

- Previous Lecture:
  - 2-d array examples

- Today's Lecture:
  - Image processing

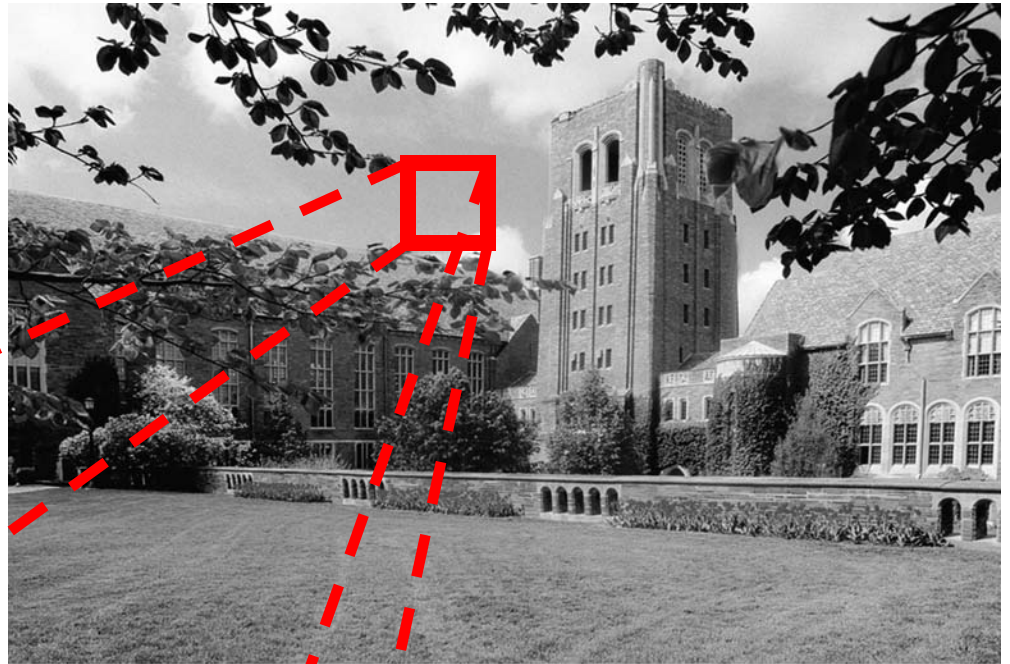
- Announcements:

- Discussion this week in UP B7 lab
- Optional review sessions: T5-6:30 and W5-6:30, both in Hollister B14. Attend one if you wish.
- Prelim 2 on Thursday, 7:30-9pm



# A picture as a matrix

1458-by-2084



Cornell University Law School  
Photograph by Cornell University Photography

150	149	152	153	152	155
151	150	153	154	153	156
153	151	155	156	155	158
154	153	156	157	156	159
156	154	158	159	158	161
157	156	159	160	159	162

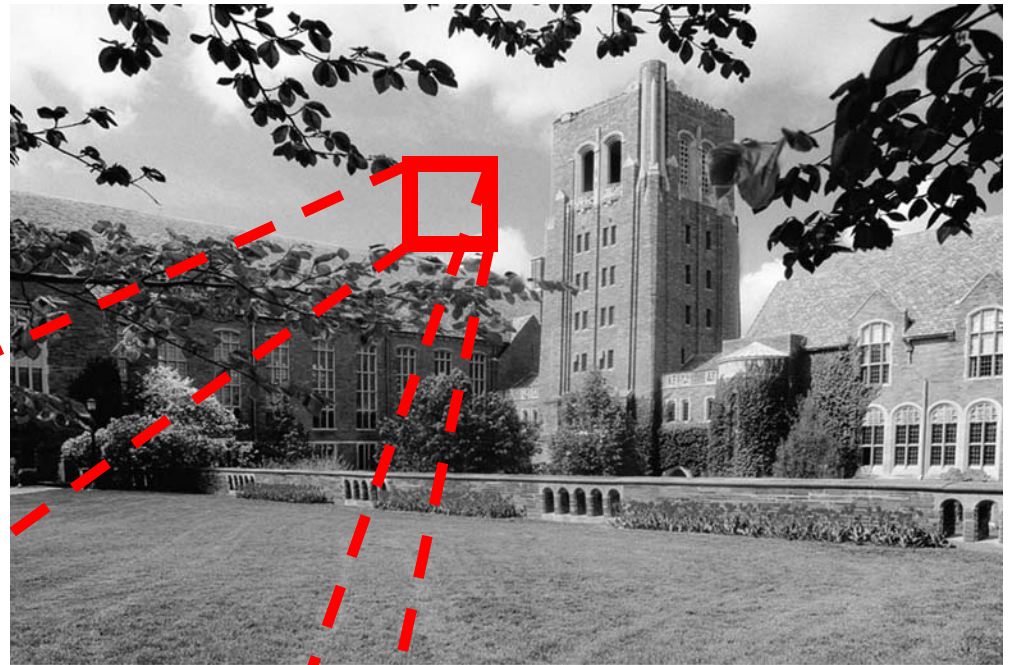
# Images can be encoded in different ways

