Name: $\qquad$ NetID: $\qquad$
(Legibly print last name, first name, middle name)
Statement of integrity: It is a violation of the Code of Academic Integrity to look at any exam other than your own, to look at any other reference material, or to otherwise give or receive unauthorized help. Understanding this, I declare I shall not give, use, or receive unauthorized aid in this examination.
(Signature)

Circle your lecture time: 9:05 or 11:15
Circle your discussion instructor's name:

|  | Tuesday | Wednesday |
| ---: | :---: | :---: |
| $10: 10$ |  | Noam Eshed |
| $11: 15$ |  | Noam Eshed |
| $12: 20$ | Zhilong Li | Joseph Kim |
| $1: 25$ | Vaishnavi Dhulkhed | Joseph Kim |
| $2: 30$ | Darian Nwankwo | Darian Nwankwo |
| $3: 35$ | Darian Nwankwo | Zhilong Li |

Instructions:

- This is a 90 -minute, closed-book exam; no calculators are allowed.
- The exam is worth a total of 100 points, so it's about one point per minute!
- Read each problem completely, including any provided code, before starting it.
- Raise your hand if you have any questions.
- Clarity, conciseness, and good programming style count for credit.
- If you supply multiple answers, we will grade only one.
- Use only Matlab code. No credit for code written in other programming languages.
- Assume there will be no input errors.
- Do not modify given code unless instructed to do so.
- Do not write user-defined functions or subfunctions unless instructed to do so.
- Do not use switch, try, catch, break, continue, or return statements.
- Do not use built-in functions that have not been discussed in the course.
- You may find the following Matlab predefined functions useful:
abs, sqrt, rem, floor, ceil, round, rand, zeros, ones, linspace, length, input, fprintf, disp, bar
Examples:
rem $(5,2) \rightarrow 1$, the remainder of 5 divided by 2
rand $(1,3) \rightarrow 1$ row 3 columns of numbers, each uniformly random in the open interval $(0,1)$
floor(6.9), floor(6) $\rightarrow 6$, rounds down to the nearest integer
ceil(8.1), ceil(9) $\rightarrow 9$, rounds up to the nearest integer
zeros $(1,4) \rightarrow 1$ row 4 columns of zeros
length $\left(\left[\begin{array}{ll}2 & 4\end{array}\right]\right) \rightarrow 3$, length of a vector


## Question 1: (17 points)

(a) Write in the box below the first six lines of output that would be produced by executing the following script. Write on the blank the total number of lines of output that would be produced by the script.

```
for t = 1:4
    for u = 5:6
        disp(u-t)
        v(u-t)= t+10;
    end
    disp(v)
end
```

First 6 lines of output:

How many lines of output will be produced in total? $\qquad$
(b) Suppose you are charged one dollar for every relational operation that is executed. (Note: $>=$ and $\sim=$ are examples of relational operators. \&\& and \| are not relational operators; they are logical operators.) What is the output and how much is the fee that you have to pay after executing the following script?

```
a=9; b=7; c=9;
if (a>=c && c>b) || a==0
    disp('D')
elseif c>b
    disp('E')
end
if b>=c || a==0
    disp('F')
end
```

| Output: | Fee (in dollars): |
| :--- | :--- |
|  |  |

(c) What will be printed when the following script is executed? Use the specified print format.

| Script | Function |
| :---: | :---: |
| $\mathrm{g}=\left[\begin{array}{ll}2 & 4\end{array}\right] ;$ | function $\mathrm{h}=$ fun ( $\mathrm{g}, \mathrm{r}$ ) |
| $\mathrm{h}=10$; | $\mathrm{g}(1)=\mathrm{g}(2)$; |
| $s=$ fun (g, h) ; | $\mathrm{g}(2)=\mathrm{g}(1)$; |
| fprintf('s is \%d\n', s) | $\mathrm{h}=\mathrm{r}-\mathrm{g}(1)$; |
| fprintf('g(1) is \% ${ }^{\text {d }} \mathrm{n}$ ', $\mathrm{g}(1)$ ) | fprintf('g(2) is \% ${ }^{\text {d }}$ ( $\mathrm{n}^{\prime}$, $\mathrm{g}(2)$ ) |
| fprintf('h is \%d\n', h) | fprintf('h is \%d\n', h) |



## Question 2: (15 points)

(a) Complete the loop condition below so that the user is prompted until they enter an odd integer between 1 and 35 (inclusive).

```
n = input('Place an odd bet (1-35): ');
```

```
while
    n = input('Place an odd bet (1-35): ');
end
```

(b) Write a function named recomputeEvens that has one input parameter v (a vector) and returns a vector of the same length whose odd-indexed elements match those of v but whose even-indexed elements are equal to the average of that element's left and right neighbors. You may assume that v has an odd length of at least 3.

Example: recomputeEvens([1-2 4]) should return [1 $\left.\begin{array}{lll}1 & 2.5 & 4\end{array}\right]$.
Note: You must write the function header along with the function body, but you do not need to write the function comment.

