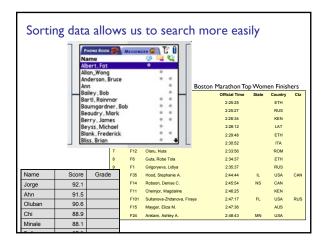


- Recursion
- Today's Lecture:
 - Sorting and searching
 - Insertion sort, linear search
 - Read about Bubble Sort in Insight "Divide and conquer" strategies
 - Binary search

Announcements

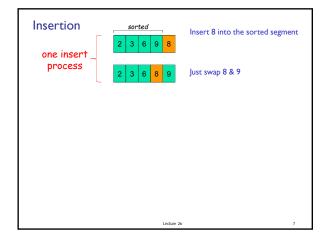
- Discussion in computer lab this week
- P6 due Thursday at 11pm
- Final exam: Dec 7th 2pm for both Lec I and Lec 2

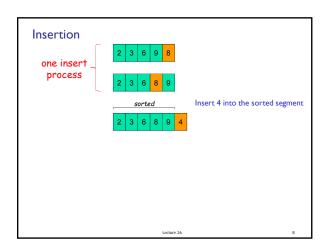


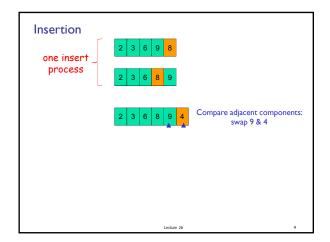
There are many algorithms for sorting

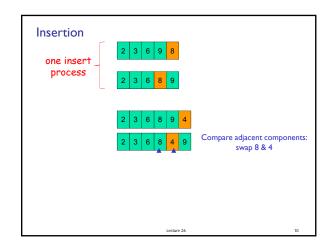
- Insertion Sort (to be discussed today)
- Bubble Sort (read Insight §8.2)
- Merge Sort (to be discussed Thursday)
- Quick Sort (a variant used by Matlab's built-in sort function)
- Each has advantages and disadvantages. Some algorithms are faster (time-efficient) while others are memory-efficient
- Great opportunity for learning how to analyze programs and algorithms!

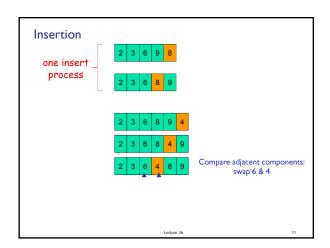
The Insertion Process • Given a sorted array x, insert a number y such that the result is sorted

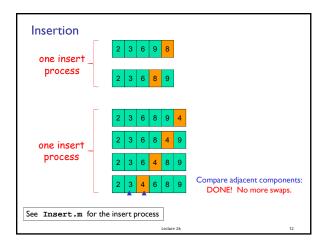












```
Sort vector x using the Insertion Sort algorithm

Need to start with a sorted subvector. How do you find one?

X

Length I subvector is "sorted"

Insert x(2): [x(1:2),C,S] = Insert(x(1:2))

Insert x(3): [x(1:3),C,S] = Insert(x(1:3))

Insert x(4): [x(1:4),C,S] = Insert(x(1:4))

Insert x(5): [x(1:5),C,S] = Insert(x(1:5))

Insert x(6): [x(1:6),C,S] = Insert(x(1:6))

InsertionSort.m
```

Insertion Sort vs. Bubble Sort
Read about Bubble Sort in Insight §8.2
Both algorithms involve the repeated comparison of adjacent values and swaps
Find out which algorithm is more efficient on average

Other efficiency considerations

- Worst case, best case, average case
- Use of subfunction incurs an "overhead"
- Memory use and access
- Example: Rather than directing the insert process to a subfunction, have it done "in-line."
- Also, Insertion sort can be done "in-place," i.e., using "only" the memory space of the original vector.

Sort an array of objects

- Given x, a 1-d array of Interval references, sort x according to the widths of the Intervals from narrowest to widest
- Use the insertion sort algorithm
- How much of our code needs to be changed?

```
A. No changeB. One or two statementsC. About half the codeD. Most of the code
```

Lecture 26

Searching for an item in an unorganized collection?

