

- Previous Lecture:

- Branching (**if**, **elseif**, **else**, **end**)
- Relational operators (<, >=, ==, ~=, ..., etc.)

- Today's Lecture:

- Logical operators (&&, ||, ~), “short-circuiting”
- More branching—*nesting*
- Top-down design

- Announcements:

- **Project 1** (P1) due Thursday at 11pm
- Observe the rules on academic integrity
- Submit real .m files (plain text, not from a word processing software such as Microsoft Word)
- Register your clicker with CIT. Use the link on course website.
- Discussion this week in Upson B7 computer lab, not classrooms listed on roster

Things to know about the **if** construct

- At most one branch of statements is executed
- There can be any number of **elseif** clauses
- There can be at most one **else** clause
- The **else** clause must be the last clause in the construct
- The **else** clause does not have a condition (boolean expression)

Consider the quadratic function

$$q(x) = x^2 + bx + c$$

on the interval $[L, R]$:

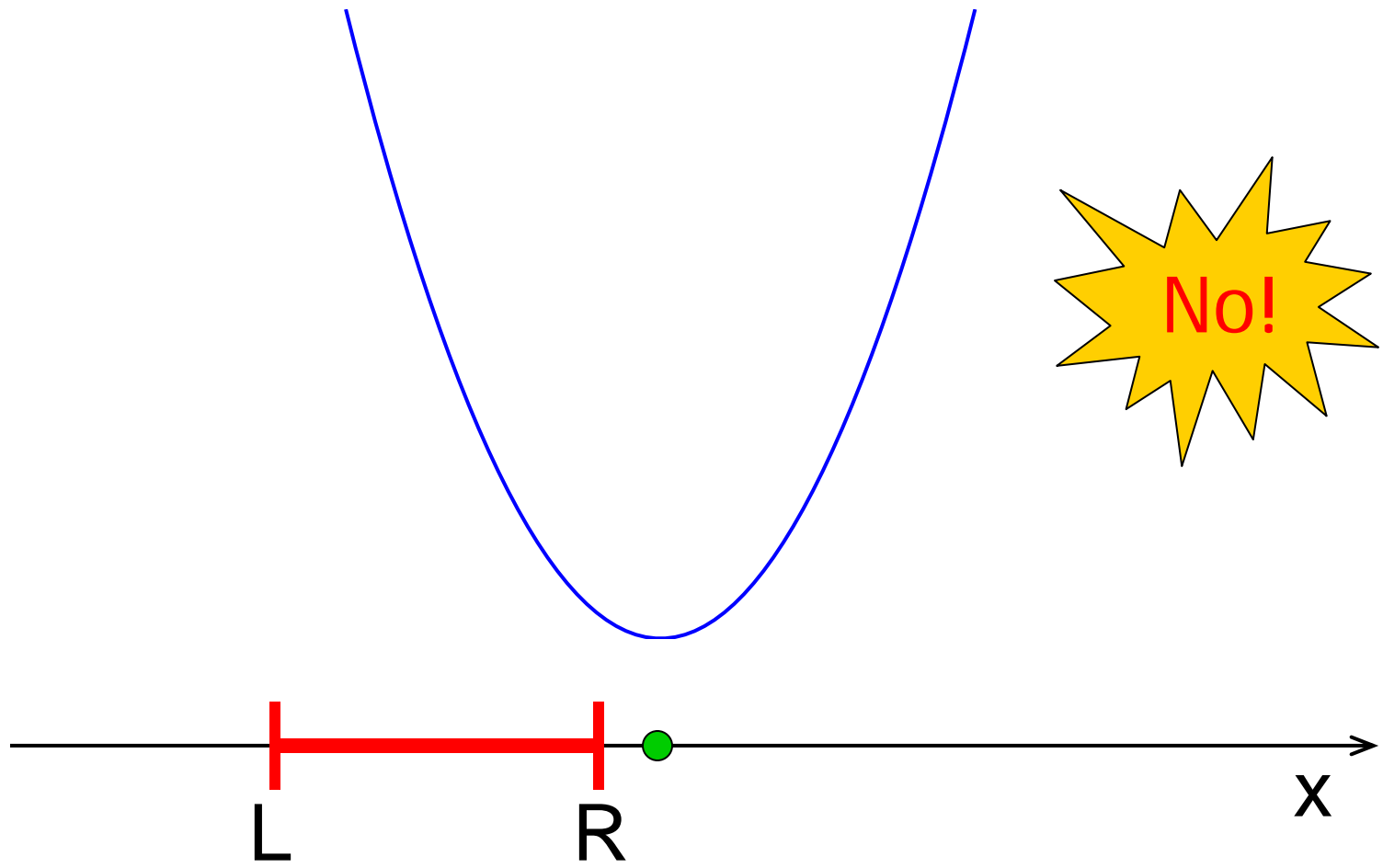
- Is the function strictly increasing in $[L, R]$?
- Which is **smaller**, $q(L)$ or $q(R)$?
- What is the **minimum value** of $q(x)$ in $[L, R]$?

