

- Previous Lecture:
  - Nesting `if`-statements
  - Boolean operations (relational, logical)
  - Logical operators short-circuit
- Today's Lecture:
  - Iteration using `for`
- Announcement
  - Discussion this week in classrooms as listed on roster

Question

A stick of unit length is split into two pieces. The breakpoint is randomly selected. On average, how long is the shorter piece?

Physical experiment? ♦  
 Thought experiment? → analysis  
 Computational experiment! → simulation ♦

♦ Need to repeat many trials!

Simulation:  
use code to imitate the physical experiment

```

% one trial of the experiment
breakPt= rand(1);
if breakPt<0.5
    shortPiece= breakPt;
else
    shortPiece= 1-breakPt;
end
    
```

Repeat n times

```

% one trial of the experiment
breakPt= rand(1);
shortPiece= min(breakPt, 1-breakPt);
    
```

Take average  
Print result

```

n= 10000; % number of trials
total= 0; % accumulated length so far

for k= 1:n
    % one trial of the experiment
    breakPt= rand(1);
    shortPiece= min(breakPt, 1-breakPt);
    total= total + shortPiece;
end

aveLength= total/n;
fprintf('Average length is %f\n', ...
        aveLength)
    
```

Example: "Accumulate" a solution

```

% Average 10 numbers from user input
n= 10; % number of data values

for k= 1:n
    % read and process input value
    num= input('Enter a number: ');
    total= total + num;
end
ave= total/n; % average of n numbers
fprintf('Average is %f\n', ave)
    
```

How many passes through the loop will be completed?

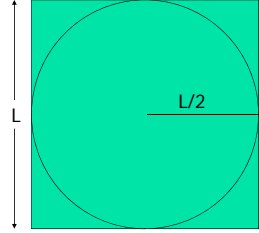
- A: 0
- B: 1
- C: 9
- D: 10
- E: 11

### Important Features of Iteration

- A task can be accomplished if some steps are repeated; these steps form the **loop body**
- Need a **starting point**
- Need to know **when to stop**
- Need to keep track of (and measure) progress—**update**

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### Monte Carlo Approximation of $\pi$



Throw  $N$  darts

Sq. area =  $N = L \times L$

Circle area =  $N_{in}$   
 $= \pi L^2 / 4$

$\pi = 4 N_{in} / N$

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### Monte Carlo Approximation of $\pi$

**For each of  $N$  trials**

Throw a dart

If it lands in circle  
 add 1 to total # of hits

**Pi is  $4 \cdot \text{hits} / N$**

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### Monte Carlo $\pi$ with $N$ darts on $L$ -by- $L$ board

```

for k = 1:N
    % Throw kth dart

    % Count it if it is in the circle

end
myPi = 4*hits/N;
    
```

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### Syntax of the **for** loop

```

for <var>= <start value>:<incr>:<end bound>
    statements to be executed repeatedly
end
    
```

Loop header specifies all the values that the index variable will take on, one for each pass of the loop.

E.g.  $k = 3:1:7$  means  $k$  will take on the values 3, 4, 5, 6, 7, **one at a time**.

Lecture 5 23

### Pattern for doing something $n$ times

```

n= _____
for k= 1:n
    % code to do
    % that something
end
    
```

Definite iteration

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**for** loop examples

```

for k= 2:0.5:3
    disp(k)
end
for k= 1:4
    disp(k)
end
for k= 0:-2:-6
    disp(k)
end
for k= 0:-2:-7
    disp(k)
end
for k= 5:2:1
    disp(k)
end
    
```

**k** takes on the values \_\_\_\_\_  
 Non-integer increment is OK

**k** takes on the values \_\_\_\_\_  
 Default increment is 1

**k** takes on the values \_\_\_\_\_  
 "Increment" may be negative

**k** takes on the values \_\_\_\_\_  
 Colon expression specifies a bound

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```

% What will be printed?
for k= 1:2:6
    fprintf('%d ', k)
end
    
```

A: 1 2 3 4 5 6  
 B: 1 3 5 6  
 C: 1 3 5  
 D: error (incorrect bounds)

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```

% What will be printed?
for k= 10:-1:14
    fprintf('%d ', k)
end
fprintf('!')
    
```

A: error (incorrect bounds)  
 B: 10 (then error)  
 C: 10 !  
 D: 14 !  
 E: !

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What will be displayed when you run the following script?

```

for k = 4:6
    disp(k)
    k= 9;
    disp(k)
end
    
```

A: 4 9  
 B: 4 4  
 C: Something else ...

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```

for k = 4:6
    disp(k)
    k= 9;
    disp(k)
end
    
```

4  5  6

With this loop header, **k** "promises" to be these values, one at a time

Output in Command Window

**k**

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```

for k = 4:6
    disp(k)
    k= 9;
    disp(k)
end
    
```

4  5  6

Not a condition (boolean expression) that checks whether  $k \leq 6$ .  
 It is an expression that specifies values:

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