CS 1110 Prelim 1 October 19th, 2021

Items in orange are additions by the Spring 2022 instructors.

This 90-minute exam has 6 questions worth a total of 100 points. Read over the whole test before starting. Budget your time wisely. Use the back of the pages if you need more space. You may tear the pages apart; we have a stapler at the front of the room.

It is a violation of the Academic Integrity Code to look at any exam other than your own, to look at any other reference material, or to otherwise give or receive unauthorized help.

You will be expected to write Python code on this exam. We recommend that you draw vertical lines to make your indentation clear, as follows:

```python
def foo():
    if something:
        do something
        do more things
    do something last
```

You should not use loops or recursion on this exam. Beyond that, you may use any Python feature that you have learned in class (if-statements, try-except, lists), unless directed otherwise.

<table>
<thead>
<tr>
<th>Question</th>
<th>Points</th>
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</thead>
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<td>Total:</td>
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</tbody>
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The Important First Question:

1. [2 points] Write your last name, first name, and netid, at the top of each page.
Throughout this exam you will be asked questions about strings and lists. You are expected to understand how slicing works. In addition, the following functions and methods may be useful.

### String Functions and Methods

<table>
<thead>
<tr>
<th>Expression or Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>len(s)</code></td>
<td>Returns: number of characters in s; it can be 0.</td>
</tr>
<tr>
<td><code>a in s</code></td>
<td>Returns: True if the substring a is in s; False otherwise.</td>
</tr>
<tr>
<td><code>s.count(s1)</code></td>
<td>Returns: the number of times s1 occurs in s.</td>
</tr>
<tr>
<td><code>s.find(s1)</code></td>
<td>Returns: index of the first character of the FIRST occurrence of s1 in s (-1 if s1 does not occur in s).</td>
</tr>
<tr>
<td><code>s.find(s1,n)</code></td>
<td>Returns: index of the first character of the first occurrence of s1 in s STARTING at position n. (-1 if s1 does not occur in s from this position).</td>
</tr>
<tr>
<td><code>s.rfind(s1)</code></td>
<td>Returns: index of the first character of the LAST occurrence of s1 in s (-1 if s1 does not occur in s).</td>
</tr>
<tr>
<td><code>s.isalpha()</code></td>
<td>Returns: True if s is not empty and its elements are all letters; it returns False otherwise.</td>
</tr>
<tr>
<td><code>s.isdigit()</code></td>
<td>Returns: True if s is not empty and its elements are all numbers; it returns False otherwise.</td>
</tr>
<tr>
<td><code>s.isalnum()</code></td>
<td>Returns: True if s is not empty and its elements are all letters or numbers; it returns False otherwise.</td>
</tr>
<tr>
<td><code>s.islower()</code></td>
<td>Returns: True if s is has at least one letter and all letters are lower case; it returns False otherwise (e.g. 'a123' is True but '123' is False).</td>
</tr>
<tr>
<td><code>s.isupper()</code></td>
<td>Returns: True if s is has at least one letter and all letters are upper case; it returns False otherwise (e.g. 'A123' is True but '123' is False).</td>
</tr>
<tr>
<td><code>s.lower()</code></td>
<td>Returns: A copy of s with all letters lower case.</td>
</tr>
<tr>
<td><code>s.upper()</code></td>
<td>Returns: A copy of s with all letters upper case.</td>
</tr>
</tbody>
</table>

### List Functions and Methods

<table>
<thead>
<tr>
<th>Expression or Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>len(x)</code></td>
<td>Returns: number of elements in list x; it can be 0.</td>
</tr>
<tr>
<td><code>y in x</code></td>
<td>Returns: True if y is in list x; False otherwise.</td>
</tr>
<tr>
<td><code>x.count(y)</code></td>
<td>Returns: the number of times y occurs in x.</td>
</tr>
<tr>
<td><code>x.index(y)</code></td>
<td>Returns: index of the FIRST occurrence of y in x (an error occurs if y does not occur in x).</td>
</tr>
<tr>
<td><code>x.index(y,n)</code></td>
<td>Returns: index of the first occurrence of y in x STARTING at position n (an error occurs if y does not occur in x).</td>
</tr>
<tr>
<td><code>x.append(y)</code></td>
<td>Adds y to the end of list x.</td>
</tr>
<tr>
<td><code>x.insert(i,y)</code></td>
<td>Inserts y at position i in list x, shifting later elements to the right.</td>
</tr>
<tr>
<td><code>x.remove(y)</code></td>
<td>Removes the first item from the list whose value is y (an error occurs if y does not occur in x).</td>
</tr>
</tbody>
</table>

The last three list methods are all procedures. They return the value `None`.
2. [8 points total] **Short Answer.**

   (a) [5 points] What is the definition of a type in Python? List at least four examples of types built into Python.
   
