

- Previous Lecture:
 - Iteration using `while`
- Today's Lecture:
 - Nested loops
 - Developing algorithms
- Announcements:
 - Discussion this week in Upson B7 lab. [Read Insight §3.2](#) before discussion section.
 - Project 2 due Thursday at 11pm
 - We do not use `break` in this course
 - Make use of Piazza, office hrs, and consulting hrs

What is the last line of output?

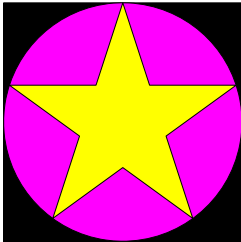
```
x = 1;
disp(x)
y = x;
while y==x && x<=4 && y<=4
    x = 2*x;
    disp(x)
end
```

A: 1 B: 2 C: 4 D: 8

Lecture 7 3

A simple 3-line script

```
DrawRect(...)
DrawDisk(...)
DrawStar(...)
```



Lecture 6 12

```
% drawDemo
close all
figure
axis equal off
hold on

DrawRect(0,0,2,2,'k')
DrawDisk(1,1,1,'m')
DrawStar(1,1,1,'y')

hold off
```

A general graphics framework

```
% drawDemo
close all
figure
axis equal off
hold on

Code fragment to draw the
objects (rectangle, disk, star)

hold off
```

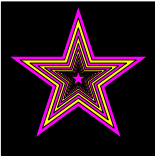
Lecture 6 14

Example: Nested Stars

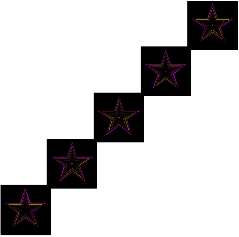


Lecture 7 15

Knowing how to draw



How difficult is it to draw



Lecture 7 17

Pattern for doing something n times

```
n= _____
for k= 1:n
    % code to do
    % that something
end
```

Lecture 7 18

```
x= 0; y= 0; % figure centered at (0,0)
s= 2.1; % side length of square
DrawRect(x-s/2,y-s/2,s,s,'k')
r= 1; k= 1;
while r > 0.1 %r still big
    % draw a star
    if rem(k,2)==1 %odd number
        DrawStar(x,y,r,'m') %magenta
    else
        DrawStar(x,y,r,'y') %yellow
    end
    % reduce r
    r= r/1.2;
    k= k + 1;
end
```

Lecture 7 19

Pattern for doing something n times

```
n= _____
for k= 1:n
    % code to do
    % that something
end
```

Lecture 7 21

Example: Are they prime?

- Given integers a and b , write a program that lists all the prime numbers in the range $[a, b]$.
- Assume $a > 1$, $b > 1$ and $a < b$.

Lecture 7 22

Example: Are they prime?

Subproblem: Is it prime?

- Given integers a and b , write a program that lists all the prime numbers in the range $[a, b]$.
- Assume $a > 1$, $b > 1$ and $a < b$.
- Write a program fragment to determine whether a given integer n is prime, $n > 1$.
- Reminder: $\text{rem}(x,y)$ returns the remainder of x divided by y .

Lecture 7 23

Developing the algorithm for the times table

| | | | | | |
|---|----|----|----|----|----|
| | 3 | 4 | 5 | 6 | 7 |
| 3 | 9 | 12 | 15 | 18 | 21 |
| 4 | 12 | 16 | 20 | 24 | 28 |
| 5 | 15 | 20 | 25 | 30 | 35 |
| 6 | 18 | 24 | 30 | 36 | 42 |
| 7 | 21 | 28 | 35 | 42 | 49 |

```
disp('Show the times table for specified range')
lo= input('What is the lower bound? ');
hi= input('What is the upper bound? ');
```

Rational approximation of π

- $\pi = 3.141592653589793\dots$
- Can be closely approximated by fractions, e.g., $\pi \approx 22/7$
- Rational number: a quotient of two integers
- Approximate π as p/q where p and q are positive integers $\leq M$
- Start with a straight forward solution:
 - Get M from user
 - Calculate quotient p/q for all combinations of p and q
 - Pick best quotient \rightarrow smallest error

```
% Rational approximation of pi
M = input('Enter M: ');

% Check all possible denominators
for q = 1:M
    % At this q, check all possible numerators
    for p = 1:M

    end
end
```

```
% Rational approximation of pi
M = input('Enter M: ');
% Best q, p, and error so far
qBest=1; pBest=1;
err_pq = abs(pBest/qBest - pi);

% Check all possible denominators
for q = 1:M
    % At this q, check all possible numerators
    for p = 1:M
        if abs(p/q - pi) < err_pq % best p/q found
            err_pq = abs(p/q - pi);
            pBest= p;
            qBest= q;
        end
    end
end
myPi = pBest/qBest;
```

Algorithm: Finding the best in a set
 Init bestSoFar
 Loop over set
 if current is better than bestSoFar
 bestSoFar \leftarrow current
 end
 end

Analyze the program for efficiency

- See Eg3_1 and FasterEg3_1 in the book

```
for a = 1:n
    disp('alpha')
    for b = 1:m
        disp('beta')
    end
end
```

How many times are "alpha" and "beta" displayed?

- A: n, m
- B: m, n
- C: $n, n+m$
- D: $n, n*m$
- E: $m*n, m$