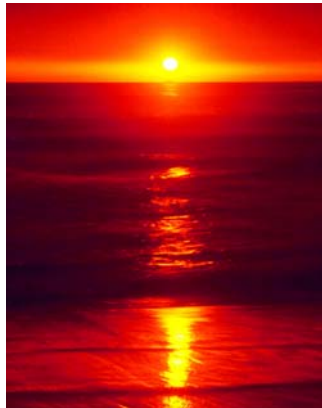




Course Review & A Few Unanswered Questions

Lecture 26
CS211 – Spring 2007

Announcements

- Final Exam
 - Monday, May 14
 - 9:00 - 11:30 am
 - Uris Auditorium
- Review Session
 - To be announced
 - Watch the website
- Check your final exam schedule!
- For exam conflicts:
 - Notify Kelly Patwell (patwell@cs.cornell.edu) *today*
 - You must provide
 - Your entire exam schedule
 - Include the course numbers
- Definition of exam conflict:
 - Two exams at the same time or
 - Three or more exams within 24 hours

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Announcements

- Check the course website for additional announcements as the final exam approaches
 - Consulting ends this week
 - No consulting on slope day
 - Office hours continue until Final Exam
 - There may be changes (TAs have exams, too)
 - Any changes will be announced on the course website
- Jealous of the glamorous life of a CS consultant?
 - We're recruiting next-semester consultants for CS100 and CS211
 - Interested students should fill out an application, available in 303 Upson Hall

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Course Evaluations

- Worth one assignment point
 - Will count as 1% of your course grade
 - This is a regular point, *not* a bonus point
 - Anonymity
 - We get a list of who completed the course evaluations and a list of responses, but no link between names & responses
- Closes Friday May 4 midnight
- <http://www.engineering.cornell.edu/CourseEval>
 - This link also appears on the CS211 Announcements page

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Course Overview

- Programming concepts
 - We use Java, but the goal is to understand the ideas rather than to become a Java expert
 - Recursion
 - Object-Oriented Programming
 - Interfaces
 - Graphical User Interfaces (GUIs)
- Data structure concepts
 - The goal here is to develop skill with a set of tools that are widely useful
 - Induction
 - Asymptotic analysis (big-O)
 - Arrays, Trees, and Lists
 - Searching & Sorting
 - Stacks & Queues
 - Priority Queues
 - Sets & Dictionaries
 - Graphs

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Programming Concepts

- Recursion
 - Stack frames
 - Exceptions
- Object-oriented programming
 - Classes and objects
 - Primitive vs. reference types
 - Dynamic vs. static types
 - Subtypes and Inheritance
 - Overriding
 - Shadowing
 - Overloading
 - Upcasting & downcasting
 - Inner & anonymous classes
- Interfaces
 - Type hierarchy vs. class hierarchy
 - The Comparable interface
 - Iterators & Iterable
- GUIs
 - Components, Containers, & Layout Managers
 - Events & listeners

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Data Structure Concepts

- Induction
- Grammars & parsing
- Asymptotic analysis (big-O)
 - Solving recurrences
 - Lower bounds on sorting
- Basic building blocks
 - Arrays
 - Lists
 - Singly- and doubly-linked
 - Trees
 - Binary Search Trees (BSTs)
- Searching
 - Linear- vs. binary-search
- Sorting
 - Insertion-, Selection-, Merge-, Quick-, and Heap-sort
- Useful ADTs (& implementations)
 - Stacks & Queues
 - Arrays & lists
 - Priority Queues
 - Heaps
 - Array of queues
 - Sets & Dictionaries
 - Bit vectors (for Sets)
 - Arrays & lists
 - Hashing & Hashtables
 - BSTs (& balanced BSTs)
 - Graphs...

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Overview of Graphs

- Mathematical definition of a graph (directed, undirected)
- Representations
 - Adjacency matrix
 - Adjacency list
- Topological sort
- Coloring & planarity
- Searching (BFS & DFS)
- Dijkstra's shortest path algorithm
- Minimum Spanning Trees (MSTs)
 - Prim's algorithm (growing a single tree)
 - Kruskal's algorithm (build a forest by adding edges in order)

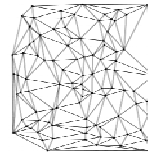
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Some Unsolved Problems

Complexity of Bounded-Degree Euclidean MST

- The Euclidean MST (Minimum Spanning Tree) problem:
 - Given n points in the plane, determine the MST
 - Can be solved in $O(n \log n)$ time by first building the Delaunay Triangulation
- Bounded-degree version:
 - Given n points in the plane, determine the MST where each vertex has degree $\leq d$
 - Known to be NP-hard for $d=3$ [Papadimitriou & Vazirani 84]
 - $O(n \log n)$ algorithm for $d=5$ or greater
 - Can show Euclidean MST has degree ≤ 5
 - Unknown for $k=4$



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Complexity of Euclidean MST in R^d

- Given n points in dimension d , determine the MST
 - Is there an algorithm with runtime close to the $\Omega(n \log n)$ lower bound?
- Can solve in time $O(n \log n)$ for $d=2$
- For large d , it appears that runtime approaches $O(n^2)$
- Best algorithms for general graphs run in time linear in m = number of edges
 - But for Euclidean distances on points, the number of edges is $n(n-1)/2$

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$O(n^2)$ Time for X+Y Sorting?