- Common formats include
  - JPEG: Joint Photographic Experts Group
  - GIF: Graphics Interchange Format
- Data are compressed
- We will work with jpeg files:
  - **imread**: read a .jpg file and convert it to a “normal numeric” array that we can work with
  - **imwrite**: write an array into a .jpg file (compressed data)

# Grayness: a value in [0..255]

0 = black  
255 = white

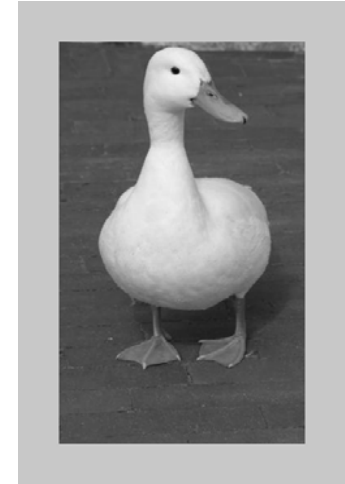
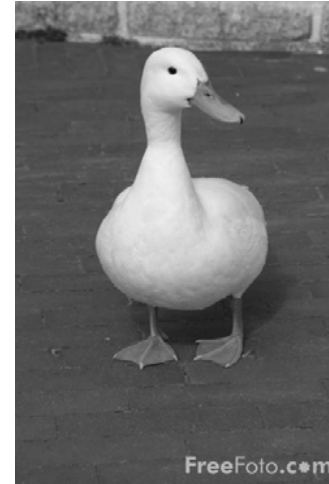
These are *integer* values  
Type: `uint8`



Cornell University Law School  
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150	149	152	153	152	155
151	150	153	154	153	156
153	151	155	156	155	158
154	153	156	157	156	159
156	154	158	159	158	161
157	156	159	160	159	162

## Let's put a picture in a frame



### Things to do:

1. Read **`bwduck.jpg`** from memory and convert it into an array
2. Show the original picture
3. Assign a gray value (frame color) to the “edge pixels”
4. Show the manipulated picture

## Reading a jpeg file and displaying the image

```
% Read jpg image and convert to  
% an array P  
P = imread( 'bwduck.jpg' );  
  
% Show the data in 3-d array P as  
% an image  
imshow(P)
```

```
% Frame a grayscale picture
```

```
P= imread('bwduck.jpg');  
imshow(P)
```

```
% Change the "frame" color
```

```
imshow(P)
```

```
% Frame a grayscale picture

P= imread('bwduck.jpg');
imshow(P)

% Change the "frame" color
width= 50;
frameColor= 200; % light gray
```

```
imshow(P)
```



```
% Frame a grayscale picture

P= imread('bwduck.jpg');
imshow(P)

% Change the "frame" color
width= 50;
frameColor= 200; % light gray
[nr,nc]= size(P);
for r= 1:nr
    for c= 1:nc
        % At pixel (r,c)

    end
end
imshow(P)
```

```
% Frame a grayscale picture
```

```
P= imread('bwduck.jpg');  
imshow(P)
```

```
% Change the "frame" color
```

```
width= 50;
```

```
frameColor= 200; % light gray
```

```
[nr,nc]= size(P);
```

```
for r= 1:nr
```

```
    for c= 1:nc
```

```
        % At pixel (r,c)
```

```
        if r<=width || r>nr-width || ...
```

```
           c<=width || c>nc-width
```

```
            P(r,c)= frameColor;
```

```
        end
```

```
    end
```

```
end
```

```
imshow(P)
```

Things to consider...

