## Question 1: (30 points)

Part (a): (2 points)
What does vector v look like after the following script is executed?

```
v = [0 1];
for k = 1:3
    v = [1 v];
end
```

Before: 01

After: __ 11101

Part (b): (2 points)
What does vector w look like after the following script is executed?

```
w= [[3 3 2 1}]|
w(w(3)) = w(1);
```

Before: 321
After: _- 321

Part (c): (10 points)
Assume that a and b are initialized scalars with $\mathrm{a}<\mathrm{b}$. Consider the following code fragment:

$$
\begin{aligned}
& x=\operatorname{linspace}(a, b, n) ; \\
& y=\sin (x) ;
\end{aligned}
$$

Write an equivalent fragment that does not use function linspace and only calls the sine function with scalar input values.

```
h= (b-a)/(n-1);
for k= 1:n
    x(k)= a + (k-1)*h;
    y(k)= sin(x(k));
end
```


## Question 1, continued

Part (d): (6 points)

Assume that score is an initialized vector containing integer values in the interval [0,100]. (For example, score is a vector of student scores on a test). Write one statement on the blank below to complete the code fragment for drawing a histogram of the scores (with one bar for each score values $0,1,2, \ldots, 100$ ).

```
count= zeros(1,101); % count will be used to store the histogram data
for k= 1:length(score)
    count(score(k)+1)= count(score(k)+1) + 1;
end
bar(0:100, count) % draw a histogram of the scores
```

Part (e): (5 points)
Given the following function:

$$
\begin{aligned}
& \text { function } f=\text { evaluateQuadratic }(a, b, c, x) \\
& f=a^{*}\left(x^{\wedge} 2\right)+b^{*} x+c
\end{aligned}
$$

What is the output when the following script is executed?

## Output:

$\mathrm{f}=$
11
$a=1 ; \quad b=-1 ; \quad c=3 ; \quad x=2$;
$f=$ evaluateQuadratic $(c, b, a, x)$

## Out

Part (f): (5 points)
Given the following function:

```
function y = flip(x)
n= length(x);
for k= 1:n
    x(n-k+1)= x(k);
end
y= x;
```

What is the output when the following script is executed?

```
y= [10 20 30 40];
y= flip(y)
```


## Output:

$y=$| $y=$ |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  | 10 | 20 | 20 | 10 |  |

## Question 2: (20 points)

Write a function s2hms to convert a time in seconds to a time in hours, minutes, and seconds. The function has one parameter (sec) and returns three numbers: h, m, and s. Read the given function comment below; write the function header and the function body.

```
function [h, m, s] = s2hms(sec)
% Convert a time expressed in seconds (sec) to the number of hours (h),
% minutes (m), and seconds (s). h and m are integer values and
% 0<=m,s<60. Assume sec>=0.
h= floor(sec/3600);
sec= sec - h*3600; % OR: sec= rem(sec,3600)
m= floor(sec/60);
s= sec - m*60;
```

Assume function s 2 hms has been written correctly. Write a script to print the number of times in a day that $\mathrm{h}>\mathrm{m}>\mathrm{s}$. Check whole seconds from 0 to $60 \times 60 \times 24-1$. You must use function s 2 hms to solve this problem.

```
maxSeconds= 60*60*24-1;
count= 0; % No. of times when h>m>s
for k= 0:maxSeconds
    [h, m, s]= s2hms(k);
    if (h>m && m>s)
        count= count + 1;
    end
end
disp(sprintf('h>m>s %d times a day', count))
```


## Question 3: (25 points)

Complete function drawFrame below to draw a "frame" made up of black and white disks. Each disk is of unit radius and the lower left disk is centered at $(0,0)$. Shown on the right is an example of a 5 -by-4 frame with a spacing of 0.5 between disks. The function call to produce this example is drawFrame $(5,4,0.5)$.

