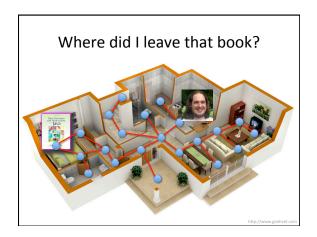


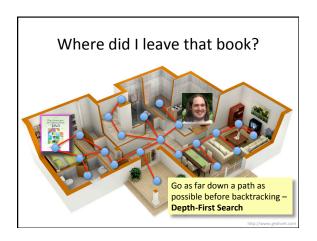
### **Announcements**

- A6 will be available tonight or tomorrow.
- Gries lunch canceled today
- Gries office hours today from 1 to 2 only

Q. Why do programmers confuse Halloween and Christmas?			
Answer. Because oct 31 = dec 25!			
Decimal	Octal	Decimal	Octal
00	00	13	15
01	01	14	16
02	02	15	17
03	03	16	20
04	04	17	21
0.5	0.5	18	22
06	06	19	23
07	07		
08	10	20	24
09	11	21	25
10	12	22	26
11	13	23	27
12	14	24	30
		25	31

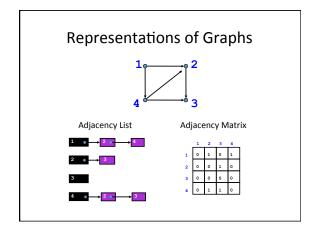






## **Graph Algorithms**

- Search
  - Depth-first search
  - Breadth-first search
- Shortest paths
  - Dijkstra's algorithm
- Minimum spanning trees
  - Prim's algorithm
  - Kruskal's algorithm



### Adjacency Matrix or Adjacency List?

- Definitions
  - -n = number of vertices
  - -m = number of edges
  - -d(u) = degree of u = number of edges leaving u
- Adjacency Matrix
- Uses space  $O(n^2)$
- Can iterate over all edges in time  $O(n^2)$
- Can answer "Is there an edge from u to v?" in O(1) time
- Better for dense graphs (lots of edges)
- Adjacency List
  - Uses space O(m + n)
  - Can iterate over all edges in time O(m+n)
  - Can answer "Is there an edge from u to v?" in O(d(u)) time
  - Better for sparse graphs (fewer edges)

## Depth-First Search

Given a graph and one of its nodes u
 (say node 1 below)



## Depth-First Search

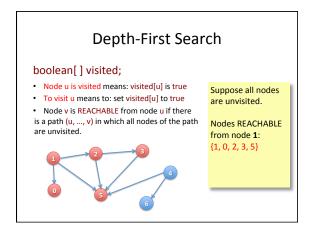
- Given a graph and one of its nodes u
   (say node 1 below)
- We want to "visit" each node reachable from u
   (nodes 1, 0, 2, 3, 5)

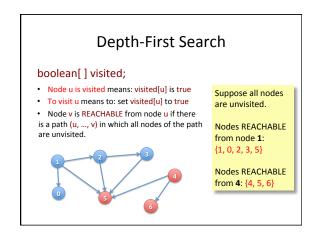


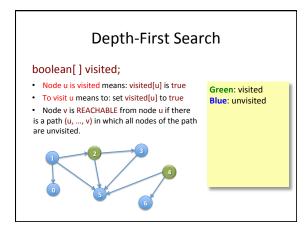
There are many paths to some nodes.

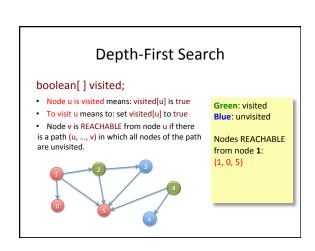
How do we visit all nodes efficiently, without doing extra work?

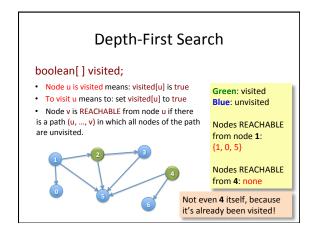
# Depth-First Search boolean[] visited; • Node u is visited means: visited[u] is true • To visit u means to: set visited[u] to true • Node v is REACHABLE from node u if there is a path (u, ..., v) in which all nodes of the path are unvisited. Suppose all nodes are unvisited.

