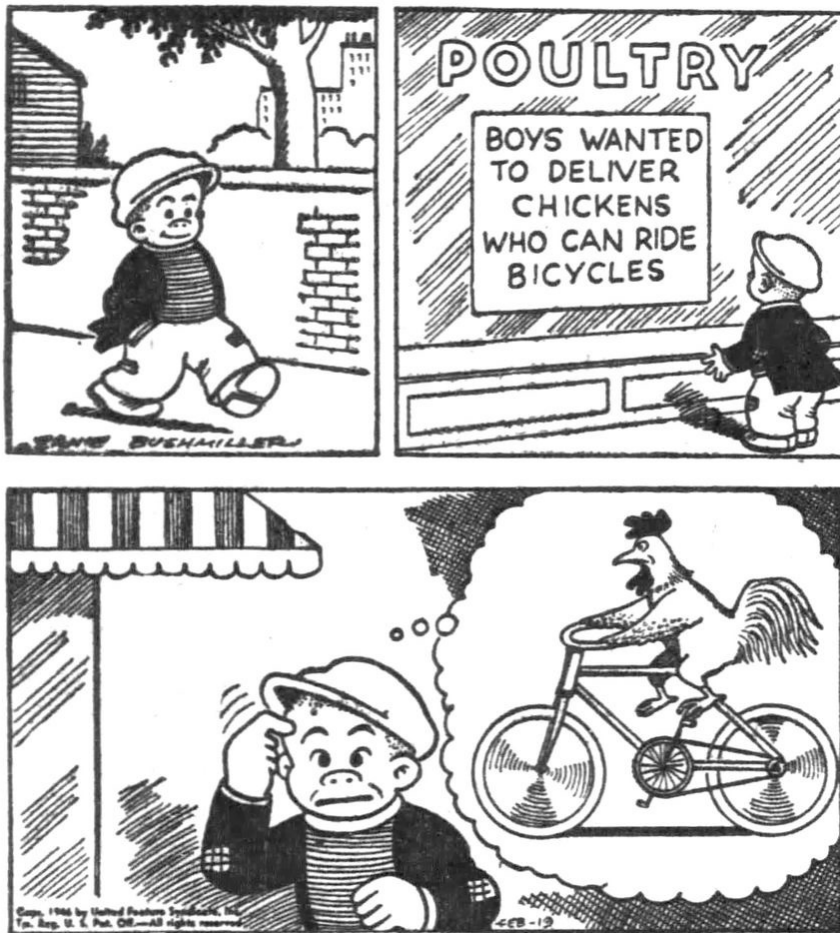


## ANNOUNCEMENTS

1. All assignments, long and short, optional and non-optional are released
  2. Kaggle competition + dataset released ; "BASELINES" out soon!
- 