1. Can we be more efficient?
2. What is the type of the values in P?

## Accessing a submatrix

**M**

2	-1	.5	0	-3
3	8	6	7	7
5	-3	8.5	9	10
52	81	.5	7	2

- **M** refers to the whole matrix
- **M(3,5)** refers to one component of **M**

# Accessing a submatrix

**M**

2	-1	.5	0	-3
3	8	6	7	7
5	-3	8.5	9	10
52	81	.5	7	2

- **M** refers to the whole matrix
- **M(3, 5)** refers to one component of **M**
- **M(2:3, 3:5)** refers to a submatrix of **M**

row indices

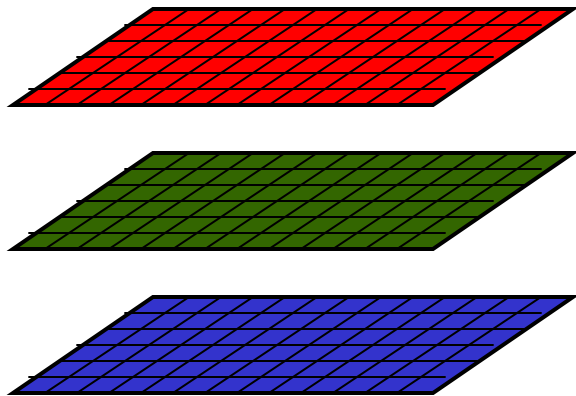


column indices



A color picture is made up of **RGB** matrices

Color image



3-d Array

$$0 \leq A(i, j, 1) \leq 255$$

$$0 \leq A(i, j, 2) \leq 255$$

$$0 \leq A(i, j, 3) \leq 255$$

Operations on images amount to operations on  
**matrices!**

## Example: Mirror Image



Cornell University Law School  
Photograph by Cornell University Photography

`LawSchool.jpg`



Cornell University Law School  
Photograph by Cornell University Photography

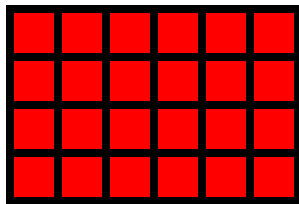
`LawSchoolMirror.jpg`

1. Read **LawSchool.jpg** from memory and convert it into an array.
2. Manipulate the Array.
3. Convert the array to a jpg file and write it to memory.

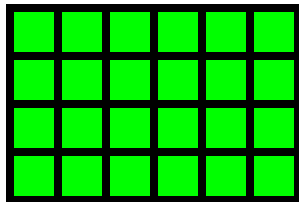
# A 3-d array as 3 matrices

```
[nr, nc, np] = size(A) % dimensions of 3-d array A
```

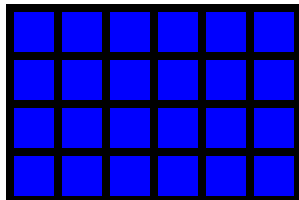
#rows                      #columns                      #layers (pages)



4-by-6



4-by-6



4-by-6

```
A(1:nr, 1:nc, 1)
```

```
M1 = A(:, :, 1)
```

```
M2 = A(:, :, 2)
```

```
M3 = A(:, :, 3)
```

**%Store mirror image of A in array B**

```
[nr,nc,np]= size(A) ;
```

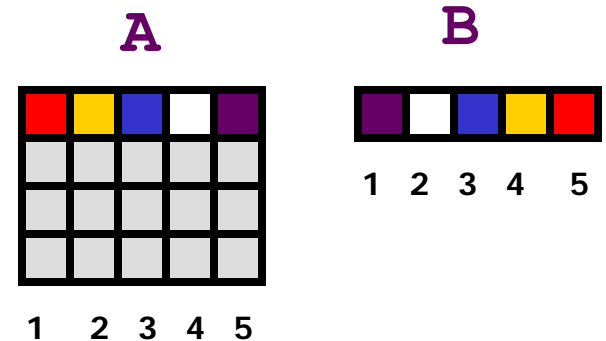
```
for r= 1:nr
```

```
    for c= 1:nc
```

```
        B(r,c )= A(r,nc-c+1 ) ;
```

```
    end
```

```
end
```





