CS100J September 27 Recursion

Read: pp. 403-408 but SKIP sect. 15.1.2

Look in ProgramLive CD, page 15-3, for some interesting recursive methods.

Download presented algorithms from the website

 $\label{lem:Recursive definition: A definition that is defined in terms of itself.}$

Recursive method: a method that calls itself (directly or indirectly).

Recursion is often a good alternative to iteration (loops), which we cover later. Recursion is an important programming tool. Functional languages have no loops —only recursion.

Recursion: If you get the point, stop; otherwise, see Recursion. **Infinite recursion**: See Infinite recursion.

```
Turn recursive definition into recursive function
Factorial:
!0 = 1
!n = n * !(n-1) \text{ for } n > 0
                                    recursive case
Thus, !3 = 3 * !2
          = 3 * 2 * !1
= 3 * 2 * 1 * !0
          = 3 * 2 * 1 * 1
                             (=6)
// = !n \text{ (for } n \ge 0)
                                      - note the precise specification
public static int fact(int n) {
  \textbf{if} \, (n == 0) \, \{
        return 1:
                                    base case
  // \{n > 0\}
                                    an assertion
  return n * fact(n-1);
                                    recursive case (a recursive call)
```

Two issues in coming to grips with recursion

1. How are recursive calls executed?

2. How do we understand a recursive method and how do we create one?

We discussed the first issue in the previous lecture. Suffice it to say that if you execute a call on a recursive method carefully, using our model of execution, you will see that it works. Briefly, a new frame is created for each recursive call.

DON'T try to understand a recursive method by executing its recursive calls! Use execution only to understand how it works.

3

```
Understanding a recursive method
Factorial:
!0 = 1
                                base case
!n = n * !(n-1) for n > 0
                               recursive case
Step 1: HAVE A PRECISE SPECIFICATION
// = !n  (for n \ge 0)
public static int fact(int n) {
  if (n == 0) {
       return 1:
                                base case
  // \{n > 0\}
  return n * fact(n-1); recursive case (a recursive call)
Step 2: Check the base case.
When n = 0, 1 is returned, which is 0!
So the base case is handled correctly.
```

```
Factorial:
                             Understanding a recursive function
!0 = 1
!n = n * !(n-1) \text{ for } n > 0
                                recursive case
Step 3: Recursive calls make progress toward termination.
                                        argument n-1 is smaller than
/** = !n (for n>=0) */
                                    parameter n, so there is progress
public static int fact(int n) {
                                        toward reaching base case 0
  if (n == 0) {
        return 1;
                            barameter n
                            argument n-1
  //\{n > 0\}
  return n * fact(n-1); recursive case
Step 4: Recursive case is correct.
```

```
Creating a recursive method
Task: Write a method that removes blanks from a String.
0. Specification:
/** = s but with its blanks removed */ ◆
                                                  precise spec!
public static String deblank(String s)
                                                             Notation:
                                                     s[i] shorthand for
1. Base case: the smallest String is "".
                                                           s.charAt[i].
   if (s.length() == 0)
                                                    s[i..] shorthand for
        return s:
                                                         s.substring(i).
2. Other cases: String s has at least 1 character.
If it's blank, return s[1..] but with its blanks removed.
If it's not blank, return
     s[0] + (s[1..] but with its blanks removed)
```

```
// = s but with its blanks removed
public static String deblank(String s) {

if (s.length() == 0) return s;

// {s is not empty}

if (s[0] is a blank)

return s[1..] with its blanks removed

// {s is not empty and s[0] is not a blank}

return s[0] + (s[1..] with its blanks removed);
}

The tasks given by the two English, blue expressions are similar to the task fulfilled by this function, but on a smaller String! Rewrite each as

deblank(s[1..]).

Notation:
s[i] shorthand for s.charAt[i].
s[i..] shorthand for s.substring(i).
```

```
// = s but with its blanks removed
public static String deblank(String s) {
    if (s.length == 0)
        return s;
    // {s is not empty}
    if (s.charAt(0) is a blank)
        return deblank(s.substring(1));
    // {s is not empty and s[0] is not a blank}
    return s.charAt(0) +
        deblank(s.substring(1));
}

Check the four points:
0. Precise specification?
1. Base case: correct?
2. Recursive case: progress toward termination?
3. Recursive case: correct?
```

Check palindrome-hood

A String with at least two characters is a palindrome if
(0) its first and last characters are equal, and
(1) chars between first & last form a palindrome:

have to be the same

e.g. AMANAPLANACANALPANAMA
has to be a palindrome

/** = "s is a palindrome" */
public static boolean isPal(String s) {

if (s.length() <= 1)
return true;

// { s has at least two characters }
return s.charAt(0) == s.charAt(s.length()-1) &&
isPal(s.substring(1, s.length()-1));
}

A man, a plan, a caret, a ban, a myriad, a sum, a lac, a liar, a hoop, a pint, a catalpa, a gas, an oil, a bird, a yell, a vat, a caw, a pax, a wag, a tax, a nay, a ram, a cap, a yam, a gay, a tsar, a wall, a car, a luger, a ward, a bin, a woman, a vassal, a wolf, a tuna, a nit, a pall, a fret, a watt, a bay, a daub, a tan, a cab, a datum, a gall, a hat, a fag, a zap, a say, a jaw, a lay, a wet, a gallop, a tug, a trot, a trap, a tram, a torr, a caper, a top, a tonk, a toll, a ball, a fair, a sax, a minim, a tenor, a bass, a passer, a capital, a rut, an amen, a ted, a cabal, a tang, a sun, an ass, a maw, a sag, a jam, a dam, a sub, a salt, an axon, a sail, an ad, a wadi, a radian, a room, a rood, a rip, a tad, a pariah, a revel, a recl, a recd, a pool, a plug, a pin, a peck, a parabola, a dog, a pat, a cud, a nu, a fan, a pal, a rum, a nod, an eta, a lag, an eel, a batik, a mug, a mot, a nap, a maxim, a mood, a leck, a grub, a gob, a gel, a drab, a citadel, a total, a cedar, a tap, a gag, a rat, a manor, a bar, a gal, a cola, a pap, a yaw, a tab, a raj, a gab, a nag, a pagan, a bag, a jar, a bat, a way, a papa, a local, a gar, a baron, a mat, a rag, a gap, a tar, a decal, a tot, a beled, a tic, a bard, a leg, a bog, a burg, a keel, a doom, a mix, a map, an atom, a gum, a kit, a baleen, a gala, a ten, a don, a mural, a pan, a faun, a ducat, a pagoda, a lob, a rap, a keep, a nip, a gulp, a loop, a deer, a lever, a hair, a pad, a tapir, a door, a moor, an aid, a raid, a wad, an alias, an ox, an atlas, a bus, a madam, a jag, a saw, a mas, an anus, a gnal, a lab, a cadet, an em, a natural, a tip, a caress, a pass, a baronet, a minimax, a sari, a fall, a ballot, a knot, a pot, a rep, a carrot, a mart, a part, a tort, a gut, a poll, a gateway, a lava, a, ay, a say, a rad, a flow, a lass, a wan, a maw, a maw, a mat, a mat, a flow, a lass, a wan, a mow, a min, a dard, a raid, a lab, a cadet, a lab, a cadet, a carrot, a mart, a part, a tort, a gut, a poll, a gateway, a lava, a yay, a cam, a ray, a ray, a ray, a ray, a ra