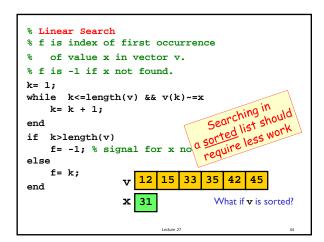
- May need to look through the whole collection to find the target item
- E.g., find value x in vector v

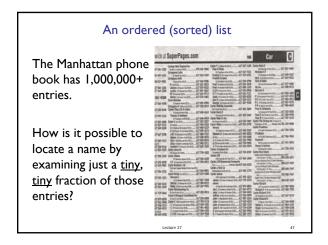


Linear search

cture 27

```
% Linear Search
% f is index of first occurrence
   of value x in vector v.
% f is -1 if x not found.
k=1;
while k \le length(v) \&\& v(k) = x
                                           A. squared
    k = k + 1;
end
                                           B. doubled
if k>length(v)
                                           C. the same
    f= -1; % signal for x not found
else
                                           D. halved
    f= k;
end
Suppose another vector is twice as long as v. The
expected "effort" required to do a linear search is ...
```





Key idea of "phone book search": repeated halving

To find the page containing Pat Reed's number...

while (Phone book is longer than I page)
Open to the middle page.
if "Reed" comes before the first entry,
Rip and throw away the 2nd half.
else
Rip and throw away the Ist half.
end
end

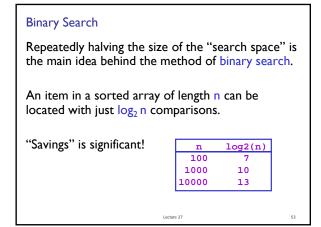
What happens to the phone book length?

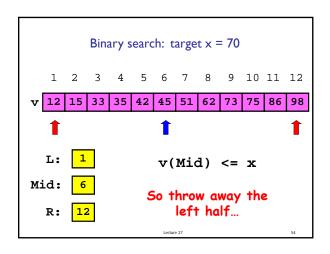
Original: 3000 pages
After 1 rip: 1500 pages
After 2 rips: 750 pages
After 3 rips: 375 pages
After 4 rips: 188 pages
After 5 rips: 94 pages
:
After 12 rips: 1 page

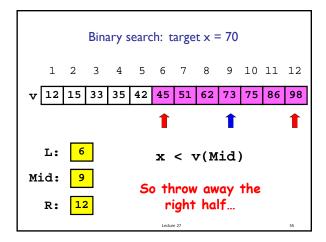
Binary Search

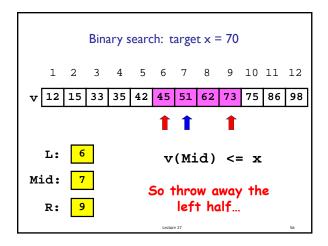
Repeatedly halving the size of the "search space" is the main idea behind the method of binary search.

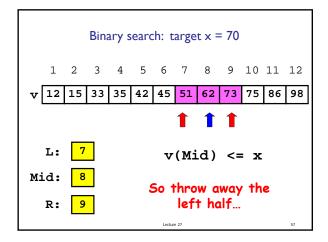
An item in a sorted array of length n can be located with just log_2 n comparisons.

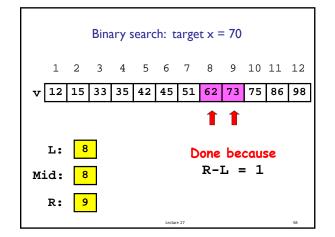












```
function L = binarySearch(x, v)
% Find position after which to insert x. v(1)<...<v(end).
% L is the index such that v(L) <= x < v(L+1);
% L=0 if x<v(1). If x>v(end), L=length(v) but x~=v(L).
% Maintain a search window [L..R] such that v(L)<=x<v(R).
% Since x may not be in v, initially set ...
L=0; R=length(v)+1;
% Keep halving [L..R] until R-L is 1,
% always keeping v(L) <= x < v(R)
while R ~= L+1
    m= floor((L+R)/2); % middle of search window
if
    else
    end
end</pre>
```

```
function L = binarySearch(x, v)
% Find position after which to insert x. v(1) < ... < v(end).
% L is the index such that v(L) \ll x \ll v(L+1);
% L=0 if x < v(1). If x > v(end), L=length(v) but x \sim = v(L).
% Maintain a search window [L..R] such that v(L)<=x<v(R).
% Since x may not be in v, initially set ...
L=0; R=length(v)+1;
% Keep halving [L..R] until R-L is 1,
% always keeping v(L) \ll x \ll v(R) while R \sim L+1
    m= floor((L+R)/2); % middle of search window
    if v(m) \ll x
        L= m;
    else
                                      This version is different!
                                      from that in Insight
    end
end
```

```
function L = binarySearch(x, v)
% Find position after which to insert x. v(1) < ... < v(end).
% L is the index such that v(L) <= x < v(L+1);
% L=0 if x<v(1). If x>v(end), L=length(v) but x\sim=v(L).
% Maintain a search window [L..R] such that v(L) <= x < v(R). % Since x may not be in v, initially set ...
L=0; R=length(v)+1;
% Keep halving [L..R] until R-L is 1,
% always keeping v(L) <= x < v(R)
while R ~= L+1
    m= floor((L+R)/2); % middle of search window</pre>
    if v(m) \ll x
         L= m;
                       20 30 40 46 50 52 68 70
    else
                                    3 4 5 6 7 8 9
         R=m;
    end
                                     Play with showBinarySearch.m
end
```