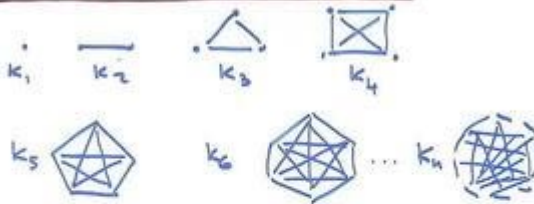


LEC 30 11/10/99

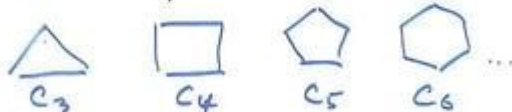
SOME SPECIAL GRAPHS

COMPLETE GRAPHS ON  $n$  VERTICES  $K_n$



ONE EDGE BETWEEN EACH PAIR OF DISTINCT VERTICES

CYCLES  $C_n, n \geq 3$



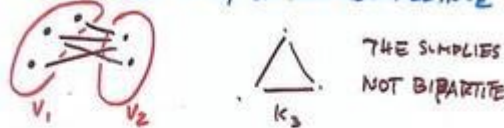
$$C_n = (V, E); V = \{v_1, \dots, v_n\}$$

$$E = \{\{v_1, v_2\}, \{v_2, v_3\}, \dots, \{v_n, v_1\}\}$$

-170-

def  $G$  IS BIPARTITE IF  $V = V_1 \cup V_2$

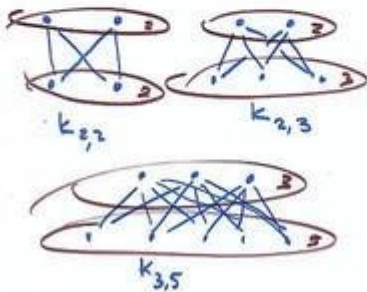
SUCH THAT NO EDGE OF  $G$  CONNECTS TWO VERTICES IN  $V_1$  OR TWO VERTICES IN  $V_2$



COMPLETE BIPARTITE  $K_{m,n}$  : (USUALLY ASSUMED  $m \leq n$ )

$$V = V_1 \cup V_2 \quad |V_1| = m \quad |V_2| = n$$

THERE IS ONE EDGE BETWEEN ANY  $v_1 \in V_1, v_2 \in V_2$



-172-

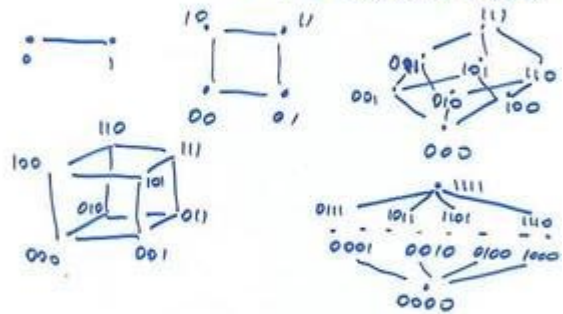
WHEELS:  $W_n$

$n$  ADDITIONAL VERTICES TO  $C_n$



CUBES:  $Q_n$

0-1 STRINGS OF LENGTH  $n$   
EDGES = CHANGING ONE BIT



-171-

NETWORKS AS GRAPHS

STAR TOPOLOGY



RING TOPOLOGY



HYBRID TOPOLOGIES



LINEAR ARRAYS



(MULTIPROCESSOR CONNECTION)

TWO-DIMENSIONAL ARRAYS



HYPERCUBES, ETC.

-173-

SUBGRAPH:  $H=(W,F)$  IS A SUBGRAPH OF  $G=(V,E)$  IF  $W \subseteq V, F \subseteq E$

 IS A SUBGRAPH OF 

$C_5$  IS A SUBGRAPH OF  $W_5$  IS SUBGRAPH OF  $K_{1,5}$   
IS SUBGRAPH OF  $K_6$

UNION OF GRAPHS  $(V_1, E_1) \cup (V_2, E_2) =$   
 $= (V_1 \cup V_2, E_1 \cup E_2)$



#W 7.2: 8 18b,c 24