## Question 3: (25 points)

(a) Assume income tax is levied as follows: the first $\$ 20,000$ of a person's income is not taxed, then the next $\$ 30,000$ is taxed at $25 \%$, the next $\$ 50,000$ above that is taxed at $30 \%$, and finally any income over $\$ 100,000$ is taxed at $40 \%$. As an example, a person earning $\$ 60,000$ of income would owe $\$ 10,500$ in tax $(0 \times \$ 20000+0.25 \times \$ 30000+0.3 \times \$ 10000)$, for an effective rate (tax divided by income) of $17.5 \%$, i.e., 0.175. Implement the following function to compute someone's tax burden (the built-in functions rem, min, and max are allowed if you want to use them, but they are not necessary):

```
function [t, r] = incomeTax(income)
% Compute the amount of tax, t, owed on income dollars, and also compute the
% effective tax rate, r, a value between 0 and 1. Do not worry about rounding
% money to the nearest cent.
```

(b) There is a proposal to introduce a new tax bracket affecting incomes over $\$ 250,000$. Write a script to analyze the impact of this change. Assume a vector incomes is present in the Workspace containing the incomes (in dollars) of everyone in the district. Your script should print the number of people who would be affected by this change, as well as the highest effective rate currently levied on one of them. You should call function incomeTax (and may assume it has been implemented correctly) from part (a), but the only built-in functions you may use are length, disp, fprintf.

```
% Assume vector incomes is given; it is not empty.
% Write your code below.
```


## Question 4: (18 points)

(a) Implement the following function as specified:

```
function rv = reverseVector(v)
% rv has the same elements as vector v but with the order reversed.
% Do NOT use vectorized code. The only built-in function allowed is length.
```

(b) The binary representation of a number is expressed in the base- 2 numeral system using only 0 s and 1s. For example, the binary representation of 5 is [ $\left.\begin{array}{lll}1 & 0 & 1\end{array}\right]$ because $5=\mathbf{1} \times 2^{2}+\mathbf{0} \times 2^{1}+\mathbf{1} \times 2^{0}$. The 0 s and 1 s are ordered left to right starting with "the most significant bit," i.e., the coefficient ( 0 or 1 ) of the highest power of 2 needed, and ending with the least significant bit, i.e., the coefficient of the 0th power of 2. To compute the binary representation (vector) of a positive integer number, you will work backwards, finding the least significant bit first:

- Divide the number by 2. Append the remainder to the results vector, and replace the number with the integer quotient.
- Repeat the above step as long as the number is positive.
- Reverse the order of the elements in the vector.

As an example, below is the process for computing the binary representation of the number 12:

| Division | Quotient | Remainder | Vector |
| ---: | :---: | :---: | :--- |
| $1 / 2$ | 6 | $\mathbf{0}$ | $\left[\begin{array}{lll}\mathbf{0}\end{array}\right]$ |
| $6 / 2$ | 3 | $\mathbf{0}$ | $\left[\begin{array}{lll}0 & \mathbf{0}\end{array}\right]$ |
| $3 / 2$ | 1 | $\mathbf{1}$ | $\left[\begin{array}{lll}0 & 0 & \mathbf{1}\end{array}\right]$ |
| $1 / 2$ | 0 | $\mathbf{1}$ | $\left[\begin{array}{llll}0 & 0 & 1 & \mathbf{1}\end{array}\right]$ |

Reverse the vector to get the binary representation: $\left.\begin{array}{llll}1 & 1 & 0 & 0\end{array}\right]$
By making effective use of function reverseVector from Part (a), implement the following function using the algorithm given above:

```
function v= binaryVector(num)
% Vector v is the binary representation of positive integer num.
% The only built-in functions allowed are rem, floor
```


## Question 5: (25 points)

Write a script that assembles and draws a stone wall using random bricks from a quarry. The end result should resemble the figure below, where stones have been colored according to their size. The parameters of the job are as follows:

- Stones are all 10 cm tall, but their widths are random, varying uniformly between 5 cm and 40 cm (not restricted to an integer number of cm )
- The wall must be at least 200 cm wide; stones may protrude past that edge, but no new stones should be placed after it
- The wall must be 100 cm ( 10 stones) high
- The skinniest $(5 \mathrm{~cm})$ stones should be colored dark grey, while the widest $(40 \mathrm{~cm})$ stones should be colored light grey; stones of intermediate width should have a color that linearly interpolates between these two shades
- The first stone should have its lower-left corner at coordinate $(0,0)$

Assume the availability of a function DrawRect (xLeft, yBottom, width, height, color) that draws a rectangle whose lower-left corner is (xLeft, yBottom), whose width and height are width and height, and which is filled with the color specified by the 3 -vector color. Your code only needs to draw the stones (axes and markers are shown above just for reference).
Hint: DECOMPOSE! First work on drawing a single row of white rectangles, then build up multiple rows, and finally revise your code to deal with different shades of grey.


Write your code on the next page.
[Question 5, continued]
\% Script to assemble and draw a stone wall figure; axis equal off; hold on darkGrey $=\left[\begin{array}{lll}0.5 & 0.5 & 0.5\end{array}\right]$;
lightGrey = [0.9 0.9 0.9];

