

- Previous Lecture:
 - Recursion
- Today's Lecture:
 - Sorting and searching
 - Insertion sort, linear search
 - Read about *Bubble Sort* in Insight
 - "Divide and conquer" strategies
 - Binary search
- Announcements
 - Discussion in Upson B7 lab this week
 - P6 due Thursday at 11pm
 - Final exam: Dec 9th 7pm, Barton Indoor Track WEST

Searching for an item in a collection

Is the collection organized?
What is the organizing scheme?



Lecture 26

Lidiana Joo and the Builders of the LoraArk

Sorting data allows us to search more easily

Phone Book

Messages

Name

Albert, Fot

Allan, Wong

Anderson, Bruce

Ann

Bailey, Bob

Bar'l, Rainmar

Baumgardner, Bob

Beaudry, Mark

Berry, James

Beys, Michael

Blank, Frederick

Bliss, Brian

Boston Marathon Top Women Finishers

Official Time	State	Country	Ctz	
2:25:25	ETH			
2:25:27	RUS			
2:26:34	KEN			
2:28:12	LAT			
2:29:48	ETH			
2:30:52	ITA			
2:33:56	ROM			
2:34:37	ETH			
2:35:37	RUS			
F35	Hood, Stephanie A.	IL	USA	CAN
F14	Robson, Denise C.	NS	CAN	
F11	Chenjon, Magdaline		KEN	
F101	Sultanova-Zhdanova, Firaya	FL	USA	RUS
F15	Mayer, Eliza M.		AUS	
F24	Anklam, Ashley A.	MN	USA	

Name	Score	Grade
Jorge	92.1	
Ahn	91.5	
Oluban	90.6	
Chi	88.9	
Minala	88.1	

There are many algorithms for sorting

- Insertion Sort (to be discussed today)
 - Bubble Sort (read *Insight* §8.2)
 - Merge Sort (to be discussed Thursday)
 - Quick Sort (a variant used by Matlab's built-in `sort` function)
- Each has advantages and disadvantages. Some algorithms are faster (**time-efficient**) while others are **memory-efficient**
- Great opportunity for learning how to analyze programs and algorithms!

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The Insertion Process

- Given a sorted array x , insert a number y such that the result is sorted

sorted

2	3	6	9
---	---	---	---

8

↓

2	3	6	8	9
---	---	---	---	---

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Insertion

one insert process

2	3	6	9	8
---	---	---	---	---

↓

2	3	6	8	9
---	---	---	---	---

one insert process

2	3	6	8	9	4
---	---	---	---	---	---

↓

2	3	6	8	4	9
---	---	---	---	---	---

↓

2	3	6	4	8	9
---	---	---	---	---	---

↓

2	3	4	6	8	9
---	---	---	---	---	---

Compare adjacent components:
DONE! No more swaps.

See `Insert.m` for the insert process

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Sort vector x using the Insertion Sort algorithm

Need to start with a *sorted* subvector. How do you find one?

```

x
■ Length 1 subvector is "sorted"
■ Insert x(2): [x(1:2),C,S] = Insert(x(1:2))
■ Insert x(3): [x(1:3),C,S] = Insert(x(1:3))
■ Insert x(4): [x(1:4),C,S] = Insert(x(1:4))
■ Insert x(5): [x(1:5),C,S] = Insert(x(1:5))
■ Insert x(6): [x(1:6),C,S] = Insert(x(1:6))
    
```

InsertionSort.m

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Insertion Sort vs. Bubble Sort

- Read about Bubble Sort in *Insight* §8.2
- Both algorithms involve the repeated comparison of adjacent values and swaps
- Find out which algorithm is more efficient on average

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Other efficiency considerations

- Worst case, best case, average case
- Use of subfunction incurs an "overhead"
- Memory use and access
- Example: Rather than directing the *insert* process to a subfunction, have it done "in-line."
- Also, Insertion sort can be done "in-place," i.e., using "only" the memory space of the original vector.

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```

function x = InsertionSortInplace(x)
% Sort vector x in ascending order with insertion sort

n = length(x);
for i= 1:n-1
    % Sort x(1:i+1) given that x(1:i) is sorted
    j= i;
    while
        % swap x(j+1) and x(j)

        j= j-1;
    end
end
    
```

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Sort an array of objects

- Given x , a 1-d array of *Interval* references, sort x according to the widths of the *Intervals* from narrowest to widest
- Use the insertion sort algorithm
- How much of our code needs to be changed?

- A. No change
- B. One statement
- C. About half the code
- D. Most of the code

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Searching for an item in an unorganized collection?

- May need to look through the whole collection to find the target item
- E.g., find value x in vector v



- Linear search

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```

% Linear Search
% f is index of first occurrence
% of value x in vector v.
% f is -1 if x not found.
k= 1;
while k<=length(v) && v(k)~=x
    k= k + 1;
end
if k>length(v)
    f= -1; % signal for x not found
else
    f= k;
end
    
```

A. squared
 B. doubled
 C. the same
 D. halved

Suppose another vector is twice as long as v. The expected "effort" required to do a linear search is ...

```

% Linear Search
% f is index of first occurrence
% of value x in vector v.
% f is -1 if x not found.
k= 1;
while k<=length(v) && v(k)~=x
    k= k + 1;
end
if k>length(v)
    f= -1; % signal for x not found
else
    f= k;
end
    
```

Searching in a sorted list should require less work

v	12	15	33	35	42	45
x	31					

What if v is sorted?

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Key idea of "phone book search": repeated halving

To find the page containing Pat Reed's number...

```

while (Phone book is longer than 1 page)
    Open to the middle page.
    if "Reed" comes before the first entry,
        Rip and throw away the 2nd half.
    else
        Rip and throw away the 1st half.
    end
end
    
```

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What happens to the phone book length?

Original:	3000 pages
After 1 rip:	1500 pages
After 2 rips:	750 pages
After 3 rips:	375 pages
After 4 rips:	188 pages
After 5 rips:	94 pages
:	
After 12 rips:	1 page

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Binary Search

Repeatedly halving the size of the "search space" is the main idea behind the method of binary search.

An item in a sorted array of length n can be located with just $\log_2 n$ comparisons.

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```

% Linear Search
% f is index of first occurrence of value x in vector v.
% f is -1 if x not found.
k= 1;
while k<=length(v) && v(k)~=x
    k= k + 1;
end
if k>length(v)
    f= -1; % signal for x not found
else
    f= k;
end
    
```

n comparisons against the target are needed in worst case, n=length(v).

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