

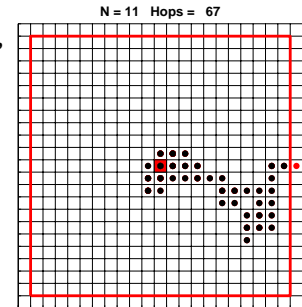
- Previous Lecture:
  - User-defined functions
    - Examples with varying numbers of input and output parameters
    - Local memory space
- Today's Lecture:
  - 1-d array—vector
  - Probability and random numbers
- Announcement:
  - Project 3 Part A posted on Tuesday; Part B to be posted. Both parts are due on Thursday 10/7.

### 2-dimensional random walk

Start in the middle tile, (0,0).

For each step, randomly choose between N,E,S,W and then walk one tile. Each tile is  $1 \times 1$ .

Walk until you reach the boundary.



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```
function [x, y] = RandomWalk2D(N)
% 2D random walk in 2N-1 by 2N-1 grid.
% Walk randomly from (0,0) to an edge.
% Vectors x,y represent the path.
```

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```
function [x, y] = RandomWalk2D(N)

k=0; xc=0; yc=0;

while not at an edge
    % Choose random dir, update xc,yc

    % Record new location in x, y

end
```

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Array index starts at 1

x	5	.4	.91	-4	-1	7
	1	2	3	4	5	6

Let  $k$  be the index of vector  $x$ , then

- $k$  must be a positive integer
- $1 \leq k \leq \text{length}(x)$
- To access the  $k^{\text{th}}$  element:  $x(k)$

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```
% Standing at (xc,yc)
% Randomly select a step
r= rand(1);
if r < .25
    yc= yc + 1; % north
elseif r < .5
    xc= xc + 1; % east
elseif r < .75
    yc= yc -1; % south
else
    xc= xc -1; % west
end
```

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RandomWalk2D.m

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1-d array: **vector**

- An array is a **named** collection of **like** data organized into rows or columns
- A 1-d array is a row or a column, called a **vector**
- An **index** identifies the **position** of a value in a vector

v

.8	.2	1
1	2	3

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## Accessing values in a vector

score

93	99	87	80	85	82
1	2	3	4	5	6

Given the vector **score** ...

```
score(4)= 80;
score(5)= (score(4)+score(5))/2;
k= 1;
score(k+1)= 99;
```

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## Here are a few different ways to create a vector

count= zeros(1,6)      count

0	0	0	0	0	0
---	---	---	---	---	---

x= linspace(10,30,5)      x

10	15	20	25	30
----	----	----	----	----

y= [3 7 2 1]      y

3	7	2	1
---	---	---	---

z= [3; 7; 2]      z

3
7
2

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## Another representation for the random step

- Observe that each update has the form
 
$$x_c = x_c + \Delta x$$

$$y_c = y_c + \Delta y$$
 no matter which direction is taken.
- So let's get rid of the if statement!
- Need to create two "change vectors"  $\Delta x$  and  $\Delta y$

deltaX

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deltaY

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RandomWalk2D\_v2.m

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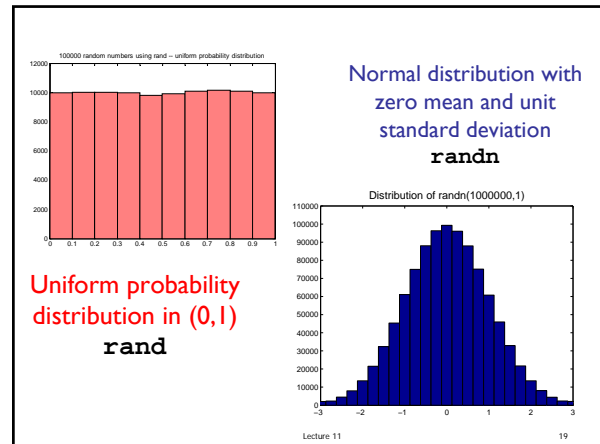
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## Random numbers

- **Pseudorandom** numbers in programming
- Function `rand(...)` generates random real numbers in the interval (0,1). All numbers in the interval (0,1) are equally likely to occur—**uniform** probability distribution.
- Examples:
  - `rand(1)` one random # in (0,1)
  - `6*rand(1)` one random # in (0,6)
  - `6*rand(1)+1` one random # in (1,7)

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## Simulate a fair 6-sided die

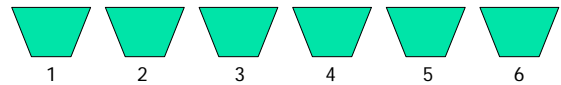
Which expression(s) below will give a random *integer* in [1..6] with equal likelihood?

- ☒ A `round(rand(1)*6)`
- ☒ B `ceil(rand(1)*6)`
- ☐ C Both expressions above

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## Possible outcomes from rolling a fair 6-sided die



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## Algorithm

Repeat the following:

```
% roll the die

% increment correct "bin"
```

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```
function count = rollDie(rolls)

FACES= 6;           % #faces on die
count= zeros(1,FACES); % bins to store counts

% Count outcomes of rolling a FAIR die
for k= 1:rolls
    % Roll the die

    % Increment the appropriate bin
end

% Show histogram of outcome
```

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