How long does it take to a sort an n -by- n table of numbers?



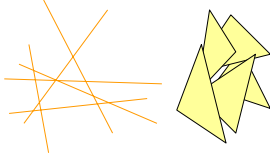
+	1	3	5	8
2	3	5	7	10
10	11	13	15	18
12	13	15	17	20
14	15	17	19	22

- $O(n^2 \log n)$ because there are n^2 numbers in the table
- What if it's an *addition table*?
 - Shouldn't it be easier to sort than an arbitrary set of n^2 numbers?
- There is a technique that uses just $O(n^2)$ comparisons [Fredman 76]
 - But it uses $O(n^2 \log n)$ time to decide which comparisons to use [Lambert 92]
- This problem is closely related to the problem of sorting the vertices of a line arrangement

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3SUM in Subquadratic Time?

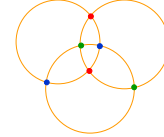
- Given a set of n integers, are there three that sum to zero?
 - $O(n^2)$ algorithms are easy (e.g., use a hashtable)
 - Are there better algorithms?
- This problem is closely related to many other problems [Gajentaan & Overmars 95]
 - Given n lines in the plane, are there 3 lines that intersect in a point?
 - Given n triangles in the plane, does their union have a hole?



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Great-Circle Graph 3-Colorable?

- Build a graph by drawing great-circles on a sphere
 - Create a vertex for each intersection
 - Assume no three great circles intersect in a point
- Is the resulting graph 3-colorable?
 - All arrangements for up to 11 great circles have been verified as 3-colorable
- For *general* circles on the sphere (or for circles on the plane) the graph can require 4 colors



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The Big Question: Is $P=NP$?

- P is the class of problems that can be solved in polynomial time
 - These problems are considered *tractable*
 - Problems that are not in P are considered *intractable*
- NP represents problems that, for a *given solution*, the solution can be *checked* in polynomial time
 - But *finding* the solution may be hard
- For ease of comparison, problems are usually stated as yes-or-no questions
- Examples
 - Given a weighted graph G and a bound k , does G have a spanning tree of weight at most k ?
 - This is in P because we have an algorithm for the MST with runtime $O(m + n \log n)$
 - Given graph G , does G have a cycle that visits all vertices?
 - This is in NP because, given a possible solution, we can check in polynomial time that it's a cycle and that it visits all vertices

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Current Status: P vs. NP

- It's easy to show that $P \subseteq NP$
- Most researchers believe that $P \neq NP$
 - But at present, no proof
- We do have a large collection of *NP-complete problems*
 - If any NP-complete problem has a polynomial time algorithm, then they *all* do
- A problem B is *NP-complete* if
 - it is in NP
 - any other problem in NP reduces to it efficiently
- Thus by making use of an *imaginary* fast subroutine for B , any problem in NP could be solved in polynomial time
 - the Boolean satisfiability problem is NP-complete [Cook 1971]
 - many useful problems are NP-complete [Karp 1972]
 - By now thousands of problems are known to be NP-complete

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Some NP-Complete Problems

- Graph coloring: Given graph G and bound k , is G k -colorable?
- Planar 3-coloring: Given planar graph G , is G 3-colorable?
- Traveling salesperson: Given weighted graph G and bound k , is there a cycle of cost $\leq k$ that visits each vertex exactly once?
- Hamiltonian cycle: Give graph G , is there a cycle that visits each vertex exactly once?
- Knapsack: Given a set of items i with weights w_i and values v_i , and numbers W and V , does there exist a subset of at most W items whose total value is at least V ?
- What if you really *need* an algorithm for an NP-complete problem?
 - Some special cases can be solved in polynomial time
 - If you're lucky, you have such a special case
 - Otherwise, once a problem is shown to be NP-complete, the best strategy is to start looking for an approximation
- For a while, a new proof showing a problem NP-complete was enough for a paper
 - Nowadays, no one is interested unless the result is somehow unexpected

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Good luck on the final!
Thanks for an enjoyable semester!
Have a great summer!

