

This purpose of this assignment is to

- Introduce you to graphics
- Give you practice with simple loops
- Give you practice with recursion
- Give you practice with helper methods and reusing previously written methods

Please read this entire document carefully. At the end of this document, we tell you what exactly to submit on the CMS. Budget your time wisely. Don't wait until the day before the deadline to do this assignment. We advise starting now and working on one or two functions a day. You may also want to experiment, drawing your own designs.

You may work with one other person. If you do so, **FORM YOUR GROUP ON THE CMS WELL BEFORE YOU SUBMIT YOUR FILES**. Remember, partners must work together and not independently.

You need not use a JUnit testing class. You will (mostly) be looking at visual output (graphics) to determine correctness.

Keep track of the time you spend on this assignment. You will be asked to put it in a comment at the top of file `A5.java`.

To save you time, we give you complete specifications of most of the methods you write. Please study them carefully. Note how precise and thorough they are. You should aim for this quality of specification when you write your own specifications.

Note on recursion in art, academic year 2009-2010: According to a 2009 article by Beth Saulnier in *Cornell Alumni Magazine*, James Siena (Cornell '79) often uses algorithms to produce his work, some of which is in the collections of the Metropolitan Museum of Art and the MoMA and has been presented at the 2004 Whitney Biennial. In the *New York Times*, critic Ken Johnson noted Siena's "recursively proliferating lattices". As a winner of the 2009 Eissner Artist of the Year award, he will have some of his pieces displayed at the Johnson Museum of Art from January to April, and will speak on campus on 16 April 2010.

Note on DrJava. Please do this immediately: In DrJava, use menu item `Edit->Preferences`; click `Interactions Pane`; and make sure the `Require variable type` box is unchecked. This will allow you to use variables in the Interactions Pane without declaring them. We also suggest changing the indent level to 4 (Preferences category `Miscellaneous`).

Directions. Download file [A5.zip](#), unzip it, and put everything in it into a new directory. It contains:

1. File `A5.java`
2. File `HSV.java`, a simple implementation of the hue-saturation-value model.
2. Package `acm`. It contains a directory of other packages, each of which contains a directory of `.class` files. These are machine-language versions of `.java` files. Do NOT load them into DrJava. The only thing you should load into DrJava is file `A5.java`. It will automatically use the `.class` files.
3. A directory `doc`, which contains specifications of all the classes in package `acm`. You will use these specs when writing method calls to draw things on the "graphics canvas". Outside of DrJava, double-click `index.html` (or open it in a browser) to see the specs. Before you do any programming in DrJava, spend some time looking at the methods that you can use in classes `GraphicsProgram`, `GTurtle`, and `GPen`,

Package `acm` was developed under the auspices of the ACM (Association for Computing Machinery), the major CS professional society. Class `A5` is a subclass of abstract class `GraphicsProgram`, which is part of the `acm` package. A `GraphicsProgram` is associated with a window on your monitor (much like class `JFrame`) that contains a "canvas" on which one can draw. When an instance of `A5` is created, the associated window appears on your monitor. You can then create "turtles" and "pens" to draw (on the canvas) in that window.

An instance of class `acm.graphics.GTurtle` maintains a pen of a certain color at a pixel (`x`, `y`) that is pointing in some direction given by an angle (0 degrees is to the right, or east; 90 degrees, north; 180 degrees, west; and 270 degrees, south). When the turtle is moved to another spot using procedure `forward`, a line is drawn if its pen is currently "down" and nothing is drawn if its pen is "up". The pen is initially black, but its color, of class `java.awt.Color`, can be changed. A footnote on page 1.5 of the ProgramLive CD contains information about class `Color`.

By following the directions above, you've already looked at `doc/index.html` and studied the specifications of methods in class `GTurtle` as given in the javadoc files. Here are some important points:

- Before an instance of `GTurtle` can be used to draw something, it has to be added to an `A5` object. You can add many turtles to the same `A5` object and draw different things with each. Function `A5.getTurtle()`, which is already written, creates a new turtle and adds it to the instance of `A5`. Read the function body carefully; make sure you understand what it is doing and how.
- The coordinates and angle of the turtle are maintained using type **double**. This is needed for maximum accuracy. If **ints** were used, errors might crop up after many calculations. However, whenever a point is to be placed in the window, its x- and y-coordinates are rounded to the nearest integer because the graphics space works with **ints**.
- Suppose `t` contains a `GTurtle`. The call `t.forward(d)` moves `t` `d` pixels in its current direction, `t.setLocation(x, y)` moves `t` to pixel `(x, y)` without drawing anything, and `t.setDirection(a)` sets its direction to angle `a`.
- A turtle `t` moves with a certain speed, which must be in the range $0 \leq \text{speed} \leq 1$, where 0 is the slowest and 1 the fastest. Not much detail on the speed is given, so we can't tell you more than that. Set the speed to `s` using `t.setSpeed(s);`.