Modified Problem 3

Write a code fragment that prints “yes” if **xc** is in the interval and “no” if it is not.

$$q(x) = x^2 + bx + c$$

• $x_c = -b/2$



So what is the requirement?

```
% Determine whether xc is in
```

```
% [L,R]
```

```
xc = -b/2;
```

```
if _____
```

```
    disp( 'Yes' )
```

```
else
```

```
    disp( 'No' )
```

```
end
```

So what is the requirement?

```
% Determine whether xc is in
```

```
% [L,R]
```

```
xc = -b/2;
```

```
if L<=xc && xc<=R
```

```
    disp( 'Yes' )
```

```
else
```

```
    disp( 'No' )
```

```
end
```

The value of a boolean expression is either true or false.

$(L \leq xc) \ \&\& \ (xc \leq R)$

This (compound) boolean expression is made up of two (simple) boolean expressions. Each has a value that is **either true or false**.

Connect boolean expressions by **boolean operators**:

and

$\&\&$

or

$||$

not

\sim

Logical operators

&& logical and: Are both conditions true?

E.g., we ask “is $L \leq x_c$ **and** $x_c \leq R$?”

In our code: **L<=xc && xc<=R**

Logical operators

&& logical and: Are both conditions true?

E.g., we ask “is $L \leq x_c$ and $x_c \leq R$?”

In our code: `L<=xc && xc<=R`

|| logical or: Is at least one condition true?

E.g., we can ask if x_c is outside of $[L,R]$,

i.e., “is $x_c < L$ **or** $R < x_c$?”

In code: `xc<L || R<xc`

Logical operators

&& logical and: Are both conditions true?

E.g., we ask “is $L \leq x_c$ and $x_c \leq R$?”

In our code: `L<=xc && xc<=R`

|| logical or: Is at least one condition true?

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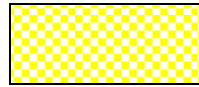
In code: `xc<L || R<xc`

~ logical not: Negation

E.g., we can ask if x_c is **not outside** $[L, R]$.

In code: `~(xc<L || R<xc)`

The logical AND operator: &&



&&



F

F

T

T

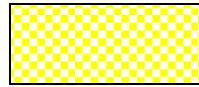
F

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F

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The logical AND operator: &&



&&



F

F

T

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The logical OR operator: ||



||



F

F

T

T

F

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F

T

The logical OR operator: \parallel



\parallel



F

F

T

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F

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T

T

The logical NOT operator: \sim



\sim



F

T

The logical NOT operator: \sim



\sim



F

T

T

F

“Truth table”

X, Y represent boolean expressions.
E.g., $d > 3.14$

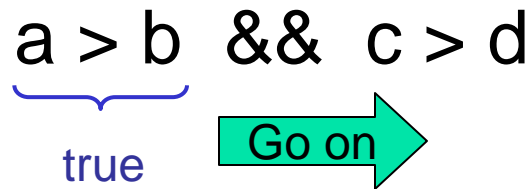
X	Y	X && Y “and”	X Y “or”	~y “not”
F	F	F	F	T
F	T	F	T	F
T	F	F	T	T
T	T	T	T	F

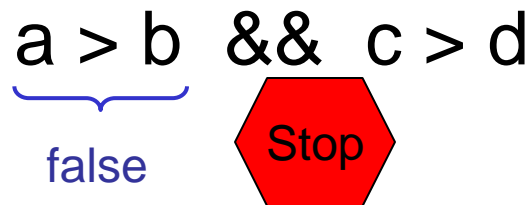
“Truth table”

Matlab uses 0 to represent false,
1 to represent true

X	Y	X && Y “and”	X Y “or”	~y “not”
0	0	0	0	1
0	1	0	1	0
1	0	0	1	1
1	1	1	1	0

Logical operators “short-circuit”

$a > b$ $\&\&$ $c > d$
A blue bracket under 'a > b' is labeled 'true'. A green arrow labeled 'Go on' points from the first condition to the second.