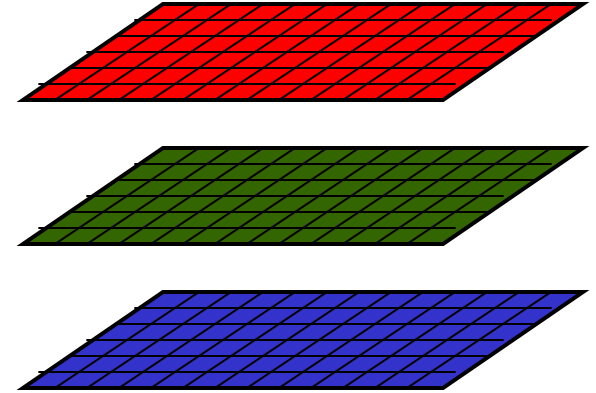
```
%Store mirror image of A in array B
```

```
[nr,nc,np]= size(A);  
for r= 1:nr  
    for c= 1:nc  
        for p= 1:np  
            B(r,c,p)= A(r,nc-c+1,p);  
        end  
    end  
end
```

```

[nr,nc,np]= size(A);
for r= 1:nr
    for c= 1:nc
        for p= 1:np
            B(r,c,p) = A(r,nc-c+1,p);
        end
    end
end
end

```



```

[nr,nc,np]= size(A);
for p= 1:np
    for r= 1:nr
        for c= 1:nc
            B(r,c,p) = A(r,nc-c+1,p);
        end
    end
end
end

```

*Both fragments  
create a mirror  
image of **A** .*

**A** true

**B** false

```

[nr,nc,np]= size(A);
for r= 1:nr
    for c= 1:nc
        for p= 1:np
            B(r,c,p)= A(r,nc-c+1,p);
        end
    end
end

```

This is non-vectorized code.

```

[nr,nc,np]= size(A);
for p= 1:np
    for r= 1:nr
        for c= 1:nc
            B(r,c,p)= A(r,nc-c+1,p);
        end
    end
end

```

Both fragments create a mirror image of **A** .

A true

B false

```
% Make mirror image of A -- the whole thing
```

```
A= imread('LawSchool.jpg');
```

```
[nr,nc,np]= size(A);
```

```
for r= 1:nr
```

```
    for c= 1:nc
```

```
        for p= 1:np
```

```
            B(r,c,p)= A(r,nc-c+1,p);
```

```
        end
```

```
    end
```

```
end
```

```
imshow(B) % Show 3-d array data as an image
```

```
imwrite(B,'LawSchoolMirror.jpg')
```

```

% Make mirror image of A -- the whole thing

A= imread('LawSchool.jpg');
[nr,nc,np]= size(A);

B= zeros(nr,nc,np);
B= uint8(B); % Type for image color values

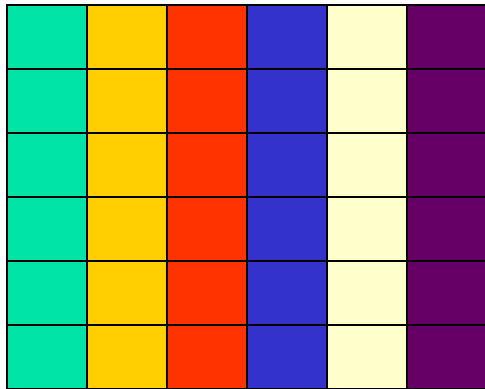
for r= 1:nr
    for c= 1:nc
        for p= 1:np
            B(r,c,p)= A(r,nc-c+1,p);
        end
    end
end
imshow(B) % Show 3-d array data as an image
imwrite(B,'LawSchoolMirror.jpg')

```

Vectorized code simplifies things...

Work with a whole column at a time

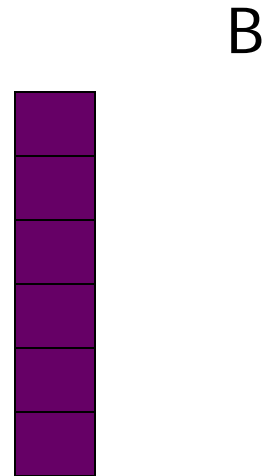
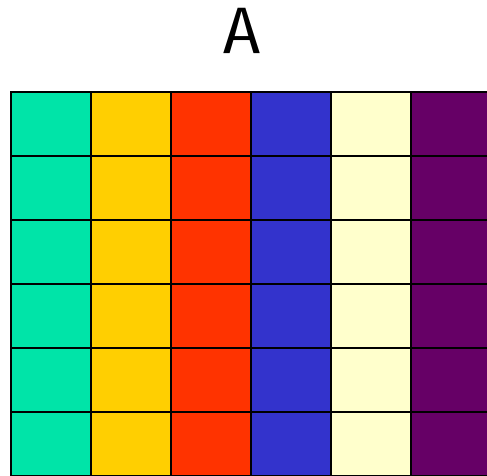
A



