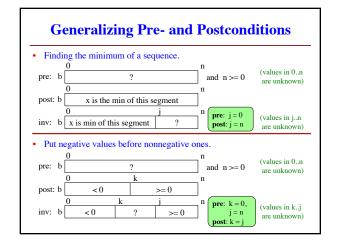
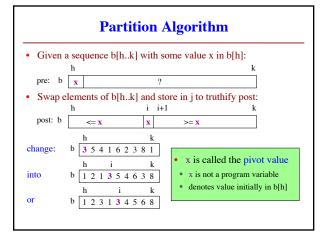
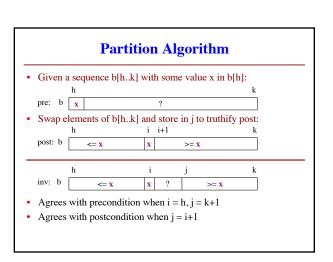


Developing Algorithms on Sequences

- Specify the algorithm by giving its precondition and postcondition as pictures.
- Draw the invariant by drawing another picture that "generalizes" the precondition and postcondition
 - The invariant is true at the beginning and at the end
- The four loop design questions
 - 1. How does loop start (how to make the invariant true)?
 - 2. How does it stop (is the postcondition true)?
 - 3. How does the body make progress toward termination?
 - 4. How does the body keep the invariant true?







Partition Algorithm Implementation def partition(b, h, k): "Partition list b[h..k] around a pivot x = b[h]""" i = h; j = k+1; x = b[h]# invariant: b[h..i-1] < x, b[i] = x, b[j..k] >= xwhile i < i-1: if b[i+1] >= x: partition(b,h,k), not partition(b[h:k+1]) # Move to end of block. Remember, slicing always copies the list! _swap(b,i+1,j-1) We want to partition the original list j = j - 1else: # b[i+1] < x _swap(b,i,i+1) # post: b[h..i-1] < x, b[i] is x, and b[i+1..k] >= xreturn i

```
Partition Algorithm Implementation
                                                    <= x | x | ? h i i+1
def partition(b, h, k):
   ""Partition list b[h..k] around a pivot x = b[h]"""
                                                                              k
 i = h; j = k+1; x = b[h]
                                                    1 2 3 1 5 0 6 3 8
  # invariant: b[h..i-1] < x, b[i] = x, b[j..k] >= x
  while i < i-1:
    if b[i+1] >= x:
       # Move to end of block
       _{	ext{swap}(b,i+1,j-1)}
      j = j - 1
    else: \# b[i+1] < x
      _swap(b,i,i+1)
  # post: b[h..i-1] < x, b[i] is x, and b[i+1..k] >= x
  return i
```

Partition Algorithm Implementation $\textcolor{red}{\textbf{def}} \hspace{0.1cm} \texttt{partition}(b, \hspace{0.1cm} h, \hspace{0.1cm} k) :$ """Partition list b[h..k] around a pivot x = b[h]""" i+1 i = h; j = k+1; x = b[h]1 2 3 1 5 0 6 3 8 # invariant: b[h..i-1] < x, b[i] = x, b[j..k] >= x while $i \le j-1$: i+1if b[i+1] >= x: 2 1 3 5 0 6 3 8 # Move to end of block. swap(b,i+1,j-1) j = j - 1 1 3 0 5 6 3 8 else: # b[i+1] < x _swap(b,i,i+1) i = i + 1# post: b[h..i-1] < x, b[i] is x, and b[i+1..k] >= x