   A type is a collection of values together with the operations on them. The four basic types are `int`, `float`, `bool`, and `str`. However, we would also allow `list` or `tuple`.

   (b) [3 points] Which of the following two expressions produces an error (none, one, or both)?
   
   \[
   \text{False and (5 / 0)} \quad (5 / 0) \text{ or True}
   \]
   
   Explain why this is the case.
   
   Only the second one produces an error. The first one does not produce an error because Python “short-circuits” the calculation; once it knows that the first value of an `and` is `False`, it does not need to evaluate anything else. But it must always evaluate the first expression, which is why the second one produces an error.

3. [20 points] **Call Frames.**

   Consider the following function definitions.

   ```python
   def double(a):
       return a + a
   def mystery(a):
       a[-1] = a[0]
       return double(a)
   ```

   Assume `p = [1, 2, 3]` is a global variable referencing a list in the heap, as shown on the next page. On the next two pages, diagram the evolution of the call

   \[
   q = \text{mystery}(p)
   \]

   Diagram the state of the *entire call stack* for the function `mystery` when it starts, for each line executed, and when the frame is erased. If any other functions are called, you should do this for them as well (at the appropriate time). This will require a total of eight diagrams, not including the (pre-call) diagram shown.

   You should draw also the state of global space and the heap at each step. You can ignore the folders for the function definitions. Only draw folders for lists or objects. You are also allowed to write “unchanged” if no changes were made to either global space or the heap.
Spring students: Ignore these solutions; we use a different notation. But so you know: the “MAYBE” at the end means: students could either include or not include the “lost” object id2.
Call Stack

Global Space

The Heap

mystery

a
id1

0
1
2
3

id1

list

0
1
2
3

id1

list

0
1
2
3

id1

list

0
1
2
3

id1

list

0
1
2
3

id2

list

0
1
2
3

mystery

a
id1

double

a
id1

mystery

a
id1

double

a
id1

b
id2

Page 5
def expand(s):
    """Returns english date expansion of s"""

    Years before 50 are 20XX. Others are 19XX.
    Precond: s a string for a VALID 'm/d/y'.
    m and d are either one or two digits.
    y is always two digits

    div1 = s.find('/')
    print('div1 is ' +str(div1)) # WATCH
    div2 = s.find('/',div1+1)
    print('div2 is ' +str(div2)) # WATCH
    m = int(s[:div1])
    print('m is ' +str(m)) # WATCH
    y = int(s[div2+1:])
    print('y is ' +str(y)) # WATCH
    m = monthize(m)
    print('month is ' +str(m)) # WATCH
    d = dayize(s[div1+1:div1+3])
    print('day is ' +str(d)) # WATCH
    y = yearize(y)
    print('year is ' +str(y)) # WATCH

    return m+' '+d+', '+y

def monthize(m):
    """Returns the month abbrev for m"""

    Precond: 1 <= m <= 12 is an int"
    # Combined TRACE and WATCH
    print('monthize on ' +str(m))
    # The list is NOT a bug
    items = ['Jan','Feb','Mar','Apr','May','Jun','Jul','Aug','Sep','Oct','Nov','Dec']
    return items[m-1]

def dayize(s):
    """Returns s with the correct suffix"""

    Precond: s a str of one or two digits"
    # Combined TRACE and WATCH
    print('dayize on ' +s)
    if len(s) == 2 and s[0] == '1':
        print('teens day') # TRACE
        suff = 'th'
    elif s[-1] == '1':
        print('ends in 1') # TRACE
        suff = 'st'
    elif s[-1] == 2:
        print('ends in 2') # TRACE
        suff = 'nd'
    elif s[-1] == '3':
        print('ends in 3') # TRACE
        suff = 'rd'
    else:
        print('other ending') # TRACE
        suff = 'th'

    return s+suff

def yearize(y):
    """Returns 4 digit year for y (as str)"

    Years before 50 are 20XX. Others are 19XX.
    Precond: 0 <= y <= 99 is an int"
    # Combined TRACE and WATCH
    print('yearize on ' +str(y))
    if y < 50:
        print('< 50') # TRACE
        pref = '20'
    if y > 50:
        print('> 50') # TRACE
        pref = '19'
    return pref+str(y)
Tests: comments give the expected answer

>>> expand('9/22/19') # 'Sep 22nd, 2019'
div1 is 1
div2 is 4
m is 9
y is 19
monthize on 9
month is Sep
dayize on 22
other ending
day is 22th
yearize on 19
< 50
year is 2019
Sep 22th, 2019

>>> expand('12/7/41') # 'Dec 7th, 2041'
div1 is 2
div2 is 4
m is 12
y is 41
monthize on 12
month is Dec
dayize on 7/
other ending
day is 7/th
yearize on 41
< 50
year is 2041
Dec 7/th, 2041