Cyan	Yellow	Red	Blue	Light Yellow	Purple
Cyan	Yellow	Red	Blue	Light Yellow	Purple
Cyan	Yellow	Red	Blue	Light Yellow	Purple
Cyan	Yellow	Red	Blue	Light Yellow	Purple
Cyan	Yellow	Red	Blue	Light Yellow	Purple
Cyan	Yellow	Red	Blue	Light Yellow	Purple

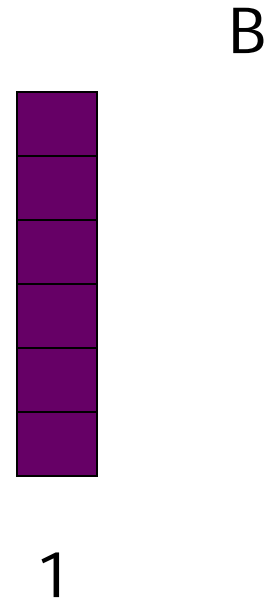
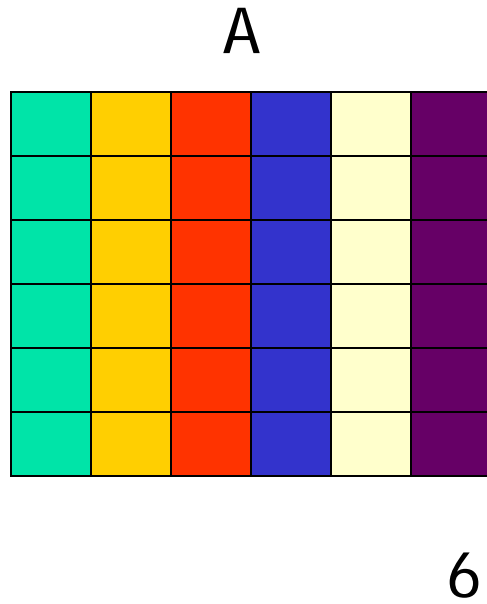
# Vectorized code simplifies things...

## Work with a whole column at a time



# Vectorized code simplifies things...

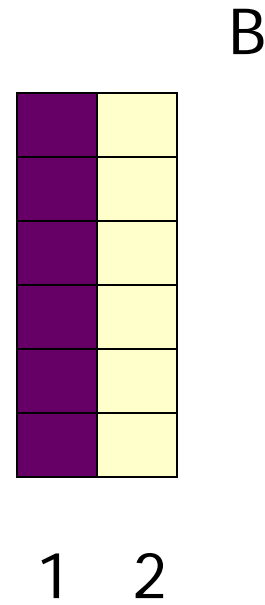
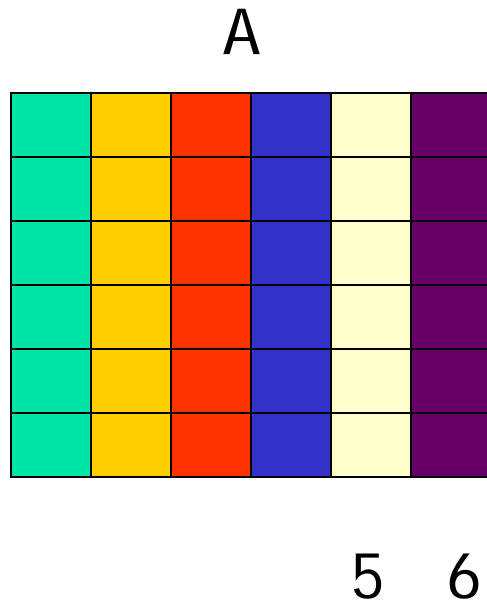
## Work with a whole column at a time





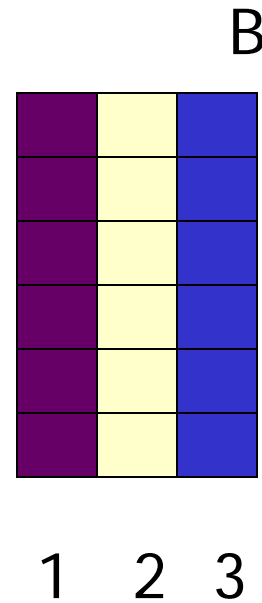
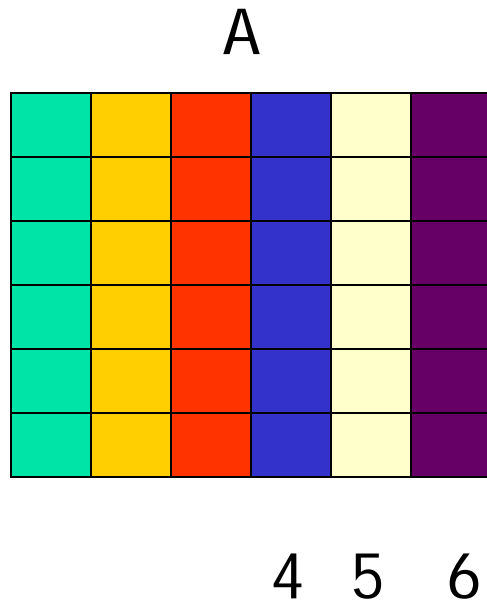
# Vectorized code simplifies things...