NANCY

BY ERNIE BUSHMILLER

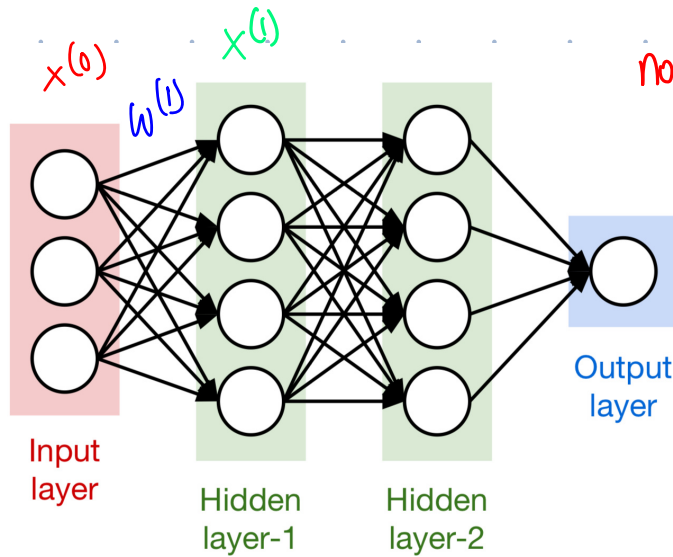


# Last few lectures ...

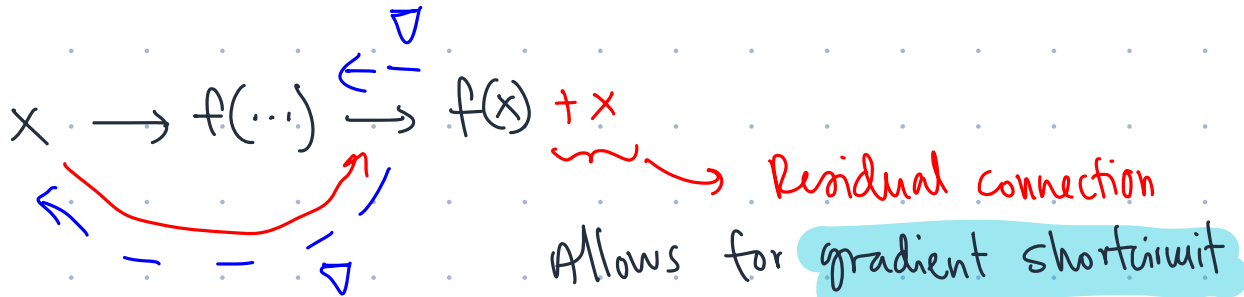
## I. FULLY-CONNECTED NETWORK

$$x^{(l)} = \sigma(w^{(l)} x^{(l-1)} + b^{(l)})$$

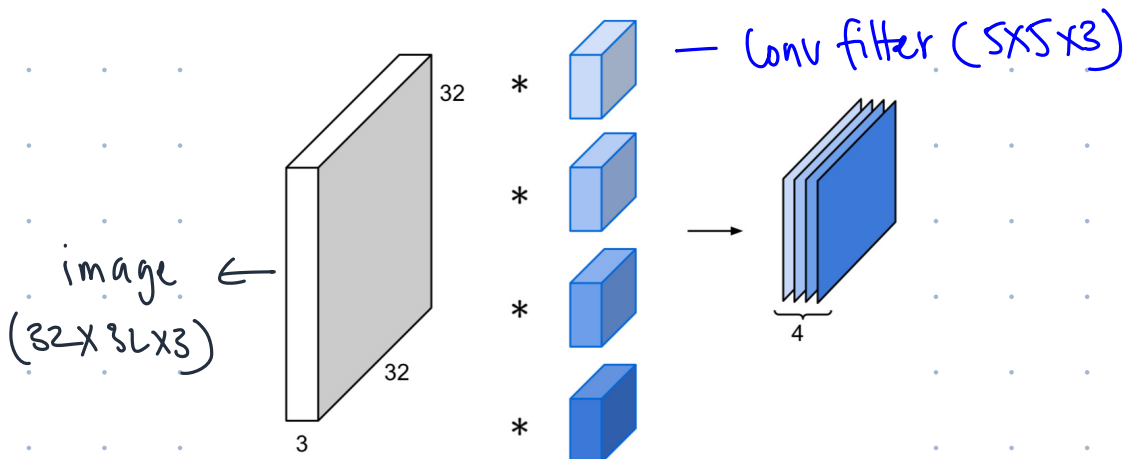
↓  
non-linearity



## II. RESIDUAL CONNECTIONS



## III. CONVOLUTIONAL NETWORKS -



TODAY: LANGUAGE! (is hard, but I might be biased!)

sense of context becomes extremely relevant!

Q. What are the atomic units, the "pixels" of language?

"berry, the llama was spotted in baker lab"

1. words = berry, the, llama, ... — the underlying dictionary / vocabulary needs to be constantly updated!
2. characters = a, b, c, ... — Scalable from a language perspective

10 words = 10T units of compute

10 byte/chars = 40T units of compute!

3. Subwords = "walk", "ing", "chat", "g", "p", "t"

The atomic units are called Tokens!

# Vector representations (+ notion of similarity)

Tokenization: Where | are | you | going | ?