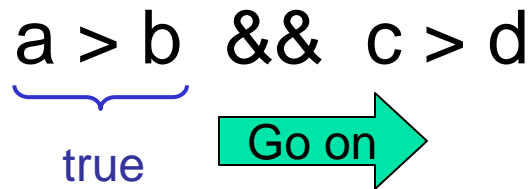
$a > b$ $\&\&$ $c > d$
A blue bracket under 'a > b' is labeled 'false'. A red hexagon labeled 'Stop' is placed between the two conditions.

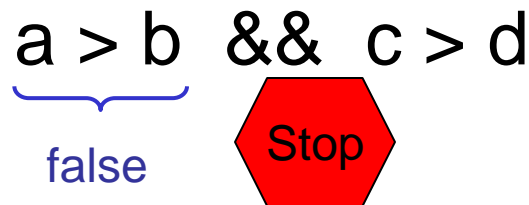
Entire expression is false since
the first part is false

A **&&** condition short-circuits to false if the left operand evaluates to *false*.

A **||** condition short-circuits to _____
if _____

Logical operators “short-circuit”

$a > b$ $\&\&$ $c > d$
The diagram shows the expression 'a > b' followed by ' && ' and then 'c > d'. A blue bracket is under 'a > b' with the word 'true' written below it. A green arrow labeled 'Go on' points from the 'true' result towards the right operand 'c > d'.

$a > b$ $\&\&$ $c > d$
The diagram shows the expression 'a > b' followed by ' && ' and then 'c > d'. A blue bracket is under 'a > b' with the word 'false' written below it. A red hexagon labeled 'Stop' is placed between the ' && ' operator and the right operand 'c > d', indicating that evaluation stops.

Entire expression is false since
the first part is false

A **&&** condition short-circuits to false if the left operand evaluates to *false*.

A **||** condition short-circuits to true if the left operand evaluates to *true*.

Always use logical operators to connect simple boolean expressions

Why is it wrong to use the expression

$$L \leq xc \leq R$$

for checking if x_c is in $[L,R]$?

Example: Suppose L is 5, R is 8, and xc is 10. We know that 10 is not in $[5,8]$, but the expression

$L \leq xc \leq R$ gives...

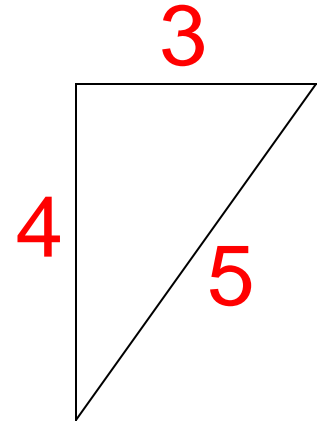
Variables **a**, **b**, and **c** have whole number values. **True** or **false**: This fragment prints “Yes” if there is a *right triangle* with side lengths **a**, **b**, and **c** and prints “No” otherwise.

```
if a^2 + b^2 == c^2
    disp('Yes')
else
    disp('No')
end
```

A: true

B: false

```
a = 5;  
b = 3;  
c = 4;  
if (a^2+b^2==c^2)  
  
    disp('Yes')  
else  
    disp('No')  
end
```



This fragment prints "No"
even though we have a right
triangle!