## Work with a whole column at a time



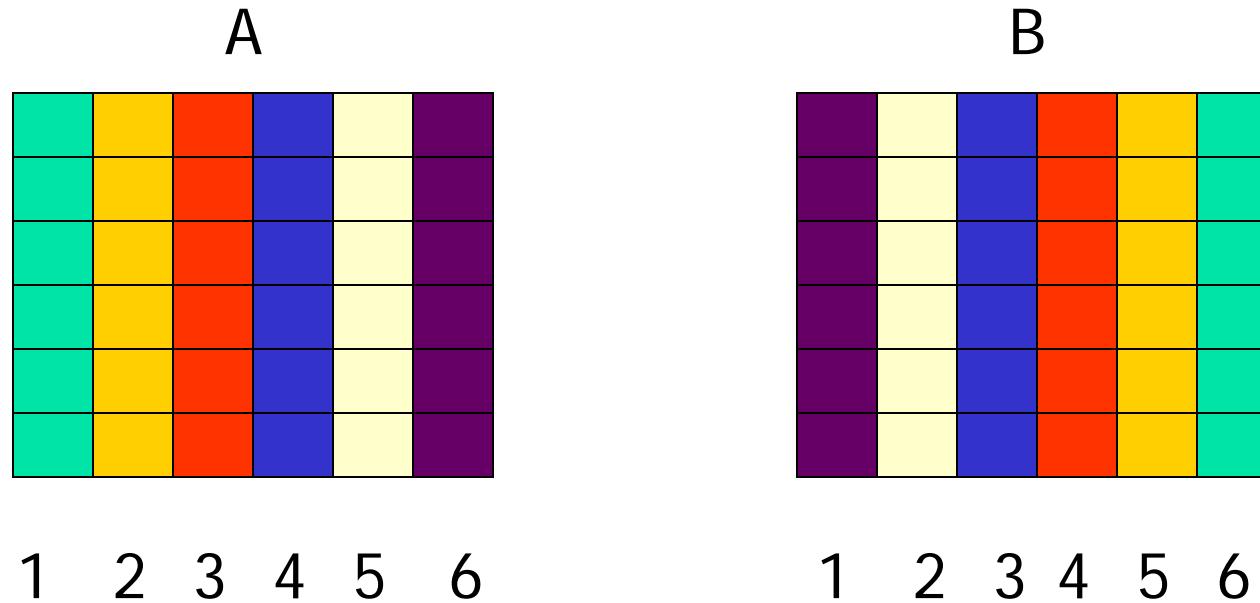
# Vectorized code simplifies things...

## Work with a whole column at a time



# Vectorized code simplifies things...

## Work with a whole column at a time



Column  $c$  in  $B$   
is column  $nc-c+1$  in  $A$

Consider a single matrix (just one layer)

```
[nr,nc,np] = size(A);
```

```
for c= 1:nc
```

```
    B( all rows, c ) = A( all rows, nc+1-c ) ;
```

```
end
```

Consider a single matrix (just one layer)

```
[nr,nc,np] = size(A);  
for c= 1:nc  
    B(1:nr,c) = A(1:nr,nc+1-c);  
  
end
```

Consider a single matrix (just one layer)

```
[nr,nc,np] = size(A);  
for c= 1:nc  
    B( : ,c ) = A( : ,nc+1-c ) ;  
  
end
```

The colon says "all indices in this dimension." In this case it says "all rows."

