CS1110 1 April 2010

Developing array algorithms. Reading: 8.3..8.5

Important point: how we create the invariant, as a picture

Haikus (5-7-5) seen on Japanese computer monitors

Yesterday it worked. Today it is not working. Windows is like that.

Serious error.

All shortcuts have disappeared.

Screen. Mind. Both are blank.

A crash reduces Your expensive computer To a simple stone. The Web site you seek Cannot be located, but Countless more exist.

Three things are certain: Death, taxes, and lost data. Guess which has occurred? Chaos reigns within.
Reflect, repent, and reboot.
Order shall return.

Developing algorithms on arrays

We develop several important algorithms on arrays.

With each, we specify the algorithm by giving its precondition and postcondition as pictures.

Then, draw the invariant by drawing another picture that "generalizes" the precondition and postcondition, since the invariant is true at the beginning and at the end.

Four loopy questions —memorize them:

- 1. How does loop start (how to make the invariant true)?
- 2. When does it stop (when is the postcondition true)?
- 3. How does repetend make progress toward termination?
- 4. How does repetend keep the invariant true?

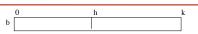
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Horizontal notation for arrays, strings, Vectors

	0		k	b.length	
b	<=	sorted	>=		

Example of an assertion about an array b. It asserts that:

- 1. b[0..k-1] is sorted (i.e. its values are in ascending order)
- 2. Everything in b[0..k-1] is \leq everything in b[k..b.length-1]



Given the index h of the First element of a segment and the index k of the element that Follows the segment, the number of values in the segment is k-h.

b[h ... k-1] has k-h elements in it.

 $\begin{array}{c|c}
h & h+1 \\
\hline
(h+1) - h = 1
\end{array}$

Invariant as picture: Combining pre- and post-condition

Finding the minimum of an array. Given array b satisfying precondition P, store a value in x to truthify postcondition Q:

Q: b x is the min of this segment

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The invariant as picture: Combining pre- and post-condition

Put negative values before nonnegative ones. given precondition P:

0 n
P: b ? (values in 0..n-1 are unknown)

Swap the values of b[0..n-1] and store in k to truthify Q:

0 k n (values in 0..k-1 are < 0, values in k..n-1 are > 0)

The invariant as picture: Combining pre- and post-condition $% \left(1\right) =\left(1\right) \left(1\right)$

Dutch national flag. Swap values of 0.n-1 to put the reds first, then the whites, then the blues. That is, given precondition P, swap value of b [0.n] to truthify postcondition Q:

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2. Compare precondition with invariant. E.g. in precondition, 0 marks first unknown. In invariant, k marks first unknown. Therefore, k and 0 must be the same.

	on algorithm: Given an array b[hk] with some value x in b[h]:
P: b [x ?
Swap el	ements of b[hk] and store in j to truthify P:
	h j k
Q: b	<= x
change:	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
or	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
x is call	ed the pivot value.
x is not	a program variable; x just denotes the value initially in $b[h]$.

Linear search

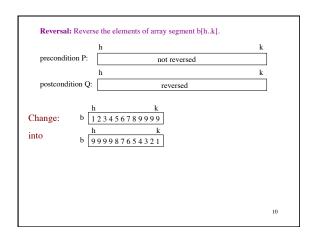
Vague spec.: Find first occurrence of v in b[h..k-1].

Better spec.: Store an integer in i to truthify postcondition Q:

Q: 1. v is not in b[h..i-1]
2. i = k OR v = b[k]
h
P: b vis in here

h
i
k
Q: b x not here x ?

OR
h
k
b x not here



Remove adjacent duplicates

change: $0 \quad n$ $b \quad 1 \quad 2 \quad 2 \quad 4 \quad 2 \quad 7 \quad 8 \quad 9 \quad 9 \quad 9$ into $b \quad 1 \quad 2 \quad 4 \quad 2 \quad 7 \quad 8 \quad 9 \quad 8 \quad 9 \quad 9 \quad 9$ into $b \quad 1 \quad 2 \quad 4 \quad 2 \quad 7 \quad 8 \quad 9 \quad 8 \quad 9 \quad 9 \quad 9$ Truthify: $b[0.h] = initial \ values \ in \ b[0..n] \ but \ with \ adj \ dups \ removed$ $h \quad k$ $Precondition P: b \quad ?$ $h \quad i \quad k$ $Postcondition Q: b \quad initial \ values \ of \ b[0.k] \quad unchanged$ $with \ no \ duplicates$

Check whether two arrays are equal

/** = "b and c are equal" (both null or both contain arrays whose elements are the same) */

public static boolean equals(int[] b, int[] c) {

}