CS 312 **Environment Model Diagrams**

Spring 2007

The Substitution Model

• Recall the substitution model:

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- Bind variables at "let" constructs
- Bind function arguments at function calls
- Substitute bindings in the let body or function body
- let val x = v in e end -> $e\{v/x\}$ $(fn x => e)(v) -> e\{v/x\}$
- Example: let val x = 3 in x * x end -> 3 * 3 -> 9

Problems

- Substitution model:
 - Useful for understanding program execution
 - Inefficient as an implementation
- Problem 1: We must traverse the code just to perform substitutions; the code will be traversed again when we execute it
- Problem 2: Substitutions can lead to code blow-up

```
let val x = (1,2)

val y = (x,x)

val z = (y,y)
       (z,z)
end
```

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Problems

Problem 3: SM doesn't work in a straightforward way with imperative features:

```
let val x = ref 1
val y = x
in y := 2; !x end
-> (ref 1) := 2; !(ref 1)
```

We would need to use a memory location "l" instead of "ref 1", then substitute l into the code, and keep track of l's value on the side

The Environment Model

- · Solution: the environment model
 - Idea: use an environment to store bindings of variables
 - No substitutions
 - Environment is a map from variables to values
 - Values are looked up lazily, when needed
- Example:

```
Program:
                               Environment:
let val x = 2
    val y = "hello"
    x + size(y)
end
```

The Environment Model

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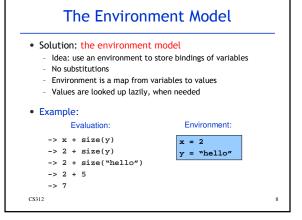
-> let val y = "hello" x + size(y)

Evaluation:

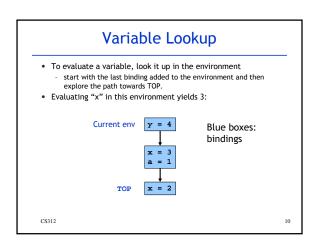
Environment:

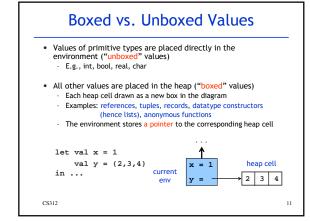
x = 2

Solution: the environment model Idea: use an environment to store bindings of variables No substitutions Environment is a map from variables to values Values are looked up lazily, when needed Example: Evaluation: x = 2 y = "hello"



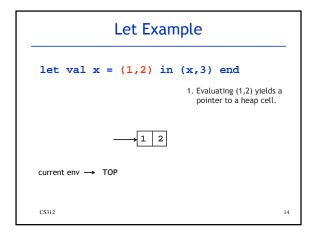
Environments Bindings added when entering a scope Bindings removed at end of scope Nested let blocks: how do we remove just the inner bindings? Idea: use a stack-like structure of bindings Entering a scope: push new bindings, record the parent Exiting a scope: move to the parent Most recent binding = current environment Least recent binding = TOP

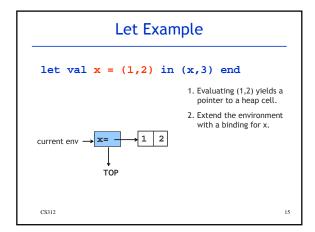


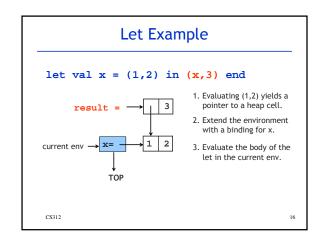


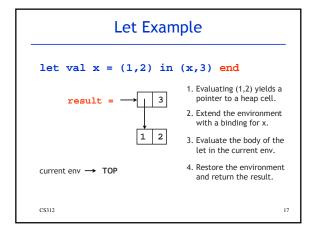
Let expressions To evaluate let val x = el in e2: 1. Evaluate el in the current environment 2. Extend the current environment with a binding that maps x to the value of el 3. Evaluate e2 in the extended environment 4. Restore the old environment (i.e., remove the binding for x) 5. Return the value of e2