Class `A5` contains procedure `drawTwoLines(s)` to show you how graphics work. Compile class `A5`. Then, in DrJava's Interactions pane, create an instance of class `A5` using `a= new A5();` The window with the canvas will appear. Execute the call `a.drawTwoLines(0);`. It should cause two lines to be drawn, waiting a few seconds before drawing each line. Study the body of `drawTwoLines` carefully, so that you know what each statement does.

In the Interactions pane (or in a method in class `A5`), draw some lines and rectangles to familiarize yourself with class `Turtle`. After that, perform the tasks given below.

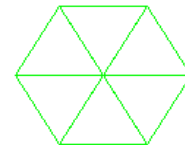
Task 1. Complete function `toString(GTurtle)` in `A5`. Follow the instructions given in the function itself. Here is an example of what our `toString` function produces, and yours should be the same:

```
"GTurtle[location=(250.0, 250.0), color=RED, direction=270.0]"
```

Your output has to be *precisely* of this format.

Task 2. Complete procedure `drawTriangle(GTurtle, int, Color)`. Then follow the instructions in the comment in the body to learn about rounding errors when using type **double** and why they don't really matter here. Note that the comment asks you to put some information at the top of file `A5.java` (as a comment).

Task 3. Complete procedure `drawGreenHex` to draw a green hexagon, as shown to the right of this paragraph. It should call procedure `drawTriangle` 6 times (either explicitly or via a loop). Some lines will be drawn twice, but that is OK. When the procedure call terminates, the turtle's properties (position, angle, pen color, and whether the pen is up or down) should be the same as when the procedure call began. Follow the directions given in the comments.

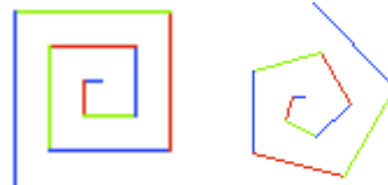


Task 4. Do TWO (repeat, 2) of 4A, 4B, or 4C. After you have completed the assignment, if you are interested, do the remaining one! It is fun to see how easy it is to do these neat things.

Note that each of these tasks involves creating a helper function with the same name (but different sets of parameters). Often, one makes helper functions private, as we've done here.

We recommend you use loops instead of recursion for this task.

Task 4A: Draw a spiral. The first picture to the right is done by drawing 10 lines. The first line has length 5; the second, 10; the third, 15, etc. After each line, 90 degrees is added to the angle. The second diagram to the right shows a similar spiral but with 75 degrees added to the angle after each line.

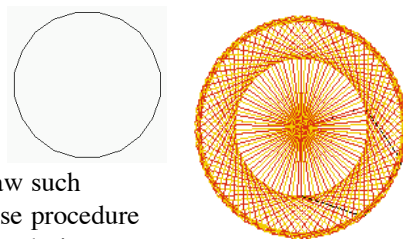


Complete the TWO procedures named `drawSpiral`. When you first test them, use 5 for `d` and 0 for `s`. Try different angles, like 90 degrees, 92 degrees, 88 degrees, etc. Use `s = 0`, or `s = .5` to see the lines drawn one at a time.

You will be amazed at what these methods do. Find out by trying these calls, assuming that `x` is an instance of `A5`:

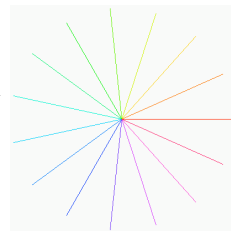
```
x.drawSpiral(.8, 300, 90, 1);    x.drawSpiral(.85, 400, 135, 1);
    x.drawSpiral(.95, 100, 60, 1);
x.drawSpiral(.9, 300, 121, 1);   x.drawSpiral(1, 400, 89, 1);
x.drawSpiral(1, 300, 150, 1);
x.drawSpiral(.99, 500, 120, 1);  x.drawSpiral(1, 500, 119, 1);
```

Task 4B: Draw many polygons. The first image to the right is a 20-sided polygon. The second image to the right is a series of 90 5-sided polygons of side length 50, the first started at angle 270, the second started at angle 274, the third at angle 278, and so on.



Complete the TWO `multiPolygons` procedures so that your program can draw such designs. It will use different colors than the second image to the right. You can use procedure `drawPolygon`, which we give you. When finished, experiment to see what neat designs come out. Try, for example, `multiPolygons(50, 5, 60)` and `multiPolygons(50, 7, 30)`.

Task 4C: Draw radiating lines. The picture to the right is done by drawing 15 lines of the same length, radiating out from the current turtle position. The angle between the lines is the same. If n lines are drawn, the angle between them is $360.0/n$. Note the colors of the lines. Each line is drawn in the HSV color (hue, 1, 1) [translated, of course, to the RGB system; we give you `HSV.class`, which you need to compile, and file `A5.java` contains function `HSV2RGB`], where hue is the hue given by the angle at which it is drawn. So, what you see is part of the color disk of the HSV system.



Complete the two `radiate` procedures. As you write them, test them with small values of n , like 4 or 8. After the procedure is completely tested, try it with 360 lines of length 200, with turtle speed .85. Isn't that neat? Also, do it with 3,000 lines and turtle speed 1; notice how much more filled in the disk becomes.

