

Lecture 17 CS 2110 Spring 2018

Announcements

- □ A5 due tonight
- □ A6 is out, remember to get started early
- For the next lecture, you MUST watch the tutorial on the shortest path algorithm beforehand: <u>http://www.cs.cornell.edu/courses/cs2110/2017f</u> a/online/shortestPath/shortestPath.html
- The class on 4/10 will assume that you understand it. Watch the tutorial once or twice and execute the algorithm on a small graph.
- □ Complete Quiz 4 by 4/9





Representing Graphs



Adjacency List



Adjacency Matrix



Graph Algorithms

Search

Depth-first search

Breadth-first search

- Shortest paths
 - Dijkstra's algorithm
- Spanning trees

Algorithms based on properties

Minimum spanning trees

- Prim's algorithm
- Kruskal's algorithm

Search on Graphs

□ Given a graph (V, E) and a vertex u ∈ V
□ We want to "visit" each node that is reachable from u

There are many paths to some nodes.

How do we visit all nodes efficiently, without doing extra work?



Depth-First Search

Intuition: Recursively visit all vertices that are reachable along unvisited paths.

```
/** Visit all nodes reachable
on unvisited paths from u.
Precondition: u is unvisited.
*/
public static void dfs(int u)
    visit(u);
    for all edges (u, v):
                                      8
         if(!visited[v]):
             dfs(v);
                                 dfs(1) visits the nodes in this
                                 order: 1, 2, 3, 5, 7, 8
```

Depth-First Search

}

Intuition: Recursively visit all vertices that are reachable along unvisited paths.

```
/** Visit all nodes reachable
on unvisited paths from u.
Precondition: u is unvisited.
*/
```

public static void dfs(int u)

```
visit(u);
for all edges (u,v):
    if(!visited(v)):
        dfs(v);
```

Suppose there are n vertices that are reachable along unvisited paths and m edges:

Worst-case running time? O(n + m)Worst-case space? O(n)

DFS Quiz

In what order would a DFS visit the vertices of this graph? Break ties by visiting the lowernumbered vertex first. **1**, 2, 3, 4, 5, 6, 7, **0 1**, 2, 5, 6, 3, 6, 7, 4, 7, 8 **1**, 2, 5, 3, 6, 4, 7, **0 1**, 2, 5, 6, 3, 7, 4, 8



Depth-First Search in Java

public class Node {
 boolean visited;
 List<Node> neighbors;

Each vertex of the graph is an object of type Node

/** Visit all nodes reachable on unvisited paths from
this node.

Precondition: this node is unvisited.

```
public void dfs() {
```

}

}

visited= true;

```
for (Node n: neighbors) {
```

No need for a parameter. The object is the node.

```
if (!n.visited) n.dfs();
```

Depth-First Search Iteratively

11

Intuition: Visit all vertices that are reachable along unvisited paths from the current node.

```
/** Visit all nodes reachable on
unvisited paths from u.
Precondition: u is unvisited. */
public static void dfs(int u) {
    Stack s= (u); // Not Java!
    while (s is not empty) {
        u= s.pop();
                                                       6
        if (u not visited) {
                                        8
            visit u:
            for each edge (u, v):
                 s.push(v);
                                                5
                                       Stack:
```

Breadth-First Search

12

Intuition: Iteratively process the graph in "layers" moving further away from the source node.

/** Visit all nodes reachable on unvisited paths from u. Precondition: u is unvisited. */ public static void bfs(int u) Queue q= (u); // Not Java! while (q is not empty) { u= q.remove(); if (u not visited) { visit u; for each (u, v): q.add(v);





Analyzing BFS

Intuition: Iteratively process the graph in "layers" moving further away from the source node.

```
/** Visit all nodes reachable on
unvisited paths from u.
Precondition: u is unvisited. */
public static void bfs(int u) {
    Queue q= (u); // Not Java!
    while (
        u= q.remove();
                               Suppose there are n vertices that
        if (u not visited)
                               are reachable along unvisited paths
             visit u;
                               and m edges:
             for each (u, v):
                 q.add(v);
                               Worst-case running time? O(n+m)
                               Worst-case space? O(m)
```

BFS Quiz

In what order would a BFS visit the vertices of this graph? Break ties by visiting the lowernumbered vertex first. **1**, 2, 3, 4, 5, 6, 7, **8 1**, 2, 3, 4, 5, 6, 6, 7, 7, 8 **1**, 2, 5, 3, 6, 4, 7, **0 1**, 2, 5, 6, 3, 7, 4, 8



Comparing Search Algorithms

DFS

- □ Visits: 1, 2, 3, 5, 7, 8
- \Box Time: O(n+m)
- \Box Space: O(n)

BFS

Visits: 1, 2, 5, 7, 3, 8
Time: 0(n + m)
Space: 0(m)