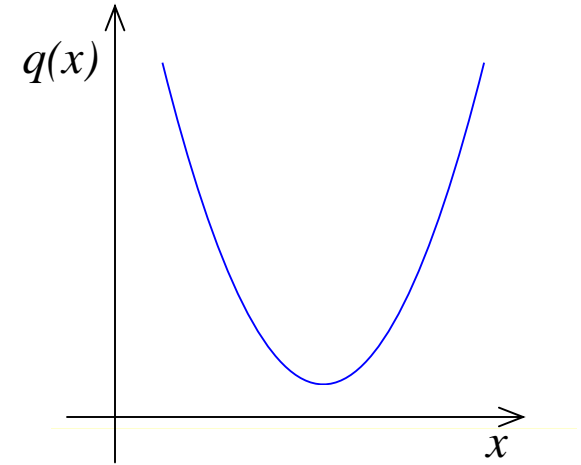

```

a = 5;
b = 3;
c = 4;
if ( (a^2+b^2==c^2) || (a^2+c^2==b^2) ...
    || (b^2+c^2==a^2) )
    disp( 'Yes' )
else
    disp( 'No' )
end

```

Consider the quadratic function

$$q(x) = x^2 + bx + c$$

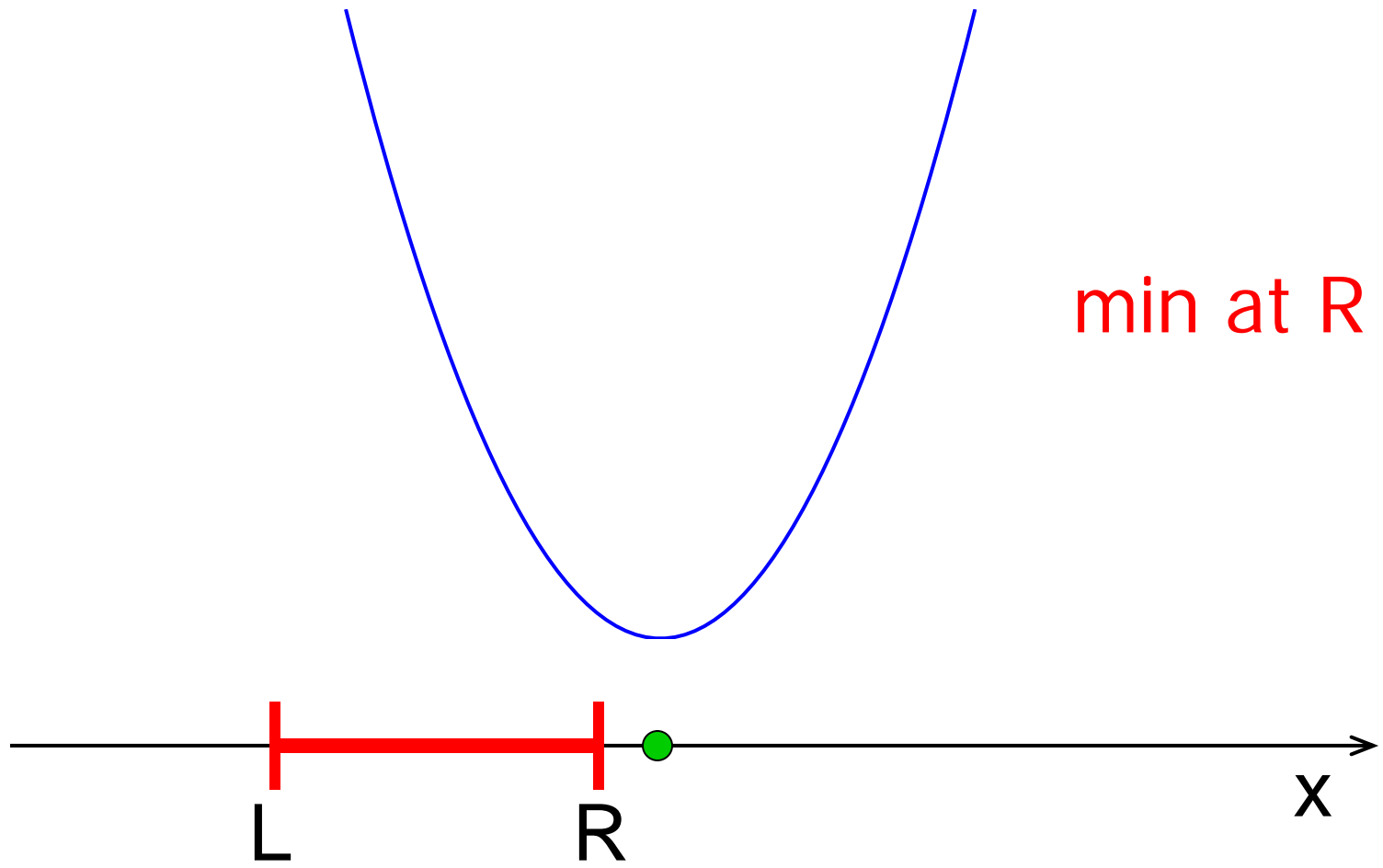


on the interval $[L, R]$:

- Is the function strictly increasing in $[L, R]$?
- Which is **smaller**, $q(L)$ or $q(R)$?
- What is the **minimum value** of $q(x)$ in $[L, R]$?

$$q(x) = x^2 + bx + c$$

$$\bullet x_c = -b/2$$



Conclusion

If x_c is between L and R

Then min is at x_c

Otherwise

Min value is at one of the endpoints

Start with pseudocode

If x_c is between L and R

Min is at x_c

Otherwise

Min is at one of the endpoints

We have **decomposed** the problem into three pieces! Can choose to work with any piece next: the if-else construct/condition, min at x_c , or min at an endpoint

Set up structure first: if-else, condition

if $L \leq x_c$ $\&\&$ $x_c \leq R$

Then min is at x_c

else

Min is at one of the endpoints

end

Now **refine** our solution-in-progress. I'll choose to work on the if-branch next

Refinement: filled in detail for task “min at xc”

```
if L<=xc && xc<=R
```

```
    % min is at xc
```

```
    qMin= xc^2 + b*xc + c;
```

```
else
```

Min is at one of the endpoints

```
end
```

Continue with refining the solution... else-branch next

Refinement: detail for task “min at an endpoint”

```
if L<=xc && xc<=R
    % min is at xc
    qMin= xc^2 + b*xc + c;
else
    % min is at one of the endpoints
    if % xc left of bracket
        % min is at L
    else % xc right of bracket
        % min is at R
    end
end
```

Continue with the refinement, i.e., replace comments with code

Refinement: detail for task “min at an endpoint”

```
if L<=xc && xc<=R
    % min is at xc
    qMin= xc^2 + b*xc + c;
else
    % min is at one of the endpoints
    if xc < L
        qMin= L^2 + b*L + c;
    else
        qMin= R^2 + b*R + c;
    end
end
```

Final solution (given b,c,L,R,xc)

```
if L<=xc && xc<=R
    % min is at xc
    qMin= xc^2 + b*xc + c;
else
    % min is at one of the endpoints
    if xc < L
        qMin= L^2 + b*L + c;
    else
        qMin= R^2 + b*R + c;
    end
end
```

An if-statement can appear within a branch—just like any other kind of statement!

