

- Previous Lecture:
 - Image processing
- Today's Lecture:
 - More image manipulation
 - "Noise" filtering
 - Edge finding
- Announcements:
 - Prelim 2 tonight 7:30-9pm
 - Last names A-O: Statler Aud. Main
 - Last names P-Z: Statler Aud. Balcony




Lecture 16 3

Grayness: a value in [0..255]

0 = black
255 = white


These are *integer* values
Type: `uint8`



150	149	152	153	152	155
151	150	153	154	153	156
153	151	155	156	155	158
154	153	156	157	156	159
156	154	158	159	158	161
157	156	159	160	159	162

Lecture 16 4

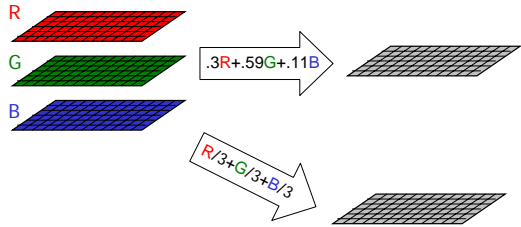
Example: color → black and white



Can "average" the three color values to get one gray value.


Lecture 16 5

Averaging the RGB values to get a gray value



Lecture 16 6

Averaging the RGB values to get a gray value




```

for i= 1:m
  for j= 1:n
    M(i,j)= .3*R(i,j) + .59*G(i,j) + .11*B(i,j)
  end
end
    
```

scalar operation

Lecture 16 7

Averaging the RGB values to get a gray value



$M = .3R + .59G + .11B$

vectorized operation

Lecture 16 8

Here are 2 ways to calculate the average. Are gray value matrices **g** and **h** the same given image data **A**?

```

for r= 1:nr
  for c= 1:nc
    g(r,c)= A(r,c,1)/3 + A(r,c,2)/3 ...
            A(r,c,3)/3;
    h(r,c)= ...
            ( A(r,c,1)+A(r,c,2)+A(r,c,3) )/3;
  end
end
    
```

A: yes

B: no

Lecture 16 9

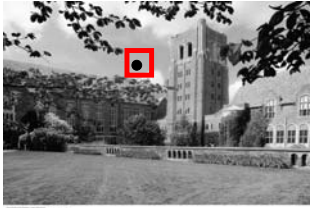
showToGrayscale.m

Matlab has a built-in function to convert from color to grayscale, resulting in a 2-d array:

$B = \text{rgb2gray}(A)$

Lecture 16 10

Dirt in the image!

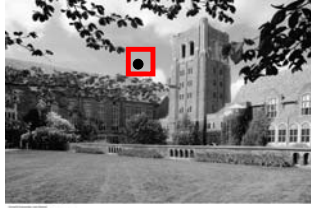


Note how the "dirty pixels" look out of place

150	149	152	153	152	155
151	150	153	154	153	156
153	2	3	156	155	158
154	2	1	157	156	159
156	154	158	159	158	161
157	156	159	160	159	162

Lecture 16 16

What to do with the dirty pixels?



Assign "typical" neighborhood gray values to "dirty pixels"


150	149	152	153	152	155
151	150	153	154	153	156
153	?	?	156	155	158
154	?	?	157	156	159
156	154	158	159	158	161
157	156	159	160	159	162

Lecture 16 17


What are "typical neighborhood gray values"?

Median

Mean



radius 1



radius 2

Lecture 16 18

Median Filtering

- Visit each pixel
- Replace its gray value by the median of the gray values in the "neighborhood"

Lecture 16 19

Using a radius 1 "neighborhood"

Before After

Lecture 16 20

Visit every pixel; compute its new value.

```

for i=1:m
  for j=1:n
    Compute new gray value for pixel (i,j).
  end
end
    
```

Lecture 16 21

Original:

$i = 1$
 $j = 1$

Filtered:

Replace with the median of the values under the window.