Now repeat for all layers

```
[nr,nc,np] = size(A);  
for c= 1:nc  
    B(:,c,1) = A(:,nc+1-c,1)  
    B(:,c,2) = A(:,nc+1-c,2)  
    B(:,c,3) = A(:,nc+1-c,3)  
end
```

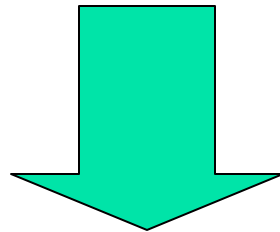
## Vectorized code to create a mirror image

```
A = imread('LawSchool.jpg')
[nr,nc,np] = size(A);
for c= 1:nc
    B(:,c,1) = A(:,nc+1-c,1)
    B(:,c,2) = A(:,nc+1-c,2)
    B(:,c,3) = A(:,nc+1-c,3)
end
imwrite(B, 'LawSchoolMirror.jpg')
```



Even more compact vectorized code to create a mirror image...

```
for c= 1:nc
    B(:,c,1) = A(:,nc+1-c,1)
    B(:,c,2) = A(:,nc+1-c,2)
    B(:,c,3) = A(:,nc+1-c,3)
end
```



```
B = A(:,nc:-1:1,:)
```

Example: color  $\rightarrow$  black and white



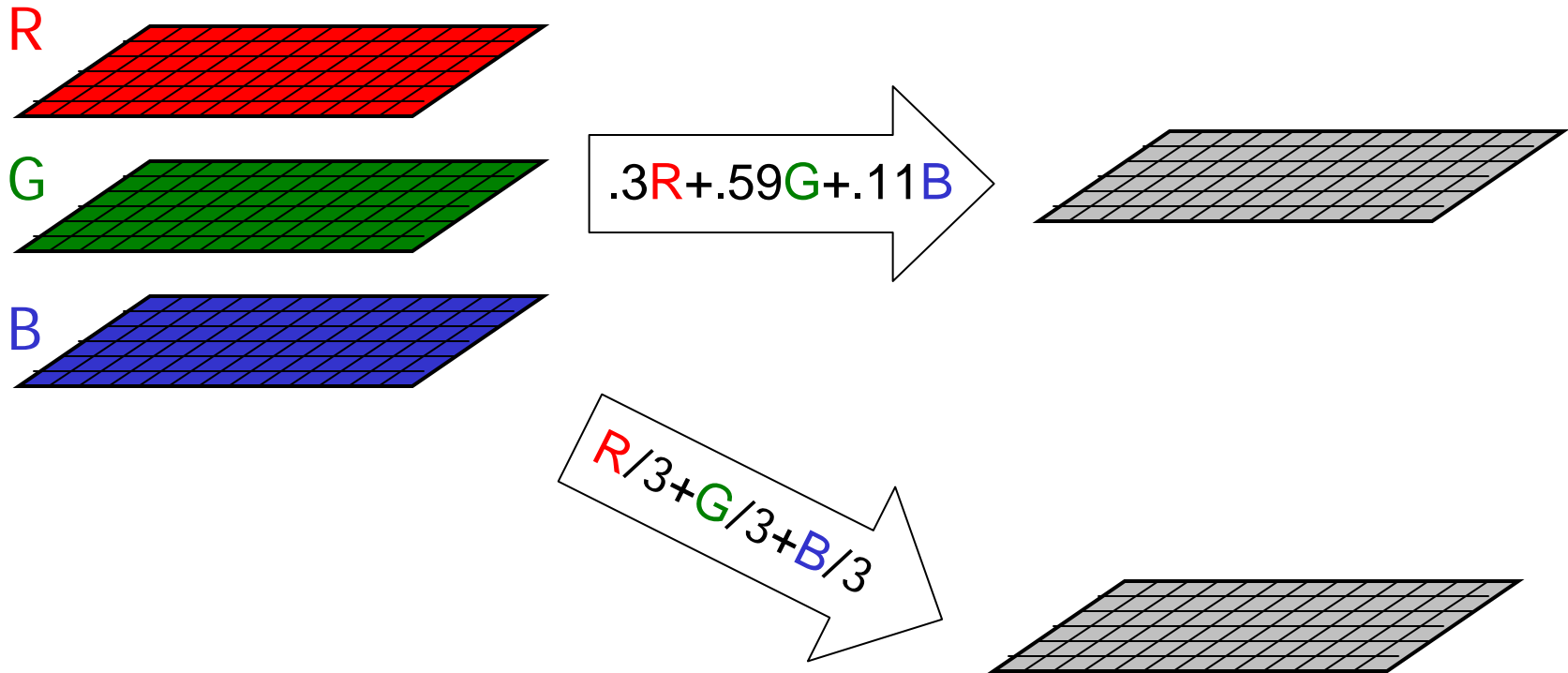
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Photograph by Cornell University Photography



