

Prelim 1 tonight!

- 5:30 prelim is very crowded. You HAVE to follow these directions:
- 1. Students taking the normal 5:30 prelim (not the quiet room) and whose last names begin with A through Da MUST go to Phillips 101.
- 2. All other 5:30 students, go to Olin 155. You will stay there or be directed to another Olin room.
- 3. All 7:30 students go to Olin 155; you will staythere or be directed to another Olin room.
- 4. EVERYONE: Bring your Cornell id card. You will need it to get into the exam room.

Important Announcements

- □ A4 will be posted this weekend
- □ Mid-semester TA evaluations are coming up; please participate! Your feedback will help our staff improve their teaching ---this semester.

Tree Overview

Tree: data structure with nodes, similar to linked list

- □ Each node may have zero or more successors (children)
- Each node has exactly one predecessor (parent) except the root, which has none
- All nodes are reachable from root

Binary tree: tree in which each node can have at most two children: a left child and a right child









Binary trees were in A1!

You have seen a binary tree in A1.

A PhD object phd has one or two advisors. Here is an intellectual ancestral tree!



Tree terminology

M: root of this tree

G: root of the left subtree of M

B, H, J, N, S: leaves (their set of children is empty)

N: left child of P; S: right child of P

P: parent of N

M and G: ancestors of D

P, N, S: descendants of W

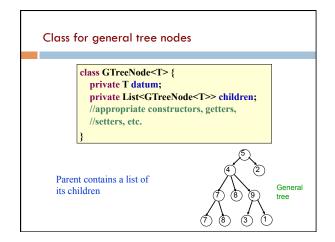
J is at *depth* 2 (i.e. length of path from root = no. of edges)

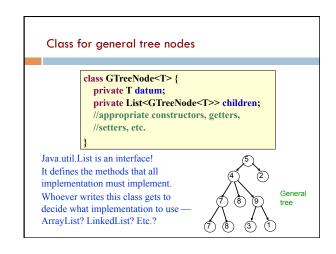
W is at *height* 2 (i.e. length of <u>longest</u> path to a leaf)

A collection of several trees is called a ...?

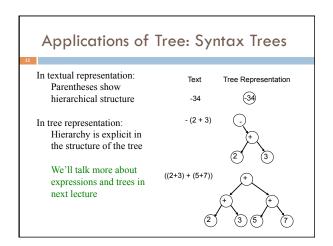
class TreeNode<T> { private T datum; private TreeNode<T> leff, right; /** Constructor: one-node tree with datum x */ public TreeNode (T d) { datum= d; left= null; right= null;} /** Constr: Tree with root value x, left tree l, right tree r */ public TreeNode (T d, TreeNode<T> l, TreeNode<T> r) { datum= d; left= l; right= r; } more methods: getValue, setValue, getLeft, setLeft, etc.

In a binary tree, each node has up to two pointers: to the left subtree and to the right subtree: One or both could be null, meaning the subtree is empty (remember, a tree is a set of nodes) In a general tree, a node can have any number of child nodes (and they need not be ordered) Very useful in some situations one of which may be in an assignment!

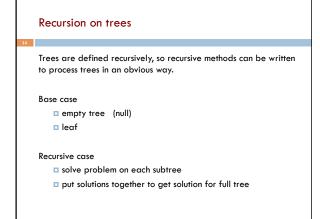


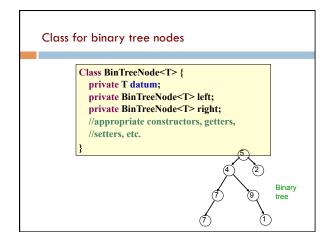


Applications of Tree: Syntax Trees Most languages (natural and computer) have a recursive, hierarchical structure This structure is implicit in ordinary textual representation Recursive structure can be made explicit by representing sentences in the language as trees: Abstract Syntax Trees (ASTs) ASTs are easier to optimize, generate code from, etc. than textual representation A parser converts textual representations to AST

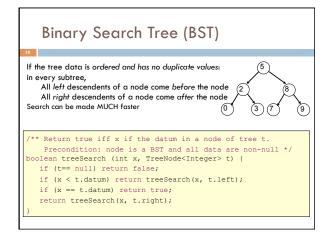


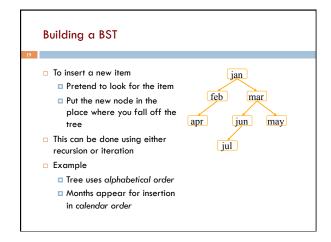
Trees are defined recursively: A binary tree is either (1) empty or (2) a value (called the root value), a left binary tree, and a right binary tree

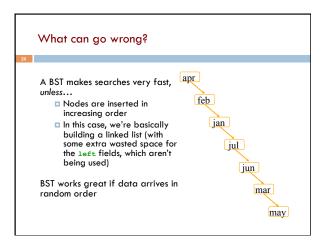




/** Return true iff x is the datum in a node of tree t*/ public static boolean treeSearch(T x, TreeNode<T>t) { if (t == null) return false; if (x.equals(t.datum)) return true; return treeSearch(x, t.left) || treeSearch(x, t.right); } VERY IMPORTANT! We sometimes talk of t as the root of the tree. But we also use t to denote the whole tree.







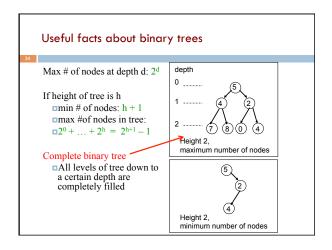
Printing contents of BST /** Print BST t in alpha order */ Because of ordering private static void print(TreeNode<T> t) { rules for a BST, it's easy if (t== null) return; to print the items in print(t.left); alphabetical order System.out.print(t.datum); ■Recursively print left subtree print(t.right); □Print the node ■Recursively print right subtree

Tree traversals Other standard kinds of "Walking" over the whole tree traversals is a tree traversal •preorder traversal Done often enough that Process root there are standard names •Process left subtree Previous example: ◆Process right subtree in-order traversal postorder traversal ■Process left subtree •Process left subtree ■Process root Process right subtree Process root ■Process right subtree •level-order traversal Note: Can do other processing •Not recursive uses a queue. besides printing We discuss later

/** Return true iff node t is a leaf */
public static boolean isLeaf(TreeNode<T> t) {
 return t!= null && t.left == null && t.right == null;
}

/** Return height of node t (postorder traversal) */
public static int height(TreeNode<T> t) {
 if (t== null) return -1; //empty tree
 return 1 + Math.max(height(t.left), height(t.right));
}

/** Return number of nodes in t (postorder traversal) */
public static int numNodes(TreeNode<T> t) {
 if (t== null) return 0;
 return 1 + numNodes(t.left) + numNodes(t.right);
}

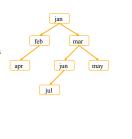


Things to think about

What if we want to delete data from a BST?

A BST works great as long as it's balanced

How can we keep it balanced? This turns out to be hard enough to motivate us to create other kinds of trees



Tree Summary

- □ A tree is a recursive data structure
 - □ Each node has 0 or more successors (children)
 - Each node except the root has exactly one predecessor (parent)
 - $\hfill\square$ All node are reachable from the root
 - □ A node with no children (or empty children) is called a leaf
- □ Special case: binary tree
 - □ Binary tree nodes have a left and a right child
 - □ Either or both children can be empty (null)
- Trees are useful in many situations, including exposing the recursive structure of natural language and computer programs