Radhi says - use some form of an encoding

need to represent in a numerical format, more precisely, we need a vector

$V = \{ \text{where, when, are, you, going, from, moving, ?} \}$

$$|V| = 8$$

	where	when	are	you	going	from	moving	?
"Where are you going?"	1	0	1	1	1	0	0	1
"When are you moving?"	0	1	1	1	0	0	1	1
"Where are you from?"	1	0	1	1	0	1	0	1

DOT-PRODUCT SIMILARITY -

$$\text{dot}(s^{(1)}, s^{(3)}) = 4, \quad \text{dot}(s^{(1)}, s^{(2)}) = 3 \leftarrow \text{"match"}$$

FLAW - SENTENCE STRUCTURE IS SOMEWHAT CAPTURED,  
BUT SEMANTICS ARE MISSED!

If  $|V| = |M|$ , each vector is  $1M$ , and sparse (= mostly zeros!)

# Capturing "semantics" — a stupid example!

$s^{(1)}$  : this building is made of stone

$s^{(2)}$  : Ezra Cornell sat in Gates Hall

$s^{(3)}$  : this illu is made of stone

$s^{(4)}$  : Tashaar went to his illu

"Bryn" — house

Matt said, "..."

SIMILAR WORDS APPEAR IN SIMILAR CONTEXTS!

↓ I ↓ II

"this illu is beautiful"

↓ word ↓

Context

target token

$S = (t_1, \dots, t_{i-w}, \dots, t_{i-1}, t_i, t_{i+1}, \dots, t_{i+w}, \dots)$

Context Context

## Binary classification that we DON'T care about!

Given a target token,  $t_i$

context tokens,  $\{t_{i-w}, \dots, t_{i-1}, t_{i+1}, \dots, t_{i+w}\} = C_i$

we want to build a binary cls,

$P(+1 | t_i, C_i) \leftarrow$  probability that  $C_i$  is a true context of  $t_i$

"Similar" tokens  
appear in similar  
ctxs  
↓

in our e.g., - "illu" = target,  
 $C_i = \{\text{this, is, beautiful}\}$   
is the true context.

we can use the notion of some similarity  
b/w  $t_i, C_i$

$$P(+1 | t_i, C_i) = \prod_{-w \leq k \leq w} P(+1 | t_i, t_{i+k})$$

What is the proba that  $t_{i+k}$   
is a true context token  
of  $t_i = \text{"illu"}?$

ensures  
normalization  
b/w 0,1

$$= \frac{1}{1 + \exp(-\text{dot}(t_i, t_{i+k}))}$$

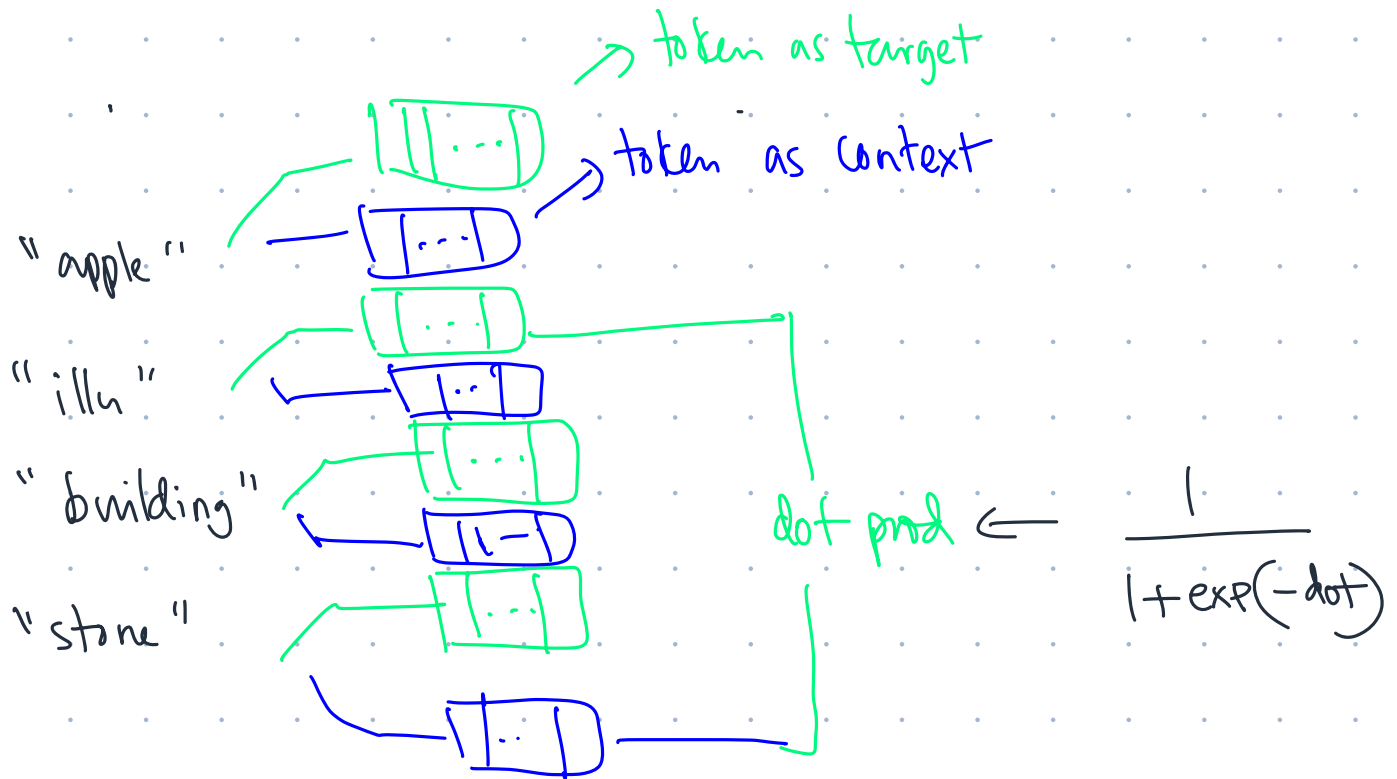
computes similarity b/w target,  
ctx token