>>> expand('12/15/50') # 'Dec 15th, 1950'
div1 is 2
div2 is 5
m is 12
y is 50
monthize on 12
month is Dec
dayize on 15
teens day
day is 15th
yearize on 50
Traceback (most recent call last):
  File "<stdin>", line 1, in <module>
  File "debug.py", line 22, in expand
    y = yearize(y)
  File "debug.py", line 80, in yearize
    return pref+str(y)
UnboundLocalError: unknown variable 'pref'

First Bug:
This is a subtle type error that we put into the code by accident, and then left in as part of the exam. Note the elif statement on line 53

    elif s[-1] == 2:
The expression s[-1] is a string, while 2 is an int. They can never be equal. The correct code is therefore

    elif s[-1] == '2':

Second Bug:
This bug is not in dayize. Instead, it is a slicing error that violates the precondition of that function. On line 20, you have the code

    d = dayize(s[div1+1:div1+3])

This only works if the day is represented by two digits. The correct code is

    d = dayize(s[div1+1:div2])

Third Bug:
This bug is caused because the variable pref is not assigned a value. That is because neither of the two if-statements in yearize are executed. The correct thing to do is to take this if-statement

    if y > 50:
and replace it with else:
Alternately, change the > to >=.
(b) [10 points] Consider the following function specification:

```python
def replace(s,a,b):
    """Returns the string s with all instances of character a replaced by b.
    Example: replace('banana', 'n', 't') returns 'batata'
    Precond: s, a, b are all strings with no characters other than lowercase
    letters. a is exactly one letter.""
```

Do not implement this function. Instead, we want you to write at least six test cases below. By a test case, we just mean an input and an expected output; you do not need to write an `assert_equal` statement. For each test case, you should explain why it is substantially different from the others.

There are many answers to this question. Here are some of the ones we had in mind.

<table>
<thead>
<tr>
<th>Input</th>
<th>Output</th>
<th>Reason</th>
</tr>
</thead>
<tbody>
<tr>
<td>s='', a='a', b='b'</td>
<td>''</td>
<td>String s is empty</td>
</tr>
<tr>
<td>s='abc', a='x', b='y'</td>
<td>'abc'</td>
<td>Nothing is replaced</td>
</tr>
<tr>
<td>s='abc', a='a', b='t'</td>
<td>'bc'</td>
<td>String b is empty (deletion)</td>
</tr>
<tr>
<td>s='abc', a='a', b='x'</td>
<td>'xbc'</td>
<td>Normal replacement</td>
</tr>
<tr>
<td>s='abba', a='a', b='x'</td>
<td>'xbbx'</td>
<td>Repeated replacement</td>
</tr>
<tr>
<td>s='abc', a='a', b='xy'</td>
<td>'xybc'</td>
<td>String b is multiple characters</td>
</tr>
</tbody>
</table>

(c) [4 points] Do not implement the function specified below. Instead, use assert statements to enforce the precondition. You do not need to provide error messages. Not fair game for Spring 2022 Prelim 1: we didn’t cover assert statements.

```python
def isnetid(s):
    """Returns True if the user identifier s is a registered netid
    Precond: s is a nonempty string of only letters and digits. All letters
    must be lowercase. The string s cannot start with a digit.""
    assert type(s) == str
    assert s.isalnum() and s.islower()
    assert len(s) > 0
    assert not s[0].isdigit()
```

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5. [25 points] **String Slicing.**

Implement the function below. You **may not use a for-loop to implement this function** (and a for-loop is not necessary). Simply use the functions and methods provided on the reference page. Pay close attention to the examples to better understand the function. In handwritten solutions, we’d like you to use a 'square u' \( _u \) to indicate a (single) space.

```python
def initials(name):
    """Returns (up to three) initials for the given name
    
    A word is a (sub)string composed of only letters. A name is a sequence of words separated by (single) spaces. The initials of a name are the first letters of each word. If there are more than three words, this function only chooses the initials of the first two words, and the last word. The initials returned are all lower case.
    
    Examples: initials('Walker') returns 'w'
                initials('Walker White') returns 'ww'
                initials('Walker McMillan White') returns 'wmw'
                initials('Daniel Michael Blake Day Lewis') returns 'dml'
    
    Precond: name is a non-empty string of letters and spaces. There are no adjacent spaces. The name does not begin or end with a space.""
    
    # Get the first initial
    first = name[0]
    
    # Get position of the first space (if any)
    pos = name.find(' ')
    if (pos == -1):
        # There are no other words for initials
        middle = '
        last = '
    elif name.count(' ') > 1:
        # There is (at least one) middle name
        middle = name[pos+1]
        # Find the last name
        pos = name.rfind(' ')
        last = name[pos+1]
    else:
        # There is no middle name
        middle = '
        last = name[pos+1]
    
    # Glue together and convert to lower case
    initials = first+middle+last
    initials = initials.lower()
    return initials
```