Task 5. Recursive graphics. We now ask you to develop a recursive procedure to draw some graphics, recursively. Do **one of**: the Sierpinski triangle problem, the Sierpinski carpet problem, and the H-tree problem (but if you like this stuff, do all of them!)

A `GTurtle` maintains a position and a direction, and when you ask it to draw using `forward(d)`, it draws a line of length d in that direction. A `GPen` (also in package `acm.graphics`) maintains a position but no direction. Use procedure `drawLine(dx, dy)` to draw a line of length (dx, dy) from the pen's current position, ending up at the end of the drawn line, `move(dx, dy)` to do the same thing but without drawing, and `setLocation(x, y)` to move to position (x, y) without drawing. A `GPen` has other useful methods. Spend 5 minutes looking through their specifications.

We use a `GPen` instead of a `GTurtle` in task 5 because (1) there is no need to maintain the direction and (2) the `GPen` methods can be used to draw regions that are filled in with a color.

Sierpinski triangles. Directly to the right is a filled-in equilateral triangle. We call it a Sierpinski triangle of size s (the length of a side) and depth 0. Next to it is a Sierpinski triangle of size s and depth 1. It is created by filling in 3 Sierpinski triangles of size $s/2.0$ and depth 0, in each of the corners of what would be a Sierpinski triangle of size s and depth 0. All the way on the right is a Sierpinski triangle of size s and depth 2; it is created by drawing 3 Sierpinski triangles of size $s/2.0$ and depth 1. In the same way, draw a Sierpinski triangle of size s and depth d by drawing three Sierpinski triangles of size $s/2.0$ and depth $d-1$ in appropriate places.



We have stubbed in two `sierpinski` procedures for you to complete. The first sets things up and calls the second. You can use procedure `fillTriangle` to draw a triangle — it is needed only at depth 0.

The most difficult part may be finding the height of the triangle with side length s . Knowing that it is an equilateral triangle, use of the Pythagorean theorem to figure this out. Using h for the height, you should be able to visualize a triangle that is $1/2$ of the equilateral triangle, with side lengths s , $s/2.0$, and h . Solve the formula $s**2 = (s/2)**2 + h**2$ for h .

3. Sierpinski carpet. To the right are three Sierpinski carpets of depth 0, 1, and 2. Here's how you draw them: (0) Draw a black filled-in square of side length s .

(1) To change it into a Sierpinski carpet of depth 0, *don't do anything*.

(2) To change it into a Sierpinski carpet of depth d ($d >$



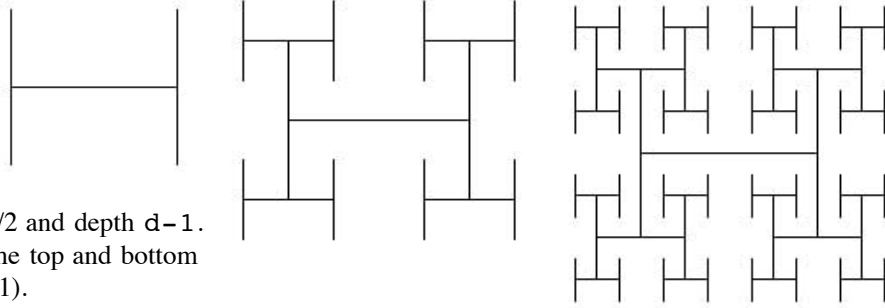
0), think of the square of size s as a grid of 9 black squares of size $s/3$. Make the middle square white. In each of the other 8 black squares of size $s/3$, draw a Sierpinski carpet of depth $d-1$.

We have stubbed in two `sierpinskiCarpet` procedures for you to complete. The first should set things up and then call the second. Procedure `fillSquare`, in A5, may be useful.

4. H-trees. To the right are three H-trees of size s and depths 0, 1, and 2. Here's how you draw them:

(1) Draw an H, with all three lines being of length s .

(2) If $d > 0$, draw four H-trees of size $s/2$ and depth $d-1$. The centers of the four H-trees are at the top and bottom of the two vertical lines drawn in step (1).



H-trees are useful in designing microprocessor chips. The lines are wires that connect circuit components in a tree of interconnections, without wires crossing.

We have stubbed in two `recursiveH` procedures for you to complete. The first should set things up and then call the second.

We have also stubbed in procedure `drawH`, which may be useful to you. Complete it if you want to use it. Draw lines drawn using procedures `setLocation` (to move the pen) and `moveAhead` (to actually draw the line).

What to submit. Put a comment at the top of your `A5.java` that contains the following information.

1. Your name(s) and netid(s);
2. The information requested in Task 2;
3. The name of your public recursive procedure;
4. What you liked best about this assignment;
5. What you most think could use improvement in this assignment; and
6. The time you spent on this assignment.

Make sure class A5 is indented properly and that all parts of the program can be seen without horizontal scrolling. Remove any `System.out.println` commands you may have put in for debugging purposes. Submit file `A5.java` on the CMS.