

2D Routines in 3D



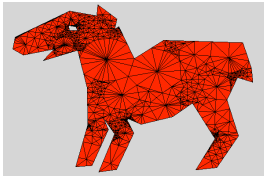
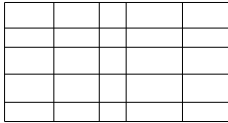
Outline

- Announcements
 - HW II--due Friday. 5PM
- HW1 & Cookie
- Grids & Meshes
- Representing $f(x,y)$
- Lines & Surfaces in 3D
- Survey

HW I

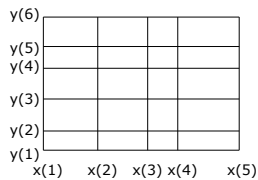
- No issues on the programs--most did well
 - sample solutions are on the web
 - Graphics functions should return handles!
- No problems figuring out colors or finding handles
 - if you don't understand a question, come find me!
- Problem 1
 - This was a bit of a trick question, but ...
 - since you have to go to the computer to do the programming, you might as well try the problems
 - `h=plot([1,2;1,2;1,2],[3,4;3,2;2,4],'ro');`
 - whos h will tell you h is length 3
 - Two additional objects: figure and axes

Interpolation & grids



- To plot with surfaces, you need some kind of mesh or grid:
 - a mesh is a collection of non-overlapping polygons that fills a region of space
 - meshes can be structured (all polygons the same size and shape) or unstructured

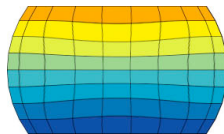
Regular Grids



- Meshes made from quadrilaterals are known as grids
 - A regular grid has only 90° angles (rectangles) and can be defined by vectors x and y
 - if $x(j+1)-x(j)$ and $y(j+1)-y(j)$ are constant, then the grid is uniform

Unstructured Grids

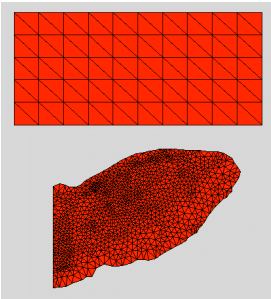
- If the cells are not rectangular, then the grid is irregular or unstructured
- X and Y are now matrices:



Visualizing Grids

- Matlab's surface-based functions want grids:
 - `pcolor`
 - `contour`
 - `surf`
 - `mesh`

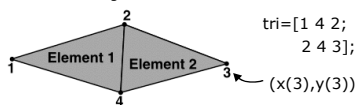
The World is not Square



- Meshes of triangles are common, especially in finite element modelling
- Triangular meshes can also be structured or unstructured
 - unstructured are more common

Triangular Meshes

- Matrices are rectangular, so it is hard to "fit" a triangular mesh into a matrix
- Typically, triangular meshes require 3 arrays:
 - vectors `x` and `y` contain the location of the vertices (in no particular order)
 - array `tri` defines how the vertices are connected
 - Each row contains indexes the three vertices forming a triangle



```
tri=[1 4 2;  
      2 4 3];
```

$(x(3), y(3))$

Plotting Triangular Meshes

- Matlab's trimesh is designed to plot $z = f(x, y)$ on a triangular mesh
 - `trimesh(tri, x, y, z, {c});`
 - `trimesh(tri, x, y)` -- just the mesh, not the data
- We can do the same thing with patch
 - More general, non-triangular meshes (e.g. PS2)
 - this is mainly to illustrate the form of x , y , z , and c data fields

Patching Triangular Meshes

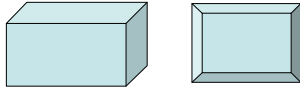
- `h = patch(X, Y, C)` creates polygons for each column of X , Y , and C
 - if our mesh has t triangles, X , Y , and C will be 3-by- t
 - `X = [x(tri(:,1)), x(tri(:,2)), x(tri(:,3))]';`
- The mesh will be plotted in 2D view with flat color: triangle colors will be set by the first vertex (first row of C);

Patching Triangular Meshes

- Suppose we want to make it 3D with elevation set by C
 - `patch(X, Y, C, C)` will work (C used for both elevation and color)
- or, if we've already plotted, with `h = patch(X, Y, C):`
 - `set(h, 'zdata', C); view(3)`

3D views

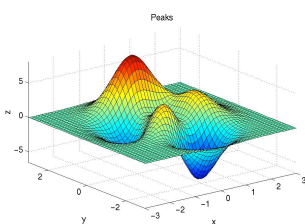
- 3D views on a computer or painting are just illusions
 - Perspective
 - lines converge towards focal point
 - Color and lighting can enhance perspective
 - Optical illusions are possible



Line Objects in 3D

- `h=plot(x,y);get(h,'zdata')`
 - ans=
 - Empty matrix: 1-by-0
- Both patch and line objects have a `zdata` field. Plot sets this to `[]`
- We can plot a line in 3D using `plot3(x,y,z)`
 - could also set `zdata` field manually

3D view

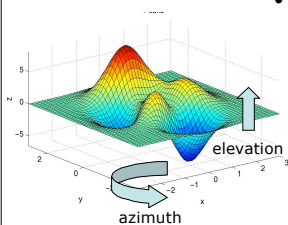


- 3D functions will set axes projection to perspective
- The axes are now a box drawn in perspective

Controlling the 3D view

- We can control the size of the axes (limits) and the way they are drawn (view)
 - `set(gca,'xlim',[minimum, maximum])`--also for y and z
 - Can also set scale to log or reverse direction (must be done manually)
- Clicking on the circle button allows you to rotate the axes in 3D

Controlling the 3D view



- Can also control the view from the command line through view:
 - `view(2)` or `view(3)` gets default 2D or 3D views
 - `view([az,el])` sets the `azimuth=az` (rotates about z) and `elevation=el` (rotates about line in x-y plane)

Surfaces in 3D

- Like lines, patch and surface objects have `zdata` fields.
- `surf(X,Y,Z)` creates a surface with vertices defined by X,Y, and Z
 - color is proportional to Z
 - `facecolor=flat`
- `mesh(X,Y,Z)` is similar, but doesn't fill polygons
 - `edgecolor=flat`

Comparing surf and pcolor

- pcolor is a special form of surf

field	pcolor(x,y,Z)	surf(x,y,Z)
xdata	x	x
ydata	y	y
zdata	<i>0*Z</i>	<i>Z</i>
cdata	<i>Z</i>	<i>Z</i>
facecolor	'faceted'	'faceted'
projection	<i>orthographic</i>	<i>perspective</i>
View	<i>[0 90]</i>	<i>[-37.5 30]</i>

- How can we change cdata?