(Similar to logistic regression!)

Q. What should  $t_i, t_{i+k}$  be?

we

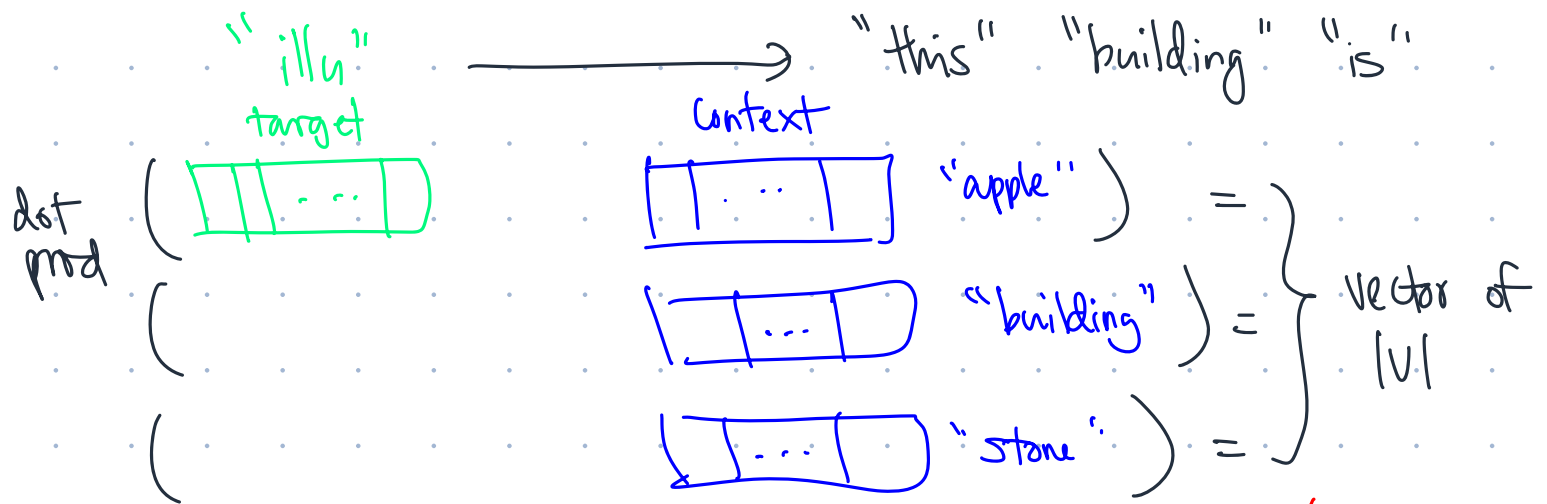
OK what  $t_i, t_{i+k}$  are, but ~~I~~ can learn them using GD!



