

THE LENGTH OF A PATH IN A WEIGHTED GRAPH =
= THE SUM OF THE WEIGHTS OF THE EDGES OF THIS PATH.

$$\begin{aligned} a &= S_0 \\ a, d(2) &= S_1, L(a) = 0 \\ a, d(2), b(4) &= S_2, L(d) = 2 \\ a, d(2), b(4), e(\text{via } d; 5) &= S_3, L(b) = 4 \\ a, d(2), b(4), e(\text{via } d; 5), z(\text{via } d, e; 6) &= S_4, L(e) = 5 \\ a, d(2), b(4), e(\text{via } d; 5), z(\text{via } d, e; 6) &= S_5, L(z) = 6 \end{aligned}$$

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procedure Dijkstra( $G$ ): weighted connected simple graph, with
all weights positive)
 $G$  has vertices  $a = v_0, v_1, \dots, v_n = z$  and weights  $w(v_i, v_j)$ 
where  $w(v_i, v_j) = \infty$  if  $\{v_i, v_j\}$  is not an edge in  $G$ 
for  $i = 1$  to  $n$ 
 $L(v_i) := \infty$ 
 $L(a) := 0$ 
 $S := \emptyset$ 
{the labels are now initialized so that the label of  $a$  is zero and all
other labels are  $\infty$ , and  $S$  is the empty set}
while  $z \notin S$ 
begin
 $u :=$  a vertex not in  $S$  with  $L(u)$  minimal
 $S := S \cup \{u\}$ 
for all vertices  $v$  not in  $S$ 
if  $L(u) + w(u, v) < L(v)$  then  $L(v) := L(u) + w(u, v)$ 
{this adds a vertex to  $S$  with minimal label and updates the
labels of vertices not in  $S$ }
end  $\{L(z) =$  length of shortest path from  $a$  to  $z\}$ 

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$$L_k(u) = \begin{cases} \text{THE SHORTEST DISTANCE BETWEEN } a \\ \text{AND } u \text{ IN } S_k \\ \text{O.O., O.W.} \end{cases}$$

$S_{k+1} = S_k \cup \{u\}$ WHERE $u \in S_k$ WITH THE MINIMAL LABEL

76. DISKTRA ALGORITHM FINDS THE LENGTH OF A SHORTEST PATH IN A CONNECTED SIMPLE UNDIRECTED, WEIGHTED GRAPH. $O(n^3)$ ADDITION AND COMPARISONS.

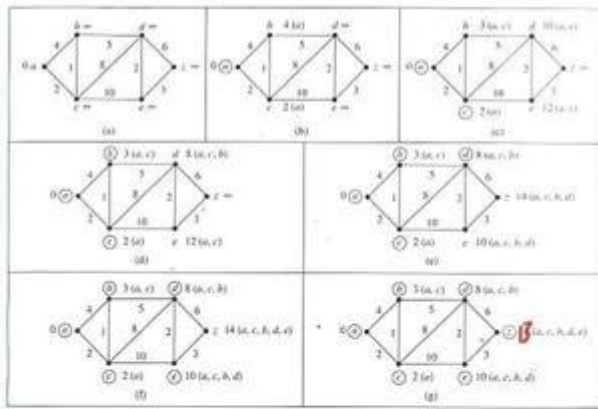


FIGURE 4 Using Dijkstra's Algorithm to Find the Shortest Path from a to z .

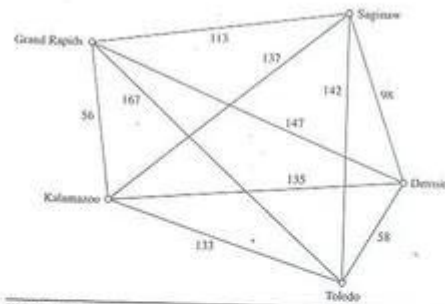


FIGURE 5 The Graph Showing the Distances Between Five Cities.

THE TRAVELING SALESMAN PROBLEM =
A HAMILTON CIRCUIT WITH MINIMUM TOTAL WEIGHT
NP-COMPLETE PROBLEM