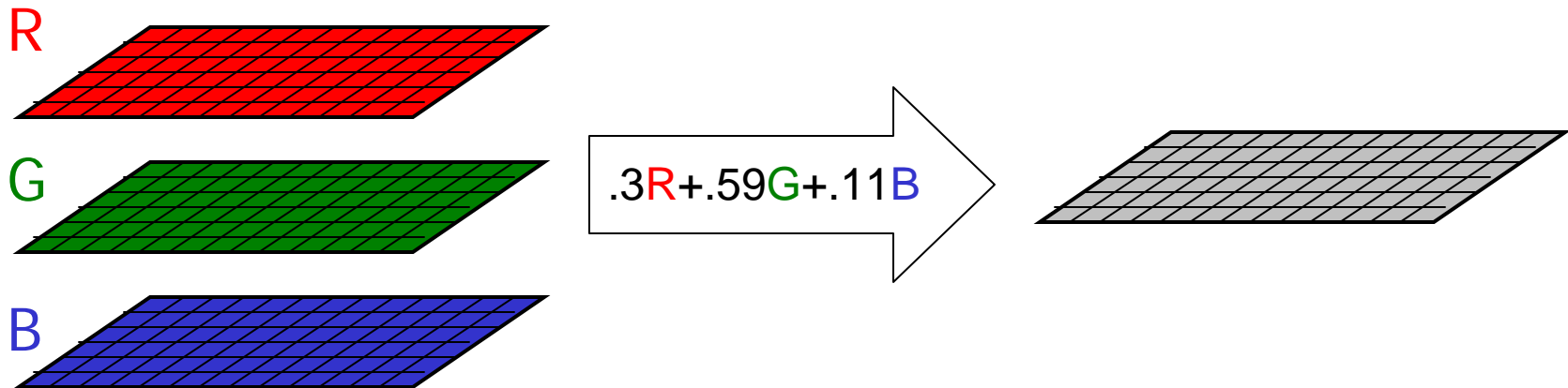
Cornell University Law School  
Photograph by Cornell University Photography

Can “average” the three color values to get one gray value.

# Averaging the RGB values to get a gray value



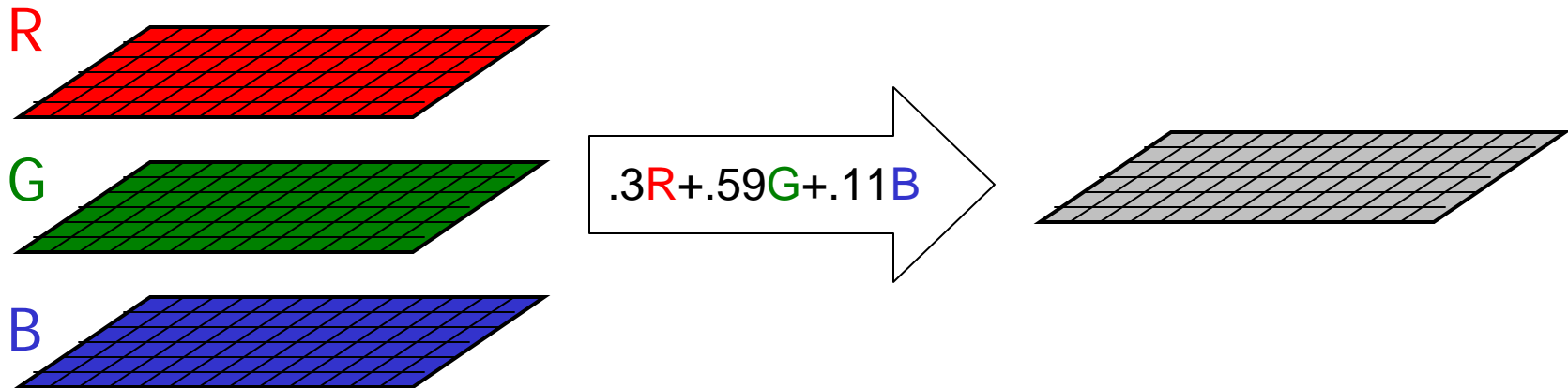
# Averaging the RGB values to get a gray value



```
for i= 1:m
  for j= 1:n
    M(i,j)= .3*R(i,j) + .59*G(i,j) + .11*B(i,j)
  end
end
```

scalar operation

# Averaging the RGB values to get a gray value



$$M = .3 * R + .59 * G + .11 * B$$

vectorized operation