# Cubex with List Comprehensions 

Ross Tate

December 5, 2013

## 1 Lexing and Parsing

### 1.1 Core and Full Languages

$$
\begin{aligned}
\text { comprehension } & c::=\varnothing|e, c| \text { if }(e) c \mid \text { for }\left(\nu_{v} \text { in } e\right) c \\
\text { expression } & e::=\nu_{v}\left|\nu_{v c}\langle\tau, \ldots, \tau\rangle(e, \ldots, e)\right| e . \nu_{v}\langle\tau, \ldots, \tau\rangle(e, \ldots, e)|[c]| e+e \mid \text { true } \mid \text { false }|n| \text { "string" }
\end{aligned}
$$

Figure 1: Changes to the Cubex Core Language Grammar
The extension to the full language differs from the core language in a few ways:

- The symbol $\varnothing$ is not in the full language.
- An expression $e$ when used in the full language where a comprehension is expected represents the comprehension $e, \varnothing$ in the core language.
- The expression [ ] in the full language represents the expression $[\varnothing]$ in the core language.


## 2 Validating

The following are the changed typing judgements and rules.

|  | Judgement | Meaning |
| :--- | :--- | :---: |
| $\Psi\|\Theta\| \Delta \mid \Gamma \vdash c: \tau$ | comprehension $c$ generates values of type $\tau$ | 2 |
| $\Psi\|\Theta\| \Delta \mid \Gamma \vdash e: \tau$ | expression $e$ has type $\tau$ | 3 |

$\Psi|\Theta| \Delta \mid \Gamma \vdash c: \tau$
$\frac{\Psi|\Theta| \Delta \mid \Gamma \vdash \varnothing: \tau}{\Psi|\Theta| \Delta|\Gamma \vdash e: \tau \quad \Psi| \Theta|\Delta| \Gamma \vdash c: \tau}$
$\left.\frac{\Psi|\Theta| \Delta \mid \Gamma \vdash e: \text { Boolean }\rangle \Psi| \Theta|\Delta| \Gamma \vdash c: \tau}{\Psi|\Theta| \Delta \mid \Gamma \vdash \text { if }(e) c: \tau} \quad \Psi|\Theta| \Delta \right\rvert\, \Gamma \vdash e:$ Iterable $\left\langle\tau^{\prime}\right\rangle \quad \Psi|\Theta| \Delta \mid \Gamma, \nu: \tau^{\prime} \vdash c: \tau$
Figure 2: Type Checking Comprehensions
$\Psi|\Theta| \Delta \mid \Gamma \vdash e: \tau$

$$
\frac{\text { for all } i, \quad \Psi|\Theta| \Delta \mid \Gamma \vdash e_{i}: \tau}{\Psi|\Theta| \Delta \mid \Gamma \vdash\left[e_{1}, \ldots, e_{n}\right]: \text { Iterable }\langle\tau\rangle} \text { becomes } \frac{\Psi|\Theta| \Delta \mid \Gamma \vdash c: \tau}{\Psi|\Theta| \Delta \mid \Gamma \vdash[c]: \text { Iterable }\langle\tau\rangle}
$$

Figure 3: Type Checking Expressions

## 3 Semantics

Any expression $[c]$ should always terminate; that is, the elements of the iterable should be determined lazily. $\varnothing$ generates no values. $e, c$ generates the value of $e$ followed by the values generated by $c$. if $(e) c$ generates no values if $e$ evaluates to false and generates all the values generated by $c$ if $e$ evaluates to true. For each element $v$ of iterable $e$, for $(\nu$ in $e) c$ generates the values generated by $c$ with $\nu$ assigned to the value $v$; this is done lazily so that the comprehension generates values even if $e$ is an infinite iterable.

If the body of a comprehension refers to a mutable variable, the comprehension should use the value of that variable at the point in time that the iterable is created.

## 4 Evaluation

The extension will be evaluated with the same process as PA4, except only testing stages 1 through 3 . Note, though, that a lot of emphasis will be placed on testing the laziness of the generated iterables.