Original:

$i = 1$
 $j = 2$

Filtered:

Replace with the median of the values under the window.

Original:

$i = 2$
 $j = 2$

Filtered:

Replace with the median of the values under the window.

What we need...

- (1) A function that computes the median value in a 2-dimensional array C:

$$m = \text{medVal}(C)$$
- (2) A function that builds the filtered image by using median values of radius r neighborhoods:

$$B = \text{medFilter}(A,r)$$

Lecture 16 29

Computing the median

`x` :

21	89	36	28	19	88	43
----	----	----	----	----	----	----

`x = sort(x)`

↓

`x` :

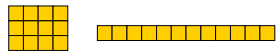
19	21	28	36	43	88	89
----	----	----	----	----	----	----

`n = length(x); % n = 7`
`m = ceil(n/2); % m = 4`
`med = x(m); % med = 36`

If `n` is even, then use : `med = x(m)/2 + x(m+1)/2`

Lecture 16 30

Median of a 2D array

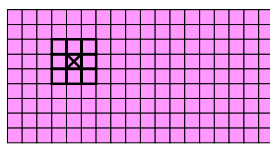


```
function med = medVal(C)
[nr,nc] = size(C);
x = zeros(1,nr*nc);
for r=1:nr
    x((r-1)*nc+1:r*nc) = C(r,:);
end
%Compute median of x and assign to med
```

See medVal.m

Lecture 16 31

Back to filtering...



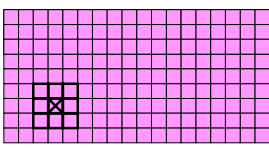
`m = 9`

`n = 18`

```
for i=1:m
    for j=1:n
        Compute new gray value for pixel (i,j)
    end
end
```

Lecture 16 32

When window is inside...



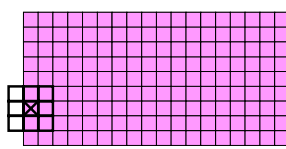
`m = 9`

`n = 18`

New gray value for pixel (7,4) =
`medVal(A(6:8,3:5))`

Lecture 16 33

When window is partly outside...



`m = 9`

`n = 18`

New gray value for pixel (7,1) =
`medVal(A(6:8,1:2))`

Lecture 16 34

```
function B = medFilter(A,r)
% B from A via median filtering
% with radius r neighborhoods.

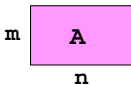
[m,n] = size(A);
B = uint8(zeros(m,n));
for i=1:m
    for j=1:n
        C = pixel (i,j) neighborhood
        B(i,j) = medVal(C);
    end
end
```

Lecture 16 36


The Pixel (i,j) Neighborhood

```

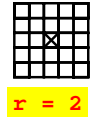
iMin = max(1,i-r)
iMax = min(m,i+r)
jMin = max(1,j-r)
jMax = min(n,j+r)
C = A(iMin:iMax,jMin:jMax)
    
```



m
A
n



r = 1



r = 2

Lecture 16 38

Mean filter fails because the mean does not capture representative values.


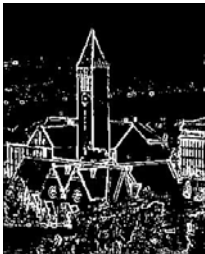
150	149	152	153	152	155
151	150	153	154	153	156
153	2	3	156	155	158
154	2	1	157	156	159
156	154	158	159	158	161
157	156	159	160	159	162

85	86
87	88

mean-filtered values

Lecture 16 42

Finding Edges





Lecture 16 46

What is an Edge?

Near an edge, grayness values change abruptly

200	200	200	200	200	200
200	200	200	200	200	100
200	200	200	200	100	100
200	200	200	100	100	100
200	200	100	100	100	100
200	100	100	100	100	100




Lecture 16 47

General plan for showing the edges in in image

- Identify the "edge pixels"
- Highlight the edge pixels
 - make edge pixels white; make everything else black

200	200	200	200	200	200
20	200	200	200	200	100
200	200	200	200	100	100
200	200	100	100	100	100
200	200	100	100	100	100
200	100	100	100	100	100



Lecture 16 49

The Rate-of-Change-Array

Suppose **A** is an image array with integer values between 0 and 255.

