

Miscellaneous A3 due Monday night. Group early! Only 325 views of the piazza A3 FAQ yesterday morning. Everyone should look at it. Pinned Piazza note on Supplemental study material. @281. Contains material that may help you study certain topics. It also talks about how to study.

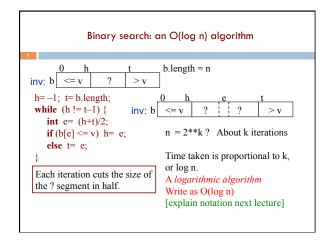
Developing methods

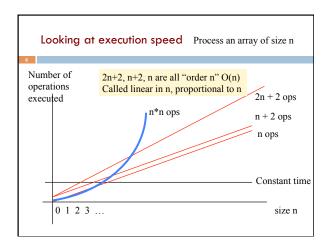
We use Eclipse to show the development of A2 function evaluate. Here are important points to take away from it.

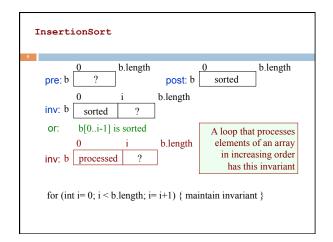
- If similar code will appear in two or more places, consider writing a method to avoid that duplication.
- 2. If you introduce a new method, write a specification for it!
- 3. Before writing a loop, write a loop invariant for it.
- 4. Have a loop exploit the structure of the data it processes.
- 5. Don't expect your first attempt to be perfect. Just as you rewrite and rewrite an essay, we rewrite programs.

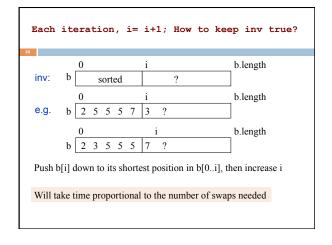
Search as in problem set: b is sorted b.length b.length pre:b b.length > v Methodology: h=-1; t=b.length; 1. Draw the invariant as a combination of pre and post **while** $(h+1 != t) {$ 2. Develop loop using 4 loopy **if** $(b[h+1] \le v) h= h+1;$ questions. else t=h+1; Practice doing this!

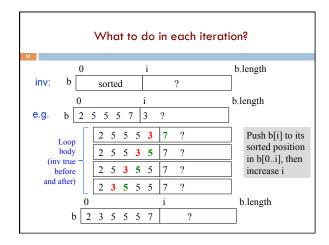
```
Search as in problem set: b is sorted
                      b.length
                                                            b.length
                                   post: b
                                            \leq v
                                 b.length
        \leq v
inv: b
                                      b[0] > v? one iteration.
 h=-1; t=b.length;
                                      b[b.length\text{-}1] \leq 0?
 while (h+1 != t) {
                                      b.length iterations
    if (b[h+1] \le v) h = h+1;
                                      Worst case: time is
    else t=h+1;
                                      proportional to size of b
 Since b is sorted, can cut? segment in half. As a dictionary search
```

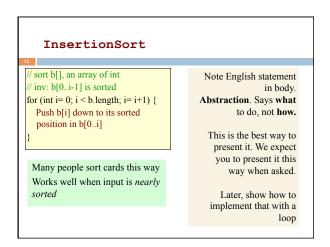




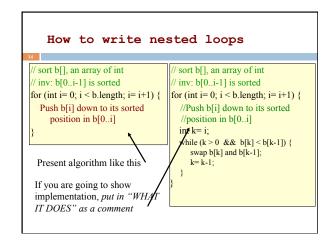




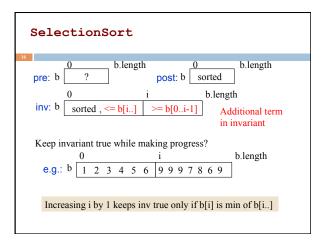




```
InsertionSort
// Q: b[0..i-1] is sorted
                                                   start?
// Push b[i] down to its sorted position in b[0..i]
                                                   stop?
int k= i;
                                                   progress?
while (k > 0 \&\& b[k] < b[k-1]) {
    Swap b[k] and b[k-1]
                                                   maintain
                                                   invariant?
    k = k-1;
// R: b[0..i] is sorted
invariant P: b[0..i] is sorted
                                       2 5 3 5 5 7
except that b[k] may be \leq b[k-1]
                                                   example
```



```
InsertionSort
// sort b[], an array of int
                                             • Worst-case: O(n2)
                                               (reverse-sorted input)
// inv: b[0..i-1] is sorted
for (int i = 0; i < b.length; i = i+1) {
                                             • Best-case: O(n)
  Push b[i] down to its sorted position
                                               (sorted input)
  in b[0..i]
                                             • Expected case: O(n2)
                                               O(f(n)): Takes time
 Pushing b[i] down can take i swaps.
                                               proportional to f(n).
                                               Formal definition later
 Worst case takes
    1 + 2 + 3 + \dots + n-1 = (n-1)*n/2
                                                   Let n = b.length
Swaps.
```