Let Example let val x = (1,2) in (x,3) end current env \rightarrow TOP



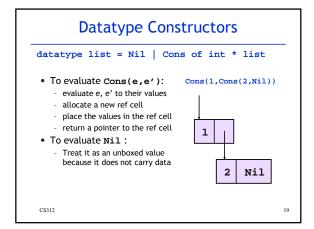


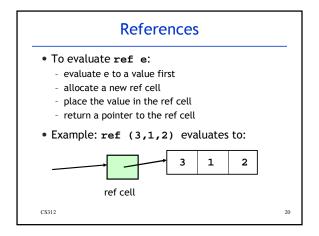


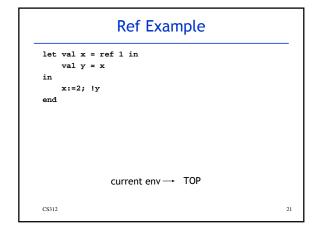


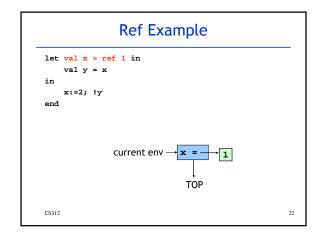
```
Multiple Declarations
To evaluate:
let val x = e1
    val y = e2
    in
        e3
        end

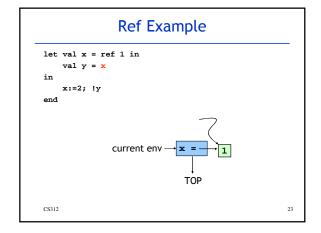
Do the same the same thing as you would for:
let val x = e1
    in let val y = e2
    in
        e3
        end
end
end
```

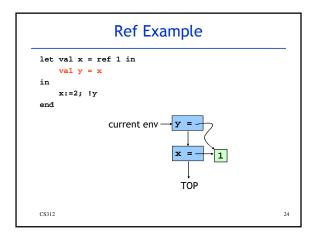


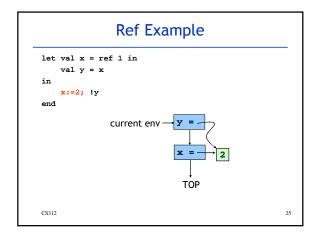


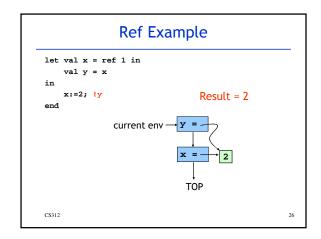


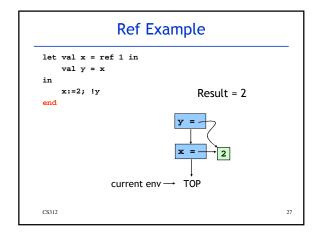


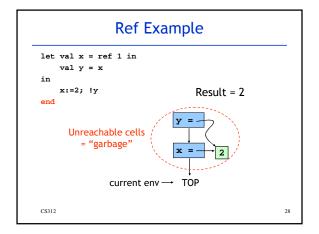












Ref Example let val x = ref 1 in val y = x in x:=2; !y Result = 2 end current env --- TOP

Garbage Collection • Garbage cells are those heap cells not reachable from: - The current environment - Or from the result • Garbage collection is the process of collecting the unreachable heap cells - Takes place as the program runs - Will discuss more about it later in the course

Functions • Consider the following code: let val x = 2 val f = fn z => z + x in f 3 end • What value do we assign to f? • Note: the body of f refers to variable x - What is the value of x? • Solution: use a closure = (env,code) pair - env = tells us about the values of unbound variables

```
Function Example

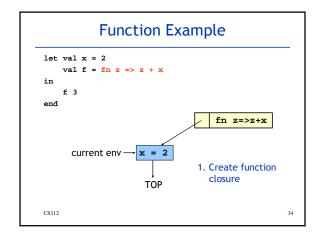
let val x = 2
 val f = fn z => z + x
in
 f 3
end

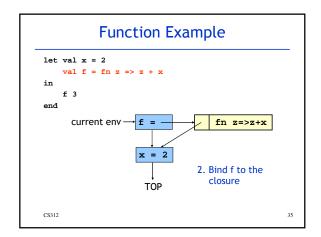
current env → TOP
```