Assume that function DrawDisk is available. To draw a black disk of unit radius at position (3,4): $\operatorname{DrawDisk}\left(3,4,1,{ }^{\prime} k^{\prime}\right)$

Write only the code to draw the disks. The grid lines are provided for your convenience-you do not need to draw them.


```
function drawFrame(h,w,s)
% Draw a frame composed of h-by-w black and white disks of unit radius
% with space s between the disks. Black disks form the border; white
% disks are in inside. The lower left disk is centered at (0,0).
% Assume h,w>2 and s>=0.
```

axis equal
hold on

```
d= 2+s; % distance from center to center
for y= 0 : d : (h-1)*d
    for x= 0 : d : (w-1)*d
        if (x==0 || x==(w-1)*d || y==0 || y==(h-1)*d) % border
            DrawDisk(x,y,1,'k')
        else
            DrawDisk(x,y,1,'w')
        end
    end
end
```

```
% An alternative
d= 2+s; % distance from center to center
for r= 1:h
    y= (r-1)*d;
    for c= 1:w
        x= (c-1)*d;
        if (r==1 || r==h || c==1 || c==w) % border
            DrawDisk(x,y,1,'k')
        else
            DrawDisk(x,y,1,'w')
        end
    end
end
```


## Question 4: (25 points)

Complete function findPrefix ( $\mathrm{p}, \mathrm{s}$ ) below to return the position of the first occurrence of a word that begins with string $p$ in string $s$. If no word in $s$ begins with string $p$, the function returns -1 . For full credit, your algorithm should be efficient-stop after the first occurrence has been found. The only built-in functions that you may use are length and strcmp. Assume that p contains only lower case letters and s contains lower case letters and blanks. Below are four examples:

| p | s | Returned value |
| :---: | :--- | :---: |
| mat | there is a mat in the lab | 12 |
| mat | there is a bat in the lab | -1 |
| mat | matt uses matlab on a mat | 1 |
| mat | format a plot in matlab | 18 |

1234567891111111111222222
0123456789012345
In the last example above, the word "format" in s includes the substring 'mat' but that doesn't count since 'mat' does not appear in the beginning of the word.

```
function k = findPrefix(p, s)
% k is the position in string s of the first occurrence of a word that
% begins with string p
% k is -1 if no word in string s begins with string p
% p contains lower case letters only
% s contains lower case letters and blanks only
```

```
len= length(p); % the length of the word pattern
s= [' ' s]; % Pad s with a leading space
k= 2; % current index in s to start checking
found= 0;
% While prefix p is not found, check every substring s(k:k+len-1) against p
while k<=length(s)-len+1 && ~found
    if s(k-1)==' ' % only need to look for p if a blank is at s(k-1)
        found= strcmp(s(k:k+len-1), p);
    end
    k= k+1;
end
if ~found % OR: if found==0
    k= -1;
else
    k= k-2; % need -1 because in loop body k incremented after comparison
                        % need another -1 because s was padded with a leading space
end
```

```
pat= [' ' p]; % the word pattern to look for
len= length(pat); % the length of the word pattern
% Pad string s with a leading blank
s= [' ' s];
k= 1;
% While prefix p is not found, check every substring s(k:k+len-1) against pat
while k<=length(s)-len+1 && strcmp(s(k:k+len-1), pat)~=1
    k= k+1;
end
if k>length(s)-len+1 % k exceeds possible starting index, so prefix not found
    k= -1;
end
% If found, k needs no adjustment since both p and s were padded with an
% extra leading blank.
```

```
pat= [' ' p]; % the word pattern to look for
len= length(pat); % the length of the word pattern
% Pad string s with a leading blank
s= [' ' s];
k= 1;
found= 0;
% While prefix p is not found, check every substring s(k:k+len-1) against pat
while k<=length(s)-len+1 && ~found
    found= strcmp(s(k:k+len-1), pat);
    k= k+1;
end
if found % OR: if found==1
    k= k-1; % need -1 because in loop body k incremented after comparison
else
    k= -1;
end
```

```
% Check first word in s
if strcmp(s(1:length(p)), p)
    k= 1;
    return
end
% Check all of s
pat= [' ' p]; % the word pattern to look for
len= length(pat); % the length of the word pattern
k= 1; % ok to start at 2 (assume s starts with a letter)
found= 0;
% While prefix p is not found, check every substring s(k:k+len-1) against pat
while k<=length(s)-len+1 && ~found
    found= strcmp(s(k:k+len-1), pat);
    k= k+1;
end
if ~found % OR: if found==0
    k= -1;
end
% If found, k needs no adjustment:
% The 1st char in pat is the padded blank, so need to add 1 to k, but
% an extra 1 was added already since in the loop body k is incremented
% after the comparison.
```