OBJ: maximize  $\mathcal{L}(y | \text{true target, true context})$

— started the idea of learnable embeddings!

Reformulation - Given a target token, can you predict the context tokens?



Normalization is done using softmax - 
$$\frac{\exp(z_j)}{\sum_{k=1}^n \exp(z_k)}$$



## Aside: PERPLEXITY

min. NLL loss — straightforward max log-likelihood  
take negative → NLL

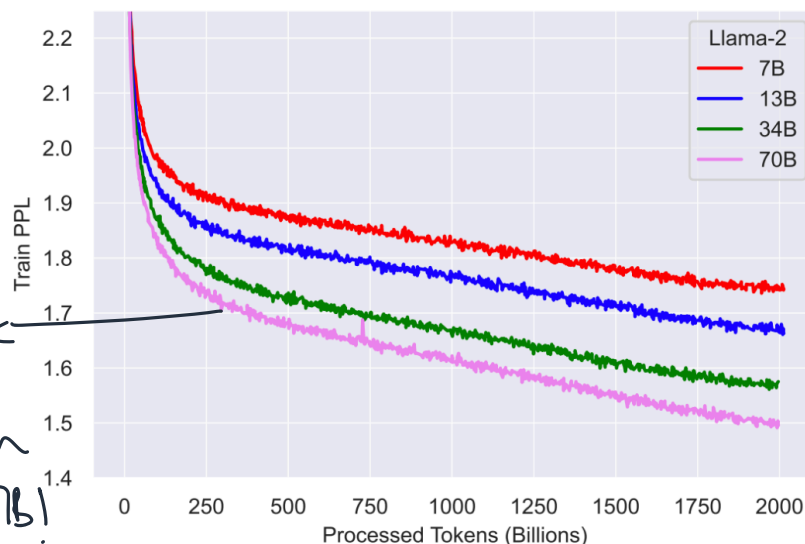
↓  
PERPLEXITY — "Complete this ?" → model predicts "sentence"  
true is "confirmation"  
RESULT — model is shocked!

Hyperparams				Dev Set Accuracy		
#L	#H	#A	LM (ppl)	MNLI-m	MRPC	SST-2
3	768	12	5.84	77.9	79.8	88.4
6	768	3	5.24	80.6	82.2	90.7
6	768	12	4.68	81.9	84.8	91.3
12	768	12	3.99	84.4	86.7	92.9
12	1024	16	3.54	85.7	86.9	93.3
24	1024	16	3.23	86.6	87.8	93.7