quadMin.m

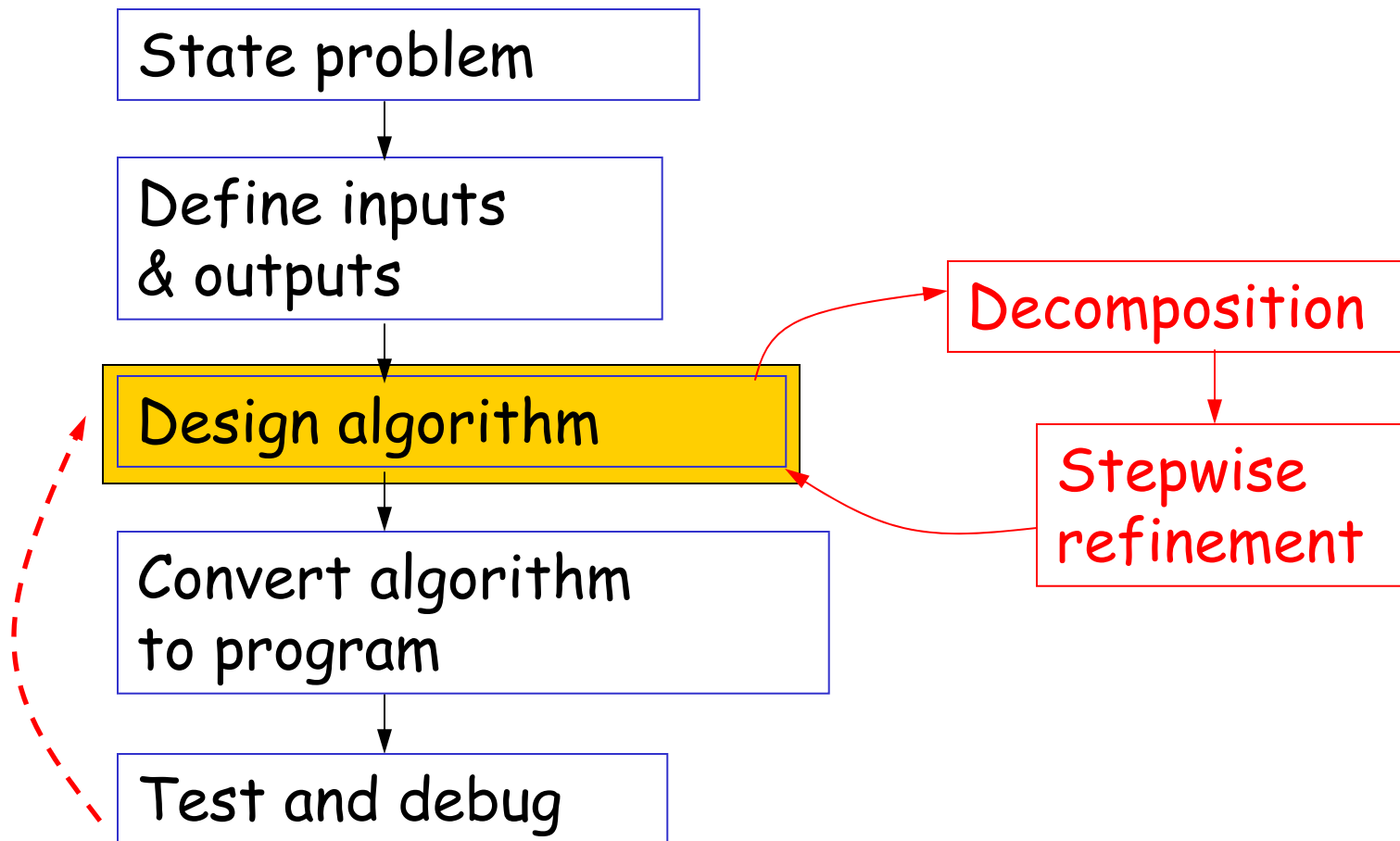
quadMinGraph.m

Notice that there are 3 alternatives → can use **elseif**!

```
if L<=xc && xc<=R
    % min is at xc
    qMin= xc^2+b*xc+c;
else
    % min at one endpt
    if xc < L
        qMin= L^2+b*L+c;
    else
        qMin= R^2+b*R+c;
    end
end
```

```
if L<=xc && xc<=R
    % min is at xc
    qMin= xc^2+b*xc+c;
elseif xc < L
    qMin= L^2+b*L+c;
else
    qMin= R^2+b*R+c;
end
```

Top-Down Design



An algorithm is an **idea**. To use an algorithm you must choose a programming language and **implement** the algorithm.

If x_c is between L and R
Then min value is at x_c

Otherwise
Min value is at one of the endpoints

```
if L<=xc && xc<=R
```

```
    % min is at xc
```

```
else
```

```
    % min is at one of the endpoints
```

```
end
```

```
if  L<=xc && xc<=R
    % min is at xc

else
    % min is at one of the endpoints

end
```



```
if  L<=xc && xc<=R
    % min is at xc
    qMin= xc^2 + b*xc + c;
else
    % min is at one of the endpoints

end
```

```
if L<=xc && xc<=R
    % min is at xc
    qMin= xc^2 + b*xc + c;
else
    % min is at one of the endpoints

end
```

```
if L<=xc && xc<=R
    % min is at xc
    qMin= xc^2 + b*xc + c;
else
    % min is at one of the endpoints
    if xc < L

    else

    end
end
```

```
if L<=xc && xc<=R
    % min is at xc
    qMin= xc^2 + b*xc + c;
else
    % min is at one of the endpoints
    if xc < L
        qMin= L^2 + b*L + c;
    else
        qMin= R^2 + b*R + c;
    end
end
end
```

Does this program work?

```
score= input('Enter score: ');  
if score>55  
    disp('D')  
elseif score>65  
    disp('C')  
elseif score>80  
    disp('B')  
elseif score>93  
    disp('A')  
else  
    disp('Not good...')  
end
```

A: yes

B: no