## Final Exam Review

CS 1110

## Introduction to Computing Using Python

[E. Andersen, A. Bracy, D. Gries, L. Lee, S. Marschner, C. Van Loan, W. White]

## Announcements

- No post-lecture office hours today
- Study Guide is published
- Extra review sessions happening
- Final Exam is Sunday, May 15


## Where and When is your Exam?

- Check on Canvas
- Final Exam Date \& Time Assignments
- Pretty much everyone is taking it in Barton
- Only a few exceptions
- Extended Time Exam Accommodations
- Closed Notes \& Book, Reference Sheet
- Bring your Cornell ID


## Expressions

An expression represents something

- Python evaluates it (turns it into a value)
- Similar to a calculator


## Examples:

- 2.3
- $(3 * 7+2) * 0.1$


## Types

Type: set of values \& operations on them Meaning of operations depends on type

Type float:

- Values: real numbers
- Ops: +, -, *, /,//, **, \%

Type int:

- Values: integers
- Ops: +, -, *, //, \%, **

Type bool:

- Values: True, False
- Ops: not, and, or

Type str:

- Values: strings
- Double quotes: "abc"
- Single quotes: ' abc'
- Ops: + (concatenation)


## Variable Assignment

## Example:

variable

equals sign
(just one!)

An assignment statement:

- takes an expression
- evaluates it, and
- stores the value in a variable


## In More Detail: Variables

- A variable
- is a named memory location (box)
- contains a value (in the box)
- Examples:


Variable $\mathbf{x}$, with value 5 (of type int)
area 20.1 Variable area, w/ value 20.1 (of type float)

## Expressions vs. Statements

## Expression

## Statement

- Represents something
- Python evaluates it
- End result is a value
- Examples:
- 2.3
- (3+5)/4
- $x==5$
- Does something
- Python executes it
- Need not result in a value
- Examples:
- $x=2+1$
- $x=5$

Executing an Assignment Statement
The command: $\quad x=3.0^{*} x+1.0$
"Executing the command":

1. Evaluate right hand side $\quad 3.0^{*} x+1.0$
2. Store the value in the variable $\times$ 's box

- Requires both evaluate AND store steps
- Critical mental model for learning Python


## Function Calls

- Function calls have the form:

- Arguments
- Separated by commas
- Can be any expression

A function might have $0,1, \ldots$ or many arguments

## Modules: Libraries vs. Scripts

## Library

## Script

- Provides functions, variables - Behaves like an application
- import it into Python shell, - At command line prompt, don't include ".py"
Within Python shell you have access to the functions and variables of the imported $\Delta$ • After running the app you're module Tell python to run the file (use full filename, including ".py") back at the command line


## Files look the same. Difference is how you use them.

## Visualizing functions \& variables

Running Example:

1. Built-in functions
2. Define a new variable
3. Import a module
4. Use a module variable

C:l> python
>>> $x=7$
>>> import math
>>> x = math.pi

What Python can access directly int()
float()
str()
type()
print()
$\times \quad$ 邓 3.14159
math


## Understanding How Functions Work

- We draw pictures to show what is in memory
- Call Frame: representation of function call
- Line number of the next statement in the

Draw parameters as
variables (named boxes)
function body to execute

- Starts with $1^{\text {st }}$ statement in function body

| function name | instruction counter |
| :--- | :--- |

parameters
local variables

Not just a pretty picture!
The information in this picture depicts exactly what is stored in memory on your computer.

## Function Access to Global Space



Python has just executed line 6.
C:l> python height3.py 5

Global Space

| print() <br> $\ldots$. <br> INCHES_PER_FT <br> get_feet( ) | 12 |
| :--- | :---: |
| answer | 5 |



## A Precondition Is a Contract

- If precondition is met, the function will work!
- If precondition is not met... no guarantees!


