## CS 2802: Homework 2

## January 28, 2019

Handed out Jan. 28; due Feb. 4

- Read Chapter 4; 10.1, 10.2, 10.6, 10.7, 10.10; 8.1 (including 8.1.1-8.1.4). (The rest of Chapter 8 is fun, but not required.)
- Do the following problems:
  - 1.9 (this has a short, cute solution)
  - -4.14
  - -10.31
  - 10.34 (just give one-line answers for each part; no need for proofs)
  - -10.37
  - 10.38 (again, just give one-line answers here)

and the following extra problems:

- Extra problem 1: Prove directly that
  - (a)  $A = (A B) \cup (A \cap B)$ . (Don't worry about going through propositional equivalences, as in the text.)
  - (b) If  $A \subseteq B$  then  $C B \subseteq C A$ .
- Extra problem 2: Prove that  $\varphi \Rightarrow \psi$  is valid iff the set of truth assignments that make  $\varphi$  true is a subset of the set that makes  $\psi$  true. (It follows that  $\varphi$  and  $\psi$  are equivalent iff  $\varphi \Leftrightarrow \psi$  is valid, although you don't have to explicitly prove this.)
- Extra problem 3: Prove that equivalence classes are either equal or disjoint.
- Extra problem 4: Prove that If  $S \neq \emptyset$ , then there is an injection from S to T iff there is a surjection from T to S.