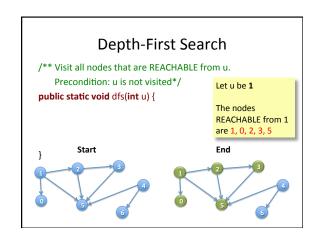


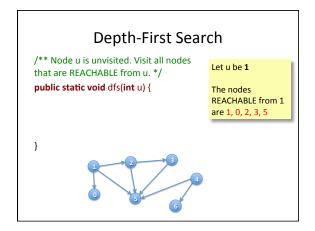


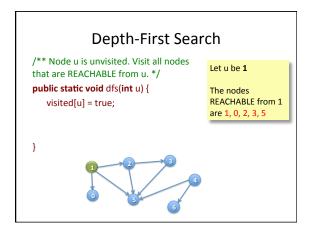


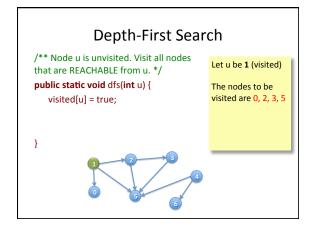


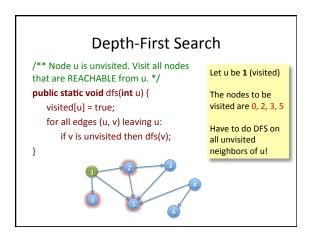


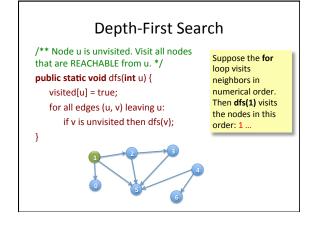


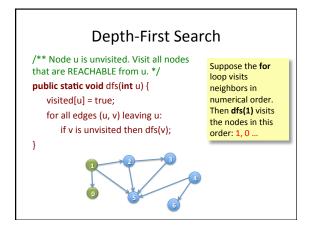


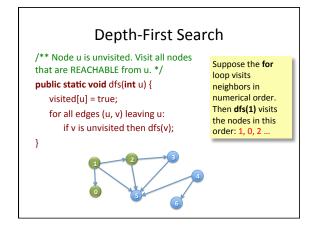


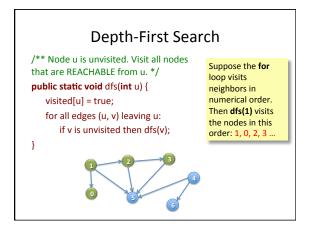












# /\*\* Node u is unvisited. Visit all nodes that are REACHABLE from u. \*/ public static void dfs(int u) { visited[u] = true; for all edges (u, v) leaving u: if v is unvisited then dfs(v); }

```
Depth-First Search

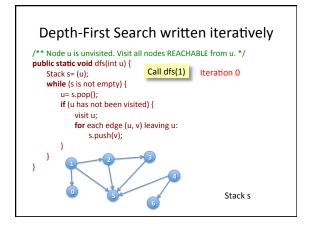
/** Node u is unvisited. Visit all nodes
that are REACHABLE from u. */
public static void dfs(int u) {
    visited[u] = true;
    for all edges (u, v) leaving u:
        if v is unvisited then dfs(v);
}

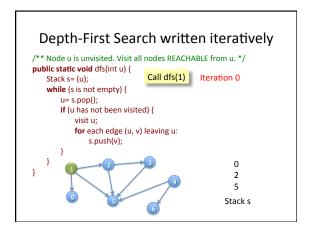
Suppose n nodes are REACHABLE along e
edges (in total). What is
    Worst-case execution?
    Worst-case space?
```

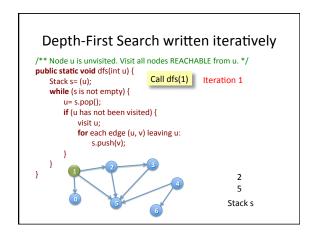
```
Depth-First Search
 /** Node u is unvisited. Visit all nodes
                                                That's all there is to
 that are REACHABLE from u. */
                                                basic DFS. You may
 public static void dfs(int u) {
                                                have to change it to
    visited[u] = true;
                                                fit a particular
                                                situation.
    for all edges (u, v) leaving u:
        if v is unvisited then dfs(v);
                                               If you don't have
                                                this spec and you
                                               do something
Example: Use different way (other than array
visited) to know whether a node has been visited
                                                different, it's
                                                probably wrong.
Example: We really haven't said what data
structures are used to implement the graph
```

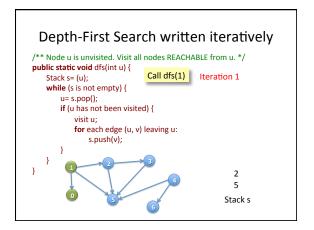
```
Depth-First Search in OO fashion
public class Node {
                                         Each node of the
   boolean visited;
                                         graph is an object
   List<Node> neighbors;
                                         of type Node
   /** This node is unvisited. Visit all nodes
       REACHABLE from this node */
                                         No need for a
   public void dfs() { <
                                         parameter. The
      visited= true;
                                         object is the node.
      for (Node n: neighbors) {
         if (!n.visited) n.dfs();
```

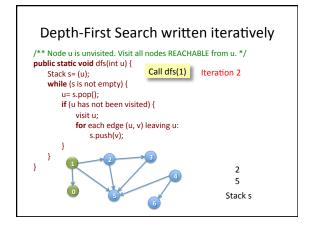
## 

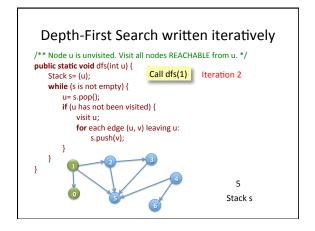


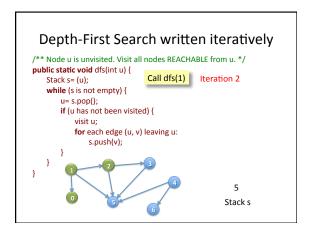












```
Depth-First Search written iteratively
/** Node u is unvisited. Visit all nodes REACHABLE from u. */
public static void dfs(int u) {
                               Call dfs(1) Iteration 2
    Stack s= (u);
    while (s is not empty) {
       u= s.pop();
                                            Yes, 5 is put on the
       if (u has not been visited) {
                                            stack twice, once for
           visit u;
                                            each edge to it. It will
           for each edge (u, v) leaving u:
                                            be visited only once.
               s.push(v);
                                                     5
                                                      5
                                                   Stack s
```