## Representative Tests

- Cannot test all inputs
- "Infinite" possibilities
- Limit ourselves to tests that are representative
- Each test is a significantly different input
- Every possible input is similar to one chosen
- An art, not a science
- If easy, never have bugs
- Learn with much practice


## Representative Tests for

 vowel_count(w)- Word with just one vowel
- For each possible vowel!
- Word with multiple vowels
- Of the same vowel
- Of different vowels
- Word with only vowels
- Word with no vowels


## Objects: Organizing Data in Folders

- An object is like a manila folder
- It contains other variables
- Variables are called attributes
- These values can change
- It has an ID that identifies it
- Unique number assigned by Python (just like a NetID for a Cornellian)
- Cannot ever change
- Has no meaning; only identifies



## Storage in Python

- Global Space
- What you "start with"
- Stores global variables
- Lasts until you quit Python
- Heap Space
- Where "folders" are stored
- Have to access indirectly
- Call Stack (with Frames)
- Parameters
- Other variables local to function
- Lasts until function returns

Global Space Heap Space
p id2 $\quad \mathrm{id} 2$

## Call Stack



## Methods: a special kind of function

Methods are:

- Defined for specific classes
- Called using objects of that class variable.method( arguments)


## Example:

>>> import shapes
>>> u = shapes.Point3(4,2,3)
>>> u.greet()
"Hil I am a 3 -dimensional point located at $(4,2,3)$ "
>>>

## Global Space

u id3

## Heap Space

 id3

## Built-in Types vs. Classes

## Built-in types

## Classes

- Built-into Python
- Refer to instances as values
- Instantiate with simple assignment statement
- Can ignore the folders
- Provided by modules
- Refer to instances as objects
- Instantiate with assignment statement with a constructor
- Must represent with folders


## Classes are user-defined Types

Defining new classes = adding new types to
Python
class name
id2

z 5

## Example Classes

- Point3
- Rect
- Freq (A3), for word frequencies
- Doll (class, lab)
- Song, Mix (A4)


## Evaluating a Constructor Expression

1. Constructor creates a new object (folder) of the class Course on the Heap

- Folder is initially empty
- Has id

2. Constructor calls__init__ (self, "CS 1110", 4)

- self = identifier ("Fill this folder!")
- Other args come from the constructor call
- commands in __init__ populate folder
- __init__ has no return value! ("I filled it!")

3. Constructor returns the id
4. LHS variable created, id is value in the box
c1 = Course("CS 1110", 4)

## Classes Have Folders Too

## Object Folders

- Separate for each instance
- Example: 2 Student objects

- Data common to all instances
Student
max_credit 20
max_credit 20
- Not just data!
- Everything common to all instances goes here!


## Object Methods

- Attributes live in object folder
- Class Attributes live in class folder
- Methods live in class folder

```
max_credit 20
__init__(self, netID,
courses, major)
```

| id5 | Student |
| :---: | :---: |
| netID | 'abc123' |
| courses | id2 |
| major | "Music" |
| n_credit | 15 |

## Defining a Subclass



## init__: write new one, access parent's

class Shape:
"""A shape @ location x,y
def __init__(self, x, y): self.x = x
self. $y=y$

- Want to use the original version of the method?
- New method = original+more
- Don't repeat code from the original
- Call old method explicitly
class Circle(Shape):


## Understanding Method Overriding

```
c1 = Circle(1,2,4.0) print(str(c1))
```

- Which __str__ do we use?
- Start at bottom class folder
- Find first method with name
- Use that definition
- Each subclass automatically inherits methods of parent.
- New method definitions override those of parent.
__str__(self)
__eq__(self)
Shape
__init__(self, $x, y$ )
__str__(self)
__eq__(self)
draw(self)

```
__init__(self)
```

```
__init__(self)
```


## Name Resolution Revisited

- To look up attribute/method name 1. Look first in instance (object folder)

2. Then look in the class (folder)

- Subclasses add two more rules:

3. Look in the superclass
4. Repeat 3. until reach object

Often called the Bottom-Up Rule

```
c1 = Circle(1,2,4.0)
r = c1.radius
c1.draw()
```



## Operator Overloading: Equality

Implement $\qquad$ eq $\qquad$ to check for equivalence of two Fractions instead
class Fraction():
"""Instance attributes:
numerator: top [int]denominator: bottom [int > 0]"""

```
def __eq__(self,q):
    """Returns: True if self, q equal,
```

    False if not, or q not a Fraction"""
    if type(q) != Fraction:
        return False
    left = self.numerator*q.denominator
    right = self.denominator*q.numerator
    return left == right
    
## eq vs. is

## == compares equality

is compares identity
id4
Circle

| c1 | id4 4 |
| :--- | :--- |
| c2 | id5 |
| c3 | id5 |

Circle

$y>1$
radius 25

## The isinstance Function

isinstance(<obj>,<class>)

- True if <obj>'s class is same as or a subclass of <class>
- False otherwise


## Example:

c1 = Circle(1, 2, 4.0)

- isinstance(c1,Circle) is True
- isinstance(c1,Shape) is True

- Generally preferable to type
- Works with base types too!