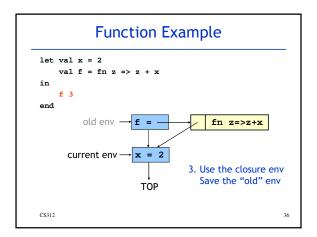
```
Function Example

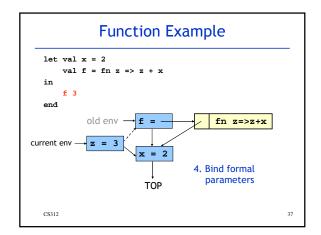
let val x = 2
val f = fn z => z + x
in
f 3
end

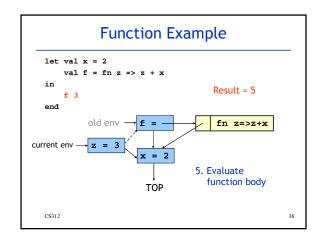
current env — x = 2
TOP
```

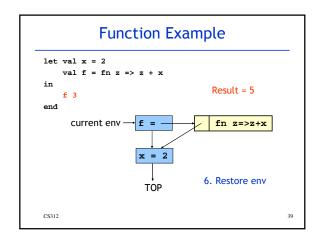


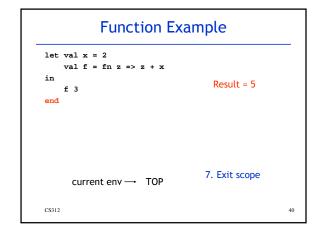












Function Calls

To evaluate e1(e2):

- 1. Evaluate e1 you must get a pointer to a closure.
- 2. Evaluate e2 to a value.
- 3. Save the current environment (and refer to it as the "old" environment).
- 4. Use the environment from the closure, extend it with binding for formal parameters.
- 5. Evaluate the body of the function within the extended environment; this is the result.
- 6. Restore the old environment (saved in step 3)
- 7. Return the result.

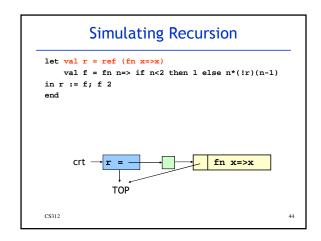
Static vs. Dynamic Scoping

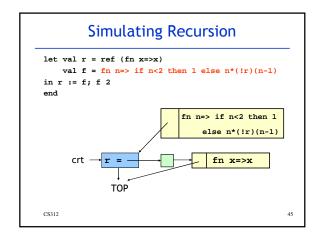
• Consider this code:

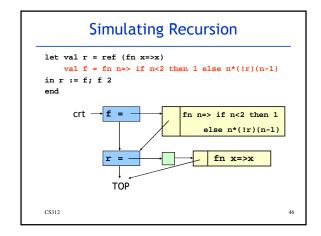
```
let val x = 2
    val f = fn z \Rightarrow z + x
    val x = 1
in
```

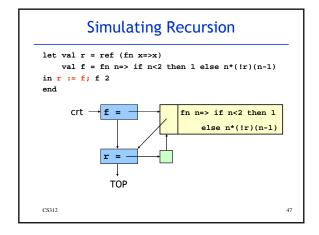
- Which binding to use for x?
- Static scoping: use the binding at the declaration (this is the environment saved in the closure) This is the case in ML, Java. Result = 5
- Dynamic scoping: use the binding at the call Other languages (older LISP, Perl). Result = 4

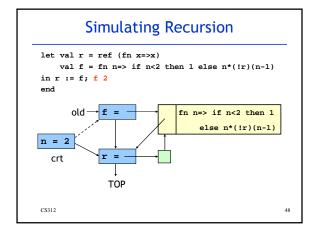
Simulating Recursion let val r = ref (fn x=>x)val f = fn n=> if n<2 then 1 else n*(!r)(n-1) in <math>r := f; f 2end $crt \longrightarrow TOP$ CS312







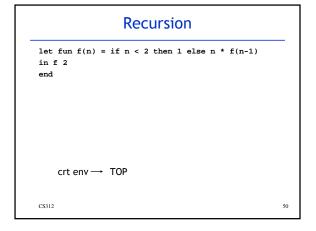




Recursive Function Definitions

- To handle truly recursive functions:
- Extend the environment first, with an "incomplete" binding for the recursive function
- 2. Next, build the closure and make the environment in the closure point to the extended environment (that includes the function)
- 3. Finally, bind the function symbol to the closure
- We get a cycle:
 - the function symbol points to the closure
 - The environment in the closure points to the symbol

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Recursion let fun f(n) = if n < 2 then 1 else n * f(n-1) in f 2 end crt env TOP Create an incomplete binding for f