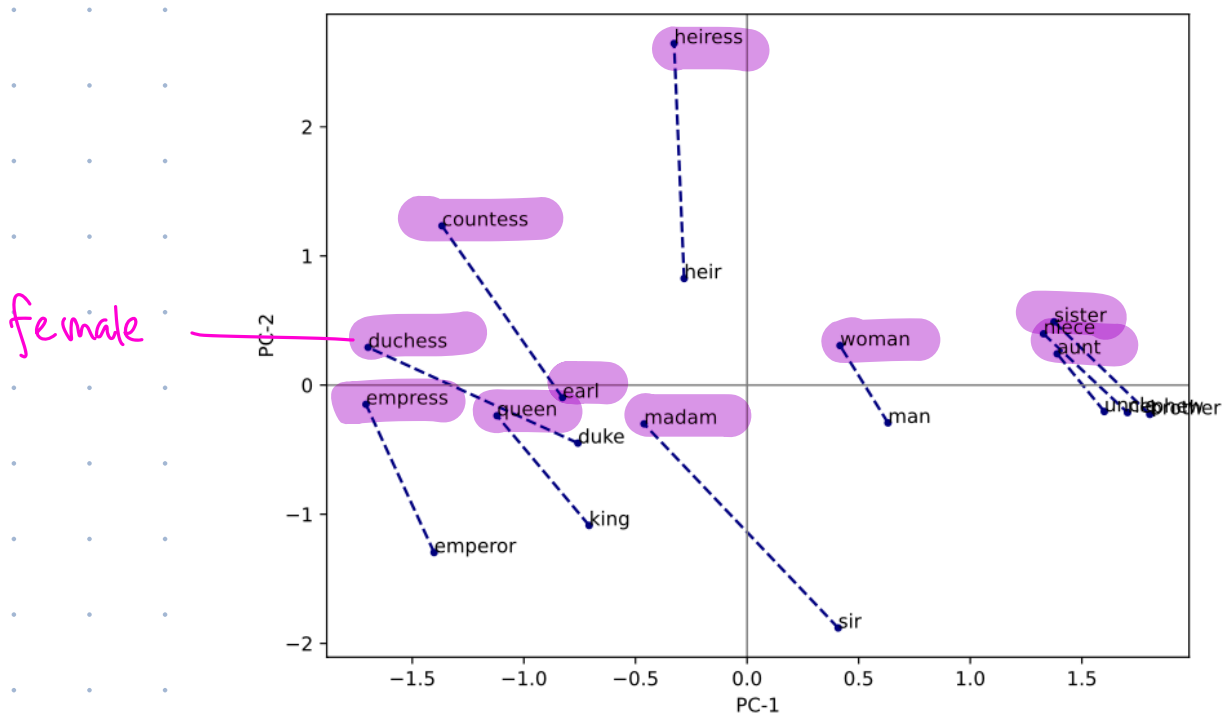
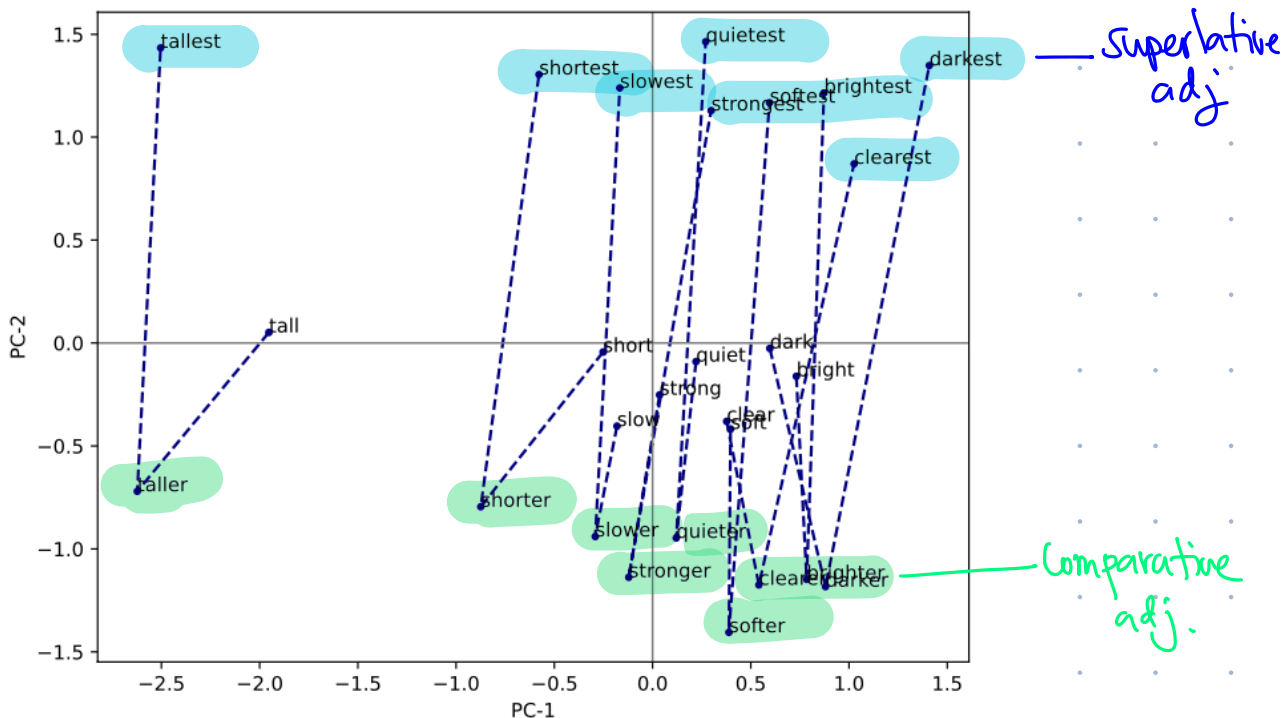
perplexity  
(lower is better)

Random NLP  
Benchmarks  
(higher is better)

Llama-70B  
is known to  
be much better  
than Llama-7B!