## Lists: objects with special "string-like" syntax

## List

- Attributes are indexed
- Example: x[2]

Global Space
$\times \quad$ id2

Heap Space


## Objects

- Attributes are named
- Example: p.x

Global Space
p id3
id3


## Sequences: Lists of Values

- $s=$ 'abc d'

| 0 | 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: | :---: |
| a | b | c |  | d |

- Put characters in quotes
- Use \' for quote character
- Access characters with []
- $s[0]$ is 'a'
- s[5] causes an error
- $s[0: 2]$ is 'ab' (excludes $c$ )
- $\mathrm{s}[2:]$ is 'c $\mathrm{d}^{\prime}$
- len(s) $\rightarrow$ 5, length of string
- $x=[5,6,5,9,15,23]$

| 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 5 | 6 | 5 | 9 | 15 | 23 |

- Put values inside [ ]
- Separate by commas
- Access values with []
- $x[0]$ is 5
- x[6] causes an error
- $x[0: 2]$ is $[5,6]$ (excludes $2^{\text {nd }} 5$ )
- $x[3:]$ is $[9,15,23]$
- len $(x) \rightarrow 6$, length of list


## List is mutable; strings are not

- Format:
<var>[<index>] = <value>
- Reassign at index
- Affects folder contents
- Variable is unchanged
- Strings cannot do this
- Strings are immutable

$$
\begin{aligned}
& x=[5,7,4,-2] \\
& x[1]=8 \\
& s=\text { "Hello!" } \\
& s[0]=‘ J \prime
\end{aligned}
$$

TypeError: 'str' object does not support item assignment

Heap Space



## Things that Work for All Sequences

$\mathrm{s}=$ 'slithy'

$$
x=[5,6,9,6,15,5]
$$

s.index('s') $\rightarrow 0$
s.count('t') $\rightarrow 1$
len(s) $\rightarrow 6$
$s[4] \rightarrow$ "h"
$\mathrm{s}[1: 3] \rightarrow$ "li"
s[3:] $\rightarrow$ "thy"
$\mathrm{s}[-2] \rightarrow$ "h"
s+'toves' $\rightarrow$ "slithy toves"
s * $2 \rightarrow$ "slithyslithy"
' t ' in $\mathrm{s} \rightarrow$ True

| methods | $x . \operatorname{index}(5) \rightarrow 0$ <br>  <br>  <br> x.count(6) $\rightarrow 2$ |
| :--- | :--- |

built-in fns $\operatorname{len}(x) \rightarrow 6$
$x[4] \rightarrow 15$
$\mathrm{x}[1: 3] \rightarrow[6,9]$
$\mathrm{x}[3:] \rightarrow[6,15,5]$
$x[-2] \rightarrow 15$
$\frac{n}{0}$
$\frac{1}{\sigma}$
$\frac{1}{0}$
0
0
$x+[1,2] \rightarrow[5,6,9,6,15,5,1,2]$
$x^{*} 2 \rightarrow[5,6,9,6,15,5,5,6,9,6,15,5]$
15 in $x \rightarrow$ True

## Dictionaries are mutable

1. Can reassign values

- d['ec1'] = 'Ellis'

2. Can add new keys

- d['psb26'] = 'Pearl'

3. Can delete keys

- del d['tm55']

$$
\begin{aligned}
& \text { d = \{'ec1':'Ezra', } \\
& \text { 'ec2':'Ezra', } \\
& \text { 'tm55':'Toni'\} } \\
& \text { d id8 } \\
& \begin{array}{cc}
\text { id8 } & \text { dict } \\
\text { 'ec1' }{ }^{\text {'Ellis' }} \\
\text { 'ec2' }{ }^{\prime} \text { 'Ezra' } \\
\text { 'tms' 'Tési' } \\
\text { 'psb26' 'Pearl' }
\end{array} \\
& \text { Deleting key deletes both } \\
& \text { key and value }
\end{aligned}
$$

## Nested Lists

- Lists can hold any objects
- Lists are objects
- Therefore lists can hold other lists!

$$
\begin{aligned}
& \mathrm{b}=[3,1] \\
& \mathrm{c}=[1,4, \mathrm{~b}] \\
& \mathrm{a}=[2,1] \\
& \mathrm{x}=[1, \mathrm{a}, \mathrm{c}, 5]
\end{aligned}
$$

## Global Space Heap



| id4 |  |
| :---: | :---: |
| 0 | 1 |
| 1 | id3 |
| 2 | id2 |
| 3 | 5 |

This is drawing accurate, but a little hard to reason about...

