CS100J 18 October, 2006

The while loop and assertions

Read chapter 7 on loops.

The lectures on the ProgramLive CD can be a big help.

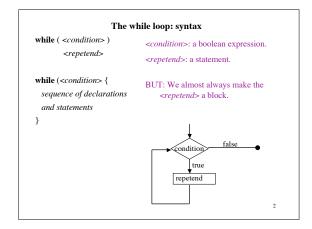
Quotes for the Day:

Instead of trying out computer programs on test cases until they are debugged, one should prove that they have the desired properties. John McCarthy, 1961, A basis for a mathematical theory of computation.

Testing may show the presence of errors, but never their absence. Dijkstra, Second NATO Conf. on Software Engineering, 1969.

A week of hard work on a program can save you 1/2 hour of thinking.

Paul Gries, CS, University of Toronto, 2005.



```
The while loop
System.out.println(5*5);
                                        To execute the while loop:
System.out.println(6*6);
                                        (1) Evaluate condition k <= 8;
System.out.println(7*7);
                                             if false, stop execution.
System.out.println(8*8);
                                        (2) Execute the repetend.
                                        (3) Repeat again from step (1).
int k= 5;
while ( k <= 8) {
                                              k= 5;
   System.out.println(k*k);\\
   k=k+1;
                                                  true
   Trace execution of the
                                              System.out.println(k*k);
   loop: Study section 7.1.2
shows you how to "trace"
                                              k= k+1:
   execution of a loop.
```

```
For loop, corresponding while loop
                                          <initialization>;
<initialization>;
                                          int k= b;
for (int k=b; k <= c; k=k+1) {
                                          while (k <= c) {
   Process k
                                             Process k;
                                             k= k+1;
```

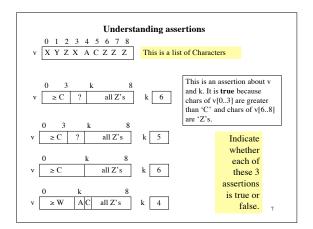
```
The while loop: 4 loopy questions
// Set c to the number of 'e's in String s.
                                      1. How does it start? (what is
int n= s.length();
                                      the initialization?)
c = 0;
// invariant: c = number of 'e's in s[0..k-1]
for (int k = 0; k < n; k = k+1) {
                                       2. When does it stop? (From
  if (s.charAt(k) == 'e')
                                       the invariant and the falsity of
                                       loop condition, deduce that
         c = c + 1;
                                       result holds.)
                                       3. How does it make progress
                                       toward termination?
```

// c = number of 'e's in s[0..n-1]

4. How does repetend keep

invariant true?

```
The while loop: 4 loopy questions. Allows us to focus on one
            thing at a time. Separate our concerns.
// Set c to the number of 'e's in String s.
int n= s.length();
                                      1. How does it start? (what is
                                      the initialization?)
c = 0: k = 0:
// invariant: c = number of 'e's in s[0..k-1]
                                      2. When does it stop? (From
while (k < n) {
                                      the invariant and the falsity of
  if (s.charAt(k) == 'e')
                                      loop condition, deduce that
         c = c + 1;
                                      result holds.)
  k = k + 1;
                                      3. How does it make progress
                                      toward termination?
// c = number of 'e's in s[0..n-1]
                                      4. How does repetend keep
                                      invariant true?
```



```
Suppose we have this while
                                    The four loopy questions
loop, with initialization:
                                    Second box helps us develop four loopy
initialization:
                                    questions for developing or understanding
while (B) {
 repetend
                                   1. How does loop start? Initialization must truthify inv P.
We add the postcondition and
also show where the invariant
must be true:
                                   At end, P and !B are true, and these must
initialization:
                                   imply R. Find !B that satisfies P &&!B
// invariant: P
while (B) {
                                   3. Make progress toward termination?
 // { P and B}
                                   Put something in repetend to ensure this.
 repetend
                                   4. How to keep invariant true? Put
 // { P }
                                   something in repetend to ensure this.
// { P }
// { Result R }
```

```
Develop loop to store in x the sum of 1..100.
We'll keep this definition of x and k true:
                 x = sum of 1..k-1
1. How should the loop start? Make range 1..k-1
                                                            Four
empty: k = 1; x = 0;
                                                           loopy
2. When can loop stop? What condition lets us
know that x has result? When k == 101
3. How can repetend make progress toward termination? k= k+1;
4. How do we keep def of x, h, k true? x = x + k;
k= 1: x= 0:
// invariant: x = \text{sum of } 1..(k-1)
while ( k != 101) {
   x = x + k;
   k = k + 1:
// \{ x = \text{sum of } 1..100 \}
```

```
Iterative version of logarithmic
                                               /** = b**c, given c \ge 0 */
 algorithm to calculate b**c.
                                               public static int exp(int b, int c) {
                                                 \quad \textbf{if} \ (c == \ 0) \ \textbf{return} \ 1;
                                                 if (c\%2 = 0) return exp(b*b, c/2);
/** set z to b**c, given c \ge 0 */
                                                 return b * exp(b, c-1);
int x = b; int y = c; int z = 1;
// invariant: z * x * * y = b * * c and 0 \le y \le c }
while (y != 0) {
   if (y % 2 == 0)
                                              Rest on identities:
        \{ x = x * x; y = y/2; \}
                                              b**0 = 1
   else { z = z * x; y = y - 1; }
                                              b**c = b * b**(c-1)
// \{ z = b**c \}
                                              for even c, b**c =
                                              (b*b)**(c/2)
                                              3*3 * 3*3 * 3*3 * 3*3 =
                                              (3*3)*(3*3)*(3*3)*(3*3) =
  Algorithm is logarithmic in c,
  since time is proportional to log c
```

```
Calculate quotient and remainder when dividing x by y  x/y = q + r/y   21/4 = 4 + 3/4  Property: x = q * y + r \text{ and } 0 \le r < y   /** Set q to and r to remainder.  Note: x >= 0 and y > 0 */ int q = 0; int r = x;  // \text{ invariant: } x = q * y + r \text{ and } 0 \le r  while (r >= y) {  r = r - y; \\ q = q + 1;  }  // \{ x = q * y + r \text{ and } 0 \le r < y \}
```