

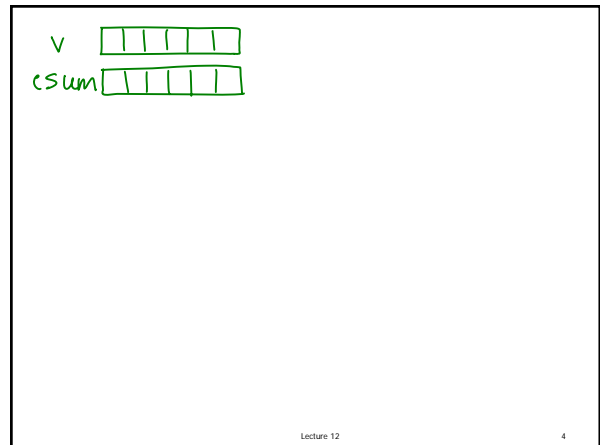
- Previous Lecture:
  - Probability and random numbers
  - 1-d array—vector
- Today's Lecture:
  - More examples on vectors
  - Simulation
- Announcement:
  - Project 3 posted. Due 3/10.
  - Prelim 2 on 3/27. Please let us know now (email Randy Hess, [rbhess@cs.cornell.edu](mailto:rbhess@cs.cornell.edu)) if you have a university-scheduled conflict.


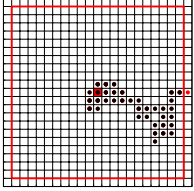
### Loop patterns for working with a vector

<pre>% Given a vector v for k = 1:length(v)      % Work with v(k)     % E.g., disp(v(k))  end</pre>	<pre>% Given a vector v k = 1; while k &lt;= length(v)      % Work with v(k)     % E.g., disp(v(k))      k = k+1;  end</pre>
---	--

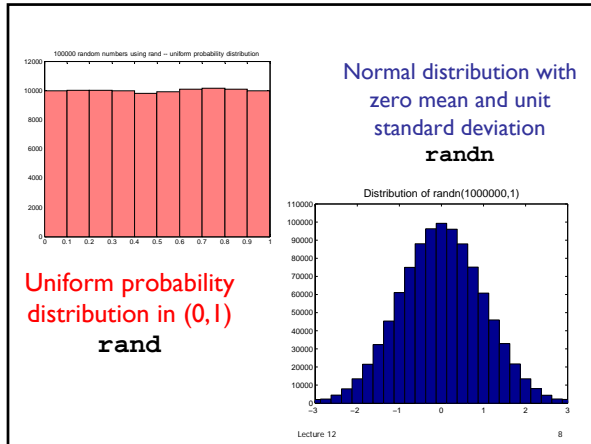
Lecture 12 2

- ### Example
- Write a program fragment that calculates the **cumulative sums** of a given vector  $v$ .
  - The cumulative sums should be stored in a vector of the same length as  $v$ .
- 1, 3, 5, 0     $v$   
 1, 4, 9, 9    cumulative sums of  $v$
- Lecture 12 3



- ### Simulation
- Imitates real system
  - Requires judicious use of random numbers
  - Requires many trials
  - → opportunity to practice working with vectors!
- 

- Lecture 12 5

- ### Random numbers
- **Pseudorandom** numbers in programming
  - Function `rand(...)` generates random real numbers in the interval (0,1). All numbers in the interval (0,1) are equally likely to occur—**uniform** probability distribution.
  - Examples:
    - `rand(1)`      one random # in (0,1)
    - `6*rand(1)`    one random # in (0,6)
    - `6*rand(1)+1` one random # in (1,7)
- Lecture 12 7



Sanity check: rand and randn

```
>> n= 1000000;
>> x= rand(n,1);
>> ave= sum(x)/n
ave =
    0.5004

>> y= randn(n,1);
>> ave= sum(y)/n
ave =
    0.0018

>> stdDev= std(y)
stdDev =
    1.0001
```

Lecture 12 9

Simulate twinkling stars

- Get 10 user mouse clicks as locations of 10 stars—our constellation
  - Simulate twinkling
    - Loop through all the stars; each has equal likelihood of being bright or dark
    - Repeat many times
  - Can use DrawStar, DrawRect
- Lecture 12 12

```
% No. of stars and star radius
N=10; r=.5;
% Get mouse clicks, store coords in vectors x,y
[x,y] = ginput(N);
% Twinkle!
for k= 1:20 % 20 rounds of twinkling

end
```

Twinkle.m

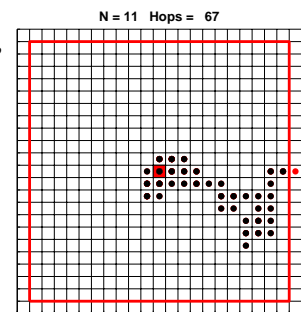
Lecture 12 15

2-dimensional random walk

Start in the middle tile, (0,0).

For each step, randomly choose between N,E,S,W and then walk one tile. Each tile is 1×1.

Walk until you reach the boundary.



```
function [x, y] = RandomWalk2D(N)
% 2D random walk in 2N-1 by 2N-1 grid.
% Walk randomly from (0,0) to an edge.
% Vectors x,y represent the path.
```

```
function [x, y] = RandomWalk2D(N)
k=0; xc=0; yc=0;
while not at an edge
    % Choose random dir, update xc,yc
    % Record new location in x, y
end
```

```
% Standing at (xc,yc)
% Randomly select a step
r= rand(1);
if r < .25
    yc= yc + 1; % north
elseif r < .5
    xc= xc + 1; % east
elseif r < .75
    yc= yc -1; % south
else
    xc= xc -1; % west
end
```

Another representation for the random step

- Observe that each update has the form
 
$$xc = xc + \Delta x$$

$$yc = yc + \Delta y$$
 no matter which direction is taken.
- So let's get rid of the if statement!
- Need to create two "change vectors" deltaX and deltaY

deltaX


deltaY


Example: polygon smoothing

x	y

First operation: centralize

Move a polygon so that the centroid of its vertices is at the origin

```
function [xNew,yNew] = Centralize(x,y)
% Translate polygon defined by vectors
% x,y such that the centroid is on the
% origin. New polygon defined by vectors
% xNew,yNew.

n = length(x);
xBar = sum(x)/n;
yBar = sum(y)/n;
xNew = x-xBar;
yNew = y-yBar;
```

Vectorized code

Lecture 12 28

### Second operation: normalize

Shrink (enlarge) the polygon so that the vertex furthest from the (0,0) is on the unit circle

Lecture 12 30

```
function [xNew,yNew] = Normalize(x,y)
% Resize polygon defined by vectors x,y
% such that distance of the vertex
% furthest from origin is 1

d = max(sqrt(x.^2 + y.^2));
xNew = x/d;
yNew = y/d;
```

Vectorized ops

Applied to a vector, **max** returns the largest value in the vector

Lecture 12 31

### Third operation: smooth

Obtain a new polygon by connecting the midpoints of the edges

Lecture 12 32

```
function [xNew,yNew] = Smooth(x,y)
% Smooth polygon defined by vectors x,y
% by connecting the midpoints of
% adjacent edges

n = length(x);
xNew = zeros(n,1);
yNew = zeros(n,1);

for i=1:n
    Compute the midpt of ith edge.
    Store in xNew(i) and yNew(i)
end
```

Lecture 12 33

### Polygon Smoothing

```
% Given n, x, y
for i=1:n
    xNew(i) = (x(i) + x(i+1))/2;
    yNew(i) = (y(i) + y(i+1))/2;
end
```

Does above fragment compute the new n-gon?

A: Yes

B: No

Lecture 12 37