# Visualizing learned embeddings using PCA



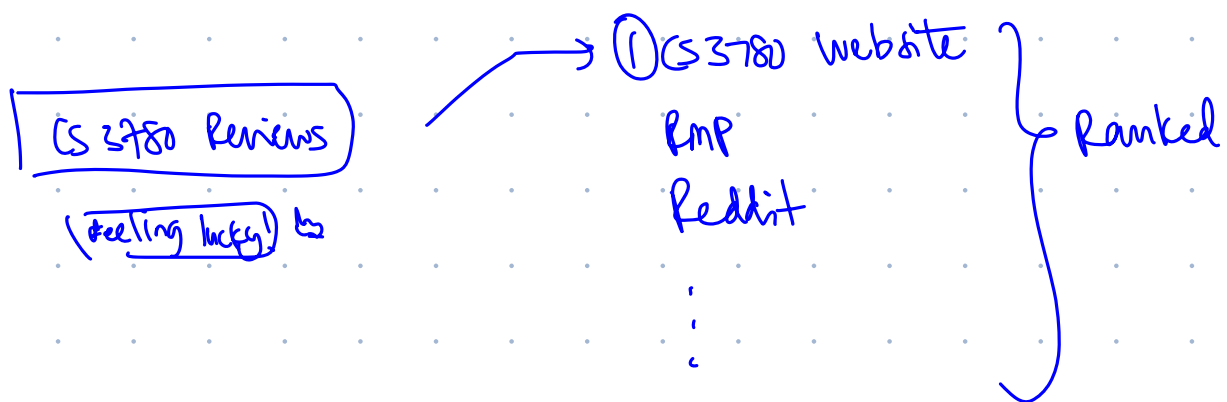
$$\vec{\text{king}} - \vec{\text{man}} + \vec{\text{woman}} = \vec{\text{queen}}$$

## Static $\rightarrow$ Dynamic embeddings

Once trained, these learnable embeddings are 'static'  
 $\Rightarrow$  One embedding for each token

"The **bank** teller" vs. "the river **bank**"  
 $\searrow$  same embedding representation  $\swarrow$

NEED DYNAMIC EMBEDDINGS!



Final document comes

80% from ① + 20% from ② + 30% from ③

## (softmax) self-attention -

"the" "bank" "teller"

interested in emb for "bank"

$\text{dot}(\text{vec}(\text{"the"}), \text{vec}(\text{"bank"}))$   
 $\text{dot}(\text{vec}(\text{"bank"}), \text{vec}(\text{"bank"}))$   
 $\text{dot}(\text{vec}(\text{"teller"}), \text{vec}(\text{"bank"}))$

dot-prod  
← Similarity b/w "the", "bank"

Returned links/  
"keys"

search query

use them

to form a weighted  
average of all  
embeddings

$$\begin{aligned} &\langle \text{"the"}, \text{"bank"} \rangle \cdot \text{vec}(\text{"the"}) + \\ &\quad \langle \text{"bank"}, \text{"bank"} \rangle \cdot \text{vec}(\text{"bank"}) + \\ &\quad \langle \text{"teller"}, \text{"bank"} \rangle \cdot \text{vec}(\text{"teller"}) \end{aligned}$$

## POSITIONAL INFORMATION

bank: "the bank teller" different from bank: "the river bank"

"the bank teller sent at the river bank"

(1) (2) (3) (4) (5) (6) (7) (8)

## Attention computations + Efficiency

$$O = \text{Softmax}(QK^T) V$$

$X$  is a " $n$ " long sequence, with  $d$ -dimensional tokens

Time -  $O(n^2d)$

Space -  $O(n^2)$  to store  $QK^T$

$$X \in \mathbb{R}^{n \times d}$$

$$\begin{array}{c} Q \quad K \quad V \in \mathbb{R}^{n \times d} \\ \text{linear}(X) \quad \text{linear}(X) \quad \text{linear}(X) \end{array}$$