

Flag of Mauritius

- Now we have four colors!
 - Negatives: 'red' = odd, 'purple' = even
 - Positives: 'yellow' = odd, 'green' = even

pre: b

h		k
	?	

post: b

h		k
< 0 odd	< 0 even	≥ 0 odd

inv: b

h	r	s	i	t	k
< 0, o	< 0, e	≥ 0, o	?	≥ 0, e	



Flag of Mauritius

< 0, o	< 0, e	≥ 0, o	?	≥ 0, e
h	r	s	i	t
-1	-3	-2	-4	7

h	r	s	i	t	k
-1	-3	-5	-4	-2	5
				7	-6

Need two swaps
for two spaces

Flag of Mauritius

< 0, o	< 0, e	≥ 0, o	?	≥ 0, e
h	r	s	i	t
-1	-3	-2	-4	7

h	r	s	i	t	k
-1	-3	-5	-4	-2	5
				7	-6

h	r	s	i	t	k
-1	-3	-5	-4	-2	-6
				7	5

h	r	s	i	t	k
-1	-3	-5	-4	-2	-6
				7	5

See algorithms.py
for Python code

Linear Search

pre: b

h		k
	?	

post: b

h	i	k
v not here	v	?

OR

b

h		k
	v not here	

inv: b

h	i	k
v not here	?	

Linear Search

```
def linear_search(b, c, h):
    """Returns: first occurrence of c in b[h..]"""
    # Store in i the index of the first c in b[h..]
    i = h

    # invariant: c is not in b[0..i-1]
    while i < len(b) and b[i] != c:
        i = i + 1

    # post: c is not in b[h..i-1]
    # i >= len(b) or b[i] == c
    return i if i < len(b) else -1
```

Analyzing the Loop

1. Does the initialization make **inv** true?
2. Is **post** true when **inv** is true and **condition** is false?
3. Does the repetend make progress?
4. Does the repetend keep the invariant **inv** true?

Binary Search

- Vague:** Look for v in **sorted** sequence segment b[h..k].

- Better:**

- Precondition: b[h..k-1] is sorted (in ascending order).
- Postcondition: b[h..i] ≤ v and v < b[i+1..k-1]

- Below, the array is in non-descending order:

pre: b

h		k
	?	

post: b

h	i	k
≤ v		> v

inv: b

h	i	j	k
< v	?	> v	

Called **binary search**
because each iteration
of the loop cuts the
array segment still to
be processed in half