=0; i<10; i++) { x[i] = x[i] + i; }
}
```

- For another call `f(b, p, 0)`, create another version `f2(...)`

## When to Apply Optimizations

High IR

Low IR

Assembly

Function inlining  
Function cloning  
Constant folding  
Constant propagation  
Value numbering  
Dead code elimination  
Loop-invariant code motion  
Common sub-expression elimination  
Strength reduction  
Constant folding & propagation  
Branch prediction/optimization  
Loop unrolling  
Register allocation  
Cache optimization

## Summary

- Many useful optimizations that can transform code to make it faster
- Whole is greater than sum of parts: optimizations should be applied together, sometimes more than once, at different levels
- Problem: when are optimizations are safe?