

## A7. Implement shortest-path algorithm

Last semester: mean time: 3.7 hrs, median time: 4.0 hrs. We give you complete set of test cases and a GUI to play with. Efficiency and simplicity of code will be graded. Read pinned Assignment A7 note carefully: 2. Important! Grading guidelines. We demo it.

A6 due <del>Thursday</del> FRIDAY. Late deadline still Sunday Working with a partner? Group before submitting!!

We will talk about prelim 2 (24 April) on Thursday.

## Dijkstra's shortest-path algorithm

Edsger Dijkstra, in an interview in 2010 (CACM):

... the algorithm for the shortest path, which I designed in about 20 minutes. One morning I was shopping in Amsterdam with my young fiance, and tired, we sat down on the cafe terrace to drink a cup of coffee, and I was just thinking about whether I could do this, and I then designed the algorithm for the shortest path. As I said, it was a 20-minute invention. [Took place in 1956]

Dijkstra, E.W. A note on two problems in Connexion with graphs. *Numerische Mathematik* 1, 269–271 (1959).

Visit <u>http://www.dijkstrascry.com</u> for all sorts of information on Dijkstra and his contributions. As a historical record, this is a gold mine.

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## Dijkstra's shortest-path algorithm

Dijsktra describes the algorithm in English:

- □ When he designed it in 1956 (he was 26 years old), most people were programming in assembly language.
- Only one high-level language: Fortran, developed by John Backus at IBM and not quite finished.

No theory of order-of-execution time —topic yet to be developed. In paper, Dijkstra says, "my solution is preferred to another one

... "the amount of work to be done seems considerably less."

Dijkstra, E.W. A note on two problems in Connexion with graphs. *Numerische Mathematik* 1, 269–271 (1959).

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## 1968 NATO Conference on Software Engineering

- In Garmisch, Germany
- Academicians and industry people attended
- For first time, people admitted they did not know what they were doing when developing/testing software. Concepts, methodologies, tools were inadequate, missing
- The term software engineering was born at this conference.
- The NATO Software Engineering Conferences: <u>http://homepages.cs.ncl.ac.uk/brian.randell/NATO/index.html</u> Get a good sense of the times by reading these reports!



Term "software engineering" coined for this conference



































S F Far off   S= { }; F= {v}; d[v]= 0; while (F ≠ {}) {   f= node in F with min d value;   Remove f from F, add it to S;   for each neighbor w of f {   if (w not in S or F) {   d[w]= d[f] + wgt(f, w);   add w to F; bk[w]= f;   } else if (d[f]+wgt(f, w);   bk[w]= d[f] + wgt(f, w);   bk[w]= f;	For what nodes do we need a distance and a backpointer?
}}	25















<b>S F</b> S= { }; F= {v}; d[	<b>Far off</b> <b>i</b> <b>v</b> ]=0; 1 x	Directed graph n nodes reachable from v e edges leaving the n nodes	
while $(F \neq \{\})$ {	true n x		
f= node in F with	min d value; <b>n x</b>		
Remove f from F,	add it to S; <b>n x</b>	Harder: In total, how many	
for each neighbor	w of f { 🗲	times does the loop	
if (w not in S or	F) {	for each neighbor w of f	
d[w] = d[f] +	wgt(f, w);	find a neighbor and execute	
add w to F; b	k[w]= f;	the repetend?	
} else if (d[f]+w	gt(f,w) < d[w])		
d[w] = d[f] +	wgt(f, w); Ans	wer: The for-each statement	
bk[w] = f;	is executed ONCE for each node. During that		
}	execution, the repetend is executed once for		
}}	each neighbor. In total then, the repetend is		
A total of e times. <sup>33</sup>			







S F Far off	Directed graph		
S= { }; F= {v}; d[v]= 0; 1 x	n nodes reachable from v		
while $(F \neq \{\})$ true n x	e edges leaving the n nodes		
f= node in E with min d value; N X	Expected-case analysis		
Remove f from F, add it to S; n x	We know how often each		
for each neighbor w of f { true e x	statement is executed.		
if (w not in S or F) { e x	Multiply by its O() time		
$ \begin{aligned} d[w] &= d[f] + wgt(f, w); \ n-1 \ x \\ add w to F; bk[w] &= f; \ n-1 \ x \\ \} else if (d[f]+wgt (f, w) < d[w]) { e+1-n \ x } \\ d[w] &= d[f] + wgt(f, w); \ e+1-n \ x \end{aligned} $			
bk[w]= f; e+1-n ; } }}	37		



S F Far off		
S= { }; F= $\{v\}; d[v]=0;$ 1 x O(1)	1	
while $(F \neq \{\})$ { true n x O(n)	2	
f = node in F with min d value; $n \ge O(n)$	3	
Remove f from F, add it to S; n x O(n log n)	4	
for each neighbor w of f { true e x $O(e)$	5	
if (w not in S or F) { $e \times O(e)$	6	
d[w] = d[f] + wgt(f, w); n-1 x O(n)	7	
add w to F; $bk[w] = f;$ n-1 x O(n log n)	8	
$else if (d[f]+wgt (f.w) < d[w]) {e+1-n x} O(e-n)$	9	
$d[w] = d[f] + wg(f, w); e^{+1-n} x O((e-n) \log n).$	10	
$bk[w] = f;$ $e+1-n \times O(e-n)$	10	
} Dense graph, so e close to $n^*n$ : Line 10 gives $O(n^2 \log n)$		
<pre>}}</pre> Sparse graph, so e close to n: Line 4 gives O(n log	n)	