Let **B(i,j)** be the maximum difference between and its eight neighbors.

So **B(i,j)** is the maximum value in

$A(\max(1,i-1):\min(m,i+1), \dots$	-	$A(i,j)$
$\max(1,j-1):\min(n,j+1))$		

Neighborhood of $A(i,j)$

Lecture 16 55

Rate-of-change example

90	81	65
62	60	59
56	57	58

Rate-of-change at middle pixel is 30

Be careful! In "uint8 arithmetic" 57 - 60 is 0

Lecture 16

56

```
function Edges(jpgIn, jpgOut, tau)
% jpgOut is the "edge diagram" of image jpgIn.
% At each pixel, if rate-of-change > tau
% then the pixel is considered to be on an edge.
```

```
A = rgb2gray(imread(jpgIn)); % Built-in function to convert to grayscale. Returns 2-d array.
[m,n] = size(A);
B = uint8(zeros(m,n));
for i = 1:m
    for j = 1:n
        B(i,j) = ?????
    end
end
```

Lecture 16

58

Recipe for rate-of-change B(i,j)

```
% The 3-by-3 subarray that includes
% A(i,j) and its 8 neighbors
Neighbors = A(i-1:i+1,j-1:j+1);
% Subtract A(i,j) from each entry
Diff= abs(double(Neighbors)- ...
         double(A(i,j)));
% Compute largest value in each column
colMax = max(Diff);
% Compute the max of the column max's
B(i,j) = max(colMax);
```

Lecture 16

59

```
function Edges(jpgIn, jpgOut, tau)
% jpgOut is the "edge diagram" of image jpgIn.
% At each pixel, if rate-of-change > tau
% then the pixel is considered to be on an edge.
```

```
A = rgb2gray(imread(jpgIn));
[m,n] = size(A);
B = uint8(zeros(m,n));
for i = 1:m
    for j = 1:n
        Neighbors = A(max(1,i-1):min(i+1,m), ...
                      max(1,j-1):min(j+1,n));
        B(i,j)=max(max(abs(double(Neighbors)- ...
                        double(A(i,j)))));
    end
end
```

end

"Edge pixels" are now identified; display them with maximum brightness (255)

1	1	1	1	1	1
1	1	1	1	1	1
1	1	1	1	90	90
1	1	1	90	90	90
1	1	90	90	90	90
1	1	90	90	90	90

threshold

```
if B(i,j) > tau
    B(i,j) = 255;
end
```

B(i,j)

0	0	0	0	0	0
0	0	0	89	89	89
0	0	89	89	0	0
0	89	89	0	0	0
0	89	0	0	0	0
0	89	0	0	0	0

0	0	0	0	0	0
0	0	0	255	255	255
0	0	255	255	0	0
0	255	255	0	0	0
0	255	0	0	0	0
0	255	0	0	0	0

Lecture 16

62

```
function Edges(jpgIn, jpgOut, tau)
% jpgOut is the "edge diagram" of image jpgIn.
% At each pixel, if rate-of-change > tau
% then the pixel is considered to be on an edge.
```

```
A = rgb2gray(imread(jpgIn));
[m,n] = size(A);
B = uint8(zeros(m,n));
for i = 1:m
    for j = 1:n
        Neighbors = A(max(1,i-1):min(i+1,m), ...
                      max(1,j-1):min(j+1,n));
        B(i,j)=max(max(abs(double(Neighbors)- ...
                        double(A(i,j)))));
        if B(i,j) > tau
            B(i,j) = 255;
        end
    end
end
imwrite(B, jpgOut, 'jpg')
```