## Nested Lists

Conceptually, you can visualize nested lists like this:

$$
\begin{aligned}
& \mathrm{b}=[3,1] \\
& \mathrm{c}=[1,4, \mathrm{~b}] \\
& \mathrm{a}=[2,1] \\
& \mathrm{x}=[1, \mathrm{a}, \mathrm{c}, 5]
\end{aligned}
$$

$$
x=[1,[2,1],[1,4,[3,1]], 5]
$$


$x=[1,[2,1]$,

$$
[1,4,[3,1]], 5]
$$



## Conditionals: "Control Flow" Statements

if $b:$
s1 \# statement
s3 \# statement


Branch Point:
Evaluate \& Choose


Flow
Program only takes one path during an execution (something will not be executed!)

## Conditionals: If-Elif-Else-Statements (2)

## Format

## Notes on Use

- No limit on number of elif
- Must be between if, else
- else is optional
- if-elif by itself is fine
- Booleans checked in order
- Once Python finds a true <Boolean-expression>, skips over all the others
- else means all <Booleanexpression> are false


## For Loops: Processing Sequences

## for $x$ in grades:

print(x)


- loop sequence: grades
- loop variable: x
- loop body: print(x)

To execute the for-loop:

1) Check if there is a "next" element of loop sequence
2) If so:

- assign next sequence element to loop variable
- Execute all of the body
- Go back to 1)

3) If not, terminate execution

## For Loop with labels

```
def num_zeroes(the_list):
```

"""Returns: the number of zeroes in the_list Precondition: the_list is a list"""

```
count = 0
for x in the_list:
    if x == 0:
            count = count + 1
```

return count

Accumulator variable
Loop sequence
Loop variable
Loop body

## Modifying the Contents of a List

def add_bonus(grades):
"""Adds 1 to every element in a list of grades (either floats or ints)""" size = len(grades)
for $k$ in range(size): grades $[k]=$ grades[k]+1 need to use range to get the indices.
lab_scores $=[8,9,10,5,9,10]$
print("Initial grades are: "+str(lab_scores))
add_bonus(lab_scores)
print("With bonus, grades are: "+str(lab_scores))
Watch this in the python tutor!

## Beyond Sequences: The while-loop

## while <condition >:

$\left.\begin{array}{l}\text { statement } 1 \\ \text {... } \\ \text { statement } n\end{array}\right\}$ body

Relationship to for-loop

- Broader notion of "keep working until done"
- Must explicitly ensure condition becomes false
- You explicitly manage what changes per iteration


## Recursion

## Recursive Function:

A function that calls itself

Two parts to every recursive function:

1. A simple case: can be solved easily
2. A complex case: can be made simpler (and simpler, and simpler... until it looks like the simple case)

## Recursion is great for Divide and Conquer

Goal: Solve problem $P$ on a piece of data

## data

Idea: Split data into two parts and solve problem


## Three Steps for Divide and Conquer

1. Decide what to do on "small" data

- Some data cannot be broken up
- Have to compute this answer directly

2. Decide how to break up your data

- Both "halves" should be smaller than whole
- Often no wrong way to do this (next lecture)

3. Decide how to combine your answers

- Assume the smaller answers are correct
- Combine them to give the aggregate answer


## Recursive Call Frames (all calls complete!)

def factorial(n):
"""Returns: factorial of $n$.
Precondition: n $\geq 0$ an int"""
1 if $\mathrm{n}=0$ :
2 return 1
3 return $n * f a c t o r i a l(n-1)$
factorial(3)


## Search Algorithms

Recall from last lecture:

- Searching for data is a common task
- Linear search: on the order of $n$
- input doubles? $\rightarrow$ work doubles!
- Binary search: on the order of $\log 2 n$
- input doubles? $\rightarrow$ work increases by just 1 unit!
- BUT data needs to be sorted...
- Sorting data now suddenly interesting...


## Sorting Algorithms

- Sorting data is a common task
- Insertion sort: on the order of $\mathrm{n}^{2}$
$\bullet$ input doubles? $\rightarrow$ work quadruples! (yikes)
- Merge sort: on the order of $n \cdot \log _{2}(n)$
- input doubles? $\rightarrow$ work increases by a bit more than double

For fun, check out the visualizations:
https://www.youtube.com/watch?v=xxcpvCGrCBc