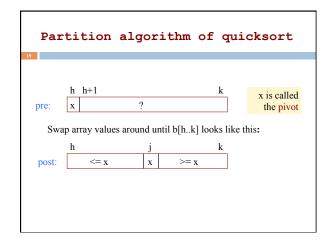


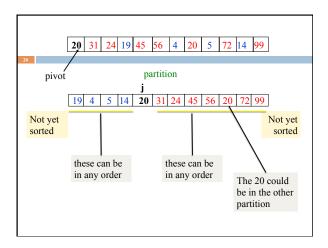
```
SelectionSort
 //sort b[], an array of int
                                         Another common way for
 // inv: b[0..i-1] sorted AND
                                         people to sort cards
      b[0..i-1] \le b[i..]
                                         Runtime
for (int i=0; i < b.length; i=i+1) {
                                         ■ Worst-case O(n<sup>2</sup>)
 int m= index of minimum of b[i..];
                                         ■ Best-case O(n<sup>2</sup>)
 Swap b[i] and b[m];
                                         ■ Expected-case O(n<sup>2</sup>)
                                                     length
 b sorted, smaller values
                                  larger values
      Each iteration, swap min value of this section into b[i]
```

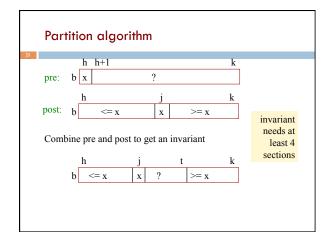
```
Swapping b[i] and b[m]

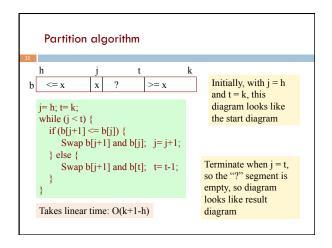
// Swap b[i] and b[m]

int t= b[i];
b[i]= b[m];
b[m]= t;
```









```
QuickSort procedure

/** Sort b[h..k]. */

public static void QS(int[] b, int h, int k) {

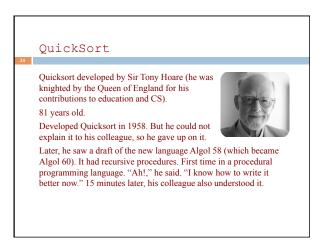
if (b[h..k] has < 2 elements) return; Base case

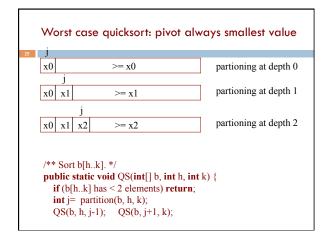
int j= partition(b, h, k);

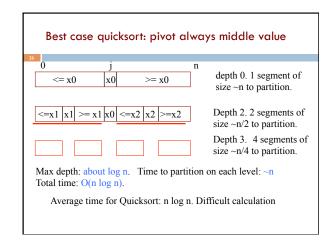
// We know b[h..j-1] <= b[j] <= b[j+1..k]

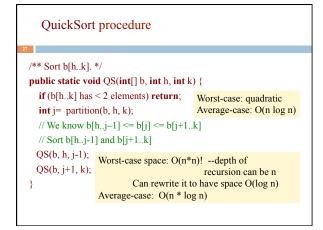
//Sort b[h..j-1] and b[j+1..k]

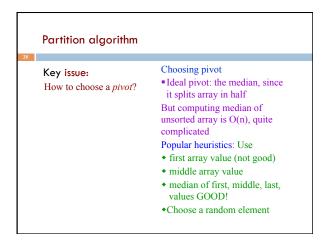
QS(b, h, j-1);
QS(b, h, j-1);
Punction does the partition algorithm and returns position j of pivot
```











Problem is that if the pivot value is always the smallest (or always the largest), the depth of recursion is the size of the array to sort. Eliminate this problem by doing some of it iteratively and some recursively

Problem is that if the pivot value is always the smallest (or always the largest), the depth of recursion is the size of the array to sort.

Eliminate this problem by doing some of it iteratively and some recursively. We may show you this later. Not today!

```
/** Sort b[h..k]. */
public static void QS(int[] b, int h, int k) {
    int h1= h; int k1= k;
    // invariant b[h..k] is sorted if b[h1..k1] is sorted
    while (b[h1..k1] has more than 1 element) {
        Reduce the size of b[h1..k1], keeping inv true
    }
}
```

QuickSort with logarithmic space /** Sort b[h..k]. */ public static void QS(int[] b, int h, int k) { int h1 = h; int k1 = k; // invariant b[h.k] is sorted if b[h1.k1] is sorted while (b[h1.k1] has more than 1 element) { int j= partition(b, h1, k1); $||b[h1..j-1]| \le |b[j]| \le |b[j+1..k1|]$ if $||b[h1..j-1]| \le ||b[j|| \le ||b[j+1..k1|]|$ Only the smaller segment is sorted { QS(b, h, j-1); h1= j+1; } recursively. If b[h1..k1] has size n, the smaller ${QS(b, j+1, k1); k1= j-1;}$ segment has size $\leq n/2$. Therefore, depth of recursion is at most log n