In the above, there is no need for the parentheses in the first if line. More compact solution on next page.
Alternate solution:

```python
if name.count(' ') == 0:  # just one name
    return name[0].lower()

# there are at least two names, get 1st two initials
space1 = name.index(' ')
outstr = name[0] + name[space1 + 1]  # WW or DM

if name.count(' ') > 1:
    lastspace = name.rfind(' ')
    outstr = outstr + name[lastspace+1]
return outstr.lower()
```
6. **[22 points total] Objects and Functions.**

Remember the class `RGB` from Assignment 3. Objects of this class have three attributes: `red`, `green`, and `blue`. These values must be integers between 0 and 255; assigning any other value to them will result in an error. `RGB` has a fourth attribute: `alpha`, which has the same restrictions. This means that when you create an `RGB` object, the proper constructor call is `RGB(r, g, b, a)` (do not worry about `introcs` for this question). We ignored this attribute in Assignment 3, but we will use it here.

The alpha attribute is used for **color composition**. Each pixel on your computer monitor can only show only one color at a time. If we want to show multiple images on top of each other, we have to combine the colors together.

(a) **[8 points]** Spring would not have had the same A3, but Spring students can do this question by reading the text. The simplest form of color composition is straight addition. We add the two red values to get the new red, the two green values to get the new green, and so on. The result of this is very similar to mixing colors in primary school, as shown below.

![Color Composition](image)

Note that the attribute invariants can never be violated. If adding together two color results in an attribute that is greater than 255, we use the value of 255 instead. With this in mind, implement the following procedure according to the specification.

```python
def add_color(color1, color2):
    """Adds the colors color1 and color2, storing the result in color1.
    Addition is on each attribute (including alpha) as described above.
    This function is a PROCEDURE and has no return value.
    Preconditions: color1 and color2 are RGB objects.""
    # Add red, and handle the case we go over 255
    red = color1.red + color2.red
    color1.red = min(red, 255)

    # Handle the remaining attributes the same
    green = color1.green + color2.green
    color1.green = min(green, 255)

    blue = color1.blue + color2.blue
    color1.blue = min(blue, 255)

    alpha = color1.alpha + color2.alpha
    color1.alpha = min(alpha, 255)

    # No return value
```

Page 12
(b) [14 points] Spring students should skip this question; it is too close to the Fall A3 to be a good question for Spring students. A more popular form of color composition is alpha-blending. The attribute \texttt{alpha} represents the amount of transparency of the color on top. An \texttt{alpha} of 255 means the color is completely opaque, while an \texttt{alpha} of 0 is completely transparent.

To perform alpha-blending, you must convert the \texttt{red}, \texttt{green}, \texttt{blue}, and \texttt{alpha} values to the range 0 to 1, just as in Assignment 3. You then apply the following formula:

\[
\begin{align*}
R' &= \alpha_1 R_1 + (1 - \alpha_1) R_2 & \text{Combine red attributes of colors 1 and 2} \\
G' &= \alpha_1 G_1 + (1 - \alpha_1) G_2 & \text{Combine green attributes of colors 1 and 2} \\
B' &= \alpha_1 B_1 + (1 - \alpha_1) B_2 & \text{Combine blue attributes of colors 1 and 2} \\
\alpha' &= \alpha_1 + (1 - \alpha_1) \alpha_2 & \text{Combine alpha attributes of colors 1 and 2}
\end{align*}
\]

In the formula above, \(R_1, G_1, \ldots\) are the attributes of the first color, \(R_2, G_2, \ldots\) are the attributes of the second color, and \(R', G', \ldots\) are the attributes of the new color. Remember to convert back to the range 0..255 when done, rounding to the nearest integer.

In practice, alpha-blending looks like the picture below.

```python
def alpha_blend(color1, color2):
    """Returns a new color blending (via the formula above) color1 and color2."

    Preconditions: color1 and color2 are RGB objects.""

    # Convert the alpha of color1 to 0..1
    alpha = color1.alpha/255.0

    # Compute the new colors as a value 0..1
    red = alpha*color1.red/255.0+(1-alpha)*color2.red/255.0
    green = alpha*color1.green/255.0+(1-alpha)*color2.green/255.0
    blue = alpha*color1.blue/255.0+(1-alpha)*color2.blue/255.0
    alpha = alpha+(1-alpha)*color2.alpha/255.0

    # Convert to integers, remembering to round
    red = int(round(red*255))
    green = int(round(green*255))
    blue = int(round(blue*255))
    alpha = int(round(alpha*255))

    # Construct a new RGB object and return it
```
return RGB(red,green,blue,alpha)